

Visualization, Identification, and Estimation in the Linear Panel Event-Study Design

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Performance of Different Estimators

Setup

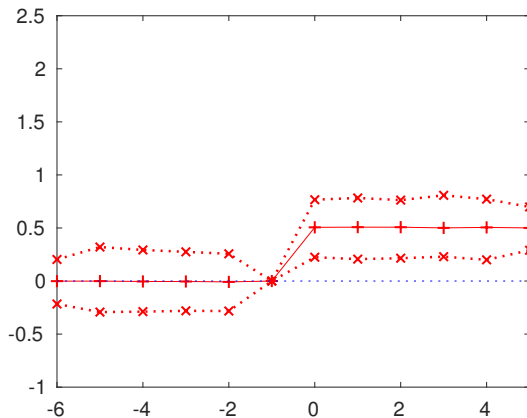
$$y_{it} = \alpha_i + \gamma_t + \mathbf{q}'_{it}\psi + \sum_{m=-G}^M \beta_m \mathbf{z}_{i,t-m} + \mathbf{C}_{it} + \varepsilon_{it} \quad (\text{linear panel model})$$

$$\begin{aligned} y_{it} = & \sum_{k=-G-L_G}^{M+L_M-1} \delta_k \Delta \mathbf{z}_{i,t-k} + \delta_{M+L_M} \mathbf{z}_{i,t-M-L_M} + \delta_{-G-L_G-1} (-\mathbf{z}_{i,t+G+L_G}) \\ & + \alpha_i + \gamma_t + \mathbf{q}'_{it}\psi + \mathbf{C}_{it} + \varepsilon_{it} \end{aligned} \quad (\text{estimating equation})$$

Simulation designs

- ▶ $N = 50, T = 40$
- ▶ Policy adopted when $(C_{i,t+P} + \text{noise})$ crosses a threshold
- ▶ Vary P and structure of C_{it}

Event-study path of unconfounded outcome $y_{it} - C_{it}$



Summary of data-generating processes

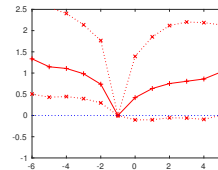
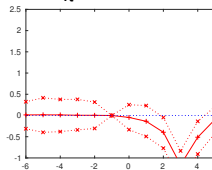
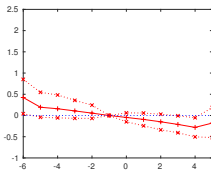
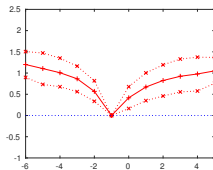
Mean-rev. trend

Monotone trend

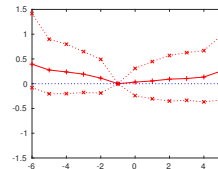
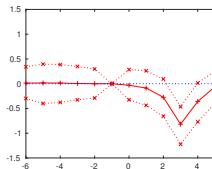
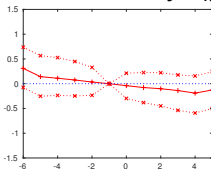
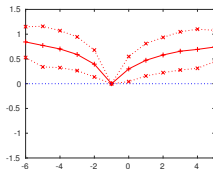
No pre-trend

Multidimensional

Confound C_{it}



Proxy x_{it} if available



Performance of different estimators

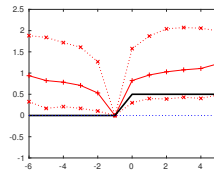
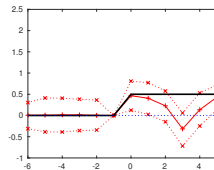
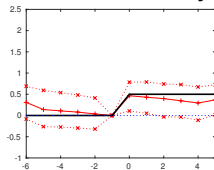
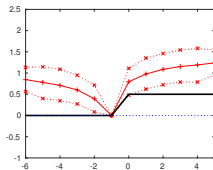
Mean-rev. trend

Monotone trend

No pre-trend

Multidimensional

Two-way fixed effects



Performance of different estimators

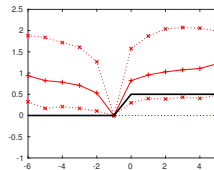
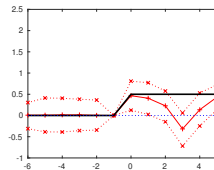
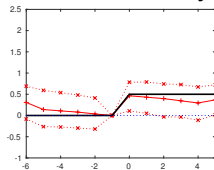
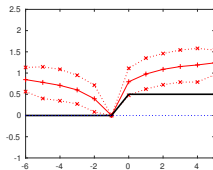
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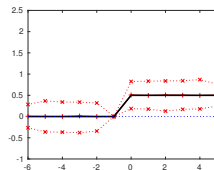
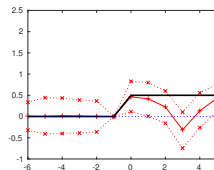
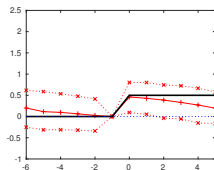
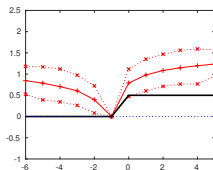
No pre-trend

Multidimensional

Two-way fixed effects



Interactive fixed-effects



Performance of different estimators

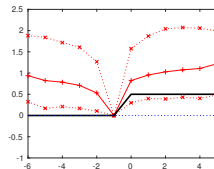
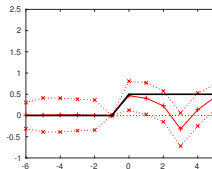
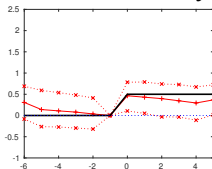
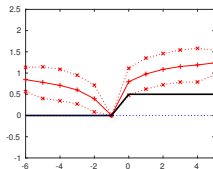
Mean-rev. trend

Monotone trend

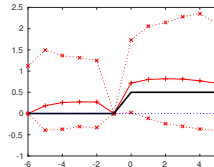
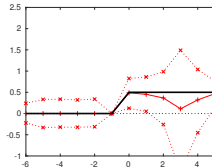
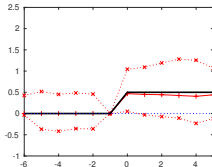
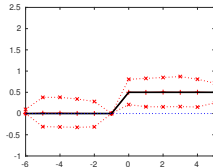
No pre-trend

Multidimensional

Two-way fixed effects



Instrumenting for x_{it} with leads of z_{it}



Takeaways

- ▶ No estimator performs well uniformly under all reasonable DGPs
- ▶ Performance of estimator cannot typically be gauged from the data at hand
- ▶ Importance of motivating modeling assumptions on economic grounds