

# Redes Inalambricas

## Capítulo I: Comunicaciones inalámbricas



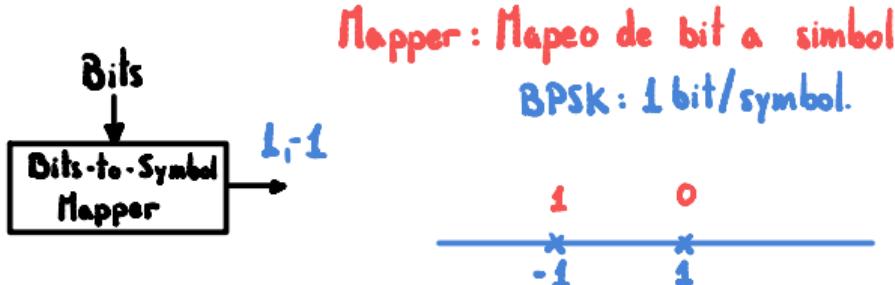
Ph.D. Alexander B. Hilario Tacuri

Universidad Nacional de San Agustín  
Arequipa - Perú

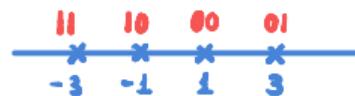
Septiembre, 2023



# Sistemas de comunicaciones inalámbricos



(Banda Base)  
4 PAM: 2 bits/simbol



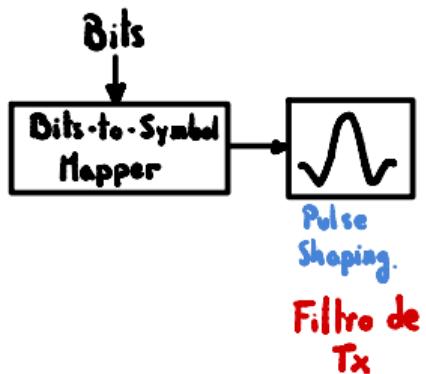
# Sistemas de comunicaciones inalámbricos



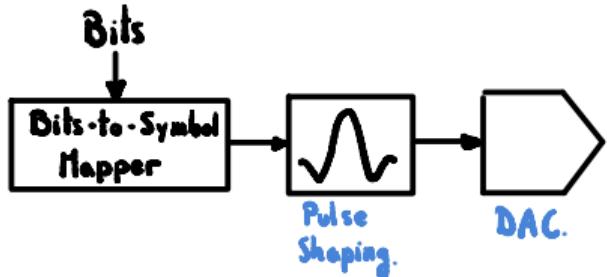
# Sistemas de comunicaciones inalámbricos



Pulse Shaping: Crea una señal digital suave



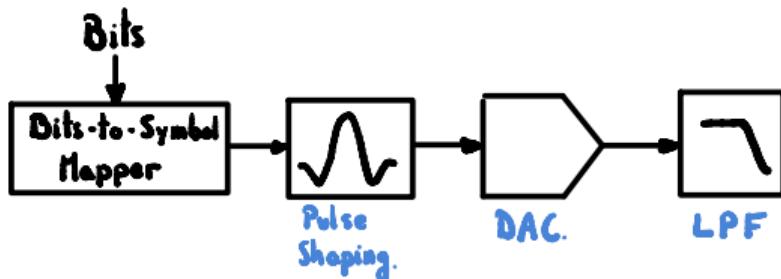
# Sistemas de comunicaciones inalámbricos



DAC : Toma los valores digitales y los transforma en una señal analógica.



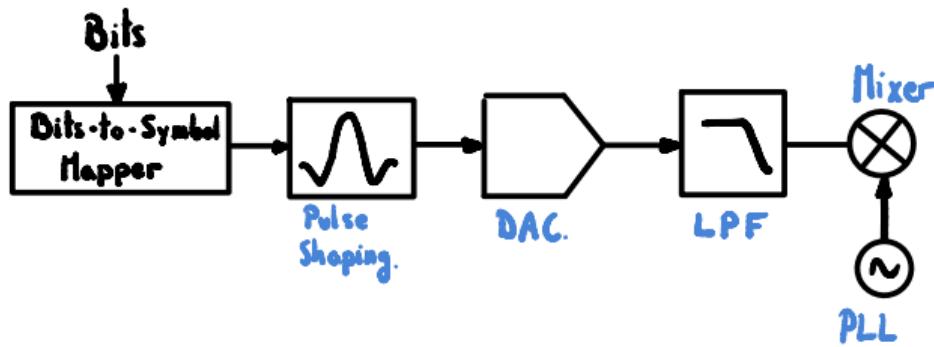
# Sistemas de comunicaciones inalámbricos



LPF: Filtro pasa bajas  
Remueve las altas frecuencias.



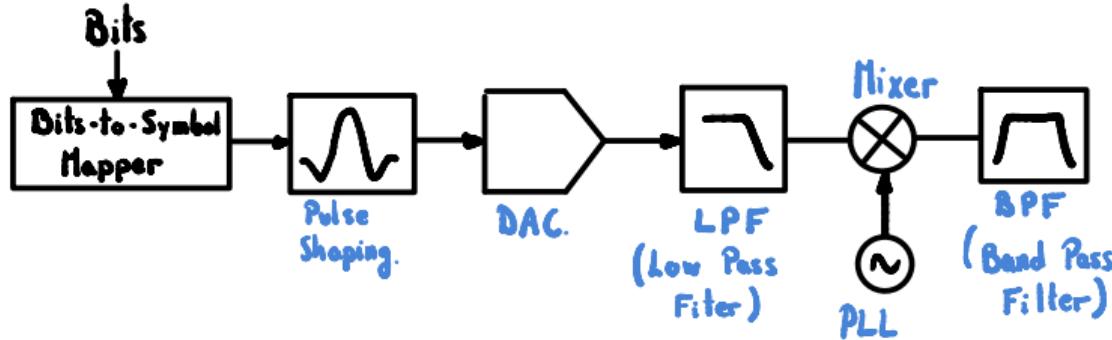
# Sistemas de comunicaciones inalámbricos



Mixer / PLL : Mueve el espectro de la señal a una frecuencia de operación



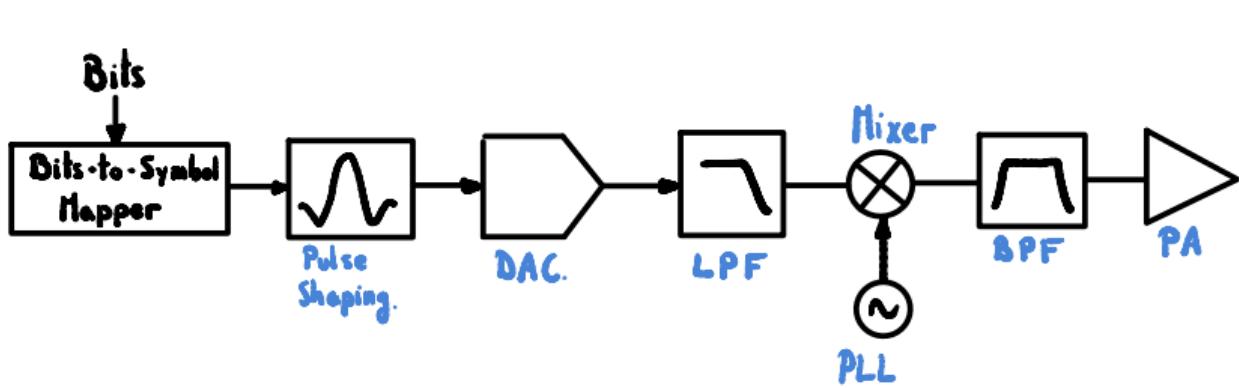
# Sistemas de comunicaciones inalámbricos



BPF: Filtro pasa-banda  
Retiene frecuencias fuera de la frecuencia de operación.



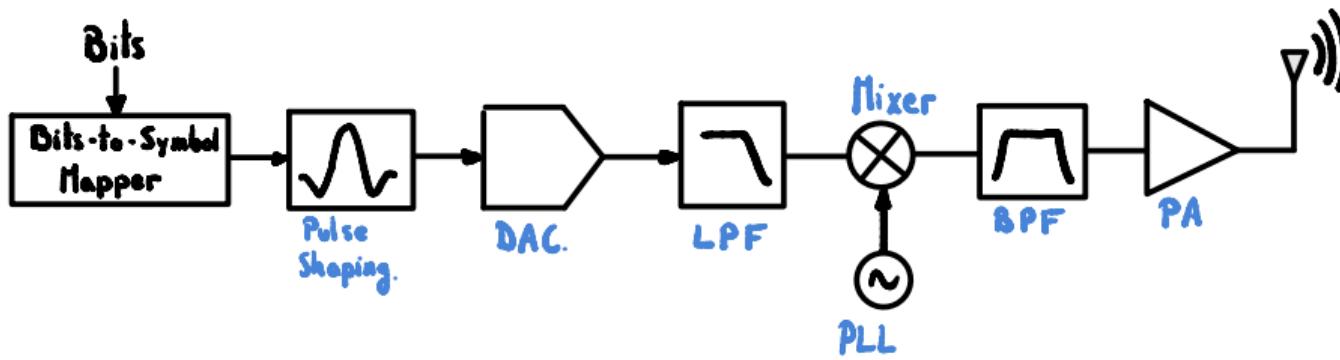
# Sistemas de comunicaciones inalámbricos



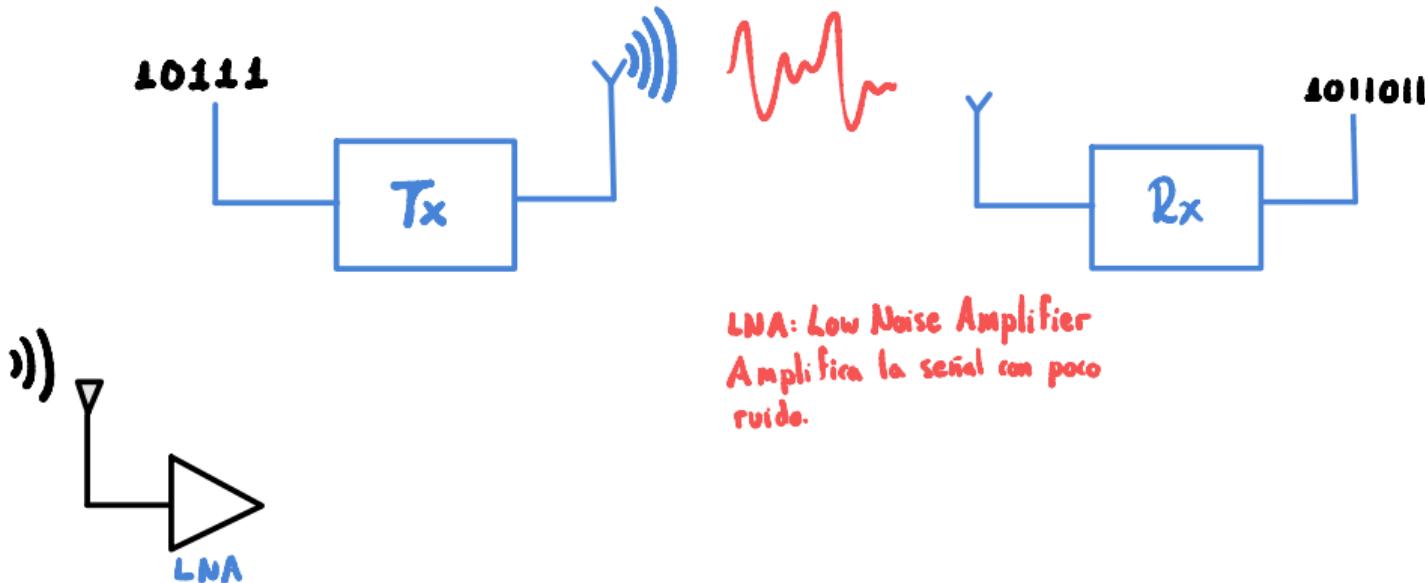
PA: Power Amplifier  
Amplifica la señal.



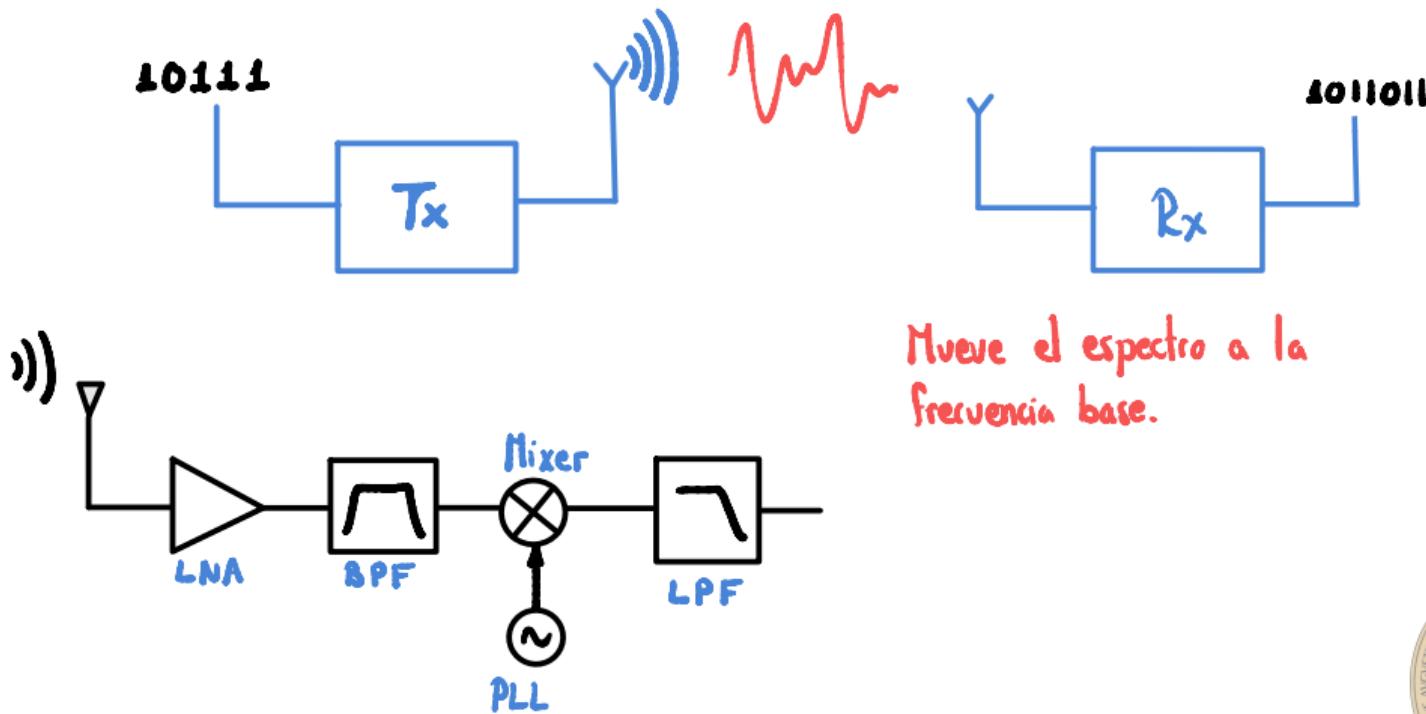
# Sistemas de comunicaciones inalámbricos



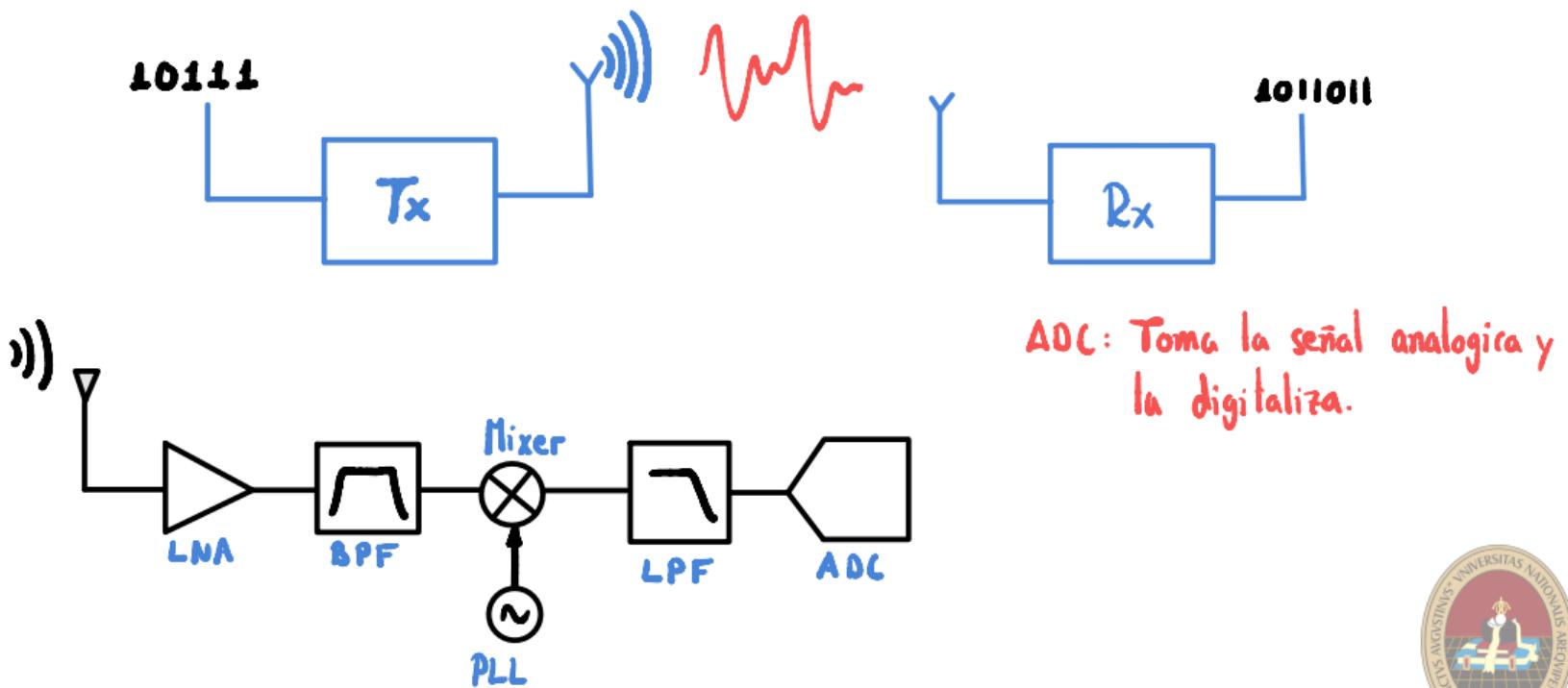
# Sistemas de comunicaciones inalámbricos



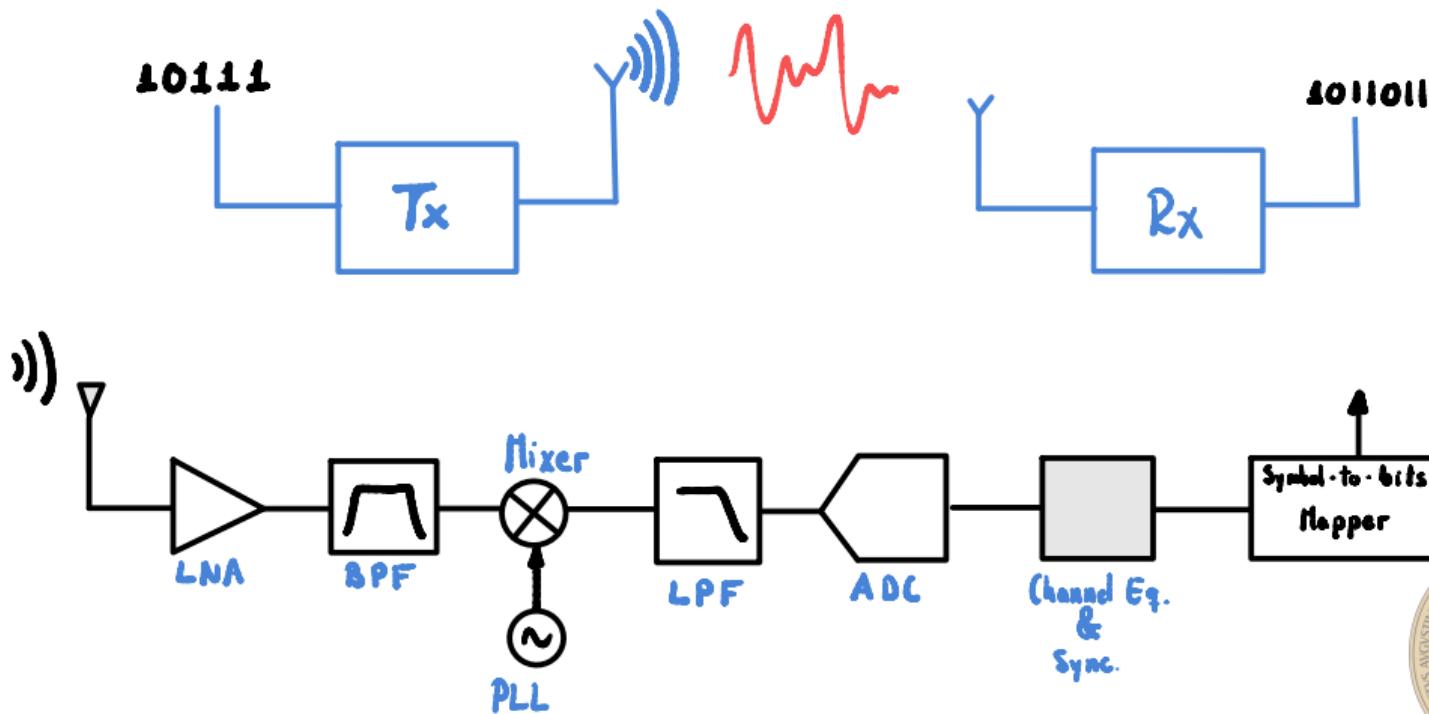
# Sistemas de comunicaciones inalámbricos



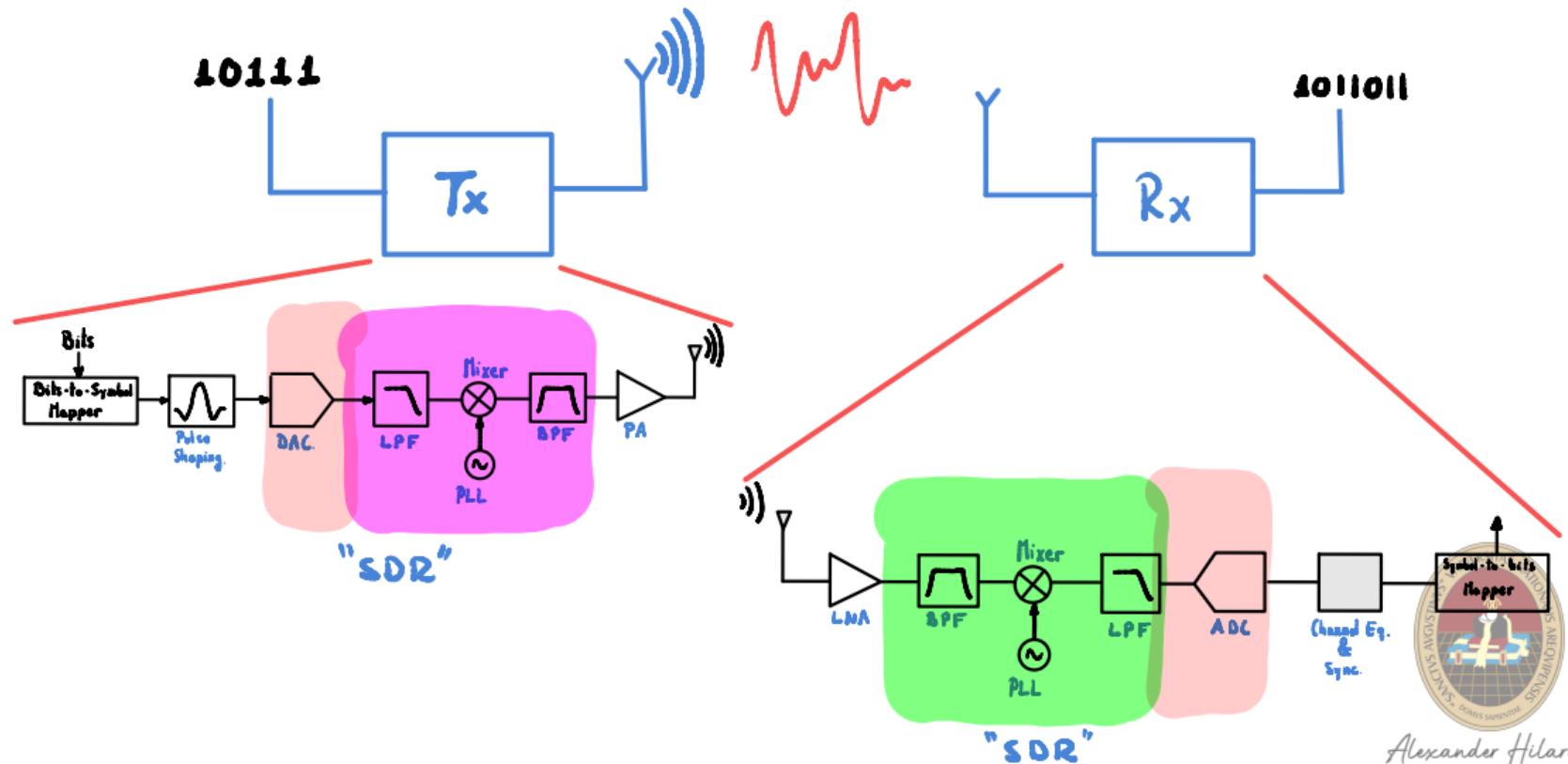
# Sistemas de comunicaciones inalámbricos



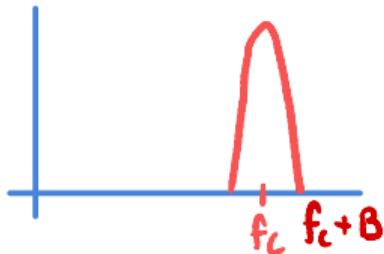
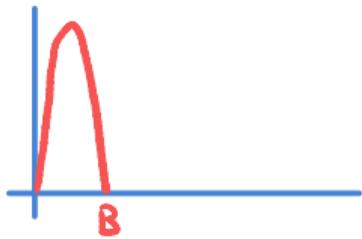
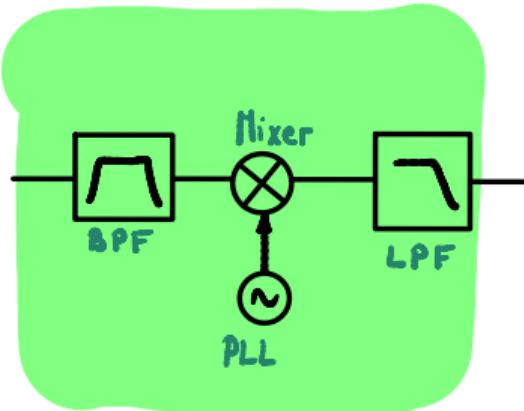
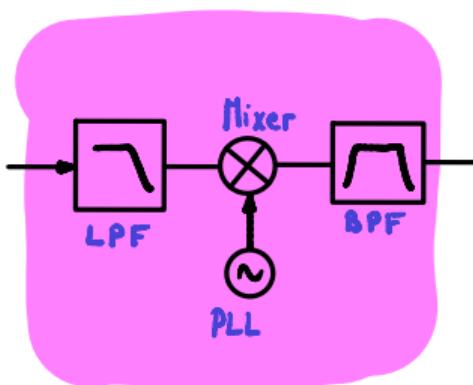
# Sistemas de comunicaciones inalámbricos



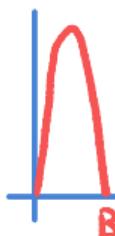
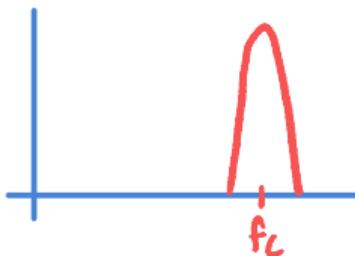
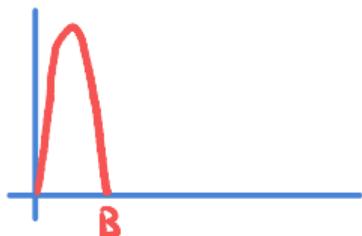
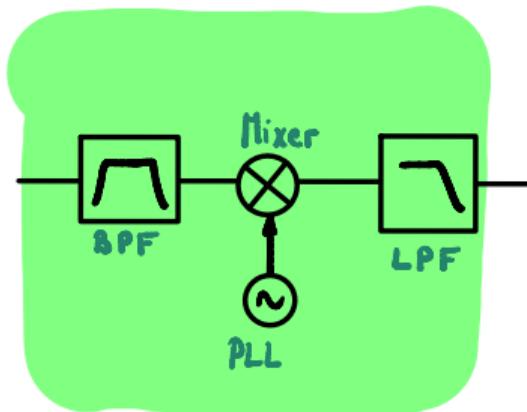
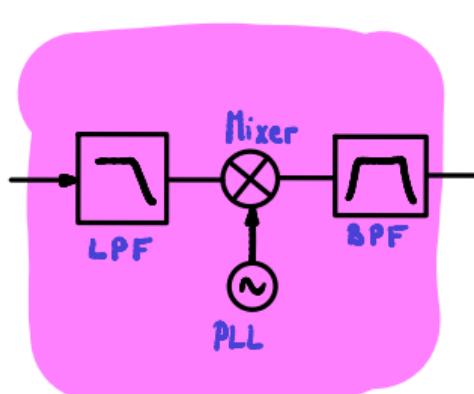
# Sistemas de comunicaciones inalámbricos



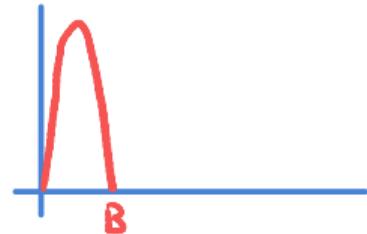
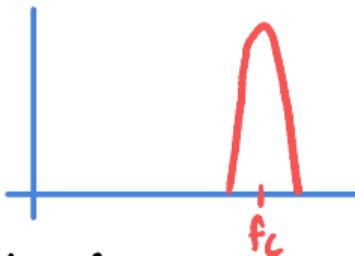
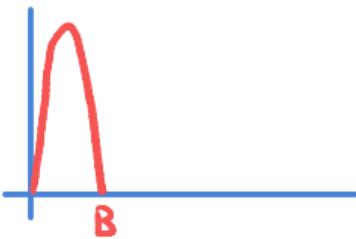
# Subida/bajada en frecuencia



# Subida/bajada en frecuencia



## Subida/bajada en frecuencia

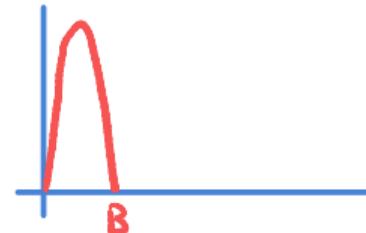
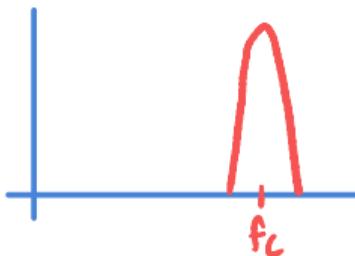
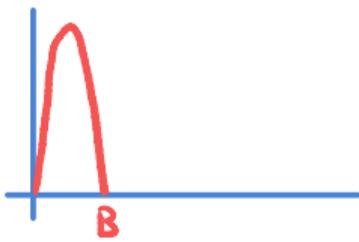


Porque no transmitimos todo a baja frecuencia?

- No hay suficiente ancho de banda
- } Velocidad de Tx  
Diferentes tecnologías
- Tamaño de la antena  $\propto$  longitud de onda.



## Subida/bajada en frecuencia



Porque necesitamos subir y bajar en la frecuencia?

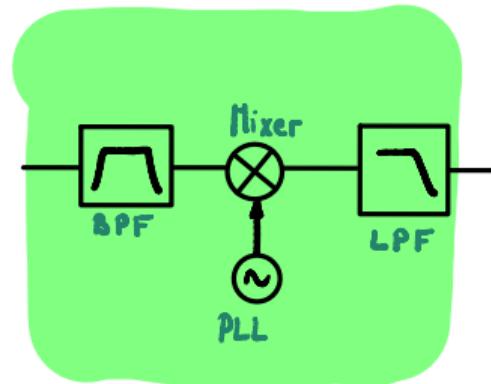
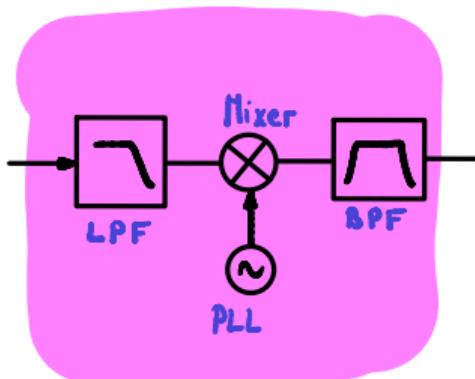
- Porque no se puede transmitir todo a baja frecuencia.
- Porque no transmitimos & recibimos todo a altas frecuencias?

Nyquist.



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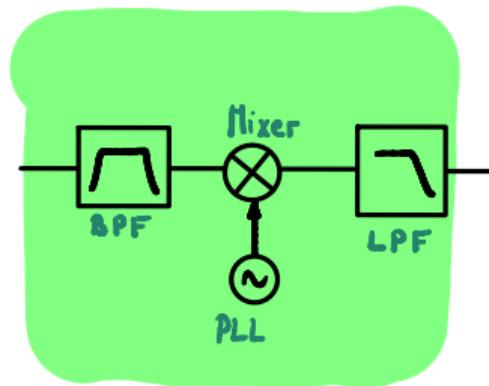
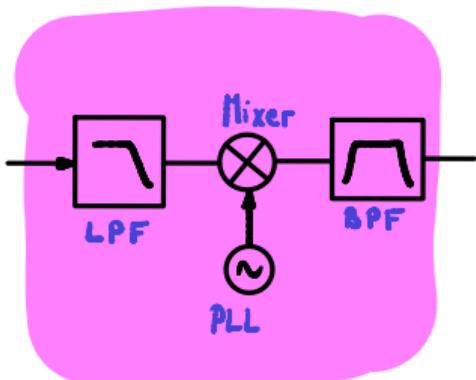
# Subida/bajada en frecuencia



$$s(t) \xrightarrow{\cos(2\pi f_{ct})} s(t) \cos(2\pi f_{ct} t) \xrightarrow{\cos(2\pi f_{ct})} s(t) \underbrace{\cos^2(2\pi f_{ct} t)}_{\frac{1}{2} + \frac{1}{2} \cos(2\pi 2f_{ct} t)}$$



# Subida/bajada en frecuencia



$$s(t) - x - s(t) \cos(2\pi f_c t)$$

$\xrightarrow{\quad}$

$$x - \underbrace{s(t) \cos^2(2\pi f_c t)}_{\frac{1}{2} + \frac{1}{2} \cos(2\pi 2f_c t)}$$

L.P.F.

$$\frac{1}{2} s(t)$$



## Subida/bajada en frecuencia

$$s(t) = x = s(t) \cos(2\pi f_c t) \xrightarrow{\quad} x \xrightarrow{\cos(2\pi f_c t)} s(t) \underbrace{\cos^2(2\pi f_c t)}_{\frac{1}{2} + \frac{1}{2} \cos(4\pi f_c t)} \xrightarrow{\text{L.P.F.}} \frac{1}{2} s(t)$$

Mapper: Mapeo de bit a simbol

BPSK: 1 bit/symbol.



2 PAM: 2 bits/symbol



## Subida/bajada en frecuencia

$$s(t) = x = s(t) \cos(2\pi f_c t) \xrightarrow{\quad} x = s(t) \underbrace{\cos^2(2\pi f_c t)}_{\frac{1}{2} + \frac{1}{2} \cos(4\pi f_c t)} \quad L.P.F.$$

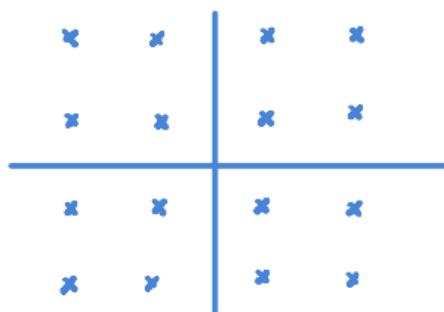
$\frac{1}{2} s(t)$

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Mapper: Mapeo de bit a simbolo

16-QAM  
4 bits/symbol

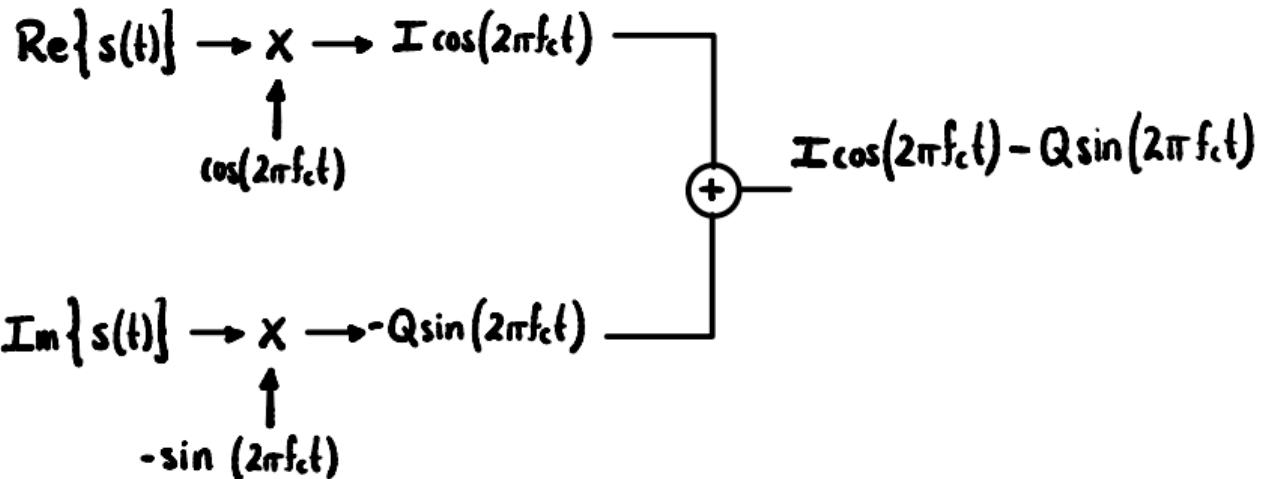
Simbolos  
Complejos!!



$s(t)$  es complejo.



# Subida en frecuencia



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## Bajada en frecuencia

$$\begin{array}{l} \xrightarrow{\cos(2\pi f_c t)} I \cos^2(2\pi f_c t) - Q \cos(2\pi f_c t) \sin(2\pi f_c t) \\ \quad \frac{1}{2} I (1 + \cos(2\pi 2f_c t)) - \frac{1}{2} Q \sin(2\pi 2f_c t) \\ \xrightarrow{-\sin(2\pi f_c t)} Q \sin^2(2\pi f_c t) - I \cos(2\pi f_c t) \sin(2\pi f_c t) \\ \quad \frac{1}{2} Q (1 - \cos(2\pi 2f_c t)) - \frac{1}{2} I \sin(2\pi 2f_c t) \end{array}$$



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## Bajada en frecuencia

$$I \cos(2\pi f_c t) - Q \sin(2\pi f_c t)$$

↓  
 $\cos(2\pi f_c t)$

$$\rightarrow X \rightarrow I \cos^2(2\pi f_c t) - Q \cos(2\pi f_c t) \sin(2\pi f_c t)$$
$$= \frac{1}{2} I (1 + \cos(2\pi 2f_c t)) - \frac{1}{2} Q \sin(2\pi 2f_c t)$$

$\cancel{\text{LPF}}$        $\cancel{\text{LPF}}$

$$= \frac{1}{2} I$$
  
  

↓  
 $-\sin(2\pi f_c t)$

$$\rightarrow X \rightarrow Q \sin^2(2\pi f_c t) - I \cos(2\pi f_c t) \sin(2\pi f_c t)$$
$$= \frac{1}{2} Q (1 - \cos(2\pi 2f_c t)) - \frac{1}{2} I \sin(2\pi 2f_c t)$$

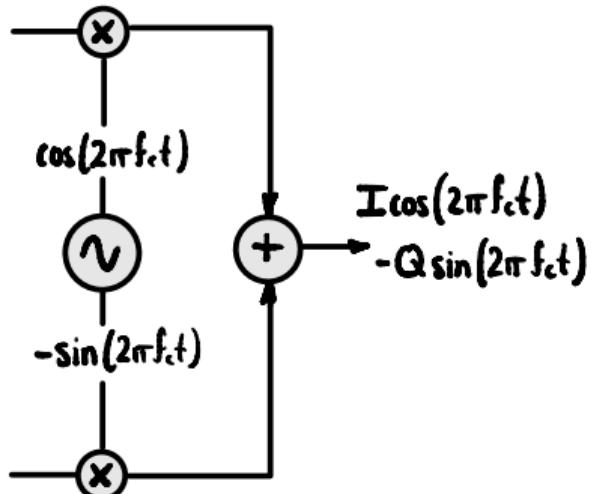
$\cancel{\text{LPF}}$        $\cancel{\text{LPF}}$

$$= \frac{1}{2} Q$$

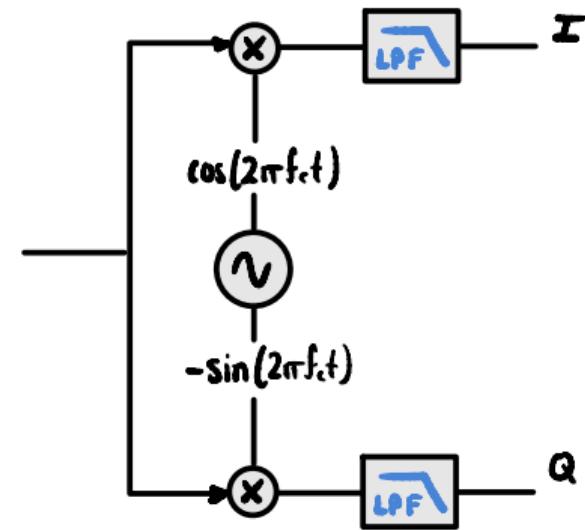


## Subida/bajada en frecuencia

$$\operatorname{Re}\{s(t)\} = I$$



$$\operatorname{Im}\{s(t)\} = Q$$

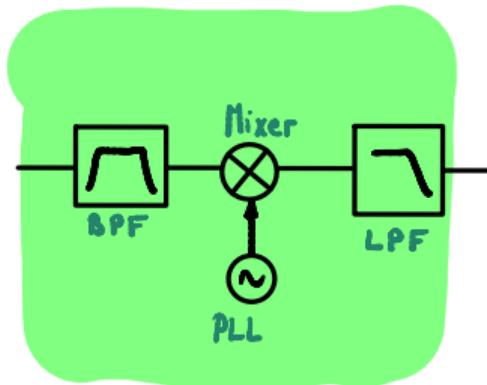
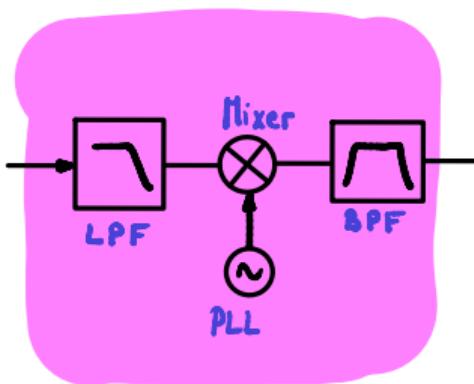


$$s(t) \times e^{j2\pi f_c t} \rightarrow \operatorname{Re}\{s(t) e^{j2\pi f_c t}\} \rightarrow x e^{-j2\pi f_c t} \rightarrow s(t)$$

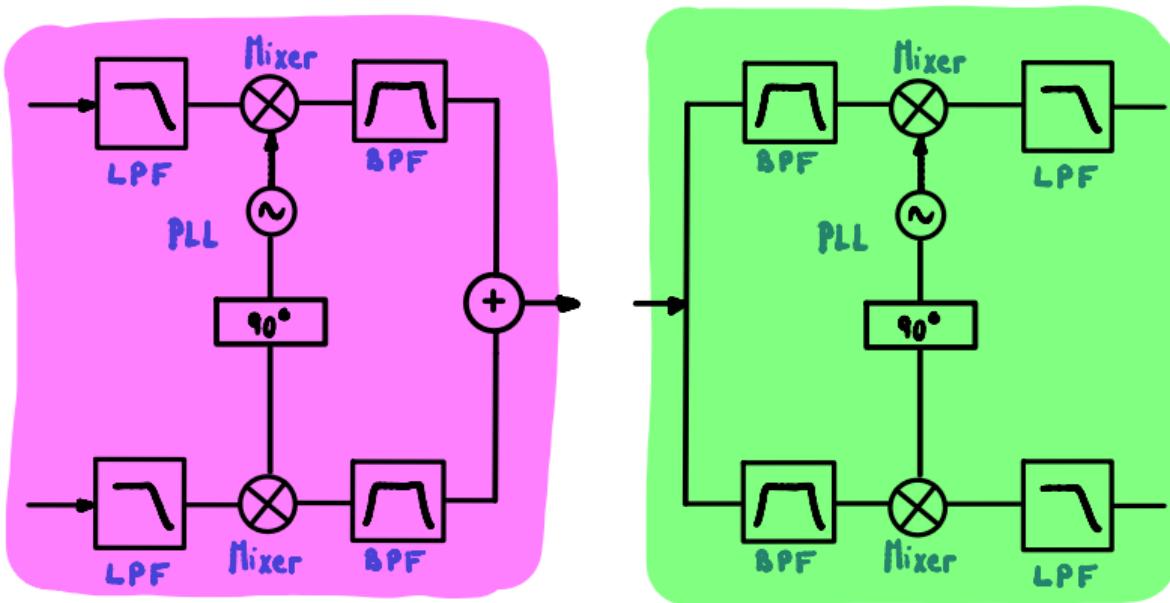
$\downarrow$   
 $\cos(2\pi f_c t) - j \sin(2\pi f_c t)$



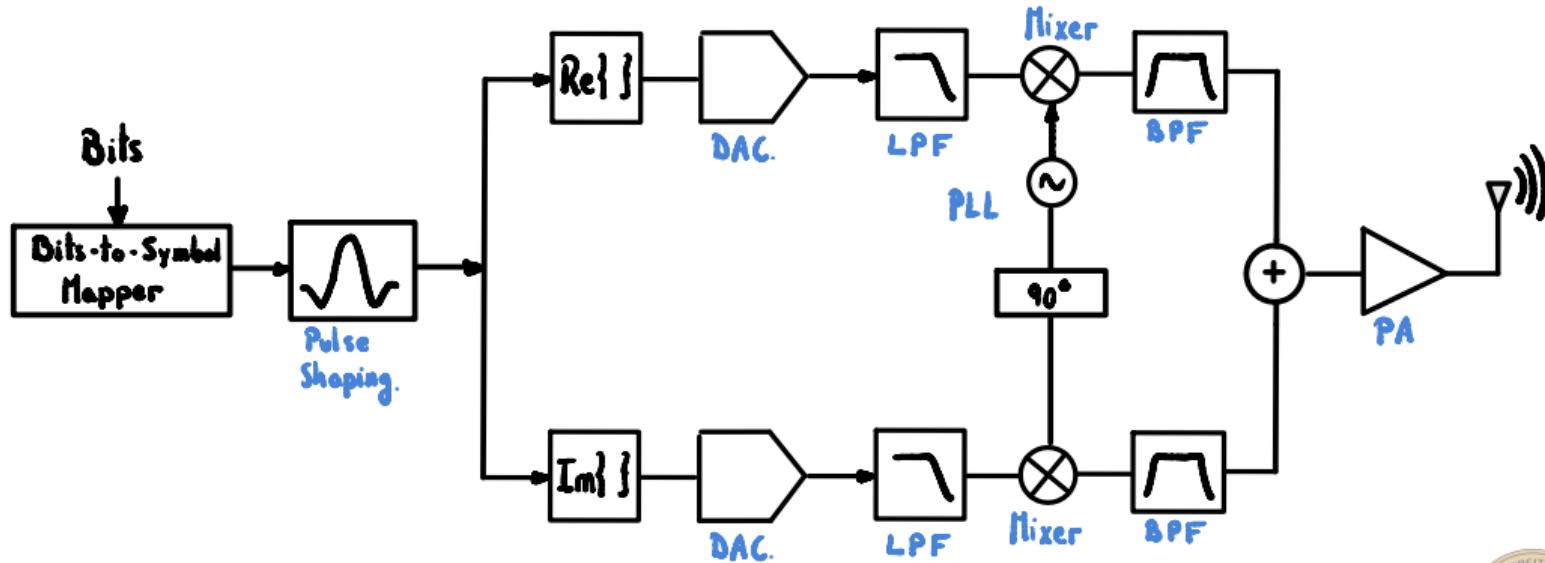
# Subida/bajada en frecuencia



# Subida/bajada en frecuencia

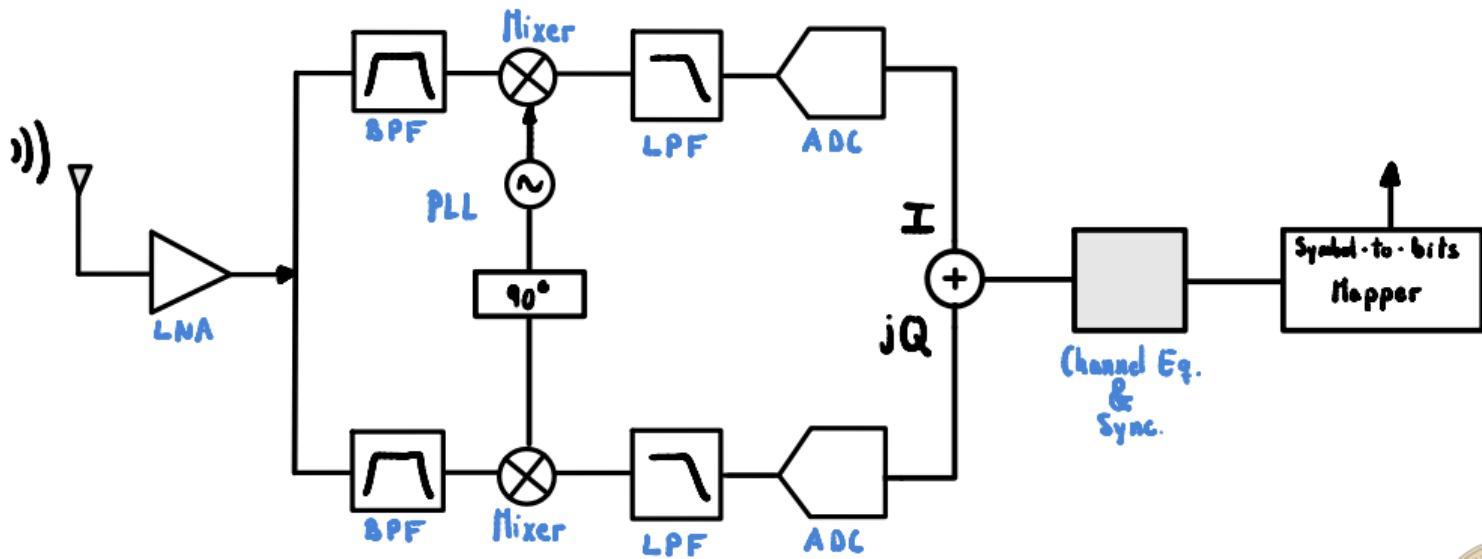


# Sistemas de comunicaciones inalámbricas



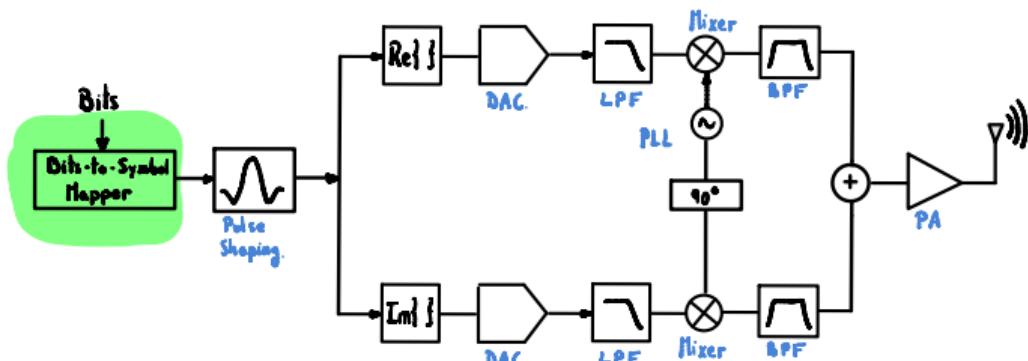
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# Sistemas de comunicaciones inalámbricas

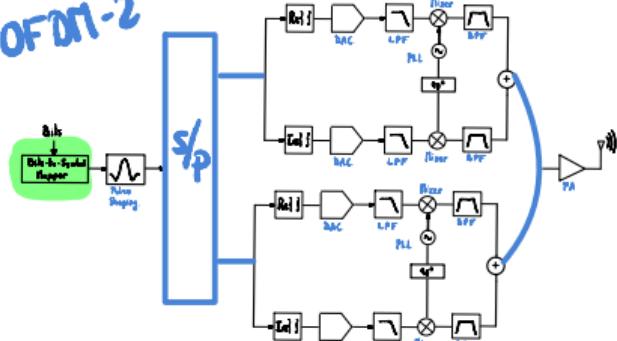


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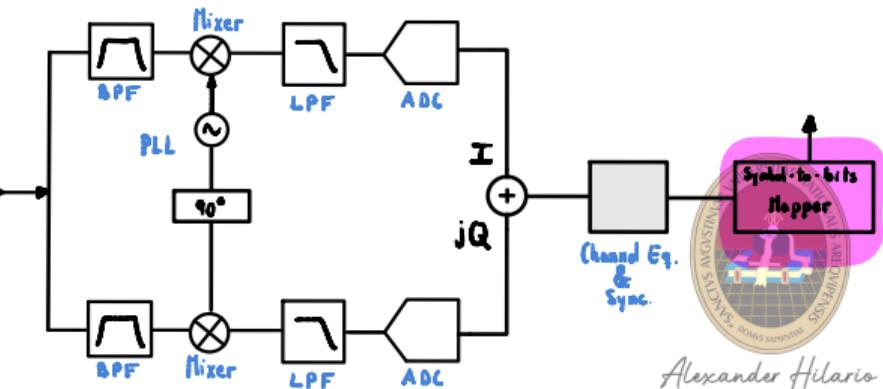
# Sistemas de comunicaciones inalámbricas



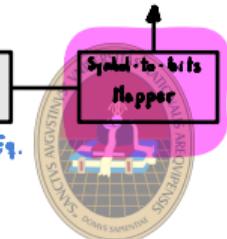
OFDM-2



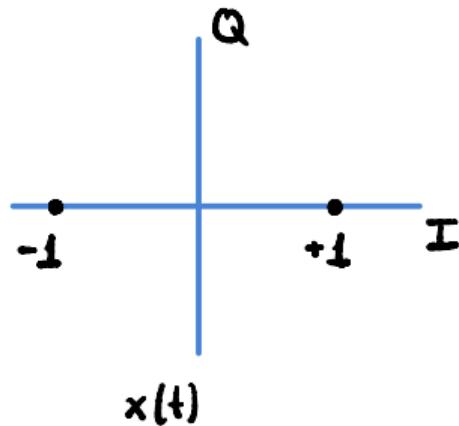
⋮



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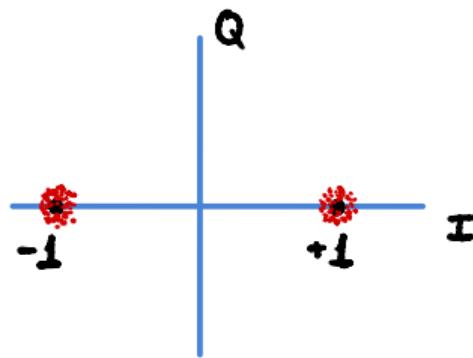
# Modulación BPSK



Constelación transmitida

$$x(t) = \sum_{k=-\infty}^{\infty} A_k g(t-kT) \cos(2\pi f_c t)$$

P.E.      V.O.

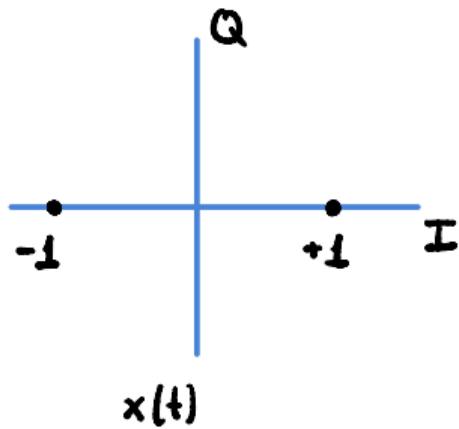


Constelación Recibida

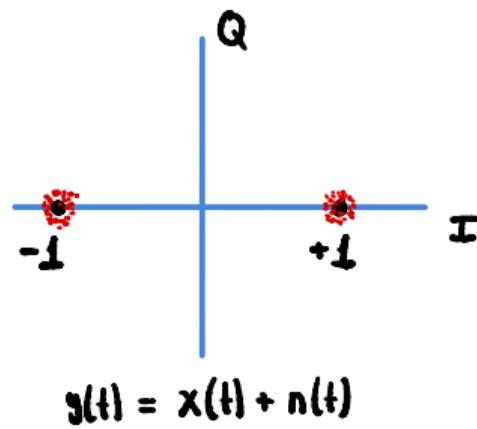


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# Modulación BPSK



Constelación transmitida



Constelación Recibida

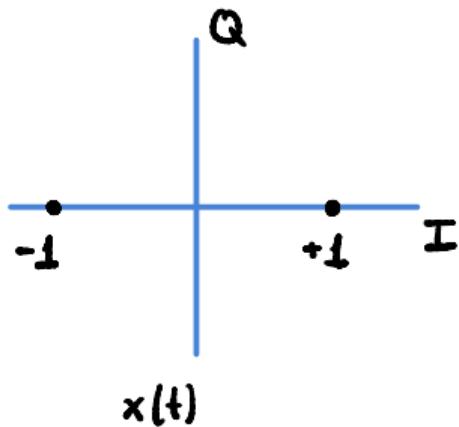
- La decodificación depende del SNR?

$$SNR = \frac{\text{Potencia de señal}}{\text{Potencia de ruido}} = \frac{E[x^2(t)]}{E[n^2(t)]} = \frac{E_s}{N_0}$$

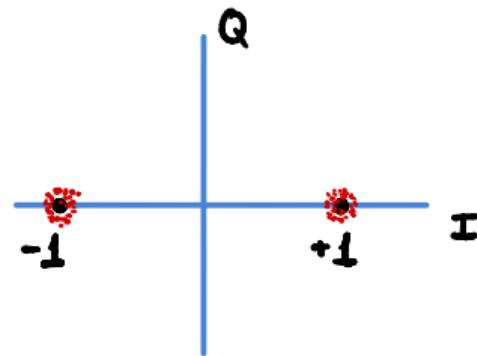


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# Modulación BPSK



Constelación transmitida



$$y(t) = x(t) + n(t)$$

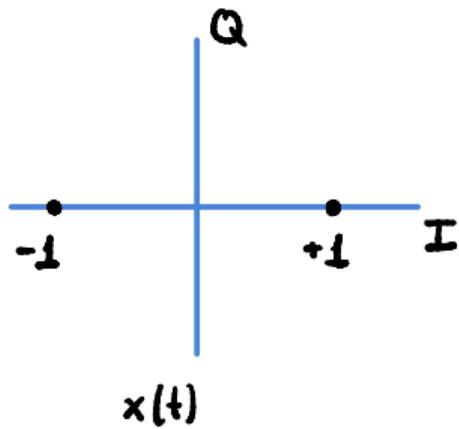
Constelación Recibida

$$SNR = \frac{E_s}{N_0} = 25\text{dB}$$

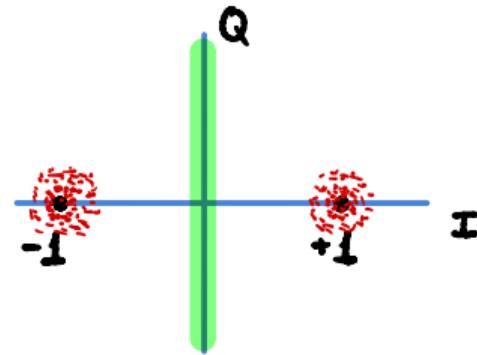


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# Modulación BPSK



Constelación transmitida



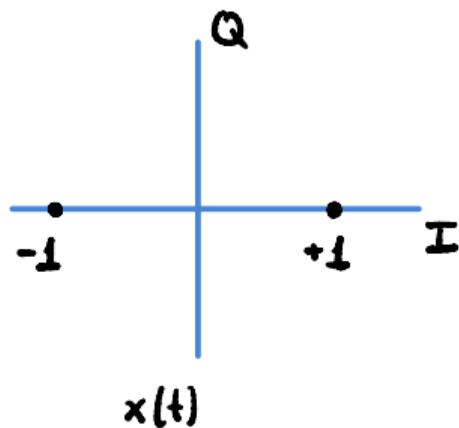
Constelación Recibida

$$SNR = \frac{E_s}{N_0} = 19 \text{ dB}$$

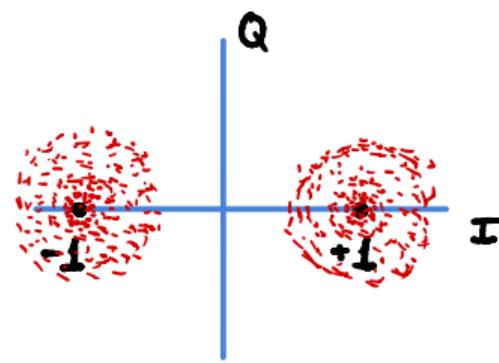


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# Modulación BPSK



Constelación transmitida



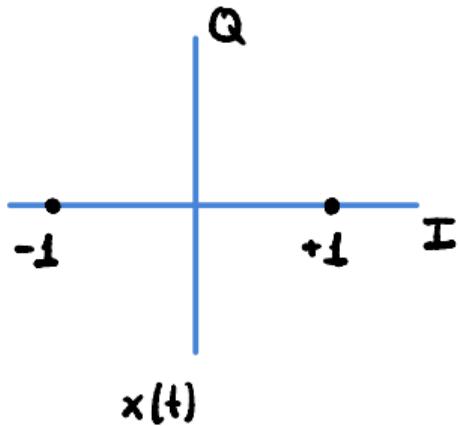
Constelación Recibida  
 $y(t) = x(t) + n(t)$

$$SNR = \frac{E_s}{N_0} = 13 \text{ dB}$$

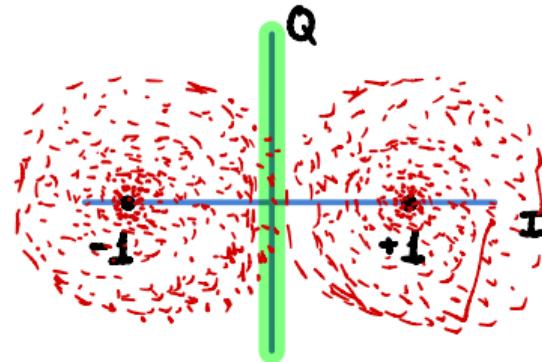


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# Modulación BPSK



Constelación transmitida



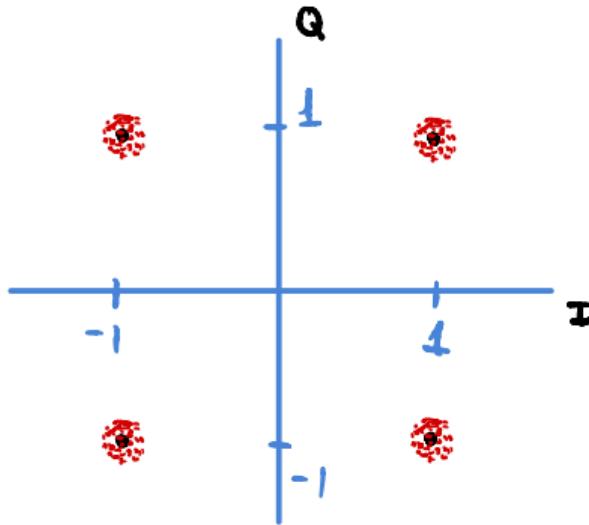
Constelación Recibida

$$SNR = \frac{E_s}{N_0} = 7 \text{ dB}$$



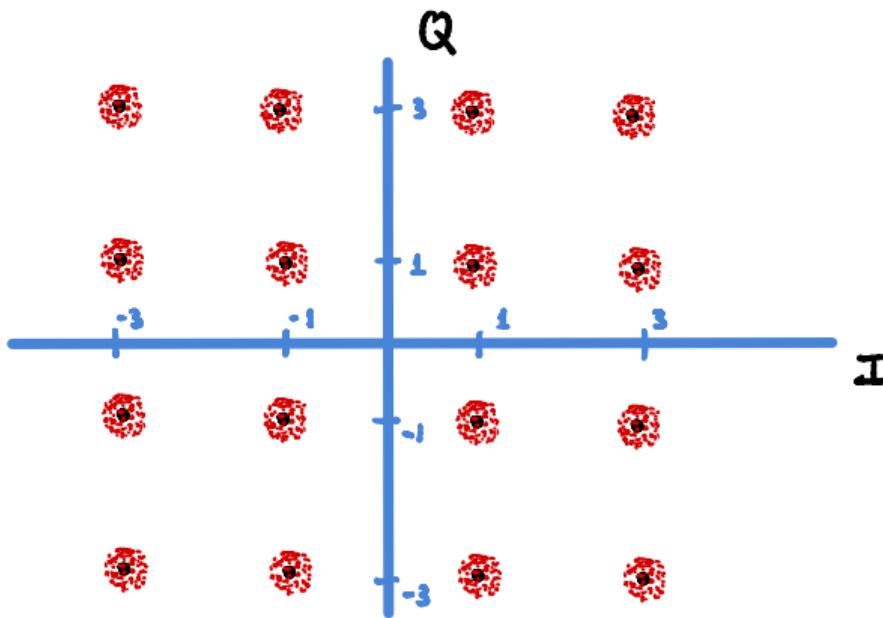
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## 4-QAM



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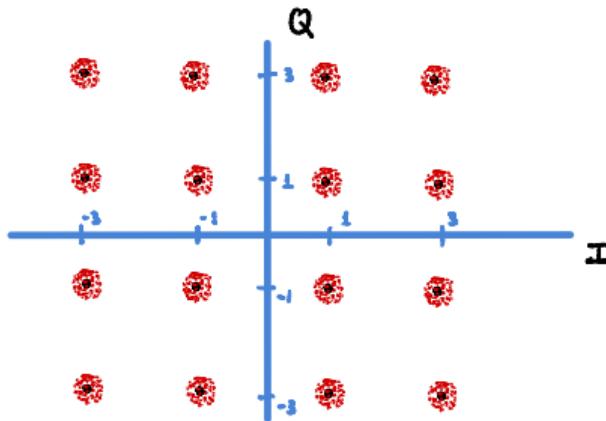
# 16-QAM



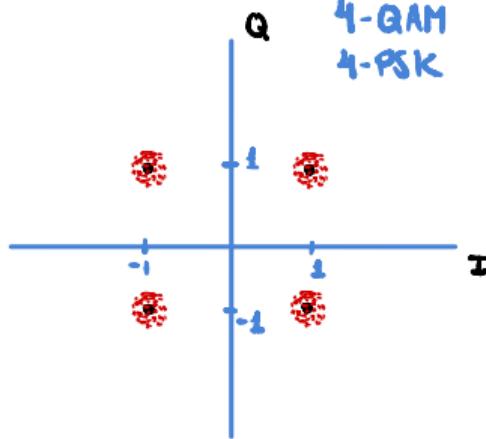
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# Modulaciones digitales

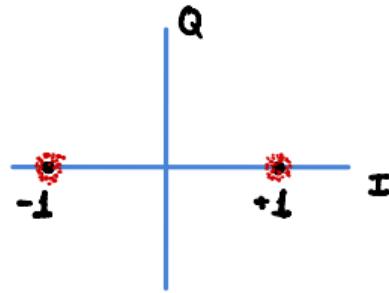
16-QAM



4-QAM  
4-PSK



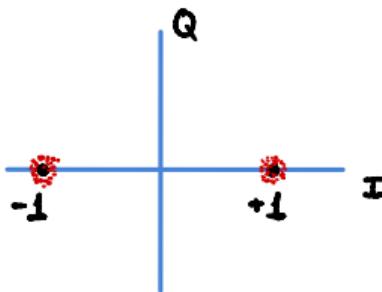
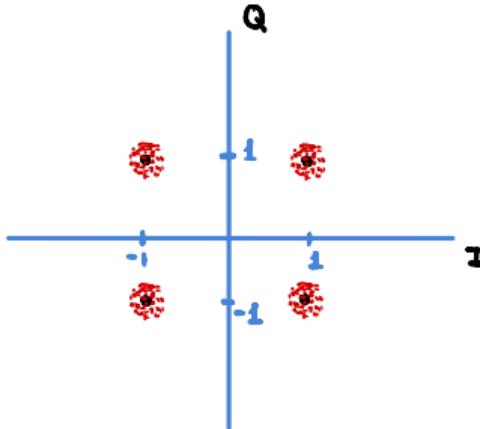
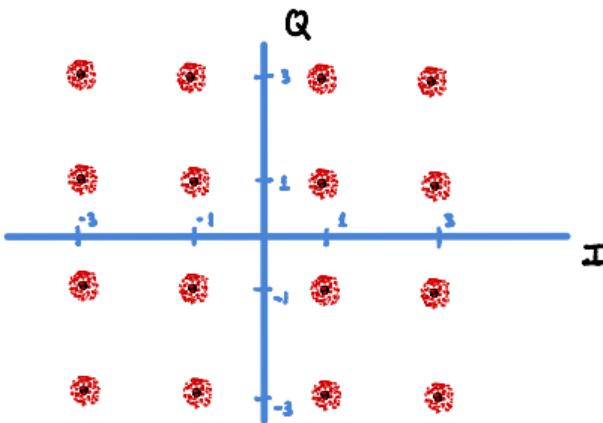
BPSK



- Estas modulaciones tienen el mismo SNR?



# Modulaciones digitales



- Estas modulaciones tienen el mismo SNR?

$$SNR = \frac{(4 \times 2 + 8 \times 10 + 4 \times 18) / 16}{N_0}$$

$$SNR = \frac{10}{N_0}$$

$$SNR = \frac{(2 \times 4) / 4}{N_0}$$

$$SNR = \frac{2}{N_0}$$

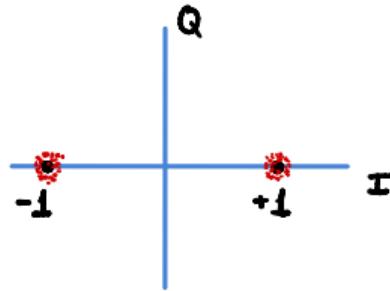
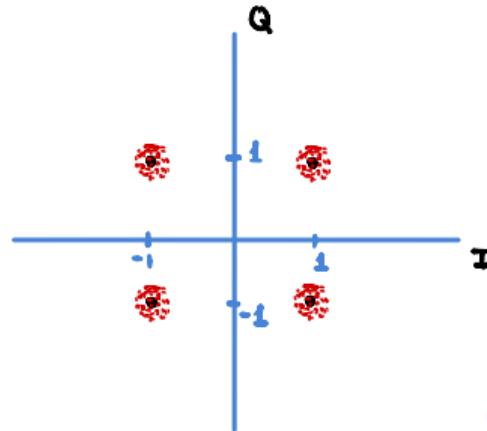
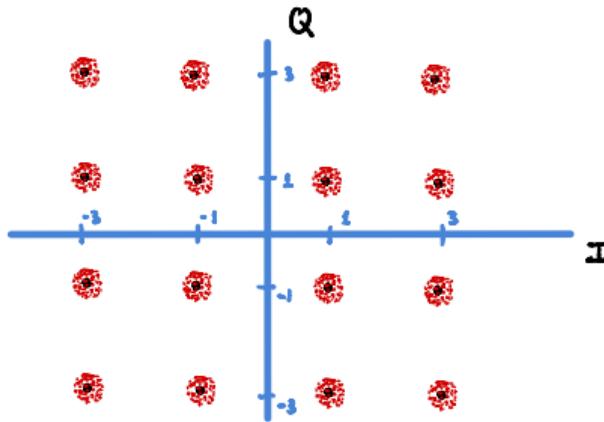
$$SNR = \frac{(2 \times 1) / 2}{N_0}$$

$$SNR = \frac{1}{N_0}$$



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# Modulaciones digitales



- Estas modulaciones tienen el mismo SNR?

$$SNR = \frac{(4 \times 2 + 8 \times 10 + 4 \times 18) / 16}{N_0}$$

$$SNR = \frac{10}{N_0}$$

$$SNR = \frac{(2 \times 4) / 4}{N_0}$$

$$SNR = \frac{2}{N_0}$$

$$SNR = \frac{(2 \times 1) / 2}{N_0}$$

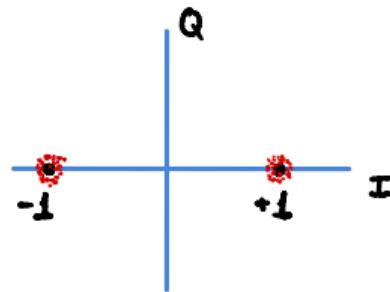
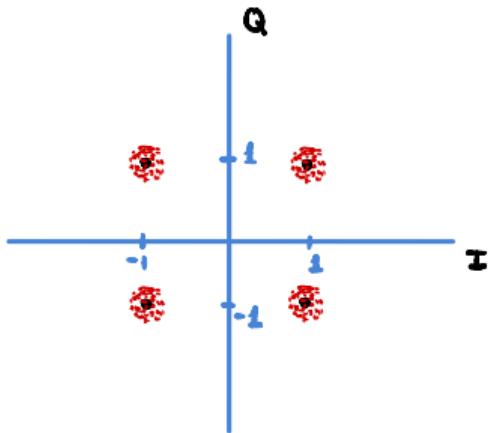
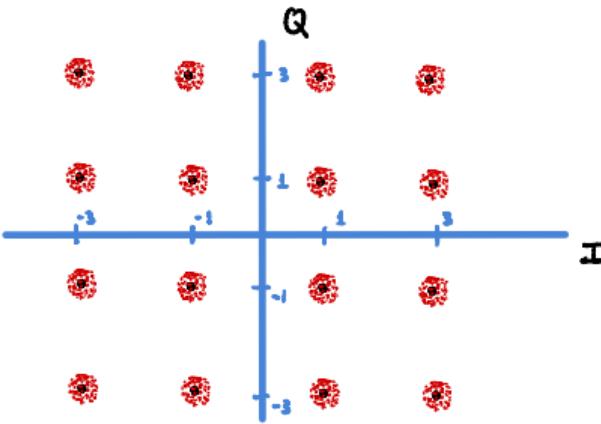
$$SNR = \frac{1}{N_0}$$

La potencia de transmisión  
no es la misma.



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# Modulaciones digitales



- Estas modulaciones tienen el mismo SNR?

$$\text{SNR} = \frac{(4 \times 2)_{10} + 8 \times 10_{10} + 4 \times 18_{10}}{N_0} / 16$$

$$\text{SNR} = \frac{(2 \times 4)_{10} / 4}{N_0}$$

$$\text{SNR} = \frac{1}{N_0}$$

$$\text{SNR} = \frac{1}{N_0}$$

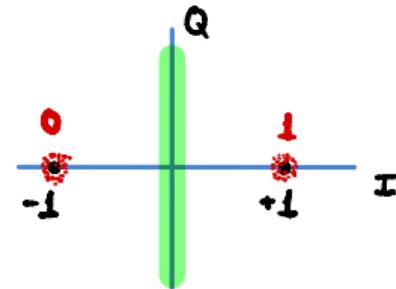
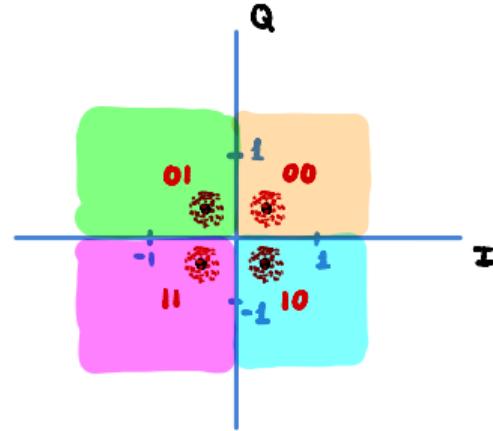
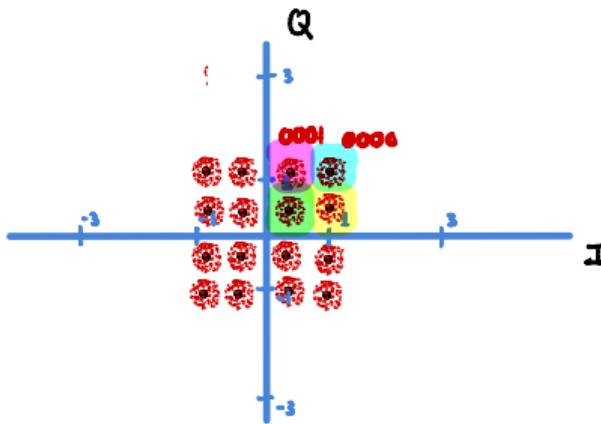
$$\text{SNR} = \frac{(2 \times 1)_{10} / 2}{N_0}$$

$$\text{SNR} = \frac{1}{N_0}$$



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# Modulaciones digitales



- Estas modulaciones tienen el mismo SNR?

$$SNR = \frac{(4 \times 2) / 10 + 8 \times 10 / 10 + 4 \times 18 / 10}{N_0}$$

$$SNR = \frac{1}{N_0}$$

$$SNR = \frac{(2 \times 4) / 4}{N_0}$$

$$SNR = \frac{1}{N_0}$$

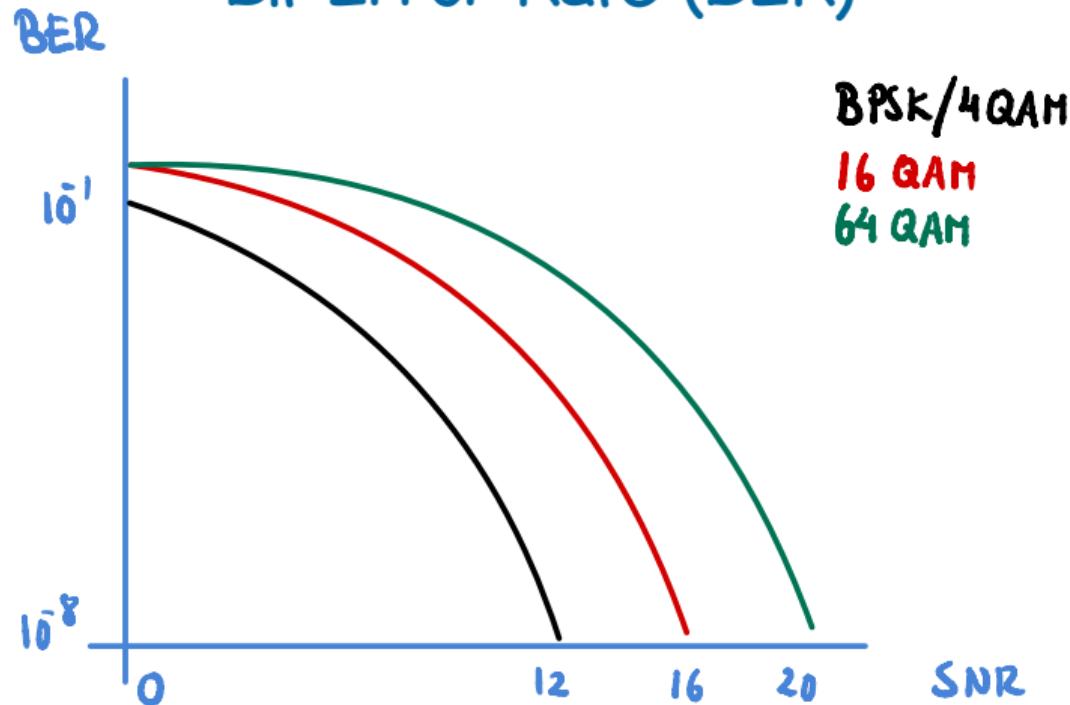
$$SNR = \frac{(2 \times 1) / 2}{N_0}$$

$$SNR = \frac{1}{N_0}$$



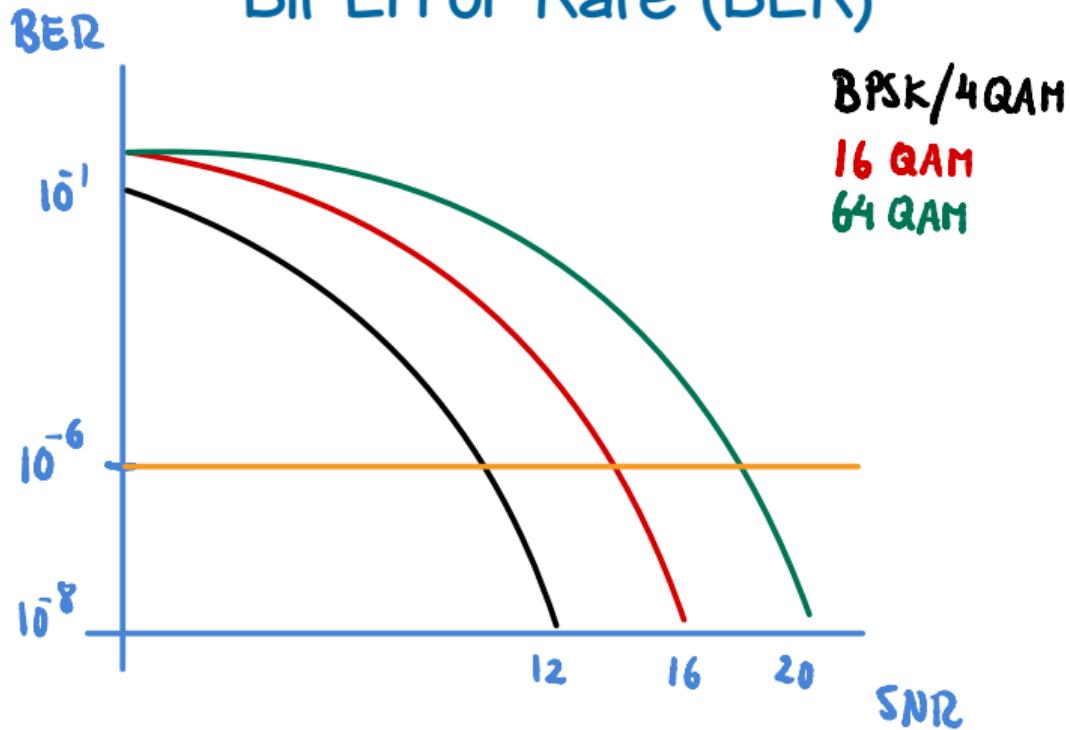
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# Bit Error Rate (BER)



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# Bit Error Rate (BER)



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# Detección de errores

- Agrega bits redundantes para detectar errores en el receptor
- Checksums
  - Detector de paridad
  - CRC: Comprobación de redundancia cíclica
  - Tasa de codificación: Data Bits/Coded Bits
- Si el paquete falla la prueba de checksum
  - El paquete es descartado
  - Paquete perdido



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# Codificación: Forward Error Correction (FEC)

- Agrega bits redundantes para corregir errores en el receptor

- FEC: Forward Error Correction

- Repetición

**0 → 000**  
**1 → 111**

|- Códigos convolucionales

- Códigos Turbo

- Códigos Polares

- Códigos LDPC

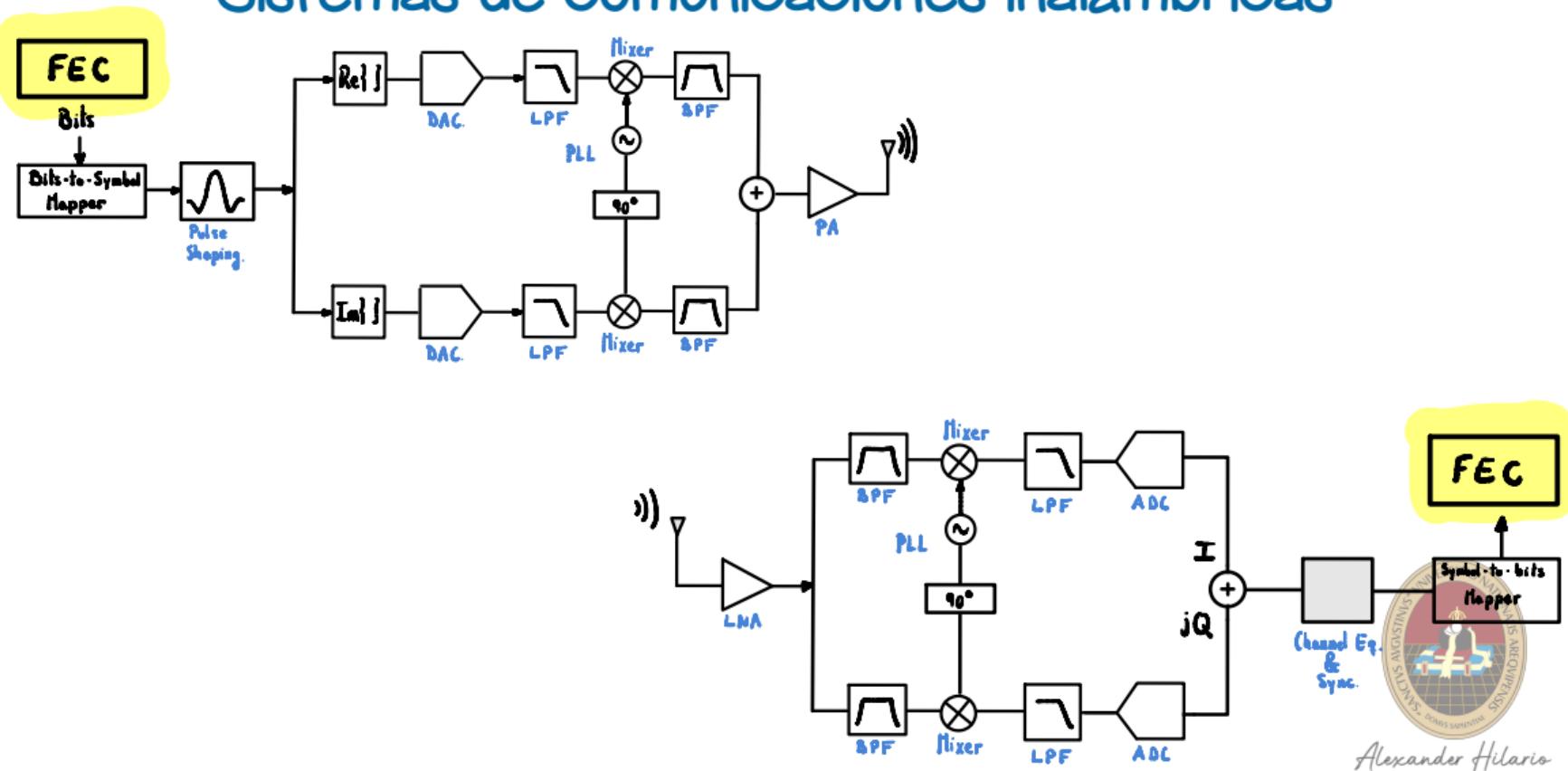
por si tengo tiempo

000	→	0
001	→	0
010	→	0
011	→	1
100	→	0
101	→	1
110	→	1
111	→	1



- Tasa de código: Nro de bits sin codificar sobre Nro de bits codificado

# Sistemas de comunicaciones inalámbricas



# Tasa de transmisión inálambrica

- Tasa de transmisión de datos
  - Ancho de banda: muestras/sec
  - Modulación: Bits/sample
  - Tasa de codificación: Data Bits/Coded Bits

- Capacidad de canal

(canal con ruido)

- Maxima tasa de datos alcanzable
- Teorema de Shannon

$$C = B \log_2 (1 + SNR) \quad \left. \begin{array}{l} \uparrow \text{Codificación} \\ \uparrow \text{Hardware (NIMO)} \end{array} \right\}$$



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# Redes Inalambricas

## Capítulo I: Comunicaciones inalámbricas



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