Concepts of programming languages Janus

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```
procedure fib
  if n = 0 then
     x1 += 1    ; -- 1st Fib nr is 1.
     x2 += 1    ; -- 2nd Fib nr is 1.
  else
     n -= 1
     call fib
     x1 += x2
     x1 <=> x2
  fi x1 = x2    ; -- Why do we need this?
```

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       x1 <=> x2
   fi x1 = x2; -- To be able to invert the procedure.
```

- Q: How do we calculate the inverse?
- A: Using the statement inverter.

```
\mathcal{I} \llbracket 	ext{if } e_1 	ext{ then } s_1 	ext{ else } s_2 	ext{ fi } e_2 
Vert = 	ext{if } e_2 	ext{ then } \mathcal{I} \llbracket s_1 
Vert 	ext{ else } \mathcal{I} \llbracket s_2 
Vert 	ext{ fi }
```

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The inverse of fib calculates n given the (n+1)-th and (n+2)-th Fibonacci numbers

```
procedure fib'          ; -- The inverse of fib.
    if x1 = x2 then
          x2 -= 1          ; -- 2nd Fib nr is 1.
          x1 -= 1          ; -- 1st Fib nr is 1.
    else
          x1 <=> x2
          x1 -= x2
          call fib'
          n += 1
    fi n = 0
```

Example 2: Probability Density Function of Exp distribution.

- ▶ PDF of exp: $\frac{1}{b}e^{\frac{-x}{b}}$
- ▶ But Janus doesn't allow negative integers, so:
- ▶ PDF of exp: $\frac{1}{b} \frac{1}{e^{\frac{x}{b}}}$
- ▶ Let's also introduce a parameter $\lambda = \frac{1}{b}$:
- ▶ PDF of exp: $\lambda \frac{1}{e^{x\lambda}}$
- ▶ PDF of exp: $\frac{\breve{\lambda}}{e^{x\lambda}}$
- ▶ This is still most probably going to be a real number...
- ► Solution: multiply everything times a very large constant

Relational Programming

Injective Programming

r-Turing Complete backwards deterministic restricted language constructs

Relational Programming

Turing Complete backwards non-deterministic search procedure (aka *resolution*)

Prolog basics

A logic programs consists of facts and rules.

```
parent(alice, joe).
parent(bob, joe).
parent(joe, mary).
parent(gloria, mary).
ancestor(X, Y) :- parent(X, Y).
ancestor(X, Y) :- parent(X, Z), ancestor(Z, Y).
descendant(X, Y) :- ancestor(Y, X).
```

The user can then *query* the runtime system, as such:

```
?- parent(X, joe).
X = alice;
X = bob.
?- ancestor(X, mary).
X = joe;
X = gloria;
X = alice;
X = bob.
?- ancestor(X, mary), descendant(X, alice).
X = joe.
```

Demonstration - Type Inference

Assume a type predicate, relating expressions with types:

```
type(expr, t) :- ... .
```

You would normally use it to perform type-checking:

```
?- type(1 + 1, int).
true.
?- type(1 + 1, string).
false.
```

But you can also performing type-inference:

```
?- type(1 + 1, Type).
Type = int.
?- type("hello world", Type).
Type = string.
?- type(\x:int -> x, Type).
Type = int -> int.
?- type(\x -> x, Type).
Type = ?42 -> ?42.
?- type(\x -> x, int -> Type).
Type = int.
```

Going in the reverse direction, you can query the expression:

```
?- type(Expr, int).
Expr = 1;
Expr = 2;
...
Expr = 1 + 1;
Expr = 1 + 2;
...
Expr = if true then 1 else 1;
...
```

Of course, this does not make much sense without a sufficiently expressive type system.

Demonstration - Program Synthesis

Assume you have implemented a relational interpreter:

```
eval(program, result) :- ... .

?- eval(map (+ 1) [1 2 3], Result).

Result = [2 3 4].
```

But you can also perform *program synthesis* by-example:

```
?- eval(F 1, 2),...,eval(map F [1 2 3], [2 3 4]).
...
F = \x -> x + 1;
...
F = \x -> x - 10 + 10 + 1;
```

Quine generation is pretty straightforward:

```
?- eval(Quine, Quine).
...
Quine = (\a -> a ++ show a) "(\\a -> a ++ show a) ";
...
```

Logic Programming IRL

In practice, bi-directionality breaks with the usage of *extra-logical* features:

- Variable projection: inspecting values at runtime
- ► Cut (!): disables backtracking in certain places
- ► **Assert/Retract**: Dynamically insert/remove facts

MiniKanren is a more recent logic programming language, which avoids extra-logical features (as much as possible).

Higher abstraction

- ► Relational programming, as well as functional programming, both belong to the *declarative* paradigm.
- ► They both raise the level of abstraction, by enabling the programmer to express what needs to be done, instead of how.

Question

How can we combine them, to get the best of both worlds?

Hanus: Janus embedded in Haskell

In our research project, we use *TemplateHaskell* and *QuasiQuotation* to embed Janus in Haskell:

```
[hanus|
  procedure encode(im :: Image, ret :: [Byte]) {
    -- Janus commands containing Haskell code
    -- e.g. janus_variable += <Haskell code>
  }

|]
encode :: Image -> [Byte]
encode = call encode
decode :: [Byte] -> Image
decode = uncall encode
```

Come and check out our poster in de Vagant!



Thanks!

Feel free to ask any questions

