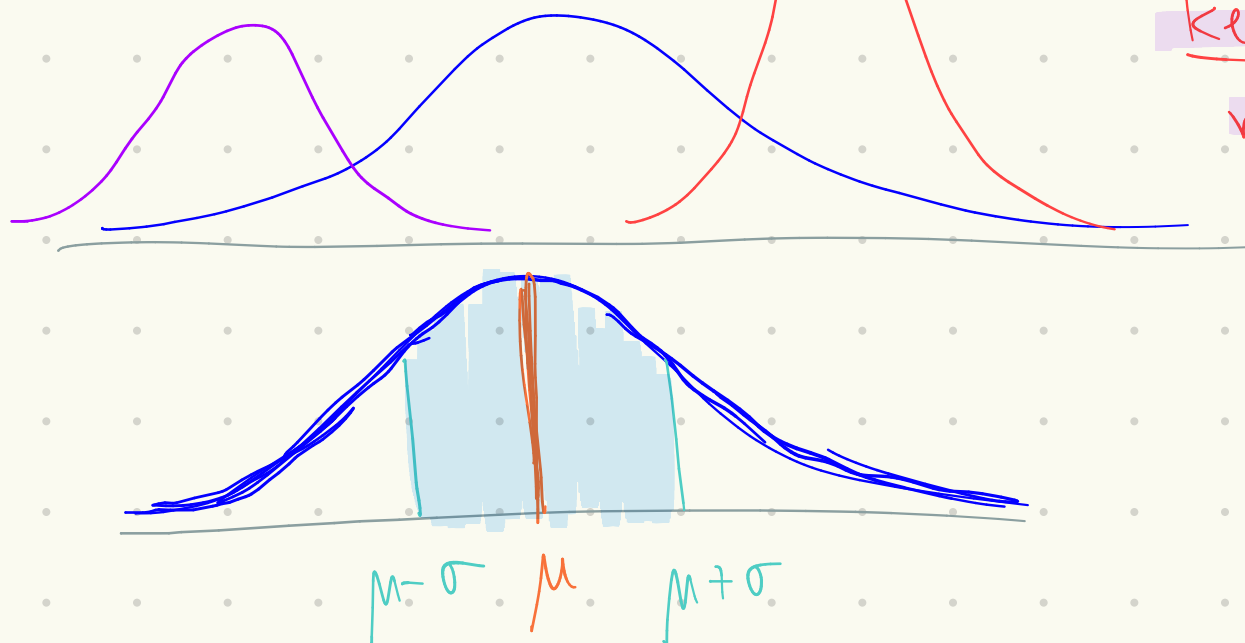


# Chapter 7 Review

Let  $X$  a continuous random variable (RV).

$X$  is normally distributed if the distribution looks like a bell-curve



key lots of normal curves depend on mean  $\mu$  & standard deviation  $\sigma$

Key Properties ① bell-shaped / symmetric

\* ② AREA = PROBABILITY

③ Mean = median = mode

Notation

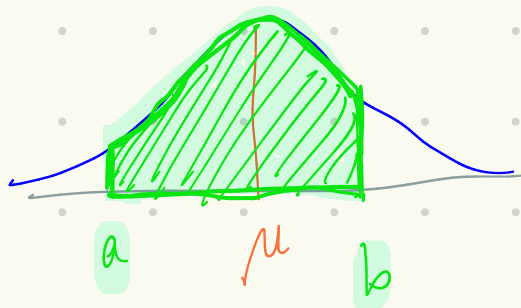
CALC 2<sup>nd</sup> + VARS  $\rightarrow$  #2. normalcdf\*

EE  
↓  
-  $\infty$  = -1E99  
+  $\infty$  = 1E99

$$P(a < x < b) = \text{normalcdf}(\overset{\text{low}}{a}, \overset{\text{high}}{b}, \overset{0}{\mu}, \overset{1}{\sigma})$$

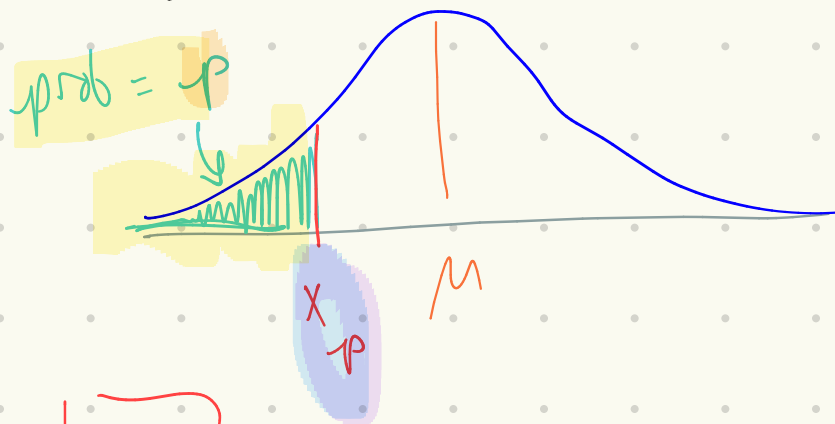
= probability of selecting ONE person/item from  $X$  having values between  $a$  and  $b$ .

= proportion of people/items from  $X$  that have values between  $a$  and  $b$ .



# Inverse Normal

Given a probability, we want to know the value of  $x$  or  $z$ .



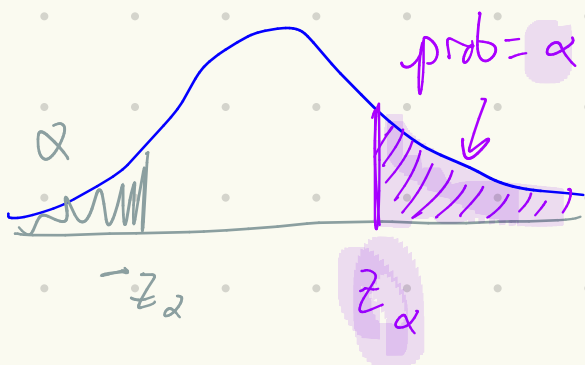
Given  $p$ ,  $x_p$  = value on  $x$ -axis that separates probability  $p$  on the left tail

$$x_p = \text{inv Norm} (p, \mu, \sigma, \text{TAIL})$$

Note older TI's don't have tail  $\rightarrow$  use LEFT

ASSUMING STANDARD NORMAL ( $\mu=0, \sigma=1$ )

Critical Value  $z_\alpha$  = z-score that separates probability  $\alpha$  on the RIGHT Tail



$$z_\alpha = \text{inv Norm} (\alpha, 0, 1, \text{RIGHT})$$

= older

$$\text{inv Norm} (1-\alpha, 0, 1)$$



$z$ -dist = standard normal dist  
 $\mu=0$  &  $\sigma=1$

# Ch 8 Review

## Sampling Distributions:

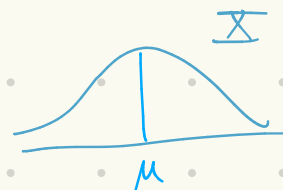
the distribution of ALL samples of size  $n$  of a RV  $X$

### Sampling Dist of MEAN

Given a RV  $X$  w/

(1) mean  $\mu$  & st. dev.  $\sigma$

(2) SRS & indep sample size  $n$



EX Height of all GCC students

• Sampling dist?

↳ distribution of all samples of 100 GCC students heights

### Conclusions

(1) distribution of all sample means  $\bar{x}$

are (approx.) normally dist

as  $n$  increases

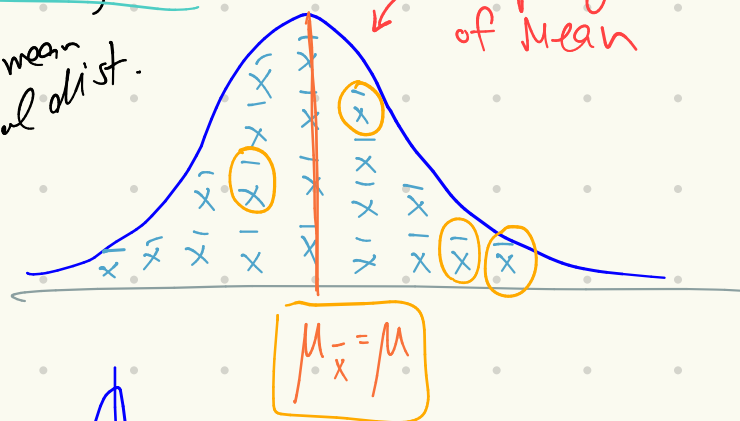
(CLT)

(2)

$$\mu_{\bar{x}} = \mu$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

population mean for original dist.



### How to use

Step 0 Are you selecting  $n$  people/items w/  $n > 1$ ?

Step 1 Is  $X$  normally dist or  $n > 30$ ?

Step 2 Find  $\mu_{\bar{x}}$  &  $\sigma_{\bar{x}}$

Step 3 Use normal cdf w/  $\mu_{\bar{x}}$  &  $\sigma_{\bar{x}}$ .

# Sampling Dist of Proportion

Given a RV  $\underline{X}$  that has

- ① population proportion  $p$ .
- ② SRS & indep. sample size  $n$

Poll Do you like  
online learning?

GCC pop  $p$   
samples of size 100  
 $\hat{p} = \frac{\# \text{yes}}{100}$

## Conclusions

(CLT)

- ① shape of distribution of all samples  $\hat{p}$  are (approx-) normally distributed as  $n$  increases

provided that  $n \cdot \hat{p} \cdot \hat{q} \geq 10$

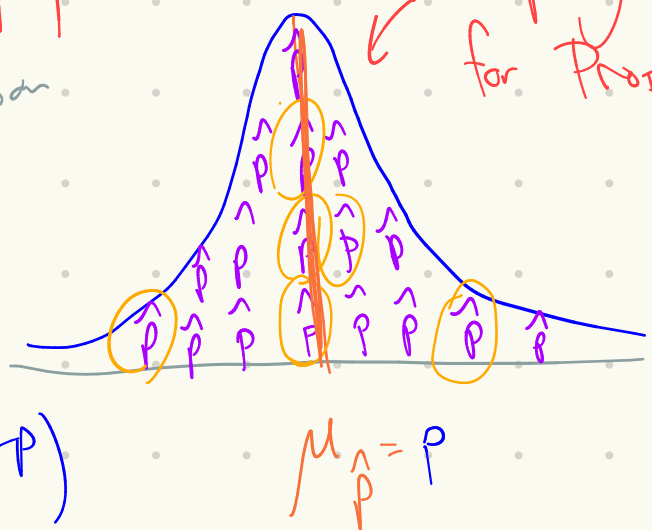
②

$$\mu_{\hat{p}} = p$$

$$\sigma_{\hat{p}} = \sqrt{\frac{pq}{n}}$$

pop. proportion

( $q=1-p$ )



## How to use

Step 0 Are you selecting  $n$  people/items w/  $n > 1$ ?

Step 1 Is  $\underline{X}$  normally dist

$n > 30$  &  $n \cdot \hat{p} \cdot \hat{q} \geq 10$

Step 2 Find  $\mu_{\underline{X}}$  &  $\sigma_{\underline{X}}$

Step 3 Use normal cdf w/  $\mu_{\hat{p}}$  &  $\sigma_{\hat{p}}$ .