Stat 50 - Elementary Statistics Exam 4 Ch 8, 9 Dr. Jorge Basilio Feb_10 Chycoliege. gbasilio@pasadena.edu

Honesty Pledge

On my honor, by printing and signing my name below, I vow to neither receive nor given any unauthorized assistance on this examination:

('	1 1-		
NAME (PRINT):	When (SIGNATURE:	
- 11 TILLE (- TOTA I),	 		$\overline{}$

Directions

- YOU ARE ALLOWED TO USE A CALCULATOR ON THIS EXAM. (Ti83/Ti83+/Ti84+/Ti84+CE-T, or scientific calculator)
- You have 80 minutes to complete this exam.
- The exam totals **108 points** but will be graded out of 100 only. (So it is possible to get 108% on this exam :).
- There are 7 problems, many of them with multiple parts.
- Place all of your belongings in the front of the classroom and I will assign you a seat. Bring with you your writing utensils.
- Cell phones must be turned off and put away in with your items in the front of the classroom.
- · Handwriting should be neat and legible. If I cannot read your writing, zero points will be given.
- Make sure to ALWAYS SHOW YOUR WORK; you will not receive any partial credits unless work is clearly shown. *If in doubt, ask for clarification.*
- · Leave answers in exact form (as simplified as possible), unless told otherwise.
- Put a box around your final answer where applicable.
- PLEASE INCLUDE UNITS where applicable
- PLEASE CHECK YOUR WORK!!!
- If you need extra space, there is extra space on the back of the cover page and clearly indicate that you are continuing your work there in the original location.
- If you finish early, you may take a break but you must come back to class by 2:45 and we will have class.
- I will take attendance at the end of class
- Some questions contain multiple-parts which you must do individually and the parts are denoted by (a), (b), (c), etc. Some questions are multiple-choice and the choices are denoted with (A), (B), (C), (D), and (E).

Score	Grade

This page is intentionally blank. It may be used for scratch paper. If you wish for me to grade your work on this page, please (i) label the problem you are working on, (ii) box your answer, (iii) indicate in the original problem's location that you will continue your work on this page.

Problem 1: 10 pts (2 pts each)

In a t-distribution when the degrees of freedom $\underline{d}f$ increases, distributions becomes

TRUE or FALSE (please spell out/write the entire word for credit). (No work needed)

(a) TRUE

	more like the z - distribution.			
(b) TRUE	The null hypothesis is a claim about a parameter assumed true until there is enough statistical evidence to reject it.			
(c) FALSE	A type Terror is made by failing to reject a false null hypothesis.			
(d) TRUE	All other things being equal, choosing a smaller value of α will increase			
	the probability of making a type II error.			
(e) TRUE	Two samples are said to be independent when the selection of the individuals in one sample has no bearing on the selection of those in the other sample.			
	Problem 2: 24 pts (2 pts each blank)			
T:11: (1 11 1	1 Toblem 2. 21 pts (2 pts each blank)			
Fill in the blanks:				
(a) In a right-tailed hypothesi	s test, the sign in the alternate hypothesis is greater then (?)			
(b) If we get a p-value of 0.015 in a hypothesis test with a significance level of $\alpha=0.02$, then we hypothesis.				
	value is the probability of selecting a sample whose test statistic is at least as extreme			
as the observed test statist	ic that we got, assuming the null hypothesis is			
(d) When converting two sam	ples into one sample using the difference, d , of matched-pairs , we use the following notation:			
Point Estimate:				
True mean difference	: Sample mean standard deviation: S_d			
Null Hypothesis:	o · $M_{ol} = O$ Alternate Hypothesis for a left-tailed test: $H_{a}: M_{ol} < O$			
Requirements are:	SRS and normaly or N>30 distributed			
	201 01. 40100			

Problem 3: 4 pts (2 pts each)

Multiple-choice. Select the correct answer:

(a) A confidence interval is an interval that is used to estimate a:



- (A) population parameter based on information from a sample.
- (B) population parameter based on information from a population.
- (C) sample statistic based on the information from a sample.
- (D) sample statistic based on the information from a population.
- (E) sample parameter based on the information from a population statistic.



- (b) When constructing a 95% confidence interval of the average yearly salary difference between females and males at a specific company (average female salary minus average male salary), our calculator gives us the interval (-18240, -1115). This can be interpreted as $\frac{1}{2} 4 \times 9$. Here $\frac{1}{2} 4 \times 9$. Here $\frac{1}{2} 4 \times 9$. Here $\frac{1}{2} 4 \times 9$. The salary $\frac{1}{2} 4 \times 9$.
 - (A) we are 95% confident that the females make between \$1,115 and \$18,240 more than males per year at this company.
 - (B) we are 95% confident that the females make between \$1,115 and \$18,240 less than males per year at this company.
 - (C) we are 95% confident that the females make between -\$1,115 and -\$18,240 per year at this company.
 - (D) we are 95% confident that the males make between \$1,115 and \$18,240 per year at this company.
 - (E) we are 95% confident that the males make between \$1,115 and \$18,240 per year at this company.

Problem 4: 10 pts (2 pts each)

Match the test with the scenario:

Write the letter of the hypothesis test or confidence interval from the list on the right that would be used for the situation on the left.

Cole wants to test if there is a difference in moisture content among turkeys that have been baked in the oven wo mompared to those that have been deep fried. He takes two in-+17 dependent samples and measures their moisture level.

(A) Test about p

(B) Test about $p_1 - p_2$

Nadine wants to estimate the average speed difference of cars on Highway 1 (between Santa Cruz and San Fransisco) and Highway 17. She selects two simple random, independent samples and measures their speeds.

(C) Test about μ

(D) Test about μ_d

(E) Test about $\mu_1 - \mu_2$

Irene wants to test if the percentage of students that different own a smartphone is different than the percentage of faculty that own a smartphone at Pasadena City College.

(F) Confidence Interval about p

(G) Confidence Interval about $p_1 - p_2$

Ethan wants to test if the average height of female wengen wolleyball players in the U.S. is more than 78 inches.

(H) Confidence Interval about μ

Jesus wants to estimate the percentage of statistics proportion students at Pasadena City College who took Math 150.

(I) Confidence Interval about $\mu_1 - \mu_2$

(J) Confidence Interval about μ_d

Problem 5: 20 pts

a proportion of heads is P = 0.5

Students conducted an experiment to determine whether the Belgium-minted Euro coin was equally likely to land heads up or tails up. Coins were spun on a smooth surface, and in 310 spins, 170 landed with the heads side up. -> sample properties of

Should the students interpret this result as convincing evidence that the proportion of the time the coin would land heads up is not 0.5? Test the relevant hypotheses using a significance level of $\alpha = 0.01$. Round final answers to three decimal places where appropriate

(3 pt) (a) Are the **requirements** met for the hypothesis test? Why or why not?

One propertion HT:

() SR& (2) "bi" binomial i) fixed trials in) "bi" two outcomes (3) NPo > 5 & nqo > 5 conditions in) independent in) probability of success 310·(0.5) = 155 310(0.5)=155

(2 pt) (b) State the **null** and **alternative hypotheses**:

fest statistic

(1 pt) (c) State the **level of significance**:

(3 pt) (d) Find the test statistic (show work!):

 $Z^{4} = \frac{\hat{p} - P_{0}}{\sqrt{\frac{p_{0}q_{0}}{h}}} = \frac{(0.548387..-0.5)}{\sqrt{(0.5)\cdot(0.5)}} = 1.70388... \quad Z^{4} = 1.70$

 $\hat{p} = \frac{170}{310} = 0.548387... \quad p_0 = 0.5 \quad q_0 = 1.0.5 = 0.5 \quad N = 310$

(4 pt) (e) Use the Critical Value Method to find the critical value:

Label the critical value and the shade the critical region in the distribution provided. Also, label the test statistic in your graph.

Critical Valve

Za/2 = inv Nom (0.005, 0,1, RIGHT) = 2.575829... | Za/2 = 2.576

a=0.01

a/2 = 0.005

(2 pt) (f) Make a decision (explain why):

2* is ortside the critical region - Fail to Rijed to

(5 pt) (g) $(M \to E)$ State your **conclusion**:

"There is not enough statistical evidence to support the claim that the twe proportion of the time teer Belgium-minted Euro coin is not 0.5 "

Problem 6: 20 pts

A researcher wanted to estimate the effect a new drug would have on systolic blood pressure. The following table gives the systolic blood pressure (in $\overline{mm Hg}$) of seven adults before taking this drug, and after having taken this drug for 2 months.

Montchal

κ_{l}	
Az	
$d=x_1-x_1$	Г

	1	2	3	Y	5	6	7
Before	210	180	195	220	231	199	224
After	195	178	186	223	218	195	224
difference	15	2	9	-3	13	4	٥

i d = 5.7143 (kep one more dist than

We will assume that the population of paired differences is normally distributed.

Construct a 90% confidence interval for the difference in systolic blood pressure before and after taking this drug. Round final answers to three decimal places where appropriate

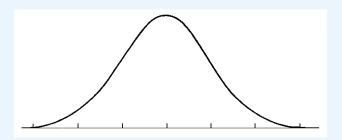
(4 pt) (a) Identify the **point estimate**:

(4 pt) (b) Determine the **critical value**:

$$C = 6.9$$
 $X = 1-CL = 0.1$

$$2L = 0.9$$

 $x = 1-CL = 0.1$ $t_{x/z} = inv T(1-0.05, 6)$
 $t_{x/z} = 0.05$ $t_{x/z} = 1.94$



(3 pt) (c) Find the margin of error:

$$E = t_{\alpha/2} \cdot \frac{s_d}{\sqrt{n}} = \frac{1.94 * 6.7753}{\sqrt{7}} = 4.9679...$$

E=4.968 mm Hg/person

(4 pt) (d) Contsruct the confidence interval:

CI: (d-E, d+E) ~ (0.746 mm Hg/person, 10.682 mm Hg/person)

1 tE= 5.714 t 4.961

(5 pt) (e) $(M \to E)$ Interpretation of CI:

" We are 90% confident that the two difference in systolic bood pressure before & after taking this drug is between 0.746 mm Hy and 10.682 nn Hg.

M. Mar

Problem 7: 20 pts

A Fair Isaac Corporation (FICO) score is used by credit agencies (such as mortgage companies and banks) to assess the creditworthiness of individuals. Values range from 300 to 850, with a FICO score over 700 considered to be a quality credit risk. According to Fair Isaac Corporation, the mean FICO score is 703. — Mo

A credit analyst wondered whether high-income individuals (incomes in excess of \$100,000 per year) had higher credit scores. He obtained a random sample of 40 high-income individuals and found the sample mean credit score to be 735 with a standard deviation of

Test the claim that high-income individuals have higher FICO scores. Round final answers to three decimal places where appropriate

(3 pt) (a) Are the **requirements** met for the hypothesis test? Why or why not?

HT: One Mean

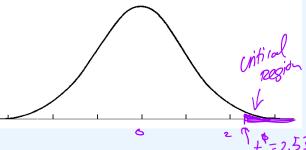
$$OSRS \qquad (2) normal or \frac{n=40}{n>30}$$

Treat as one mean since arn't given two sample sizes

(2 pt) (b) State the **null** and **alternative hypotheses**:

$$\begin{cases} H_0: & \mu = 703 \quad (m_0 = 702) \\ H_A: & \mu > 703 \quad (Right Tailed Test) \end{cases}$$

(1 pt) (c) State the level of significance:
$$(1 \text{ pt}) = (1 \text{ pt}) =$$



(3 pt) (d) Find the test statistic (show work):

$$t^{*} = \frac{\bar{x} - M_{o}}{\frac{s}{\sqrt{N}}} = \frac{(735 - 703)}{(\frac{80}{\sqrt{90}})} = 2.529 g2...$$
 $t^{*} = 2.53$

n=40 $\bar{x}=735$ $M_0=703$ S=80

(4 pt) (e) Use the *P*-Value Method to find the *P*-value:

Label and shade the critical region in the distribution provided.

$$P(t>a.53) = 0.5 - P(0 < t < a.53)$$

$$= 0.5 - t < cdf(0, a.53, 39)$$

$$= 0.00778$$

(2 pt) (f) Make a **decision** (explain why):

(5 pt) (g) $(M \to E)$ State your **conclusion**:

"There is enough statistical evidence to support claim that high income individuals have higher FICO scores

Post Exam Survey

Now that you have finished the exam, please take a few minutes to reflect on how you prepared for the exam and how you think you did. Then answer these questions.

	When taking the exam I felt (a) Rushed. I wanted more time. (b) Relaxed. I had enough time. (c) Amazed. I had tons of extra time.		
	The week before the test I did all my homework on time: YES NO		
3.	The week before the test, in addition to the homework I followed a study plan. YES NO (a) I think this helped: YES NO		
4.	The day before the test I spend hours studying and reviewing. (a) I think that was enough time: YES NO		
5.	 (a) I stayed up very late cramming for the test (b) I stayed up very late, but I wasn't doing math (c) I didn't need to cram because I was prepared (d) I got a good night's sleep so my brain would function well. 		
6.	I think I got the following grade on this test:		
7.	Strategies that worked well for me were (please elaborate):		
8.	Next time I will do an even better job preparing for the test by:		