## MACHINE LEARNING



#### **CONVOLUTIONS**

## Convolutions



Understanding convolution

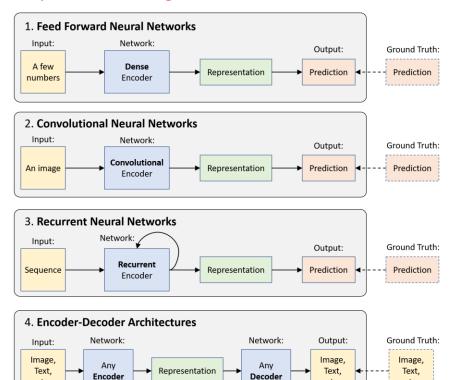
Creating custom nn.Module subclasses

Building a convolutional neural network

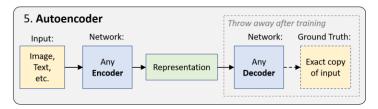
etc.

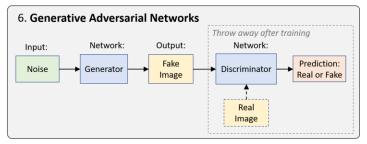


#### **Supervised Learning**



#### **Unsupervised Learning**

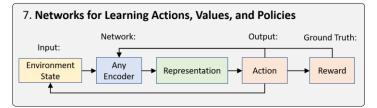




#### Reinforcement Learning

etc.

etc.





## **CONVOLUTIONS**

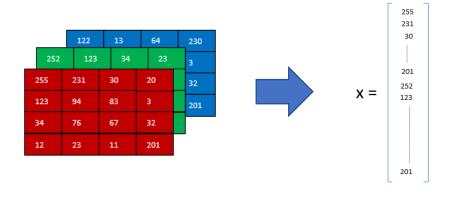
► Understanding convolutions

## Spatial structure of data



With the nn.Linear design, we have lost the spatial structure of the data:

- Consider the effect of the translation of an image of an airplane in the classifier
- Consider the relevance of neighboring pixels when interpreting a pixel as forming part of wing



No matter what the spatial distribution is, the x\_train vector will be the same

#### Convolution



#### Objective, to create:

- a translation invariant model, that
- retains spatial relationship between pixels (locality)

Convolution, or more precisely, discrete is defined for a 2D image as the scalar product of a weight matrix, the kernel, with every neighborhood in the input.



#### The Kernel

Kernel/Filter K: the element involved in carrying out the convolution operation in the first part of a Convolutional Layer

We select K as a 3x3x1 matrix.



```
Kernel/Filter, K =

1  0  1
0  1  0
1  0  1
```

#### Convolution



<b>1</b> <sub>×1</sub>	1,0	<b>1</b> <sub>×1</sub>	0	0
0,0	1,	1,0	1	0
<b>0</b> <sub>×1</sub>	0,×0	<b>1</b> <sub>×1</sub>	1	1
0	0	1	1	0
0	1	1	0	0

4	

Image

Convolved Feature

So, why is this Convolution useful for our purpose?

$$\begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix} = 1 \cdot 1 + 0 \cdot 0 + 0 \cdot 1 + 1 \cdot 0 + 1 \cdot 1 = 4$$

$$\begin{bmatrix} 1 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix} = 1 \cdot 1 + 1 \cdot 0 + 0 \cdot 1 + 1 \cdot 0 + 1 \cdot 1 = 3$$

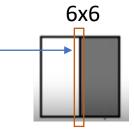
$$\begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix} = 1 \cdot 1 + 1 \cdot 0 + 1 \cdot 1 + 0 \cdot 0 + 1 \cdot 1 + 1 \cdot 0 + 0 \cdot 1 + 0 \cdot 0 + 1 \cdot 1 = 4$$



#### The convolution operators helps the model to define the Edge of the figures

#### **Edge Detection**

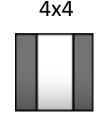
It has found the edge



\*



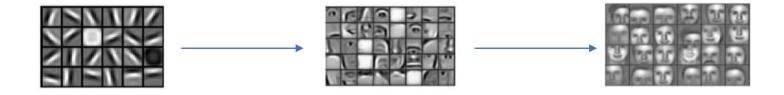
=

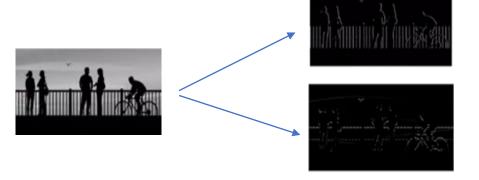


## Edge detection in image recognition



# Edge detection is the way used by the living beings to recognize the environments





Vertical Edge

Horizontal Edge

## Learning the best kernel to use



## The classic literature of convolutions is plenty of different Kernels for **Edge Detection**

$$\begin{bmatrix} 1 & 0 & -1 \\ 1 & 0 & -1 \\ 1 & 0 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 1 & 0 & -1 \\ 1 & 0 & -1 \end{bmatrix} \qquad \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix} \qquad \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix} \qquad \begin{bmatrix} 3 & 0 & -3 \\ 10 & 0 & -10 \\ 3 & 0 & -3 \end{bmatrix}$$

Vertical Edge

Horizontal Edge

Sobel Filter

Scharr Filter

How do we choose the best filter for our convolution (for example cats?



## Let's the Machine Learning choose the kernel for us!

$$\begin{bmatrix} 3 & 2 & 10 & 20 & 21 & 10 \\ 1 & 6 & 11 & 35 & 22 & 12 \\ 5 & 8 & 25 & 23 & 25 & 13 \\ 2 & 0 & 56 & 12 & 67 & 14 \\ 4 & 9 & 45 & 11 & 50 & 67 \\ \end{bmatrix} * \begin{bmatrix} w_1 \cdot 1 & w_2 \cdot 0 & w_3 \cdot 1 \\ w_4 \cdot 1 & w_5 \cdot 0 & w_6 \cdot 1 \\ w_7 \cdot 1 & w_8 \cdot 0 & w_9 \cdot 1 \end{bmatrix} = \begin{bmatrix} \\ \\ \end{bmatrix}$$



## Check out the dimensions of the following convolutional operation

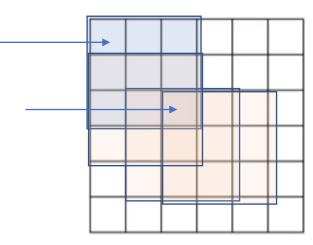
(6,6) 
$$(3,3)$$
  $(4,4)$   $(n,n)$   $(m,m)$   $(n-m+1,n-m+1)$ 



#### There are several setbacks of the convolution you would like to avoid

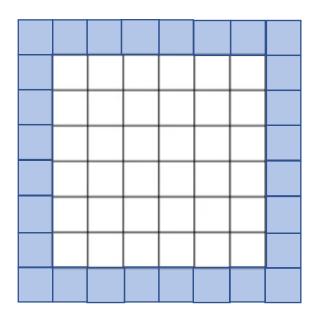
- The result matrix is smaller
- The padding takes into account values in the center more than values in the edge

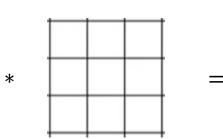
Values in the center of the convoluted matrix are overused

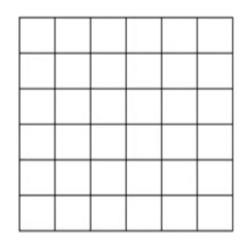




## We can augment the dimension of the matrix padding with new columns







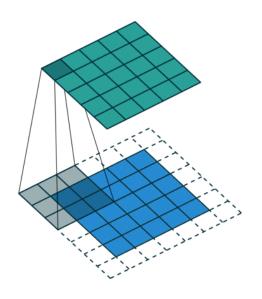
(8,8)

(3,3)

(6,6)



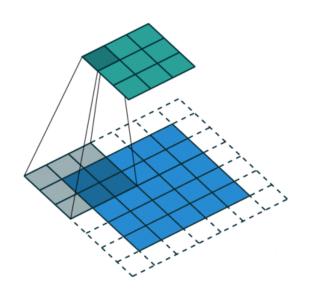
#### You've managed to keep the dimensions our convoluted matrix



- Same padding: When we augment the 5x5x1 image into a 6x6x1 image and then apply the 3x3x1 kernel over it, we find that the convolved matrix turns out to be of dimensions 5x5x1.
- Valid padding: if we perform the same operation without padding, the result matrix is smaller



#### Instead of moving kernel step-by-step, we can move it further



The chart convolutes a (5,5) matrix padded to (7,7) dimension with a (3,3) and stride=2

Matrix (n, n)

Padding p

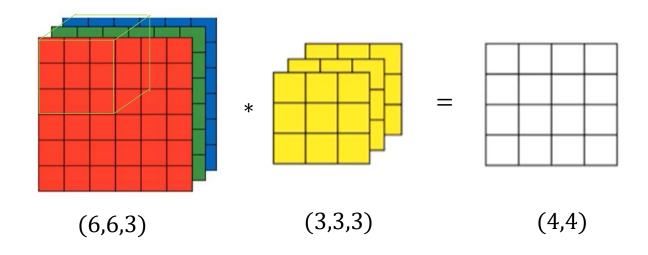
Stride *s* 

Kernel 
$$(f, f)$$
 
$$\left(\frac{n + 2p - f}{s} + 1, \frac{n + 2p - f}{s} + 1\right)$$

## Convolution over 3-dimensional volumes



#### RGB pictures are represented by (n,m,3) matrices

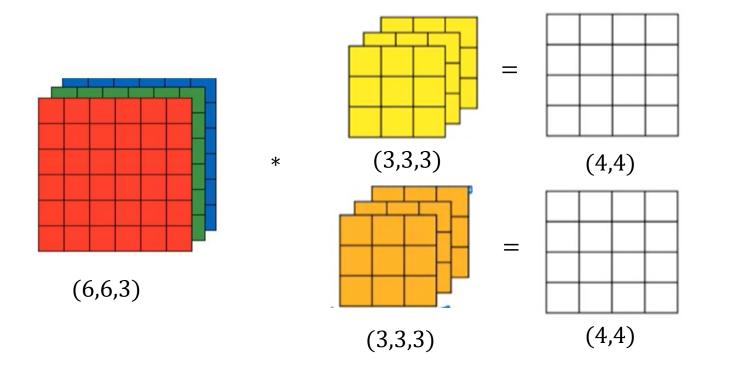


What happened to the third dimension?

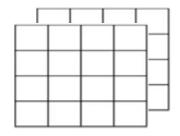
The first value of the convoluted Matrix will be the the sum of the first 9+9+9 values



#### We can apply as many filters as we want



## **Stacking**

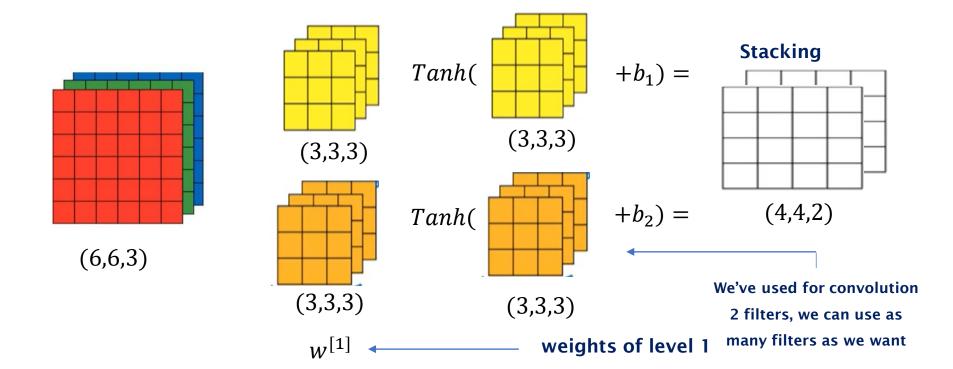


(4,4,2)

## Creating a Layer of a Convolutional Neural Network



#### Now we understand how Convolution Works, let's build a Convolution Neural Network

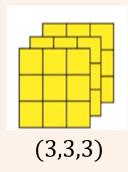




#### Meausuring the size of your Convolutional Neural Network (CNN)

Your team decided to apply a Convolutional Neural Network with 10 filters, each filter will have a 3x3 matrix per color.

How many parameters will your CNN have?



$$3 \times 3 \times 3 = 27 + bias = 28$$

$$28 \times 10 \text{ filters} = 280 \text{ parameters}$$

## Downsampling



Small kernel size: how do we aggregate the learned micro-structures to "find" relationships at a larger scale?

Strategy in convolutional nets: stacking convolutions layers and, at the same time, downsampling the image between successive convolutions.

#### Strategies to downsample:

- Average pooling
- Max pooling
- Strided convolution (calculate only every n-th pixel)

## Convolutional Neural Network Example



#### Let's check the notation we're going to use

$$f^{[l]} = filter \ size$$
  
 $p^{[l]} = padding \ size$   
 $s^{[l]} = stride \ size$   
 $n_c^{[l]} = depth \ of \ filter$ 

$$Input: (n_h^{[l-1]}, n_w^{[l-1]}, n_c^{[l-1]})$$

*Output*: 
$$(n_h^{[l]}, n_w^{[l]}, n_c^{[l]})$$

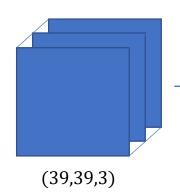
$$n_h^{[l]} = \left[\frac{n_h^{[l-1]} + 2p^{[l]} - n_c^{[l]}}{s^{[l]}} + 1\right]$$

I = number of level, usually 3

## Convolutional Neural Network Example

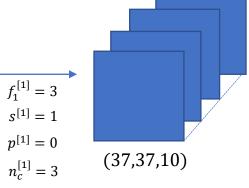
10 filters

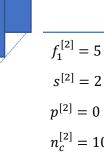




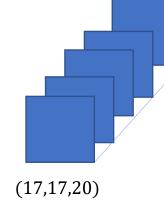
$$n_h^{[0]} = n_w^{[0]} = 39$$

$$n_c^{[0]} = 3$$





 $p^{[2]}=0$  $n_c^{[2]} = 10$ 20 filters





 $f_1^{[3]} = 5$ 

 $s^{[3]} = 2$ 





(7,7,40)

$$n_h^{[1]} = \left[ \frac{n_h^{[0]} + 2p^{[1]} - f^{[1]}}{s^{[1]}} + 1 \right] = \frac{39 + 0 - 3}{1} + 1 = 37$$

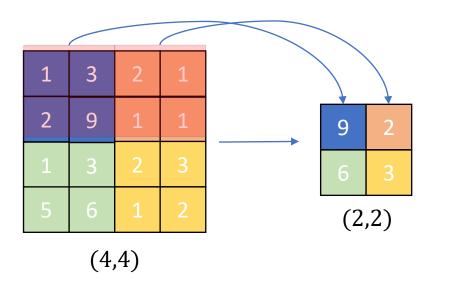
$$n_h^{[2]} = \left[ \frac{n_h^{[1]} + 2p^{[2]} - f^{[2]}}{s^{[2]}} + 1 \right] = \frac{37 + 0 - 5}{2} + 1 = 17$$

$$n_h^{[3]} = \left[ \frac{n_h^{[2]} + 2p^{[3]} - f^{[3]}}{s^{[3]}} + 1 \right] = \frac{17 + 0 - 5}{2} + 1 = 7$$

## Pooling Layer



#### Useful tool to speed calculation up a make features more robust



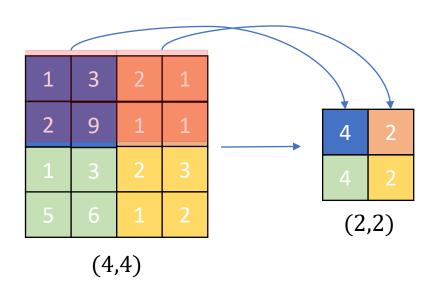
Max Pooling: The máximum value of the área

- f=2 (filter size)
- s=2 (stride=2)

You've just applied a convolutional filter with kernel size (2,2) and stride 2



#### **Average Pooling**



Average Pooling: The mean value of the área

- f=2 (filter size)
- s=2 (stride=2)

You've just applied a convolutional filter with kernel size (2,2) and stride 2

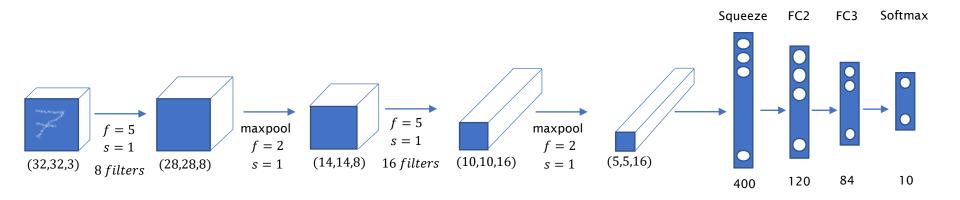


#### Some considerations about pooling

- Pooling doesn't involve parameters to learn, it's just a pretty straighforward technique for dimension reduction
- Padding is seldom used with Pooling
- Max pooling is much more used than average pooling



#### **Built by Yann LeCun for digit recognition**



## Parameters in LeNet-5



	Activation Shape	Activation Size	nº parameters
Input	(32,32,3)	3072	0
Conv2D 1 (f=5,s=1)	(28,28,8)	6072	208
Pool1	(14,14,8)	1568	0
Conv2D (f=5,s=1)	(10,10,16)	1600	416
Pool2	(5,5,16)	400	0
FC2	(120,1)	120	48120
FC3	(84,1)	84	10164
Softmax	(10,1)	10	850

Total: 59758 parameters to optimize



## Understading parameters



#### Think about all parameters shown in the previous spreadsheet

- Figure out how all the numbers are calculated
- Why the softmax has 10 outputs (instead, for example 5)



## **CONVOLUTIONS**

- ► Understanding convolutions
- Building a convolutional neural network

## Convolutions in PyTorch



The torch.nn module provides convolutions for 1, 2, and 3 dimensions:

- nn.Conv1d for time series,
- nn.Conv2d for images,
- and nn.Conv3d for volumes or videos.

For our CIFAR-10 data, we'll resort to nn.Conv2d.

#### Need to provide (at a minimum):

- Number of input features: in this case, 3 for the RGB channels
- Number of output features: arbitrary, more output features, higher capacity of the model
- Size of the kernel

### Conv2d Module



#### Please, read the documentation

#### CONV2D

Applies a 2D convolution over an input signal composed of several input planes.

In the simplest case, the output value of the layer with input size  $(N,C_{\rm in},H,W)$  and output  $(N,C_{\rm out},H_{\rm out},W_{\rm out})$  can be precisely described as:

$$\mathrm{out}(N_i, C_{\mathrm{out}_j}) = \mathrm{bias}(C_{\mathrm{out}_j}) + \sum_{k=0}^{C_n-1} \mathrm{weight}(C_{\mathrm{out}_j}, k) \star \mathrm{input}(N_i, k)$$

where  $\star$  is the valid 2D cross-correlation operator, N is a batch size, C denotes a number of channels, H is a height of input planes in pixels, and W is width in pixels.

This module supports TensorFloat32.

On certain ROCm devices, when using float16 inputs this module will use different precision for backward.

- . stride controls the stride for the cross-correlation, a single number or a tuple.
- padding controls the amount of padding applied to the input. It can be either a string {'valid', 'same'} or a tuple of
  ints giving the amount of implicit padding applied on both sides.
- dilation controls the spacing between the kernel points; also known as the à trous algorithm. It is harder to
  describe, but this link has a nice visualization of what dilation does.
- groups controls the connections between inputs and outputs. in\_channels and out\_channels must both be divisible
  by groups. For example,
  - At groups=1, all inputs are convolved to all outputs.
  - At groups=2, the operation becomes equivalent to having two conv layers side by side, each seeing half the input channels and producing half the output channels, and both subsequently concatenated.
  - At groups= in\_channels, each input channel is convolved with its own set of filters (of size out\_channels).

## Convolutions in PyTorch



#### Quick reminder of how to load cifar10



## Convoluting a sample



```
# Defining de convolution operation
conv = nn.Conv2d(in channels = 3,
                 out channels = 16,
                 kernel size = 3,
                 stride
                             = 1,
                 padding
                             =0
# Converting to a 4-dimension Tensor
img unsqueezed = img.unsqueeze(0)
img output = conv(img unsqueezed)
print ("Size of tensor previous to the convolution: {0:s}"
      .format(str(img unsqueezed.size())))
print("Size of tensor after the convolution: {0:s}"
      .format(str(img output.size())))
```

Calculating output dimensions...

$$n_h = \left(\frac{n+2p-f}{s} + 1\right) = \frac{32+0-3}{1} + 1 = 30$$

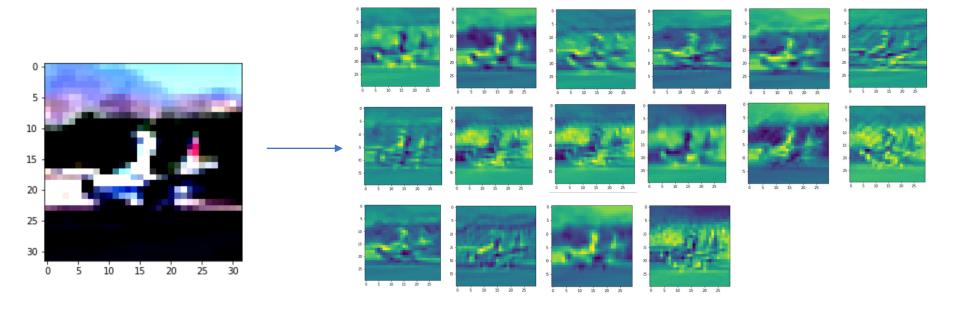
Size of tensor previous to the convolution: torch.Size([1, 3, 32, 32])

Size of tensor after the convolution: torch.Size([1, 16, 30, 30])

Picture dimensión has been reduced from (32,32) to (30,30)



#### Convolution generates 16 blurred pictures according to the 16 filters used.



```
for n in range(0,15):
   plt.imshow(img_output[0,n,:,:].detach())
   plt.show()
```





## Why are all the outputs different?

Are we using the same kernel?



## **CONVOLUTIONS**

- ► Understanding convolutions
- Building a convolutional neural network

# Testing different kernels



#### Blurring: a kernel with constant weights

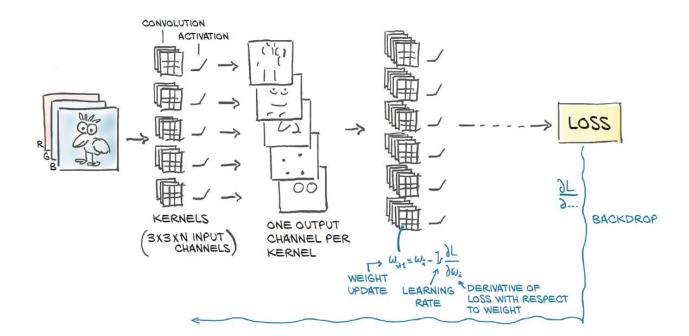
## Edge detection: differences between neighboring pixels

## Feature generation



The job of a convolutional neural network is to estimate the kernel of a **set of filter banks** in successive layers

• will transform a multichannel image into another multichannel image, where different channels correspond to different features



# Idea of downsampling



Output tensors from a convolution layer (usually followed by an activation just like any other linear layer) tend to have high values where certain features corresponding to the estimated kernel are detected (such as vertical lines).

- Through training, kernel weights adjust to detect important features
- These features, where detected, produce high value in some parts of the tensor
- With downsampling, these parts "survive" at the expense of weaker responses

## nn.MaxPool2d module



#### Max pooling provided in Pytorch by the nn.MaxPool2d module

- Takes as input the size of the neighborhood over which to operate the pooling operation.
- Example, to downsample our image by half, use a size of 2

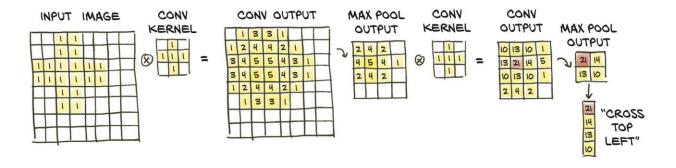
```
IPdb [6]: img_unsqueezed.size()
Out [6]: torch.Size([1, 3, 32, 32])

IPdb [7]: img_output_pool.size()
Out [7]: torch.Size([1, 3, 16, 16])
```

## Combining convolutions and downsampling



Effect of stacking convolutions and downsampling: a large cross is highlighted using two small, cross-shaped kernels and max pooling.



First set of kernels operates on small neighborhoods on first order, low-level features

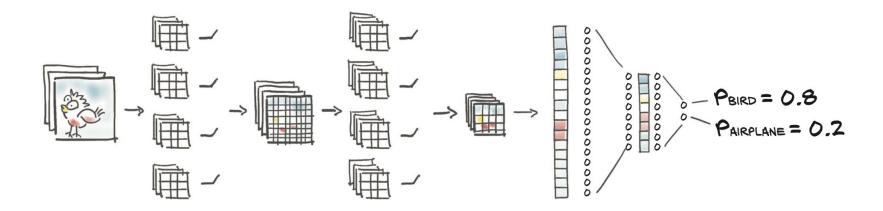
Second set of kernels effectively operates on wider neighborhoods, producing features that are
compositions of the previous features.

# Obtaining probabilities



#### Procedure:

- Covert the 8-channel  $8 \times 8$  image into a 1D vector (plus batch dimension); and
- · Complete our network with a set of fully connected layers





## **CONVOLUTIONS**

- Understanding convolutions
- Building a convolutional neural network
- ► Creating custom nn.Module subclasses

# Subclassing nn.Module



#### Subclass nn.Module

Define a forward function that takes the inputs to the module and returns the output

- Typically, forward will use other modules—premade like convolutions or customized.
- To include these submodules, we define them in the constructor \_\_init\_\_\_
- Need to call super().\_\_init\_\_()



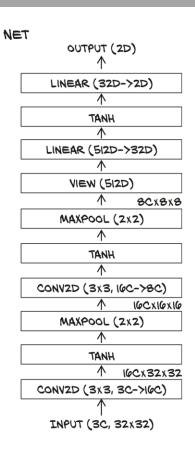
```
class Net(nn.Module):
   def init (self):
       super(). init ()
       self.convl = nn.Conv2d(3, 16, kernel size=(3, 3), padding=1)
       self.actl = nn.Tanh()
       self.pool1 = nn.MaxPool2d(2)
       self.conv2 = nn.Conv2d(16, 8, kernel size=(3, 3), padding=1)
       self.act2 = nn.Tanh()
       self.pool2 = nn.MaxPool2d(2)
       self.fcl = nn.Linear(8 * 8 * 8, 32)
       self.act3 = nn.Tanh()
       self.fc2 = nn.Linear(32, 2)
   def forward(self, x):
       out = self.pooll(self.actl(self.convl(x)))
       out = self.pool2(self.act2(self.conv2(out)))
       out = out.view(-1, 8 * 8 * 8) # <1>
       out = self.act3(self.fcl(out))
       out = self.fc2(out)
       return out
```

Missing conversion: we need to modify the output of the second MaxPool2d using view.

We will now see a new, more versatile way of building a neural nets.

## Baseline convolutional network architecture







## Loading the dataset (the loader with handle batches and shuffling):

### **Activating GPU**



```
def training loop (n epochs: int,
                  optimizer: torch.optim,
                  model: nn.Module,
                  loss fn: nn.Module,
                  train loader: DataLoader,
                  device: torch.device):
                                                                               Loop
    for epoch in range(1, n epochs + 1):
        loss train = 0.0
        for imgs, labels in train loader:
            imgs = imgs.to(device=device) # <1>
                                                                               Loading images and labels to GPU
            labels = labels.to(device=device)
                                                                              Forward Pass
            outputs = model(imgs)
            loss = loss fn(outputs, labels)
                                                                              Calculating Loss
            optimizer.zero grad()
                                                                               Backward Pass
            loss.backward()
                                                                               Repetition
            optimizer.step()
            loss train += loss.item()
        if epoch == 1 or epoch % 10 == 0:
            print('{} Epoch {}, Training loss {}'.format(
                datetime.datetime.now(), epoch,
                loss train / len(train loader)))
```

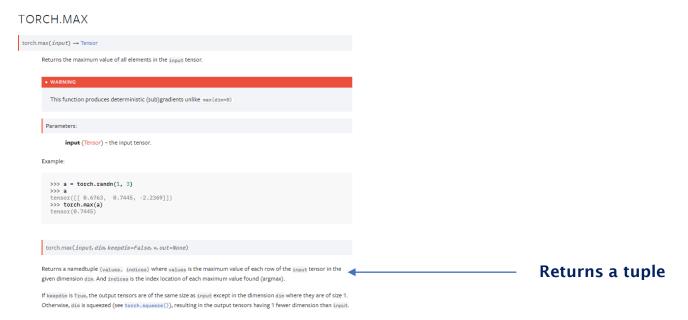


```
def validate (model: nn.Module,
             train loader: DataLoader,
             val loader: DataLoader,
             device: torch.device):
    accdict = {}
    for name, loader in [("train", train loader), ("val", val loader)]:
                                                                                        Checking accuracy from both
                                                                                        train and validation datasets
        correct = 0
        total = 0
        with torch.no grad():
            for imgs, labels in loader:
                                                                                        Sending the batch of pictures
                imgs = imgs.to(device=device)
                                                                                        and labels to device
                labels = labels.to(device=device)
                                                                                        Predicting
                outputs = model(imgs)
                _, predicted = torch.max(outputs, dim=1) # <1>
                                                                                        Chossing the max value of
                total += labels.shape[0]
                                                                                        prediction
                correct += int((predicted == labels).sum())
        print("Accuracy {}: {:.2f}".format(name, correct / total))
        accdict[name] = correct / total
    return accdict
```

# Understading torch.max



# torch.max returns the máximum value of the given set of values and "optionally" the index of the maximum value



## Understading torch.max



# The output of the model

```
Pdb [20]: outputs
tensor([[ 1.3349, -1.9178],
        [ 1.9040, -1.6632],
        [ 1.5620, -1.0870],
        [ 2.0129, -1.5942],
        [-0.3770, 0.6652],
        [ 0.1299, 0.5198],
        [ 0.5858, -0.4821],
        [-1.7611, 1.8181],
        [ 3.7983, -3.1361],
        [-2.4987, 2.0394],
        [-2.5485, 2.5286],
        [ 3.0376, -2.5142],
        [ 0.2787, -0.1730],
        [-3.0452, 2.9423],
        [ 0.6357, -0.9466],
        [ 2.4407, -2.3764],
        [-3.2843, 3.0517],
        [ 0.2308, -0.1195],
        [ 3.7184, -3.4098],
        [-3.1932, 3.6036],
        [-2.5922, 1.8526],
        [ 0.3395, -0.1361],
        [ 2.0941, -1.5432],
        [-3.3572, 3.3926],
        [-2.3391, 2.0032]
```

## The output of torch.max

We can compare the position of our maximum value with the ground truth.

Remember! {0:airplane, 1:bird}

```
correct += int((predicted == labels).sum())
```

# Saving and loading the model



#### Saving the model:

```
torch.save(model.state_dict(), data_path + 'birds_vs_airplanes.pt')
```

### Loading the model (restores same device it was saved from):

```
loaded_model = Net()
loaded_model.load_state_dict(torch.load(data_path + 'birds_vs_airplanes.pt'))
```

## Setting the device