

PRACTICE

COMPETE

JOBS

LEADERBOARD

Search Questions, problems, etc



LOGIN

SIGN UP

Signup and get free access to 100+ Tutorials and Practice Problems

Start Now

[All Tracks](#) > [Basic Programming](#) > [Recursion](#) > [Recursion and Backtracking](#)

Basic Programming

Solve any problem to achieve a rank
[View Leaderboard](#)

Input/Output



Complexity Analysis



Implementation



Operators



Bit Manipulation



Recursion

[Recursion and Backtracking](#)

Recursion and Backtracking

[Problems](#)[Tutorial](#)

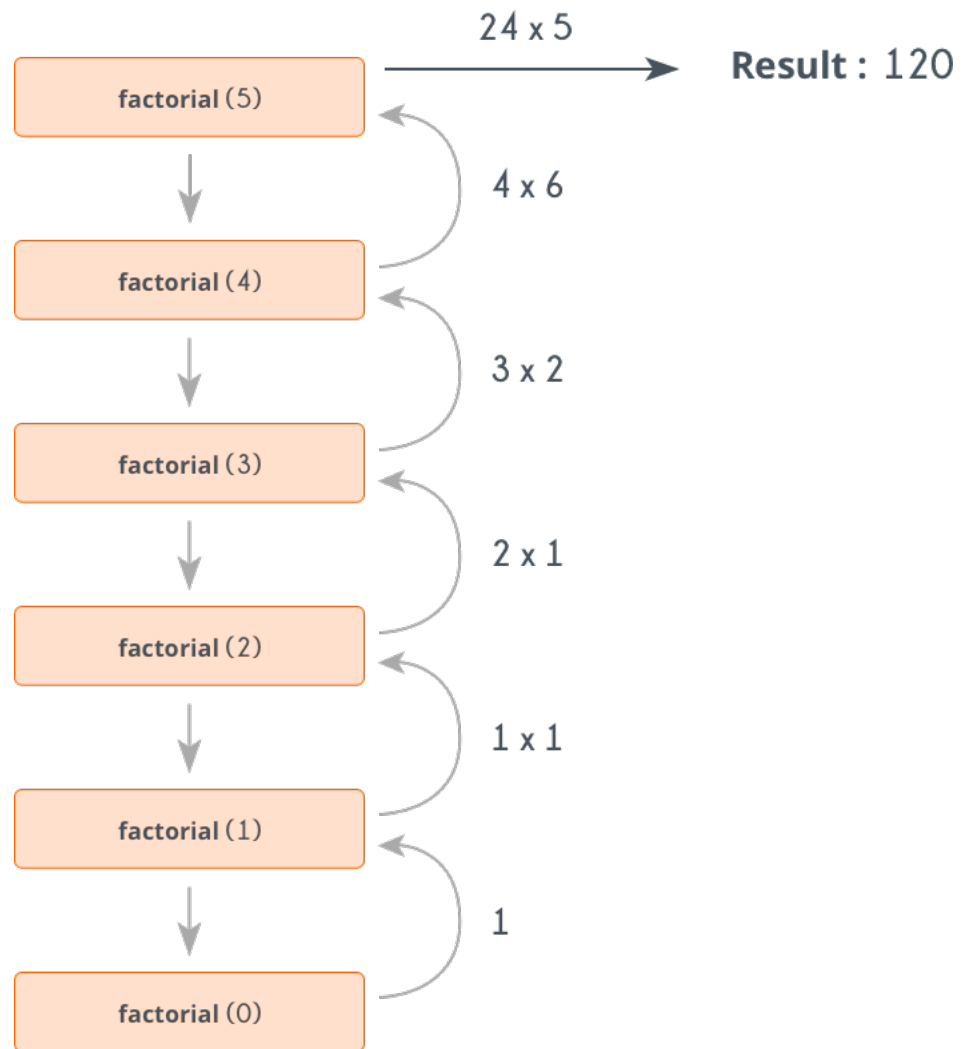
When a function calls itself, its called Recursion. It will be easier for those who have seen the movie Inception. Leonardo had a dream, in that dream he had another dream, in that dream he had yet another dream, and that goes on. So it's like there is a function called ***dream()***, and we are just calling it in itself.

```
function dream()  
  print "Dreaming"  
  dream()
```

Recursion is useful in solving problems which can be broken down into smaller problems of the **same** kind. But when it comes to solving problems using Recursion there are several things to be taken care of. Let's take a simple example and try to understand those. Following is the pseudo code of finding factorial of a given number **X** using recursion.

```
function factorial(x)  
  if x is 0 // base case  
    return 1  
  return x*factorial(x-1) // break into smaller problem(s)
```

The following image shows how it works for ***factorial(5)***.



Base Case: Any recursive method must have a terminating condition. Terminating condition is one for which the answer is already known and we just need to return that. For example for the factorial problem, we know that **factorial(0) = 1**, so when x is 0 we simply return 1, otherwise we break into smaller problem i.e. find factorial of $x - 1$. If we don't include a Base Case, the function will keep calling itself, and ultimately will result in stack overflow. For example, the **dream()** function given above has no base case. If you write a code for it in any language, it will give a runtime error.

Number of Recursive calls: There is an upper limit to the number of recursive calls that can be made. To prevent this make sure that your base case is reached before stack size limit exceeds.

So, if we want to solve a problem using recursion, then we need to make sure that:

- The problem can be broken down into smaller problems of **same type**.
- Problem has some base case(s).
- Base case is reached before the stack size limit exceeds.

Backtracking:

So, while solving a problem using recursion, we break the given problem into smaller ones. Let's say we have a problem **A** and we divided it into three smaller problems **B**, **C** and **D**. Now it may be the case that the solution to **A** does not depend on all the three subproblems, in fact we don't even know on which one it depends.

Let's take a situation. Suppose you are standing in front of three tunnels, one of which is having a bag of gold at its end, but you don't know which one. So you'll try all three. First go in tunnel **1**, if that is not the one, then come out of it, and go into tunnel **2**, and again if that is not the one, come out of it and go into tunnel **3**. So basically in backtracking we attempt solving a subproblem, and if we don't reach the desired solution, then undo whatever we did for solving that subproblem,

and try solving another subproblem.

Let's take a standard problem.

N-Queens Problem: Given a chess board having $N \times N$ cells, we need to place N queens in such a way that no queen is attacked by any other queen. A queen can attack horizontally, vertically and diagonally.

So initially we are having $N \times N$ unattacked cells where we need to place N queens. Let's place the first queen at a cell (i, j) , so now the number of unattacked cells is reduced, and number of queens to be placed is $N - 1$. Place the next queen at some unattacked cell. This again reduces the number of unattacked cells and number of queens to be placed becomes $N - 2$. Continue doing this, as long as following conditions hold.

- The number of unattacked cells is not 0.
- The number of queens to be placed is not 0.

If the number of queens to be placed becomes 0, then it's over, we found a solution. But if the number of unattacked cells become 0, then we need to backtrack, i.e. remove the last placed queen from its current cell, and place it at some other cell. We do this recursively.

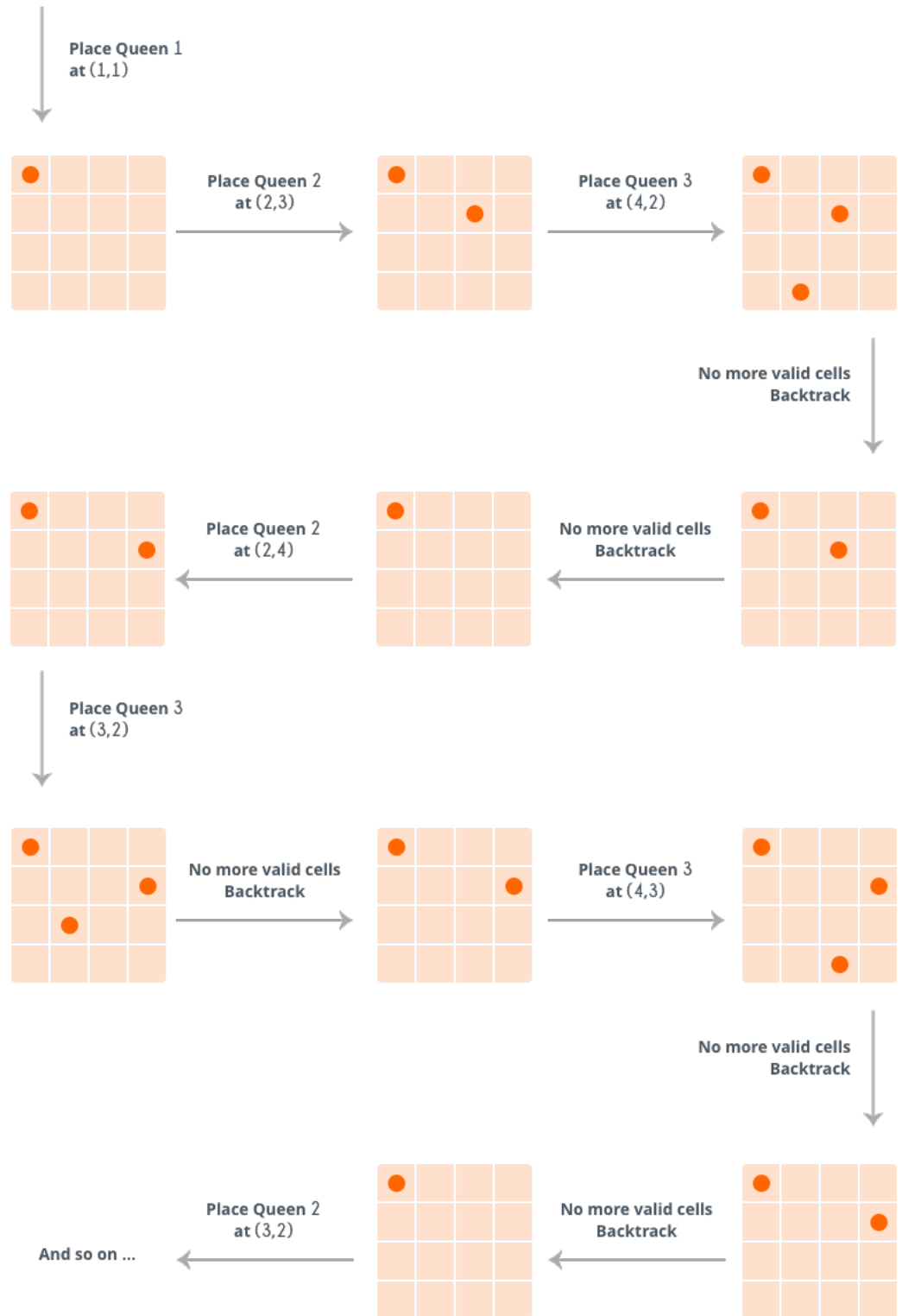
Complete algorithm is given below:

```
is_attacked( x, y, board[ ][ ], N)
    //checking for row and column
    if any cell in xth row is 1
        return true
    if any cell in yth column is 1
        return true

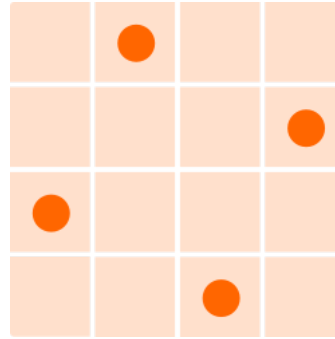
    //checking for diagonals
    if any cell (p, q) having p+q = x+y is 1
        return true
    if any cell (p, q) having p-q = x-y is 1
        return true
    return false

N-Queens( board[ ][ ], N )
    if N is 0                                //All queens have been placed
        return true
    for i = 1 to N {
        for j = 1 to N {
            if is_attacked(i, j, board, N) is true
                skip it and move to next cell
            board[i][j] = 1                    //Place current queen at cell (i,j)
            if N-Queens( board, N-1) is true    // Solve subproblem
                return true                    // if solution is found return true
            board[i][j] = 0                    /* if solution is not found undo whatever changes
                                                were made i.e., remove current queen from (i,j)*/
        }
    }
    return false
```

Here's how it works for $N = 4$.



So, at the end it reaches the following solution:



So, clearly, the above algorithm, tries solving a subproblem, if that does not result in the solution, it undo whatever changes were made and solve the next subproblem. If the solution does not exists ($N = 2$), then it returns **false**.

Contributed by: Vaibhav Jainini

Did you find this tutorial helpful?



Yes



No

TEST YOUR UNDERSTANDING

N-Queens

Given a chess board having $N \times N$ cells, you need to place N queens on the board in such a way that no queen attacks any other queen.

Input:

The only line of input consists of a single integer denoting N .

Output:

If it is possible to place all the N queens in such a way that no queen attacks another queen, then print "YES" (without quotes) in first line, then print N lines having N integers. The integer in i^{th} line and j^{th} column will denote the cell (i, j) of the board and should be 1 if a queen is placed at (i, j) otherwise 0. If there are more than way of placing queens print any of them.

If it is not possible to place all N queens in the desired way, then print "NO" (without quotes).

Constraints:

$1 \leq N \leq 10$.

SAMPLE INPUT	SAMPLE OUTPUT
4	YES 0 1 0 0 0 0 0 1 1 0 0 0 0 0 1 0

Enter your code or [Upload your code](#) as file.

Save

⌵ (gcc 10.3)

```

1  #include <stdio.h>
2
3  int main(){
4      int num;
5      scanf("%d", &num);

```

// Reading input from STD

```
6         printf("Input number is %d.\n", num);           // Writing output to STDOUT
7     }
8
```

1:1 vscode



Test against custom input ▼

Compile & Test code

Submit code

View all comments

For Developers

- Hackathons
- Challenges
- Jobs
- Practice
- Campus Ambassadors

For Businesses

- Hackathons
- Assessments
- FaceCode
- Learning and Development

Knowledge

- Practice
- Interview Prep
- Codemonk
- Engineering Blog

Company

- About us
- Careers
- Press
- Support
- Contact
- Privacy Policy

+1-650-461-4192
For sales enquiry
contact@hackerearth.com
For support
support@hackerearth.com

