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CPSC 335-02
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CPSC 335 Project 1

Alternate Algorithm

CODE FOR ALTERNATE ALGORITHM

```
int algorithm = 0;                                1
for (size_t i = 0; i < before.light_count(); i++)
    for (size_t n = i; n < before.total_count() - 1; n++)
        if (before.get(n) > before.get(n + 1))
            const_cast <disk_state&> (before).swap(n);
            algorithm++;
        endif
    endfor
endfor
return sorted_disks(before, algorithm);
```

PSEUDO-CODE FOR ALTERNATE ALGORITHM

```
int algo = 0                                     1
for i = 0 to n
    for n = i to 2n-1
        if (n > n+1)                             2 + (max(3,2))
            Swap                                  3
            algo = algorithm + 1                  2
        endif
    endfor
endfor
return sorted_disks(before, algo);
```

STEP COUNT AND BIG (O) PROOF FOR ALTERNATE ALGORITHM

Step Count:

$$\begin{aligned}& \sum_{i=0}^n \sum_{n=i}^{2n-1} 5 \\& \sum_{i=0}^n 5(2n-1) + 1 \\& \sum_{i=0}^n 10n - 4 \\& 10 \sum_{i=0}^n n - \sum_{i=0}^n 4 \\& = 10 \cdot \frac{n(n+1)}{2} - 4n \\& = \frac{10n^2 + 10n}{2} - 4n \\& = 5n^2 + 5n - 4n \\& = \boxed{5n^2 + n}\end{aligned}$$

Big O Proof:

Show that $f(n) = 5n^2 + n \in O(n^2)$

Find $C > 0$ and $n_0 \geq 0$ S.T. $5n^2 + n \leq (C)n^2 \quad \forall n \geq n_0$

$C = 5 + 1 = 6, n = 1$

$5n^2 + n \leq 6n^2$

$6n^2 - 5n^2 - n \geq 0$

$n^2 - n \geq 0$

$0 \geq 0$

Yes, it belongs to $O(n^2)$.

Lawnmower Algorithm

CODE FOR LAWNMOWER ALGORITHM

```
int algorithm = 0;
for (size_t i = 0; i < before.light_count(); i++)
{
    for (size_t j = i; j < before.total_count() - 1; j++)
    {
        if (before.get(j) > before.get(j + 1))
        {
            const_cast<disk_state&>(before).swap(j);
            algorithm++;
        }
    }
}
for (size_t j = before.total_count() - 1; j > 0; j--)
{
    if (before.get(j) < before.get(j - 1))
    {
        const_cast<disk_state&>(before).swap(j - 1);
        algorithm++;
    }
}
return sorted_disks(before, algorithm);
}
```

PSEUDO-CODE FOR LAWNMOWER ALGORITHM

Note: n = light_count
 $2n$ = total count

```
int algo = 0;
for int i = 0 to n
    for j = i to 2n - 1
        if (j > (j+1))
            swap()
            algo = algo + 1
        endfor
    for j = 2n - 1 to 0
        if (j < (j - 1))
            swap()
            algo = algo + 1
        endfor
    endfor
return sorted_disks()
```

STEP COUNT AND BIG (O) NOTATION FOR LAWNMOWER ALGORITHM

Step Count

int algo

$$\sum_{i=0}^n \sum_{j=i}^{2n-1} 5 = \sum_{i=0}^n 5(2n-1)$$

$$= \sum_{i=0}^n 10n - \sum_{i=0}^n 5$$

$$= 10 \cdot \frac{n(n+1)}{2} - 5n$$

$$= \frac{10n^2 + 10n}{2} - 5n$$

$$= 5n^2 + 5n - 5n$$

$$= 5n^2$$

$$\text{for } i = 0 \text{ To } n \quad \text{for } j = 2n-1 \text{ To } 0 \quad \left(\frac{0 - 2n-1}{-1} + 1 \right) \\ s$$

$$n+1 \cdot [5(2n+1+1)]$$

$$(n+1)(10n+10)$$

$$10n^2 + 10n + 10n + 10$$

$$10n^2 + 20n + 10$$

$$5n^2 + 10n^2 + 20n + 10$$

$$= 15n^2 + 20n + 10$$

$$\text{Big O} = \mathcal{O}(n^2)$$

Big O Proof:

Show that $f(n) = 15n^2 + 20n + 10 \in \mathcal{O}(n^2)$

Find $C > 0$ and $n_0 \geq 0$ s.t. $15n^2 + 20n + 10 \leq (C)n^2 \quad \forall n \geq n_0$

$$C = 15 + 20 + 10 = 45, n_0 = 0$$

$$15n^2 + 20n + 10 \leq 45n^2$$

$$45n^2 + 15n^2 + 20n + 10 \geq 0$$

$$45n^2 + 15n^2 + 20n + 10$$

$$n \geq 0$$

Yes, it belongs to $\mathcal{O}(n^2)$.

TUFFIX SCREENSHOTS

