Master's Thesis Proposal

Memoization of Incremental Computation for Generic Data Types

Jort van Gorkum Computing Science - Programming Technology

Supervisors
Dr. Wouter Swierstra, Dr. Trevor McDonell

February 10, 2022

Todo list

Example Haskell Data Type	1
Calculate a result over the Data Type	1
Cache the incremental computation over the data type	1
What type of data structures / dsl can be used to keep track of the incremental computations	1
Describe how hdiff compares	4

1 Introduction

• What is the problem? Illustrate with an example.

Example Haskell Data Type

Calculate a result over the Data Type

Cache the incremental computation over the data type

1.1 Research Questions

• What is/are your research questions/contributions?

What type of data structures / dsl can be used to keep track of the incremental computations

Can be used to perform static analysis in a more performant manner.

2 Background

2.1 An Efficient Algorithm for Type-Safe Structural Diffing

The paper An Efficient Algorithm for Type-Safe Structural Diffing by Victor Cacciari Miraldo and Wouter Swierstra presents an efficient datatype-generic algorithm called hdiff to compute the difference between two values of any algebraic datatype. In particular, the algorithm readily works over the abstract syntax tree (AST) of a programming language [7].

To make the *hdiff* algorithm work, an implementation of which common subtree needs to be defined. The wcs function is a function that when given two trees and a subtree, returns the position of the subtree inside the trees if both contain the subtree. Otherwise, the function returns nothing. An example of a naive implementation would be:

```
wcs :: Tree -> Tree -> Tree -> Maybe Int
wcs s d x = elemIndex x (subtrees s \cap subtrees d)
```

Here the function **subtrees** enumerates all the subtrees of a given tree. Then **elemIndex** returns the index when the subtree is found, otherwise it returns nothing.

The paper identifies two inefficiencies using this naive implementation. (A) Furthermore, enumerating all subtrees is exponential; (B) checking trees for equality is linear in the size of the tree.

To improve the first inefficiency of the naive wcs implementation is to use cryptographic hash functions to compare the equality of the trees. To check the trees for equality in constant time the trees are decorated with a hash at every node in the tree. Then, using the precomputed hash and the root node of the given tree, the hash of a subtree is calculated in constant time.

The second inefficiency of the naive wcs implementation is improved by using a Trie[1] datastructure. Given that a Hash is just a [Char], this makes the Trie datastructure the preferred choice to store the enumerated subtrees. And because the Hash has a constant size the Trie lookups are efficient and runs in amortized constant time.

2.2 Sums of Products for Mutually Recursive Datatypes

The paper Sums of Products for Mutually Recursive Datatypes written by Victor Cacciari Miraldo and Alejandro Serrano[6] presents a new approach to generic programming using recursive positions to handle mutually recursive families and the sum-of-products structure. This work (generics-msrop) is later used by the paper An Efficient Algorithm for Type-Safe Structural Diffing by Victor Cacciari Miraldo and Wouter Swierstra[7] to define the generic version of their diffing algorithm. Compared to existing generic programming libraries, generics-mrsop has deep explicit recursion, sums of products and supports mutually recursive datatypes.

Explicit recursion There are two ways to represent values. One contains the information on what properties of a datatype are recursive. The other does not contain that information. If we do not know explicitly if the property is recursive, then only one layer of the value can be formed into a generic representation. This is called *shallow* encoding. If we explicitly keep track of the recursive property, then the entire value can be transformed into a generic representation. This is called *deep* encoding. Using the *deep* encoding more datatypes can be defined generically (e.g., a generic *map* or generic Zipper datatype).

Sums of Products The generic-sop library uses a list of lists of types. The outer list represents the sum and the inner list represents the product. The sum represents the choice between two constructors; the product represents a combination of two constructors. An example of a Code representation of a BinTree is

Here the `sign in the code promotes the definition to the type-level instead of a run-time value. The use of *Sums of Products* makes it considerably easier to represent generic datatypes.

Mutually recursive datatypes Most of the generic programming libraries are restricted to only allowing recursion on the same datatype, which is the one being defined. Mutually recursive datatypes are recursively defined in each other's terms, meaning that most generic programming libraries do not support mutually recursive datatypes. This limits the ability to generically represent the syntax of many programming languages. Thus generic-sop introduces recursive positions on a type level, which can be used to define mutually recursive datatypes.

2.3 Concise, Type-Safe, and Efficient Structural Diffing

The paper Concise, Type-Safe, and Efficient Structural Diffing written by Erdweg, Sebastian and Szabó, Tamás and Pacak, André presents a structural diffing algorithm called truediff[3]. truediff ensures that the patches produces are concise and type safe, and with a performance by an order of magnitude higher than Gumtree[4] and the hdiff[7] algorithm.

To compute the difference between a source tree and a target tree, *truediff* operates in four steps: (1) prepare subtree equivalence relations; (2) find reusable candidates; (3) select reusable candidates; (4) and compute the edit script.

The equivalence relations used in step 1, exist out of two equivalence relations, both encoded through cryptographic hashes. The first equivalence relation is used to identify reusable candi-

dates. The second equivalence relation is used to identify preferred reusable candidates. The paper found that using structural equivalence to identify candidates and literal equivalence to select preferred candidates yields very concise edit scripts.

Describe how hdiff compares

3 Preliminary Results

Before writing the algorithm using the generic library generic-msrop[6], the algorithm is written using simpler self-defined generic datatypes with a fixpoint, which are defined in Appendix A and B. An example of how the generic datatypes can be used is:

Using the generic datatypes a merkle function can be defined, where at every recursive step of the datatype a Hash is stored. To merkelize a datatype, the datatype has to have the Merkelize constraint. The Merkelize type class is a class containing a single function merkleIn which converts the once unpacked Fix datatype into a unpacked Fix which contains a Hash at every recursive step¹.

The generic datatypes can also use a cata function. The cata or catamorphism is a generalization of the concept of a fold, which means it deconstructs a data structure into its underlying functor[2].

```
cata :: Functor f => (f a -> a) -> Fix f -> a
cata alg t = alg (fmap (cata alg) (unFix t))
```

The cata function can then be used to, for example, calculate the sum of all the values of the nodes and the leaves of the tree.

¹The implementation of the generic datatypes for the Merkelize type class can be found in Appendix C.

To keep track of the incremental computation of the summation of the tree, a HashMap[5] is used. The calculation of the incremental step is inserted into the HashMap and a pair of the HashMap and the result is returned. The implementation for the TreeG datatype is:

Then using the previously generated HashMap, we can then calculate the result reusing the previously incremental computations:

```
cataMerkleTreeWithMap :: Map Hash Int -> TreeG Int -> (Int, Map Hash Int)
cataMerkleTreeWithMap m (In (Pair (x, K h))) =
  case lookup h m of
   Just n -> (n, m)
   Nothing -> case x of
   Inl (K x) -> (x, insert h x empty)
   Inr (Pair (Pair (I l, K x), I r)) -> (x', m')
        where
        (xl, ml) = cataMerkleTreeWithMap m l
        (xr, mr) = cataMerkleTreeWithMap ml r
        x' = x + xl + xr
        m' = insert h x' mr
```

Using the previously defined cata functions we can determine the performance of the functions by using the criterion[8] package. For a benchmark in criterion, first, the environment is set up. Then the bench function is executed multiple times within a certain timeframe. The result of the multiple executions is used to calculate the mean and standard deviation of the

time executed.

The results of the cataSum, cataMerkleTree and cataMerkleTreeWithMap is seen in the graph.

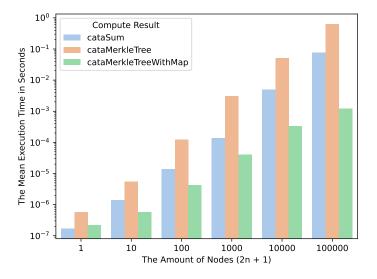


Figure 1: Compute the result

3.1 Future improvements

The problem with this implementation is that it only works for the TreeG datatype. The goal would be to create a generic function, where only the cataSum would be defined and the result would automatically contain the intermediate results. A generic definition could look something like this:

```
cataMerkle :: (f a -> a) -> Fix (f :*: K Hash) -> State (Map Hash a) a
```

Using the cataMerkle function would lead to only needing to implement the cataSum function and the intermediate results are then automatically stored.

4 Timetable and Planning

- What will I do with the remainder of my thesis?
- Give an approximate estimation/timetable for what you will do and when you will be done.

4.1 Exploratory topics

- 1. Writing a generic library to automatically cache the incremental computation
- 2. Which parameters can be tweaked to have the best performance / memory
- 3. What type of equivalence do you need to reuse incremental computation
- 4. What type of datastructures are the best to use for caching
 - Storing the results in a Trie data structure

4.2 Schedule

Week	Date	Category	Work			
Week 1	28 feb - 04 mar	Implementation	Generic CataMerkle			
Week 2	07 mar - 11 mar	Implementation	Generic CataMerkle			
Week 3	14 mar - 18 mar	Implementation	Using Generic MSROP library		Using Generic MSROP library	
Week 4	$21~\mathrm{mar}$ - $25~\mathrm{mar}$	Implementation	Using Generic MSROP library			
Week 5	28 mar - 01 apr	Experiments	Creating benchmarks			
Week 6	04 apr - $08 apr$	Experiments	Creating benchmarks			
Week 7	11 apr - 15 apr	Experiments	Using real-world data for benchmarks			
Week 8	18 apr - 22 apr	Experiments	Using real-world data for benchmarks			
Week 9	25 apr - 29 apr	Analysis	Test using different parameters			
Week 10	$02~\mathrm{may}$ - $06~\mathrm{may}$	Analysis	Test using different parameters			
Week 11 - 10	08 mar - 15 apr	Writing	Experiments			
Week 12 - 13	$18~\rm{apr}$ - $06~\rm{may}$	Writing	Discussion			
Week 13	$09~\mathrm{may}$ - $13~\mathrm{may}$	Writing	Conclusion			
Week 14 - 17	16 may - 3 jun	Feedback	Process final feedback			
Week 18 - 19	6 jun - 17 jun	Time Left	Vacation / Overdue work			
Week 20	20 jun - 24 jun	Finalize	Finalizing the Thesis			
Week 21	27 jun - 1 jul	Vacation	-			
Week 27	08 aug - 12 aug	Submission	Presentation & Thesis hand-in			
Week 28	15 aug	Finish	End Date Research Project			

Table 1: Planning per week

5 Appendix

A Definition Generic Datatypes

B Definition Fixpoint

```
data Fix f = In { unFix :: f (Fix f) }
instance Eq (f (Fix f)) => Eq (Fix f) where
   f == g = unFix f == unFix g

instance Show (f (Fix f)) => Show (Fix f) where
   show = show . unFix
```

C Implementation Merkelize

```
instance (Show a) => Merkelize (K a) where
    merkleIn (K x) = Pair (K x, K h)
    where
        h = hashConcat [hash "K", hash x]

instance Merkelize I where
    merkleIn (I x) = Pair (I prevX, K h)
    where
        prevX@(In (Pair (_, K ph))) = merkle x
        h = hashConcat [hash "I", ph]

instance (Merkelize f, Merkelize g) => Merkelize (f :+: g) where
    merkleIn (Inl x) = Pair (Inl prevX, K h)
    where
        (Pair (prevX, K ph)) = merkleIn x
        h = hashConcat [hash "Inl", ph]
    merkleIn (Inr x) = Pair (Inr prevX, K h)
```

```
where
    (Pair (prevX, K ph)) = merkleIn x
h = hashConcat [hash "Inr", ph]

instance (Merkelize f, Merkelize g) => Merkelize (f :*: g) where
merkleIn (Pair (x, y)) = Pair (Pair (prevX, prevY), K h)
    where
    (Pair (prevX, K phx)) = merkleIn x
    (Pair (prevY, K phy)) = merkleIn y
h = hashConcat [hash "Pair", phx, phy]
```

D Results of computing the sum of a Tree

Amount	Action	Mean	Stddev
1	Generate (Result, Map)	5.662 e-07	1.195e-08
1	Generate (Result, Map) with Map	2.208e-07	5.237e-09
1	Generate Result	1.713e-07	1.721e-09
10	Generate (Result, Map)	5.456 e - 06	6.462 e-08
10	Generate (Result, Map) with Map	5.744e-07	8.788e-09
10	Generate Result	1.401 e-06	1.132e-08
100	Generate (Result, Map)	1.205 e-04	2.379 e-06
100	Generate (Result, Map) with Map	4.165 e-06	6.188e-08
100	Generate Result	1.358 e - 05	1.826 e - 07
1000	Generate (Result, Map)	3.024 e-03	9.485 e-05
1000	Generate (Result, Map) with Map	3.955 e-05	6.024 e-07
1000	Generate Result	1.387e-04	1.708e-06
10000	Generate (Result, Map)	5.018e-02	2.108e-03
10000	Generate (Result, Map) with Map	3.280 e-04	5.800 e-06
10000	Generate Result	4.994 e-03	1.123e-04
100000	Generate (Result, Map)	6.253 e-01	2.174e-02
100000	Generate (Result, Map) with Map	1.228e-03	1.836e-05
100000	Generate Result	7.592e-02	1.505 e-03

Table 2: Compute the result

References

- [1] Peter Brass. Advanced data structures. Vol. 193. Cambridge University Press Cambridge, 2008, pp. 336–356.
- [2] Catamorphisms. URL: https://wiki.haskell.org/Catamorphisms (visited on Jan. 26, 2022).
- [3] Sebastian Erdweg, Tamás Szabó, and André Pacak. "Concise, type-safe, and efficient structural diffing". In: Proceedings of the 42nd ACM SIGPLAN International Conference on Programming Language Design and Implementation. 2021, pp. 406–419.
- [4] Jean-Rémy Falleri et al. "Fine-grained and accurate source code differencing". In: Proceedings of the 29th ACM/IEEE international conference on Automated software engineering. 2014, pp. 313–324.
- [5] Map type. URL: https://hackage.haskell.org/package/containers-0.4.0.0/docs/Data-Map.html (visited on Feb. 8, 2022).
- [6] Victor Cacciari Miraldo and Alejandro Serrano. "Sums of products for mutually recursive datatypes: the appropriationist's view on generic programming". In: *Proceedings of the 3rd ACM SIGPLAN International Workshop on Type-Driven Development.* 2018, pp. 65–77.
- [7] Victor Cacciari Miraldo and Wouter Swierstra. "An efficient algorithm for type-safe structural diffing". In: *Proceedings of the ACM on Programming Languages* 3.ICFP (2019), pp. 1–29.
- [8] Bryan O'Sullivan. URL: http://www.serpentine.com/criterion/ (visited on Feb. 8, 2022).