Thesis Title

A subtitle of your thesis

Author name



Thesis submitted for the degree of Master in Master's Program Name <change at main.tex>
60 credits

Department Name <change at main.tex> Faculty name <change in duoforside.tex>

UNIVERSITY OF OSLO

Spring 2022

Thesis Title

A subtitle of your thesis

Author name

© 2022 Author name

Thesis Title

http://www.duo.uio.no/

Printed: Reprosentralen, University of Oslo

Abstract

Contents

1	Intr	oduction	1
I	The	eory	3
2	Hig	h-Entropy alloys	4
	2.1	Fundamentals	4
	2.2	Core effects and properties	7
3	Mod	deling of random alloys	9
	3.1	The Special Quasi-random Structure model	9
		3.1.1 Mathematical description	10
		3.1.2 Applications to high-entropy alloys	12
4	Den	sity Functional Theory	16
	4.1	Review of Quantum Mechanics	17
		4.1.1 The Shrodinger equation	17
		4.1.2 Approximations to the many-body Shrodinger equa-	
		tion	18
	4.2	Kohn-Sham density functional theory	20
		4.2.1 Density functional theory	20
		4.2.2 The Kohn-Sham Equation	21
	4.3	Limitations of DFT - Insert refs	22
II	Me	ethodology and Implementation	24
5	Prac	tical application of DFT	25
	5.1	The Exchange-Correlation functional	25
		5.1.1 Local density approximation	25
		5.1.2 Generalized gradient approximation	26
		5.1.3 Meta-GGA	26
		5.1.4 Hybrid functionals	27
		5.1.5 Outlook	27
	5.2	Fundamental aspects of practical DFT calculations	28
	5.3	Self-consistent field calculation	30

6	Con	putational details	32
	6.1	Vienna Ab initio Simulation Package	32
	6.2	Generation of SQS	34
	6.3	Utility scripts	35
III	Re	esults and Discussion	37
2	The	results of eqvimolar (CrFeMnNi)Si ₂ in the β -FeSi ₂ structure	7
	2.1	The band gap	9
	2.2	Local and projected density of states	12
	2.3	Results from SCAN and HSE06 functionals	14
	2.4	Pair distribution functions	20
	2.5	SQS size	22
3	Perr	nutations of (CrFeMnNi)Si ₂	26
4	Diff	erent compositions and crystal structure	31
	4.1	New compositions	31
	4.2	Crystal structures	34
10		rview and outlook	65
		Literature	65
		General thoughts	66
		Other things	70
		$Cr_4Fe_4Mn_4Ni_4Si_{32}$ in different crystal structures	73
	10.5	Overview	7 5
IV	C	onclusion	76
Α	Con	positions	73
		Projected density of states	73
		Probability distribution functions	76
В		imolar alloy DOS	78
C	Cha	rge density	80

List of Figures

2.1	Formation of HEA based on δ and N . Figures adopted from [hea2016_ch2]	6
2.2	A schematic illustration of lattice distortion in high-entropy alloys. Figure from [owen_jones_2018]	8
3.1	PDFs of (a) 20 and (b) 250 atom SQS models of CrFeMnNi [hea2016_ch10]	13
3.2	Density of states with SQS and MC/MD of FCC CoCrFeNi, figure from [hea2016_ch10]	14
3.3	Probability distribution functions with SQS and MC/MD of HCP CoOsReRu [hea2016_ch10]	14
4.1	Number of DFT studies per year from 1980 to 2021 [dimensions]	16
5.1	Calculated to experimental band gap measurements of Becke-Johnsoon, modified Becke-Johnson and SCAN func-	
5.2	tionals [xc_benchmark]	27
	from lecture notes fys-mena4111 cite	31
6.1	48 atom SQS based on eqvimolar distribution of Cr, Fe, Mn and Ni in and $FeSi_2$ cell	36
2.1	Density of states of SQS D (CrFeMnNi)Si ₂ with PBE	9
2.22.3	Density of states of SQS B (CrFeMnNi)Si ₂ with PBE	9 12
2.3	Local density of states of Si (SQS D)	12
2.4	Projected density of states SQS D CFMN (fesi2) from PBE	
2.6	calculation	13
2.6 2.7	Projected density of states of SQS D and B around E_F Density of states illustrating the band gaps from PBE and	13
	SCAN calculations for SQS E and D	15
2.8	Density of states of SQS B with HSE06	16
2.9	Something	16
2.10	Probability distribution function of SQS D (top) and B (bottom)	20
2.11	CPU time, Make log plot instead	22
2.12	Density of states of SQS E 192 atom SQS	24

2.13	(middle) 96 atoms, (bottom) 192 atoms	25
3.1	Projected density of states of (a) Cr ₃ Fe ₃ Mn ₇ Ni ₃ Si ₃₂ (SQS B), (b) Cr ₅ Fe ₅ Mn ₃ Ni ₃ Si ₃₂ (SQS C), (c) Cr ₅ Fe ₃ Mn ₅ Ni ₃ Si ₃₂ (SQS A), (d) Cr ₃ Fe ₅ Mn ₅ Ni ₃ Si ₃₂ (SQS D)	29
3.2	Projected density of states of $Cr_3Fe_3Mn_3Ni_7Si_{32}$ around E_F .	30
A.3 A.4 A.5 A.6	chCo4Fe4Mn4Ni4Si32	73 74 74 75 75 76
B.1 B.2	Density of states SQS A (CrFeMnNi)Si ₂ with PBE Density of states SQS E (CrFeMnNi)Si ₂ with PBE	78 79

List of Tables

2.1	Total energy per atom, final magnetic moment and band gap of 5 unique SQS of (CrFeMnNi)Si ₂ based on the β – FeSi ₂ unit	
	cell	8
2.2	Band gap of the 5 SQSs of (CrFeMnNi)Si ₂ calculated from the	
	eigenvalues in spin up, down and total	10
2.3	Band gap of SQS D as a function of occupancy in the eigenvalues	11
2.4	Band gap calculated with PBE, SCAN and HSE06 XC-functionals of (CrFeMnNi)Si ₂ SQSs	14
2.5	Minimum gap between k-point in valence band and conduction band in SQS B from PBE, SCAN and HSE06	17
2.6	Band gap from HSE06 calculations with gaussian smearing and smearing width <i>sigma</i> equal to 0.05 and 0.005, and the tetrahedron method (TBC). "-" mean unchanged values,	1,
	"ND" means not done	18
2.7	Overivew 48, 96 and 192 SQSs	22
2.8	Band gap of SQSs of 48, 96 and 192 atoms each of (CrFeMnNi)Si ₂ . The names are arbitrary, ie A in 48 does not equal A in 96 or 192	23
3.1 3.2	Summary composition diagram	26
	from the table due to unsuccessful calculations	28
4.1 4.2	Overview new compositions	31
4.4	composition	32
4.3	Band gaps of the most stable SQS of β – FeSi ₂ high-entropy silicide compositions as a function of occupancy in the eigenvalues	33
	eigenvalues	55
10.1	Mean and stadard deviation of the total energy and magnetic moment per atom, plus enthalpy of formation of the listed mean energies (FeSi ₂)	68

10.2	Total and spin dependent band gap of 4 permutations of	
	CFMN (fesi2) with PBE GGA calculation. The structures that	
	are excluded from this list either failed in calculations, or	
	does not show any band gap.<	70

Preface

Chapter 1

Introduction

some introduction on the importance of discovering new materials and alloying.

Need something on thermoelectricity related to both the band gap and high-entropy alloys.

High-entropy alloys is a novel class of materials based on alloying multiple components, as opposed to the more traditional binary alloys. This results in an unprecedented opportunity for discovery of new materials with a superior degree of tuning for specific properties and applications. Recent research on high-entropy alloys have resulted in materials with exceedingly strong mechanical properties such as strength, corrosion and temperature resistance, etc **find references**. Meanwhile, the functional properties of high-entropy alloys is vastly unexplored. In this study, we attempt to broaden the knowledge of this field, the precise formulation of this thesis would be an exploration on the possibilities of semiconducting high-entropy alloys.

A key motivation of this thesis is the ability to perform such a broad study of complex materials in light of the advances in material informatics and computational methods. In this project, we will employ Ab initio methods backed by density functional theory on top-of the line supercomputers and software. 20 years ago, at the breaking point of these methods, this study would have been significantly narrower and less detailed firstly, but secondly would have totaled ... amount of CPU hours to complete (Calculate this number). In the addition to the development in computational power, is also the progress of modeling materials, specifically we will apply a method called Special Quasi-random Structures (SQS) to model high-entropy alloys or generally computationally complex structures. Together with the open landscape of high-entropy alloys described above, these factors produce a relevant study in the direction of applying modern computational methods to progress the research of a novel material class and point to promising directions for future research.

In specifics, this thesis revolve around the electrical properties of highentropy alloys, mainly the band gap as this is the key indicator for a semiconducting material and it's applicability. Semiconductors are the building blocks in many different applications in today's world, ranging from optical and electrical devices, to renewable energy sources such as solar and thermoelectricity. Given the economic and sustainable factors concerning silicon, in addition to its role in relevant applications such as microelectronics and solar power. Silicon emerges as a natural selection to build our alloys around. Furthermore, the development and research on both high entropy alloys and metal silicides have been heavily centered around 3d transition metals. Keeping in line with the economic and environmental factors, we will continue this direction by focusing on high entropy stabilized sustainable and economic 3d metal silicides **Not happy with this writing**. Throughout the study we will analyze a great number of permutations of 3d silicides, from different initial metal silicides such as $CrSi_2$, $FeSi_2$, $MnSi_{1.75}$, Fe_2Si , each with distinct properties relating to the band gap, crystal structure and metal to silicon ratio. In addition, the permutations include numerous metal distributions and elements within the 3d-group of metals. Examples are Co, Cr, Fe, Mn, and Ni.

Given a background in high-entropy alloys, one could ask if this study is truly sensible. In the later sections we will cover the details of this field, and it quickly become clear that the materials investigated in this study does not fall under the precise definition of high-entropy alloys, nor do we intend to explore the properties and factors relating to high-entropy stabilized alloys such as the configurational entropy, phase stability and finite temperature studies. However this study is motivated from the discovery of these materials and promising properties, and venture into a more hypothetical space of materials, enabled by the computational methods available to study the potential properties of such materials. On the other hand, very recent studies **Mari, and other HEA silicide study** have experimentally synthesized high-entropy disilicides, thus in some way justifying the direction of this project.

We begin this project by reviewing key concepts of solid-state physics for readers lacking a background in materials science, and an introduction to the base 3d silicides of the experimental work. Later follows a theoretic walk-through of the relevant concepts of this thesis, these topics include high-entropy alloys, special quasi-random structures, and density functional theory. Next we shine light on the implementation of DFT in this project, and other computational details required to reproduce the results in this thesis, such as the use of the Vienna Ab Initio Simulation Package (VASP) and implementation of SQS. Finally we present the results of our study, these include the band gap and electronic properties of various structures and the success and challenges of the computational methods applied throughout the study.

Part I Theory

Part II Methodology and Implementation

Part III Results and Discussion

Chapter 4

Different compositions and crystal structure

4.1 New compositions

In similar fashion to the previous sections, we here begin by presenting the mean and standard deviation of the total energy and magnetization of a set of SQSs corresponding to different high-entropy silicides of the Fesi₂ unit cell. The compositions we have tested are deliberate combinations intended to investigate both the impact of manganese by replacing the element with Co or Ti, and concepts related to HEA theory such as the atomic size effect. Furthermore Co is a very common element in many stable HEA, as seen in section 2.2, thus we include 3 compositions with Co to study the impact on stability and the functional properties. The results of the aforementioned alloys can be seen bellow in table 9.1, note that all compounds contain a total of 48 atoms as before.

Composition	Toten (eV)		Mag (μ_B)		ΔH (eV)
	mean	std	mean	std	mean
Cr ₄ Fe ₄ Co ₄ Ni ₄ Si ₃₂	- 6.4655	0.0056	0.0083	0.0155	- 12.7536
Co ₄ Fe ₄ Mn ₄ Ni ₄ Si ₃₂	- 6.4731	0.0046	0.0000	0.0000	- 15.0836
Cr ₄ Fe ₄ Ti ₄ Ni ₄ Si ₃₂	- 6.4217	0.0087	0.0305	0.0293	- 7.5040
Cr ₄ Fe ₄ Mn ₄ Ti ₄ Si ₃₂	-6.6994	0.0071	0.1142	0.0641	- 7.3060
$Cr_4Fe_4Mn_4Co_4Si_{32}$	-6.7687	0.0034	0.1331	0.0326	- 13.7796

Table 4.1: Overview new compositions

From table 9.1 we see that the stability of the relative compositions vary greatly. By introducing cobalt to the alloys, particularly at the cost of manganese result in a large positive effect on the stability, contrary replacing either manganese or nickel with titanium significantly lowers the stability. **Wait for new formation enthalpies.** In table 9.1 we have listed the mean magnetic moment of the compositions, in line with previous results

in this project the magnetization is very dependent on chromium and manganese. This is seen by the overall lowest magnetic moments in the two compositions without these elements, and reversely the highest magnetic moments is found for compositions with both Cr and Mn. Comparing the magnetic moment of (CrFeCoNi)Si2 and (CoFeMnNi)Si2 it seems in our study that chromium is most responsible for the magnetic moment in these alloys. Furthermore we find that substituting Ni with both Ti and Co result in more magnetic compounds. These are truly surprising results, one would expect that the magnetic moments would be larger in the ferromagnetic elements Ni, Fe and Co than Cr, Mn and ti. This could go back to our simplistic and superficial study of the magnetic properties in this project, additionly the PBE functional as we covered in section .. have shown limitations for 3d elements and particularly Ni. Thus this could be a factor affecting our results. Another factor is that we here based our comparison on the mean values between 5 SQSs. As we have experienced throughout this project the unieqeness of the SQSs can be troublesome to handle, and our best guess is to study the most stable super-cell. Bellow in table 9.2 we list the magnetic moments of the most stable SQSs. Here we find several dissimilarities to the mean value such as the Cr₄Fe₄Co₄Ni₄Si₃₂ being nonmagnetic in the most stable supercell. Thus based on the utmost stable configurations we can state that replacing either Cr or Mn (with Co) removes the magnetic moment in the alloy. Furthermore we find from these supercells that the magnetic moment is reduced by replacing Ni with Ti, and increased from Co. These results are in much better accordance with previous knowledge of ferromagnetic elements and their interplay in highentropy alloys.

Composition	Magnetic moment (μ_B)
Cr ₄ Fe ₄ Co ₄ Ni ₄ Si ₃₂	0
Co ₄ Fe ₄ Mn ₄ Ni ₄ Si ₃₂	0
Cr ₄ Fe ₄ Ti ₄ Ni ₄ Si ₃₂	0,0653
$Cr_4Fe_4Mn_4Ti_4Si_{32}$	0,0785
$Cr_4Fe_4Mn_4Co_4Si_{32}$	0,1666

Table 4.2: Final magnetic moment of the most stable supercell of each composition.

In regards to the band gap of the compositions, we can report that a heavy majority are metals. We found no evidence of a band gap in both the CrFeCoNiSi2 and CrFeMnTiSi2 alloys across all supercells, as seen in the density of states in figure 9.1. Further also the most stable SQSs of the CrFeTiNiSi alloy point to a metal. Similarly the most stable SQSs of the CoFeMnNiSi2 alloy are clearly metals. Noteworthy of this composition however is that we find clear evidence of a narrow band gap in two SQSs (A and B). In terms of stability, these lie around the mean total energy of the set. The respective band gaps are 0.033 eV in A and 0.0058 eV in B.

Composition	осс	E _G ^{up, eigen} (eV)	E ^{dw, eigen} (eV)	E _G ^{tot, eigen} (eV)
	0.5	0	0	0
CrFeCoNiSi ₂	0.1	0.00095	0.0399	0.00095
	0.01	0.063	0.063	0.063
	0.5	0.0067	0	0
CrFeTiNiSi ₂	0.1	0.061	0.0087	0.0087
	0.01	0.061	0.037	0.037
	0.5	0	0	0
CoFeMnNiSi ₂	0.1	0.0037	0.0037	0.0037
	0.01	0.0268	0.0268	0.0268
	0.5	0	0	0
CrFeMnTiSi ₂	0.1	0.021	0.00049	0
	0.01	0.03	0.03	0.022
	0.5	0.461	0	0
CrFeMnCoSi ₂	0.1	0.607	0.0218	0.0218
	0.01	0.607	0.0245	0.0245

Table 4.3: Band gaps of the most stable SQS of β – FeSi₂ high-entropy silicide compositions as a function of occupancy in the eigenvalues.

skiiiiiaaaat! To follow is details on the gaps in A and B, is it worth to include this? In the density of states plotted in figure .., the band gap in A is clearly visible. On the other hand the very narrow gap in B is not as apparent, as the states around Ef contain very small nonzero values. This could be related to the low resolution of 2500 points in the density of states as seen before, especially considering the size of the gap. In opposite to the CFMN calculations previous we here experience excellent cohesion between PBE and SCAN simulations on the band gap. With the meta-GGA functional the band gap of SQS A and B respective is 0.04 eV and the 0.003 eV. Moreover we find the identical gap transition with both functionals, which was not the case in previous endeavors with this functional. Additionally we also find that the HSE06 functional produce dissimilar results to previous experiences. In this scenario, the HSE06 functional fails to recognize the observed band gap of PBE and SCAN in both supercells. The greater number of k-points in the GGA and meta-GGA calculations offer more accurate band gaps, however lesser k-points will not result in a smaller gap, only bigger. Thus the uncertainties of previous calculations of the HSE06 functional does not apply in this case. For this reason in addition to the reputation of hybrid functionals and the lack of other factors to negatively affect the validity of the result, we find it challenging to conclude on the band gap of these structures between functionals.

4.2 Crystal structures

In the discussion above we have covered in great detail the possibilites of high-entropy silicides based on the $\beta-$ FeSi $_2$ unit cell with twice as many silicon atoms to 3d elements. The primary outcome and conclsion of this research was that particularly the combination of Cr, Fe, Mn and Ni resulted in superiour properties in the light of the motivatian behind this project. The next question we wish to answer is if the promising results of the CFMN system be reproduced in other symetries. In this section we will implement the CFMN composistion in crystal structures based on hexagonal CrSi $_2$ ($P6_{42\bar{2}}$), both tetragonal and orthorombic Mn $_{16}$ Si $_{28}$ ($P\bar{4}c2and$, Pcca), and trigonal Fe $_2$ Si ($P\bar{3}m1$) where we test the CFMN system to varying metal and silicon ratioes, and crystal structures. As before, the total energy, enthalpy of formation and magnetic moment per atom can be found bellow in table ..

	Total energy per energy		Enthalpy of formation	Mag per atom	
CrSi2	-6.4837	0.0087	-8.1205	0.0887	0.0387
MnSi	-6.6658	0.0071	-9.1848	0.0687	0.0398
Fe2Si	-7.5082	0.0107	-10.2474	0.3848	0.0588

CrSi2

From our calculations with PBE DFT we find the bulk crsi2 material to be an indirect semiconductor with a band gap of 0.33 eV, slightly bellow the listed value of 0.36 eV in materials project cite, suprinsingly we find a smaller gap of 0.32 eV from the SCAN functional. The compound is also nonmagnetic in agreement with materials project. Fore the bulk material we employed a 9 atom cell, with 6 silicon and 3 cr atoms, from this we generated SQSs of 72 atoms with the same ratio. Include toten per atom for the unit cell? and figure of SQS + unit cell? For this given composistion and system we observe very similar results to that of the composistions discussed above, the eigenvalues of several SQSs report a small band gap, but its not appearant from neither the density of states or from the bandgap.py script of pymatgen. Additiontly, we can not repreoduce the gap with the SCAN functional, as was possible for the CFMN (fesi2) system.

MnSi

In the tetragonal configuration, the bulk material is a nonmagnetic indirect semiconductor with a band gap of 0.76 eV according to our PBE calculations, and 0.78 eV from SCAN. Materials project find a band gap of 0.76 eV, in good agreement with our own PBE results. The unit cell consist of 44 total atoms, 16 manganese and 28 silicon. In the orthoromibic cell, with equal number of elements we find a band gap of 0.76 eV (0.77 ev SCAN) as well. In contrast, the CFMN alloy of both these cells produce metalic compounds. It should be noted that structures B and D in the tetragonal ssystem did not fully relax, same for D in the orthorombic cell, so these results could be inaccurate.

Fe2Si

In this cell, we drasticly alter the metal-silicon ratio, this is seen both in the band gap and magnetic properties of the material. The magnetic moment of this cell consisting of 4 iron atoms and 2 silicon atoms is 0.67, from the iron atoms. This magnetic charachter can also be observed from the discrepency between the two spin channels. In spin down we find a band gap of 0.21 eV, while there is no gap in spin up. This gap can also be seen in the density of states **Include figure**. This however is an abnormal result in regard to other experimental work and littereature on the Fe2Si **cite** https: //www.sciencedirect.com/science/article/pii/S0925838816329796?casatoken =

g9DRpU9IClcAAAAA: 6Gd12A4Kh9J2igUWMVwHN8OSIKzD27VACA052FNsSAWhRY6PE Our results are subject to errors, particularly we note that the eigenvalues used to calculate the gap contain nonphysical values in the spin down channel. However, the gap is evident in the density of states thus we include the result in this report, but acknowlendge the uncertainties revolving the value.

From this unit cell we generate 54 atom SQSs. From table .. we see that the magnetic nature remains, producing the overall highest magnetic moment of all studied supercells, which is not a surprising result considering the 3d metal to silicon ratio. **More on magnetic and total energy.** The magnetism can also be seen in the difference between the two spin channels, the bands where the occupancy transistion from 1 to 0, ie occupied to not occupied is very different. In the most magnetic supercell D, we saw a distance of 22 bands between the spin down transistion and spin down transistion. Most supercells are metals from our PBE calculations. B and D show a very small gap of around 0.01 eV in one spin channel. In E we find a very narrow gap semiconductor with a total gap of 0.002 eV. This gap is surrounded by the same uncertainties as discussed previosly.

Part IV Conclusion

Write conclusion here