

1. In each question part below, I will list a set S and a rule that defines a relation R on S as follows: $(m, n) \in R$ if m and n satisfy the given rule. For each set and rule, do the following five things:
 - i List the order pairs in the relation.
 - ii Draw the associated arrow diagram.
 - iii Give the matrix representation of the relation. Be sure to label the rows and columns with the elements of S .
 - iv Identify which properties the relation has: reflexive, antireflexive, or neither; symmetric, antisymmetric, or neither; transitive or not transitive. Be sure to explain your answers.
 - v Decide whether the relation is an equivalence relation. If so, identify the equivalence classes.
 - (a) $S = \{4, 9, 17\}$; $m \geq n$.
 - (b) $S = \{0, 2, 5\}$; $mn = 0$.
 - (c) $S = \{1, 2, 6, 7, 11\}$; $m \equiv n \pmod{3}$
2. Suppose X is the set $\{a, b, c, d, e\}$ and $P(X)$ is the power set of X . The domain of each of the relations below is $P(X)$. For each relation, describe the relation in words. Then determine whether it is reflexive, antireflexive, or neither; symmetric, anti-symmetric, or neither; and transitive or not transitive.
 - (a) A is related to B if $|A - B| = 1$. The vertical bars mean the cardinality of $A - B$.
 - (b) A is related to B if $A \subset B$. Note that this notation means proper subset.
3. Determine whether the following relations are equivalence relations. If so, show that the relation fulfills the requirements for an equivalence relation, and describe the equivalence classes. If not, show how the relation fails to fulfill the requirements.
 - (a) The relation \mathcal{C} is defined by $(x, y) \in \mathcal{C}$ iff $\cos(x) = \cos(y)$, where $x, y \in \mathbb{R}$.
 - (b) The relation \propto on the domain $\mathbb{Z}^+ \times \mathbb{Z}^+$ is defined by $(m, n) \propto (p, q)$ iff $mq = np$.