Optimization - Minitest 3

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Question 1

$$\mathbb{E}_{\xi_k} \left[F(w_{k+1}) \right] - F(w_k) \le \alpha_k \left(\mu - \frac{1}{2} \alpha_k L M_G \right) \|\nabla F(w_k)\|^2 + \frac{1}{2} \alpha_k^2 L M \qquad (1)$$

What does equation (1) imply? If α_k is small enough, $\mathbb{E}[F(w_{k+1})] \leq F(w_k)$, so we can hope that the gradient method leads to the minimum of F.

Question 2

What is the role of each of the components $(\alpha_k, L, M, ...)$?