Principles of Concurrent and Distributed Programming

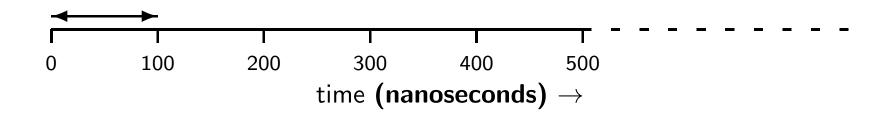
(Second Edition)

Addison-Wesley, 2006

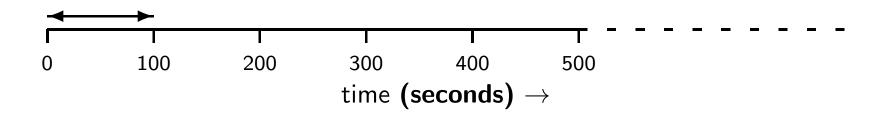
Mordechai (Moti) Ben-Ari

http://www.weizmann.ac.il/sci-tea/benari/

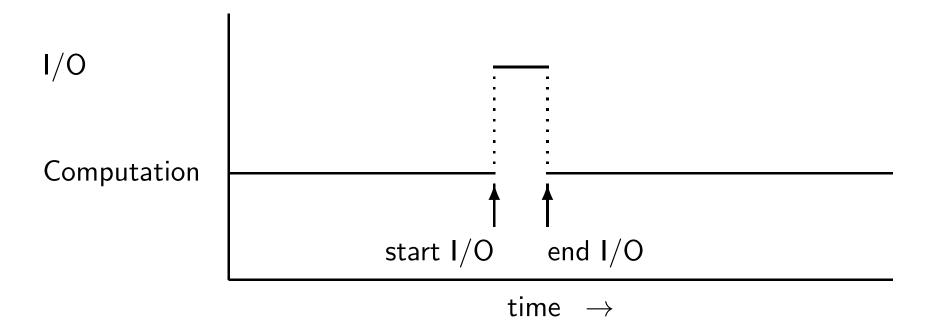
Computer Time



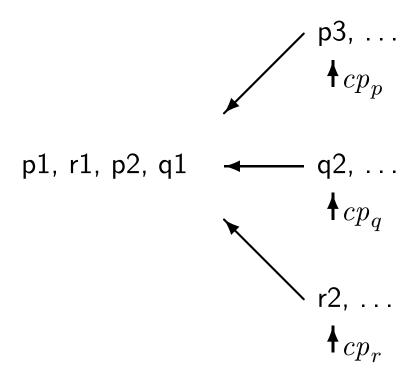
Human Time



Concurrency in an Operating System



Interleaving as Choosing Among Processes



Possible Interleavings

$$p1 \rightarrow q1 \rightarrow p2 \rightarrow q2,$$

 $p1 \rightarrow q1 \rightarrow q2 \rightarrow p2,$
 $p1 \rightarrow p2 \rightarrow q1 \rightarrow q2,$
 $q1 \rightarrow p1 \rightarrow q2 \rightarrow p2,$
 $q1 \rightarrow p1 \rightarrow p2 \rightarrow q2,$
 $q1 \rightarrow q2 \rightarrow p1 \rightarrow p2.$

Algorithm 2.1: Trivial concurrent program			
integer n \leftarrow 0			
p			
integer k $1 \leftarrow 1$	integer $k2 \leftarrow 2$		
p1: n ← k1	q1: n ← k2		

Algorithm 2.2: Trivial sequential program

integer $n \leftarrow 0$

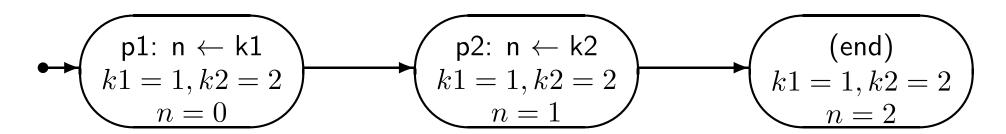
integer k $1 \leftarrow 1$

integer $k2 \leftarrow 2$

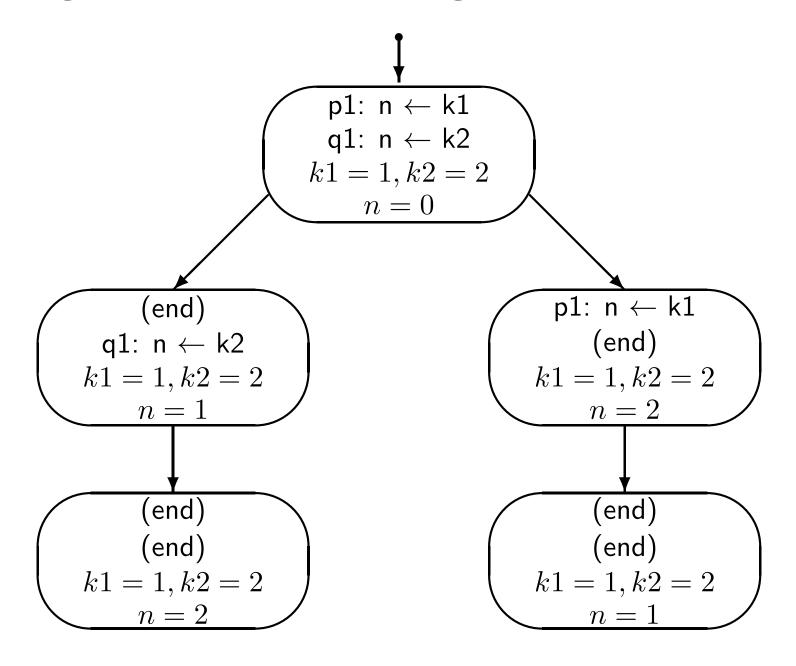
p1: $n \leftarrow k1$

p2: $n \leftarrow k2$

State Diagram for a Sequential Program



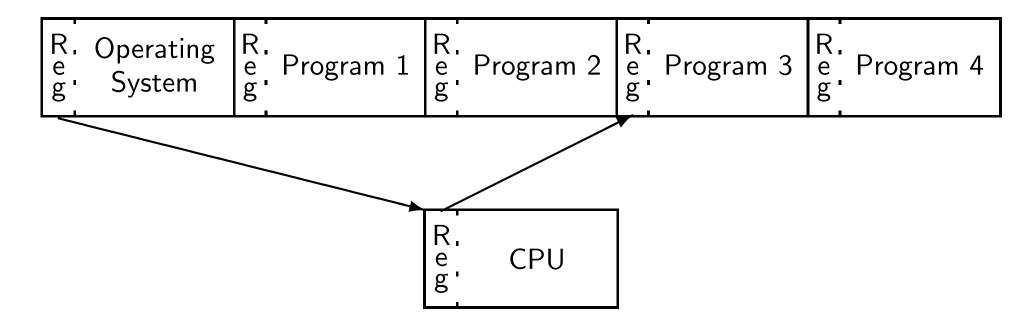
State Diagram for a Concurrent Program



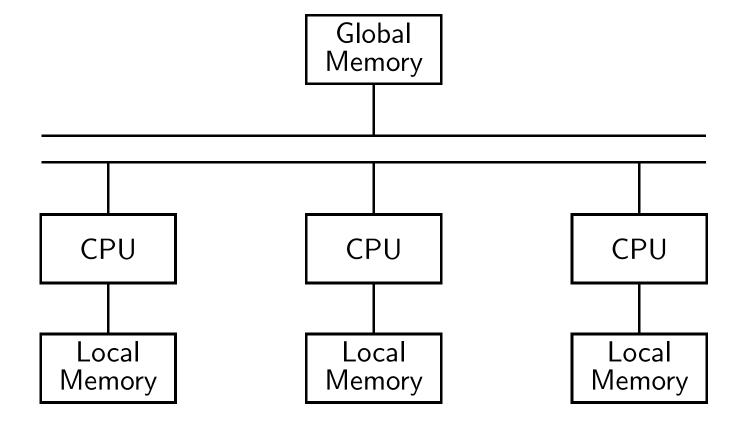
Scenario for a Concurrent Program

Process p	Process q	n	k1	k2
p1: n←k1	q1: n←k2	0	1	2
(end)	q1: n←k2	1	1	2
(end)	(end)	2	1	2

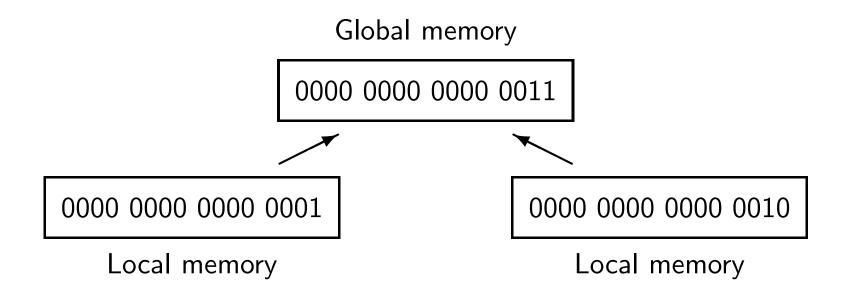
Multitasking System



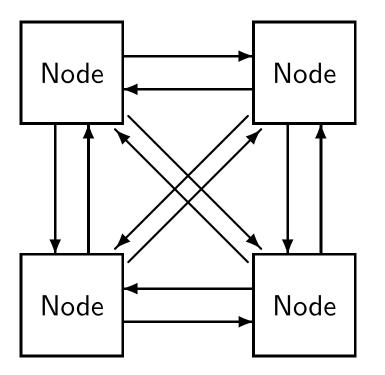
Multiprocessor Computer

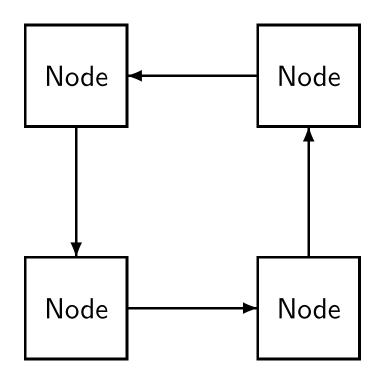


Inconsistency Caused by Overlapped Execution



Distributed Systems Architecture





Algorithm 2.3: Atomic assignment statements		
integer n ← 0		
p		
p1: $n \leftarrow n+1$ q1: $n \leftarrow n+1$		

Scenario for Atomic Assignment Statements

Process p	Process q	n
p1 : n←n+1	q1: n←n+1	0
(end)	q1: n←n+1	1
(end)	(end)	2

Process p	Process q	n
p1: $n\leftarrow n+1$	q1: n←n+1	0
p1 : n←n+1	(end)	1
(end)	(end)	2

Algorithm 2.4: Assignment statements with one global reference integer $n \leftarrow 0$ p q integer temp integer temp $\mathsf{temp} \leftarrow \mathsf{n}$ p1: temp \leftarrow n q2: $n \leftarrow temp + 1$ $n \leftarrow temp + 1$

Correct Scenario for Assignment Statements

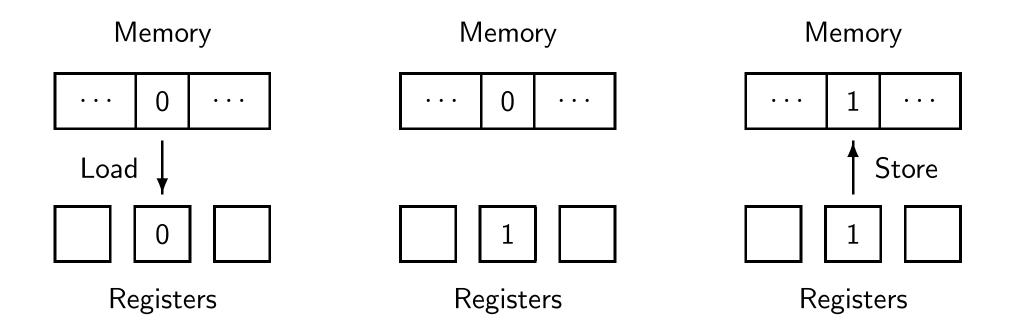
Process p	Process q	n	p.temp	q.temp
p1: temp←n	q1: temp←n	0	?	?
p2: n←temp+1	q1: temp←n	0	0	?
(end)	q1: temp←n	1	0	?
(end)	q2: n←temp+1	1	0	1
(end)	(end)	2	0	1

Incorrect Scenario for Assignment Statements

Process p	Process q	n	p.temp	q.temp
p1: temp←n	q1: temp←n	0	?	?
p2: n←temp+1	q1: temp←n	0	0	?
p2: n←temp+1	q2: n←temp+1	0	0	0
(end)	q2: n←temp+1	1	0	0
(end)	(end)	1	0	0

Algorithm 2.5: Stop the loop A			
integer n \leftarrow 0			
boolean flag \leftarrow false			
p	q		
p1: while flag = false	q1: flag ← true		
p2: $n \leftarrow 1 - n$ q2:			

Register Machine

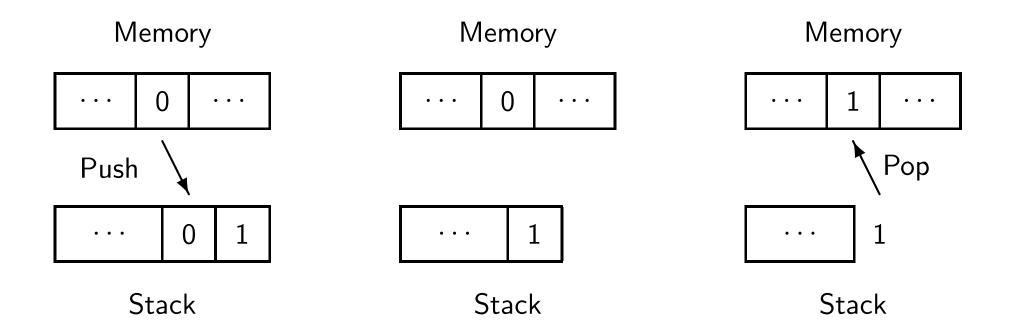


Scenario for a Register Machine

Process p	Process q	n	p.R1	q.R1
p1: load R1,n	q1: load R1,n	0	?	?
p2: add R1,#1	q1: load R1,n	0	0	?
p2: add R1,#1	q2: add R1,#1	0	0	0
p3: store R1,n	q2: add R1,#1	0	1	0
p3: store R1,n	q3: store R1,n	0	1	1
(end)	q3: store R1,n	1	1	1
(end)	(end)	1	1	1

Algorithm 2.7: Assignment statement for a stack machine		
integer n \leftarrow 0		
p	q	
p1: push n	q1: push n	
p1: push n p2: push $\#1$	q2: push $\#1$ q3: add	
p3: add	q3: add	
p4: pop n	q4: pop n	

Stack Machine



Algorithm 2.8: Volatile variables			
integer n ↔	integer n \leftarrow 0		
p	q		
integer local1, local2	integer local		
p1: n ← some expression	q1: local ← n + 6		
p2: computation not using n	q2:		
p3: $local1 \leftarrow (n + 5) * 7$	q3:		
p4: local2 ← n + 5	q4:		
p5: n ← local1 * local2	q5:		

Algorithm 2.9: Concurrent counting algorithm			
integer n \leftarrow 0			
p	q		
integer temp	integer temp		
p1: do 10 times	q1: do 10 times		
p2: temp ← n	q2: temp ← n		
p3: $n \leftarrow temp + 1$	q3: $n \leftarrow \text{temp} + 1$		

Concurrent Program in Pascal

```
program count;
    var n: integer := 0;
3
4
    procedure p;
    var temp, i: integer;
6
    begin
      for i := 1 to 10 do
8
         begin
9
           temp := n; n := temp + 1
10
         end
11
    end;
12
    procedure q;
13
    var temp, i: integer;
14
    begin
15
      for i := 1 to 10 do
16
         begin
17
18
           temp := n; n := temp + 1
19
         end
20
    end;
21
    begin
22
23
      cobegin p; q coend;
      writeln('The value of n is ', n)
24
                Principles of Concurrent and Distributed Programming. Slides © 2006 by M. Ben-Ari.
25
    end.
```

Concurrent Program in C

```
int n = 0;
   void p() {
     int temp, i;
   for (i = 0; i < 10; i++) {
     temp = n;
    n = temp + 1;
8
9
10
   void q() {
11
     int temp, i;
12
   for (i = 0; i < 10; i++)
13
14
   temp = n;
   n = temp + 1;
15
16
17
18
   void main() {
19
    cobegin \{ p(); q(); \}
20
     cout << "The value of n is " << n << "\n";
21
22
```

Concurrent Program in Ada

```
with Ada.Text_IO; use Ada.Text_IO;
     procedure Count is
 2
        N: Integer := 0;
 3
        pragma Volatile(N);
 4
 5
        task type Count_Task;
 6
        task body Count_Task is
 7
           Temp: Integer;
 8
        begin
 9
10
           for l in 1..10 loop
              Temp := N;
11
              N := Temp + 1;
12
           end loop;
13
        end Count_Task;
14
15
    begin
16
        declare
17
           P, Q: Count_Task;
18
19
        begin
           null:
20
21
        end;
        Put_Line("The value of N is " & Integer' Image(N));
22
    end Count; Principles of Concurrent and Distributed Programming. Slides © 2006 by M. Ben-Ari.
23
                                                                                Slide – 2.27
```

Concurrent Program in Java

```
class Count extends Thread {
        static volatile int n = 0;
 2
 3
        public void run() {
 4
 5
          int temp;
          for (int i = 0; i < 10; i++) {
 6
 7
            temp = n;
8
            n = temp + 1;
9
10
11
        public static void main(String[] args) {
12
          Count p = new Count();
13
          Count q = new Count();
14
15
          p.start ();
16
          q.start();
          try {
17
18
            p. join ();
            q.join ();
19
20
          catch (InterruptedException e) { }
21
          System.out.println ("The value of n is " + n);
22
23
24
```

Concurrent Program in Promela

```
#include "for.h"
    #define TIMES 10
    byte n = 0;
 3
4
    proctype P() {
 5
6
        byte temp;
        for (i,1, TIMES)
8
            temp = n;
9
            n = temp + 1
        rof (i)
10
11
12
13
    init {
        atomic {
14
            run P();
15
            run P()
16
17
        (\_nr\_pr == 1);
18
        printf ("MSC: The value is %d\n", n)
19
20
```

Frog Puzzle



















One Step of the Frog Puzzle



















Final State of the Frog Puzzle











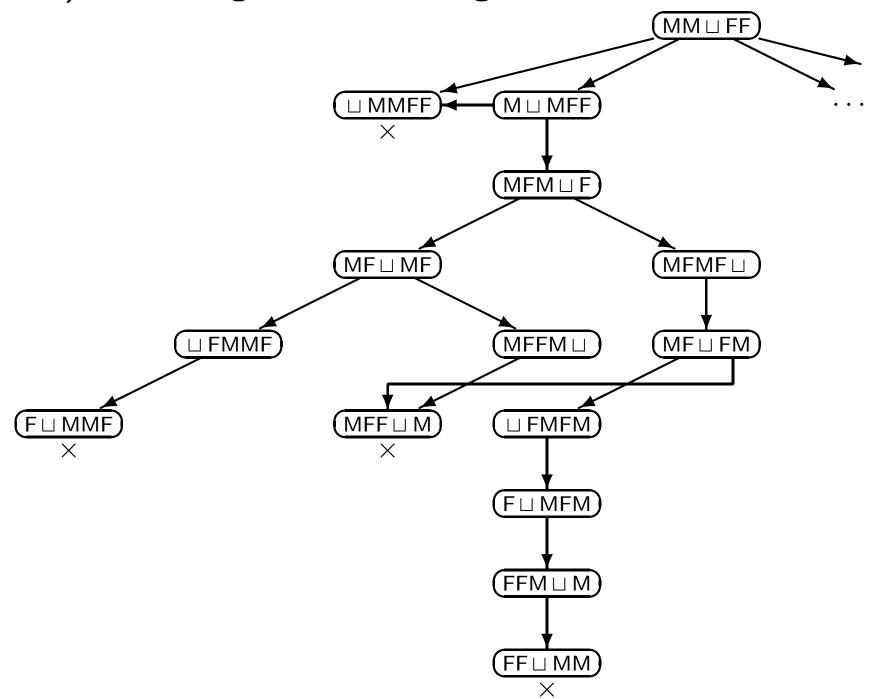








(Partial) State Diagram for the Frog Puzzle



Algorithm 2.10: Incrementing and decrementing		
integer n ← 0		
p	q	
integer temp	integer temp	
p1: do K times	q1: do K times	
p2: temp ← n	q2: temp ← n	
p3: $n \leftarrow temp + 1$	q3: $n \leftarrow temp - 1$	

Algorithm 2.11: Zero A			
boolean found			
p			
integer i ← 0	integer j $\leftarrow 1$		
p1: found ← false	q1: found ← false		
p2: while not found	q2: while not found		
p3: $i \leftarrow i + 1$	q3: $j \leftarrow j-1$		
p4: found $\leftarrow f(i) = 0$	q4: found $\leftarrow f(j) = 0$		

Algorithm 2.12: Zero B			
boolean found \leftarrow false			
p			
integer i ← 0	integer j $\leftarrow 1$		
p1: while not found	q1: while not found		
p2: $i \leftarrow i + 1$	q2: $j \leftarrow j - 1$ q3: found \leftarrow f(j) = 0		
p3: found \leftarrow f(i) = 0	q3: found $\leftarrow f(j) = 0$		

Algorithm 2.13: Zero C			
boolean found \leftarrow false			
р	q		
integer i ← 0	integer j $\leftarrow 1$		
p1: while not found	q1: while not found		
p2: $i \leftarrow i + 1$	q2: $j \leftarrow j - 1$		
p3: if $f(i) = 0$ p4: found \leftarrow true	q3: if $f(j) = 0$		
p4: found ← true	q4: found ← true		

Algorithm 2.14: Zero D			
boolean found \leftarrow false			
integer turn $\leftarrow 1$			
p	q		
integer i ← 0	integer j $\leftarrow 1$		
p1: while not found	q1: while not found		
p2: await turn $= 1$	q2: await turn $= 2$		
turn ← 2	$turn \leftarrow 1$		
p3: $i \leftarrow i + 1$	q3: $j \leftarrow j-1$		
p4: if $f(i) = 0$	q4: if $f(j) = 0$		
p5: found ← true	q5: found ← true		

Algorithm 2.15: Zero E		
boolean found ← false		
integer turn $\leftarrow 1$		
p	q	
integer i ← 0	integer j $\leftarrow 1$	
p1: while not found	q1: while not found	
p2: await turn $= 1$	q2: await turn $= 2$	
turn ← 2	$turn \leftarrow 1$	
p3: $i \leftarrow i + 1$	q3: $j \leftarrow j-1$	
p4: if $f(i) = 0$	q4: if $f(j) = 0$	
p5: found ← true	q5: found ← true	
p6: turn ← 2	q6: turn \leftarrow 1	

Algorithm 2.16: Concurrent algorithm A

integer array [1..10] C \leftarrow ten *distinct* initial values integer array [1..10] D

integer myNumber, count

p1: $myNumber \leftarrow C[i]$

p2: count \leftarrow number of elements of C less than myNumber

p3: $D[count + 1] \leftarrow myNumber$

Algorithm 2.17: Concurrent algorithm B		
integer n \leftarrow 0		
p	q	
p1: while $n < 2$	q1: $n \leftarrow n + 1$	
p2: write(n)	q2: $n \leftarrow n + 1$	

Algorithm 2.18: Concurrent algorithm C		
integer n $\leftarrow 1$		
p	q	
p1: while $n < 1$	q1: while $n >= 0$	
p2: $n \leftarrow n + 1$	q2: n ← n − 1	

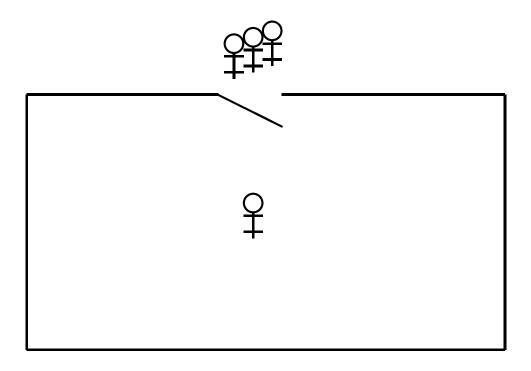
Algorithm 2.19: Stop the loop B		
integer n \leftarrow 0		
boolean flag \leftarrow false		
p	q	
p1: while flag = false	q1: while flag = false	
p2: $n \leftarrow 1 - n$	q2: if $n = 0$	
p3:	q3: flag ← true	

Algorithm 2.20: Stop the loop C			
integer n \leftarrow 0			
boolean flag \leftarrow false			
p			
p1: while flag = false	q1: while $n = 0 // Do nothing$		
p2: $n \leftarrow 1 - n$	q2: flag ← true		

```
Algorithm 2.21: Welfare crook problem
                integer array[0..N] a, b, c \leftarrow ...(as required)
               integer i \leftarrow 0, j \leftarrow 0, k \leftarrow 0
     loop
        if condition-1
p1:
        i \leftarrow i + 1
p2:
       else if condition-2
p3:
       j \leftarrow j + 1
p4:
      else if condition-3
p5:
         \mathsf{k} \leftarrow \mathsf{k} + \mathsf{1}
p6:
         else exit loop
```

Algorithm 3.1: Critical section problem			
global variables			
p q			
local variables	local variables		
loop forever	loop forever		
non-critical section	non-critical section		
preprotocol	preprotocol		
critical section	critical section		
postprotocol	postprotocol		

Critical Section



	Algorithm 3.2: First attempt		
	integer turn $\leftarrow 1$		
p q			
	loop forever		oop forever
p1:	non-critical section	q1:	non-critical section
p2:	await turn $=1$	q2:	await turn $= 2$
p3:	critical section	q3:	critical section
p4:	$turn \leftarrow 2$	q4:	turn $\leftarrow 1$

Algorithm 3.3: History in a sequential algorithm

integer a \leftarrow 1, b \leftarrow 2

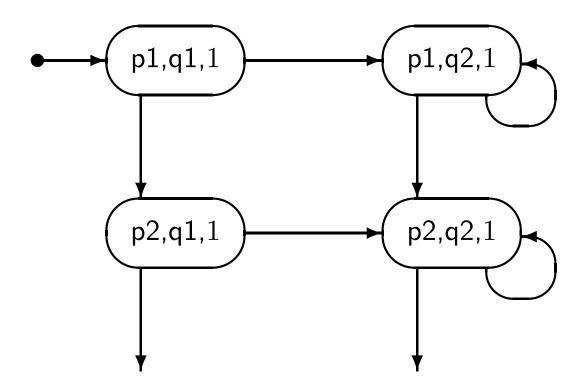
p1: Millions of statements

p2: $a \leftarrow (a+b)*5$

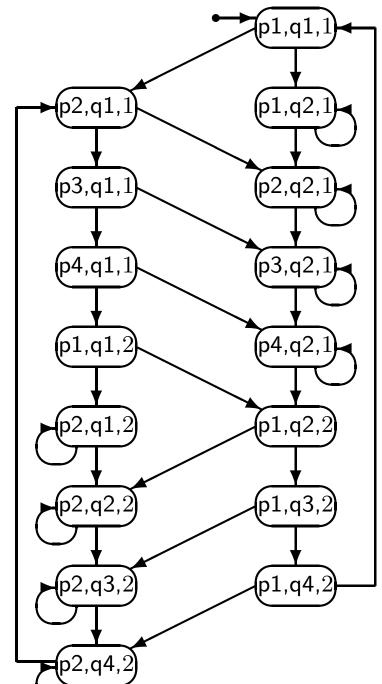
p3: ...

Algorithm 3.4: History in a concurrent algorithm				
integer a \leftarrow 1, b \leftarrow 2				
p q				
p1: Millions of statements	q1: Millions of statements			
p2: $a \leftarrow (a+b)*5$	q2: $b \leftarrow (a+b)*5$			
p3:	q3:			

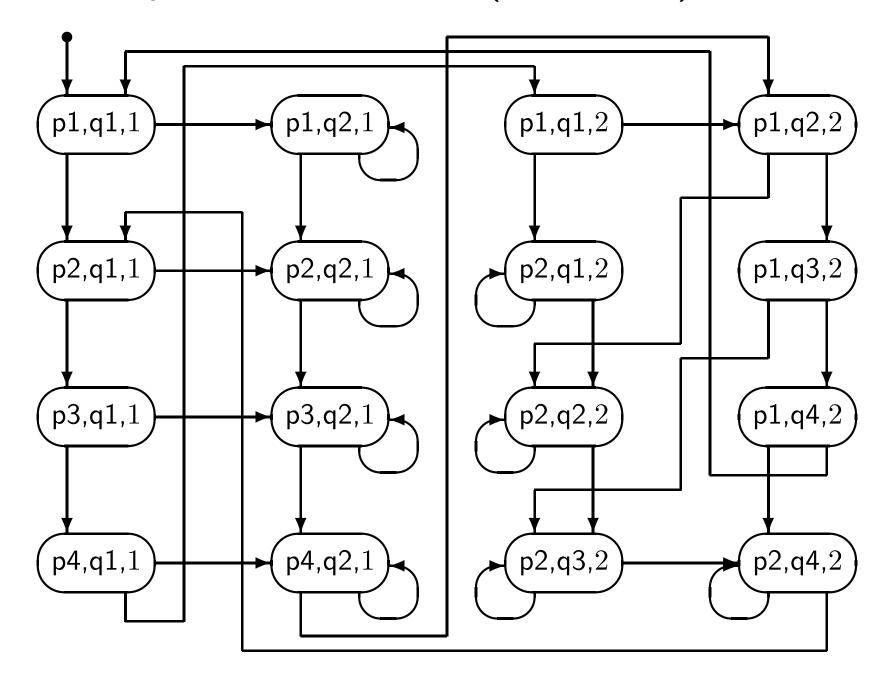
First States of the State Diagram



State Diagram for the First Attempt

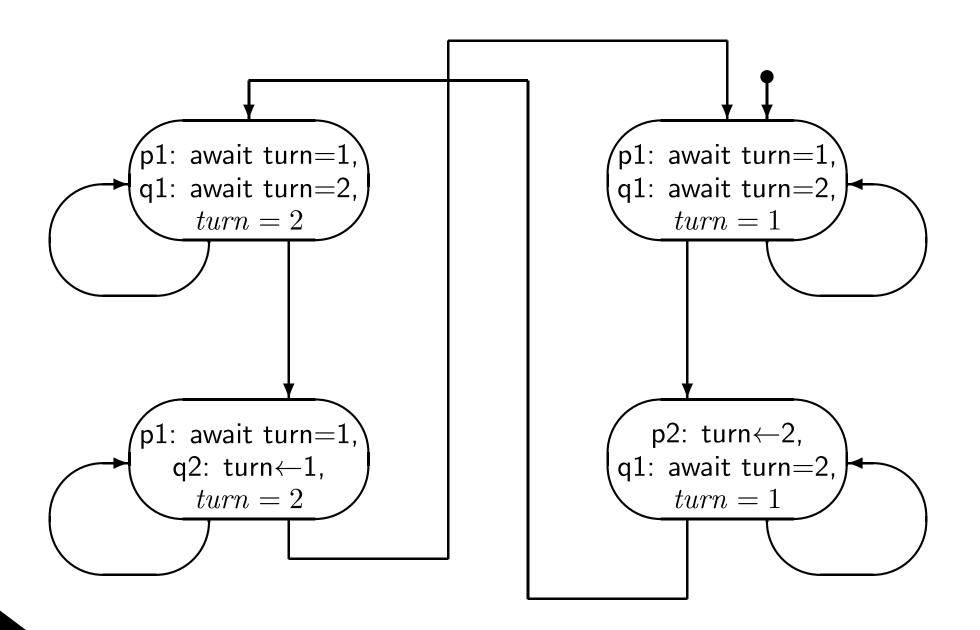


Alternate Layout for First Attempt (Not in book)

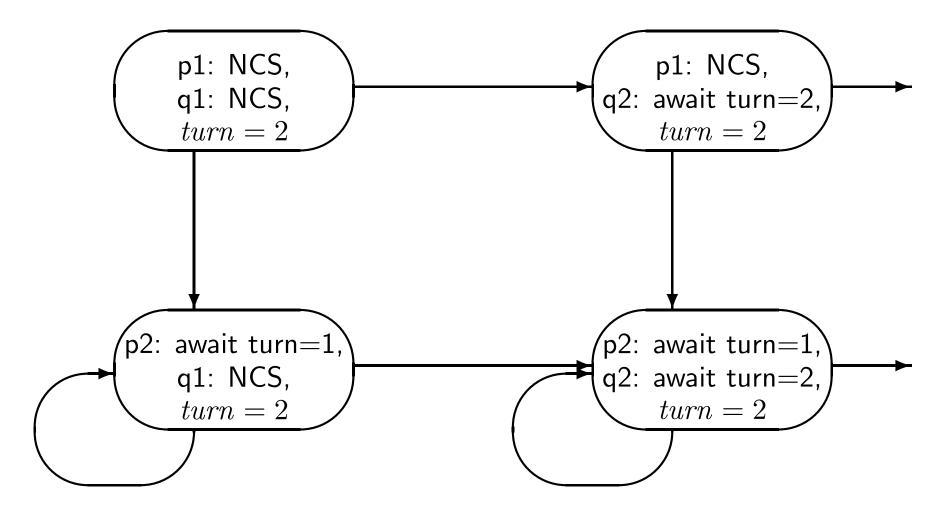


Algorithm 3.5: First attempt (abbreviated)				
integer turn $\leftarrow 1$				
p q				
loop forever	loop forever			
p1: await turn $= 1$	q1: await turn $= 2$			
p2: turn \leftarrow 2	q2: turn \leftarrow 1			

State Diagram for the Abbreviated First Attempt



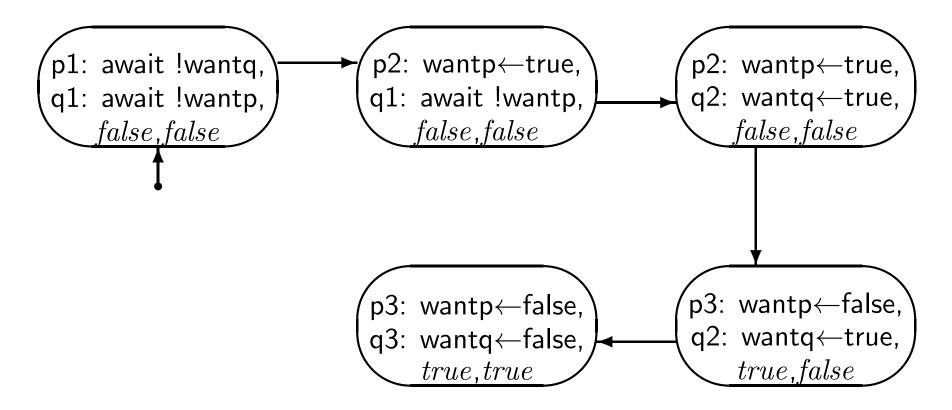
Fragment of the State Diagram for the First Attempt



	Algorithm 3.6: Second attempt				
	boolean wantp \leftarrow false, wantq \leftarrow false				
	p q				
loop forever		loop forever			
p1:	non-critical section	q1:	non-critical section		
p2:	await wantq = false	q2:	await wantp = false		
p3:	wantp ← true	q3:	wantq ← true		
p4:	critical section	q4:	critical section		
p5:	wantp ← false	q5:	wantq ← false		

	Algorithm 3.7: Second attempt (abbreviated)			
	boolean wantp \leftarrow false, wantq \leftarrow false			
	p q			
	loop forever loop forever		loop forever	
p1:	await wantq = false	q1:	await wantp = false	
p2:	wantp ← true	q2:	wantq \leftarrow true	
p3:	wantp ← false	q3:	wantq ← false	

Fragment of State Diagram for the Second Attempt



Scenario: Mutual Exclusion Does Not Hold

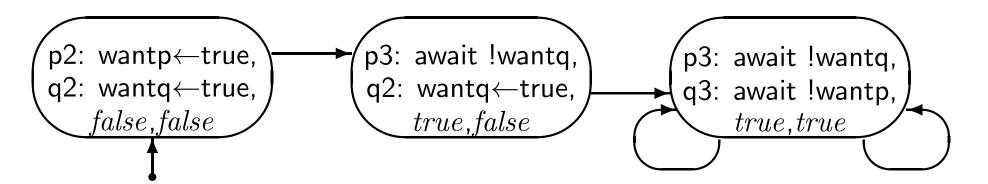
Process p	Process q	wantp	wantq
p1: await wantq=false	q1: await wantp=false	false	false
p2: wantp←true	q1: await wantp=false	false	false
p2: wantp←true	q2: wantq←true	false	false
p3: wantp←false	q3: wantq←true	true	false
p3: wantp←false	q3: wantq←false	true	true

	Algorithm 3.8: Third attempt				
	boolean wantp \leftarrow false, wantq \leftarrow false				
	p q				
	loop forever	forever loop forever			
p1:	non-critical section	q1:	non-critical section		
p2:	wantp ← true	q2:	wantq ← true		
p3:	await wantq = false	q3:	await wantp = false		
p4:	critical section	q4:	critical section		
p5:	wantp ← false	q5:	wantq ← false		

Scenario Showing Deadlock in the Third Attempt

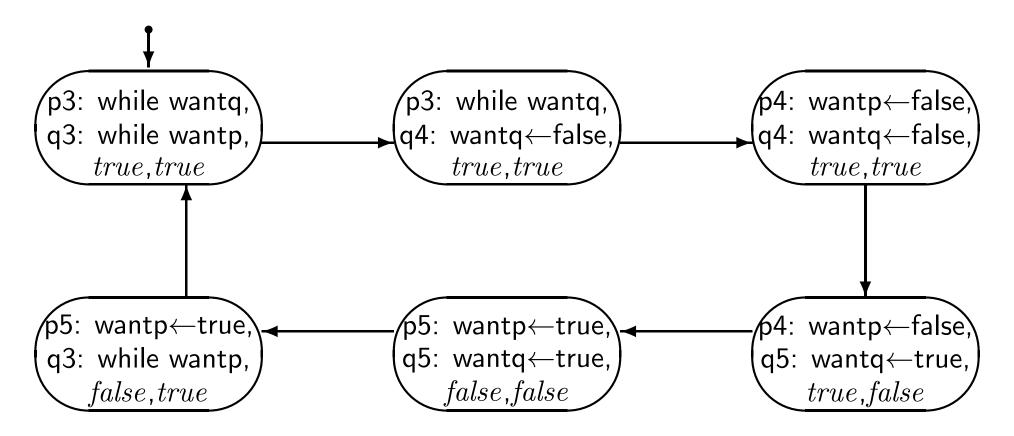
Process p	Process q	wantp	wantq
p1: non-critical section	q1: non-critical section	false	false
p2: wantp←true	q1: non-critical section	false	false
p2: wantp←true	q2: wantq←true	false	false
p3: await wantq=false	q2: wantq←true	true	false
p3: await wantq=false	q3: await wantp=false	true	true

Fragment of the State Diagram Showing Deadlock



	Algorithm 3.9: Fourth attempt				
	boolean wantp \leftarrow false, wantq \leftarrow false				
	p q				
loop forever			loop forever		
p1:	non-critical section	q1:	non-critical section		
p2:	wantp ← true	q2:	wantq \leftarrow true		
p3:	while wantq	q3:	while wantp		
p4:	$wantp \leftarrow false$	q4:	$wantq \leftarrow false$		
p5:	wantp ← true	q5:	$wantq \leftarrow true$		
p6:	critical section	q6:	critical section		
p7:	wantp ← false	q7:	wantq \leftarrow false		

Cycle in the State Diagram for the Fourth Attempt



	Algorithm 3.10: Dekker's algorithm				
	boolean wantp \leftarrow false, wantq \leftarrow false				
	integer turn $\leftarrow 1$				
	p				
loop forever loop forever			oop forever		
p1:	non-critical section	q1:	non-critical section		
p2:	wantp ← true	q2:	wantq \leftarrow true		
p3:	while wantq	q3:	while wantp		
p4:	if $turn = 2$	q4:	$if\;turn=1$		
p5:	$wantp \leftarrow false$	q5:	$wantq \leftarrow false$		
p6:	await turn $=1$	q6:	await turn $= 2$		
p7:	$wantp \leftarrow true$	q7:	$wantq \leftarrow true$		
p8:	critical section	q8:	critical section		
p9:	$turn \leftarrow 2$	q9:	$turn \leftarrow 1$		
p10:	wantp ← false	q10:	$wantq \leftarrow false$		

Algorithm 3.11: Critical section problem with test-and-set				
	integer common ← 0			
р			q	
	integer local1		integer local2	
	loop forever	loop forever		
p1:	non-critical section	q1:	non-critical section	
	repeat	repeat		
p2:	test-and-set(q2:	test-and-set(
	common, local1)		common, local2)	
p3:	until local $1=0$	q3:	until $local2 = 0$	
p4:	critical section	q4:	critical section	
p5:	$common \leftarrow 0$	q5:	$common \leftarrow 0$	

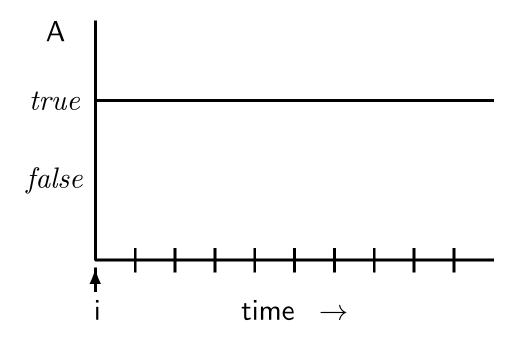
Algorithm 3.12: Critical section problem with exchange				
	integer common $\leftarrow 1$			
р		q		
ir	nteger local $1 \leftarrow 0$	ir	nteger local $2 \leftarrow 0$	
lo	oop forever	loop forever		
p1:	non-critical section	q1:	non-critical section	
repeat		repeat		
p2:	exchange(common, lo-	q2:	exchange(common, lo-	
cal1)		cal2)		
p3:	$until\ local 1 = 1$	q3:	until $local2 = 1$	
p4:	critical section	q4:	critical section	
p5:	exchange(common, local1)	q5:	exchange(common, local2)	

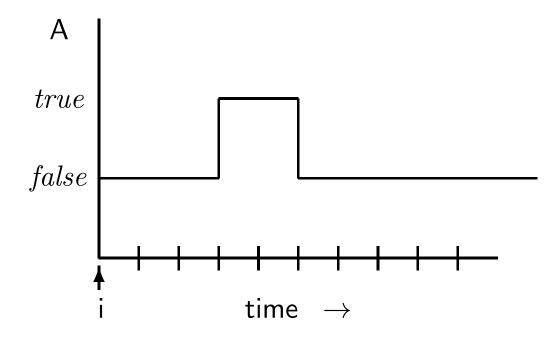
	Algorithm 3.13: Peterson's algorithm				
	boolean wantp \leftarrow false, wantq \leftarrow false				
	integer last \leftarrow 1				
	p q				
loop forever		loop forever			
p1:	non-critical section	q1:	non-critical section		
p2:	wantp ← true	q2:	wantq ← true		
p3:	$last \leftarrow 1$	q3:	$last \leftarrow 2$		
p4:	await wantq $=$ false or	q4:	await wantp $=$ false or		
	last = 2		last = 1		
p5:	critical section	q5:	critical section		
p6:	$wantp \leftarrow false$	q6:	$wantq \leftarrow false$		

	Algorithm 3.14: Manna-Pnueli algorithm				
	integer wantp \leftarrow 0, wantq \leftarrow 0				
	p		q		
loop forever			oop forever		
p1:	non-critical section	q1:	non-critical section		
p2:	if $wantq = -1$	q2:	if $wantp = -1$		
	$wantp \leftarrow -1$		wantq $\leftarrow 1$		
	else wantp $\leftarrow 1$		else wantq $\leftarrow -1$		
p3:	await wantq $ eq$ wantp	q3:	await wantp $ eq -$ wantq		
p4:	critical section	q4:	critical section		
p5:	wantp ← 0	q5:	wantq \leftarrow 0		

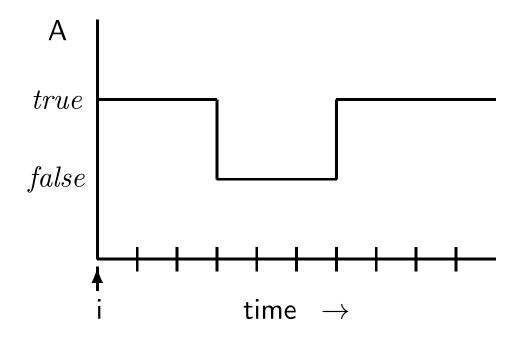
	Algorithm 3.15: Doran-Thomas algorithm				
	boolean wantp \leftarrow false, wantq \leftarrow false				
	integer turn $\leftarrow 1$				
	р		q		
lo	oop forever	I	oop forever		
p1:	non-critical section	q1:	non-critical section		
p2:	$wantp \leftarrow true$	q2:	wantq ← true		
p3:	if wantq	q3:	if wantp		
p4:	if $turn = 2$	q4:	$if\;turn=1$		
p5:	$wantp \leftarrow false$	q5:	$wantq \leftarrow false$		
p6:	await turn $=1$	q6:	await turn $= 2$		
p7:	$wantp \leftarrow true$	q7:	$wantq \leftarrow true$		
p8:	await wantq = false	q8:	await wantp = false		
p9:	critical section	q9:	critical section		
p10:	$wantp \leftarrow false$	q10:	$wantq \leftarrow false$		
p11:	$turn \leftarrow 2$	q11:	$turn \leftarrow 1$		

	Algorithm 4.1: Third attempt				
	boolean wantp \leftarrow false, wantq \leftarrow false				
	p q				
loop forever		loop forever			
p1:	non-critical section	q1:	non-critical section		
p2:	wantp ← true	q2:	wantq ← true		
p3:	await wantq = false	q3:	await wantp = false		
p4:	critical section	q4:	critical section		
p5:	wantp ← false	q5:	wantq ← false		

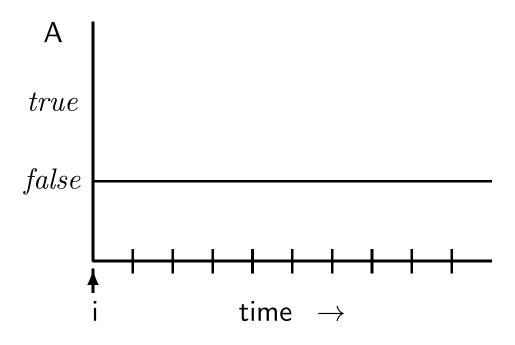


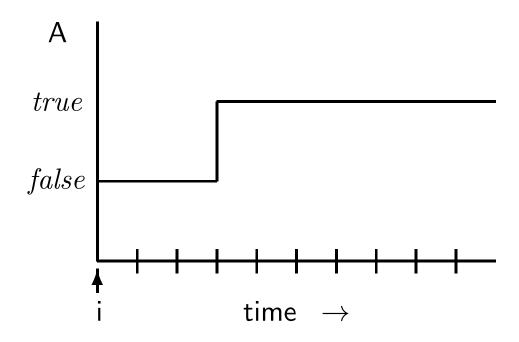


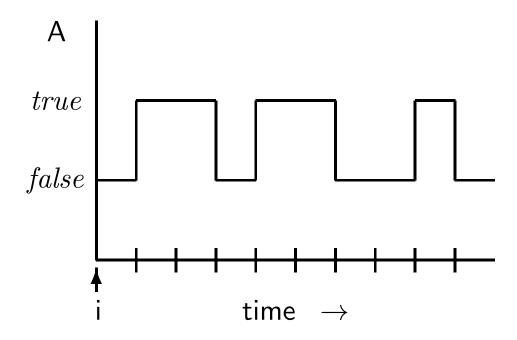
Duality: $\neg \Box A$

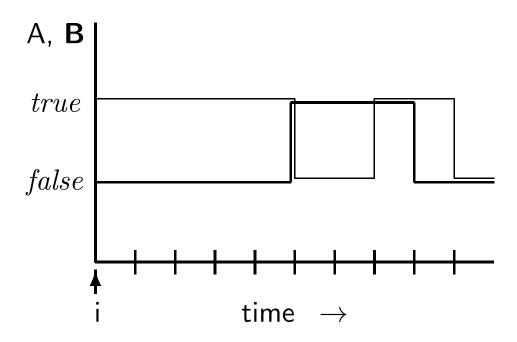


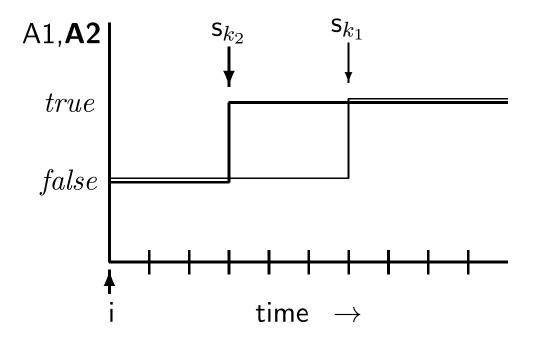
Duality: $\neg \Diamond A$

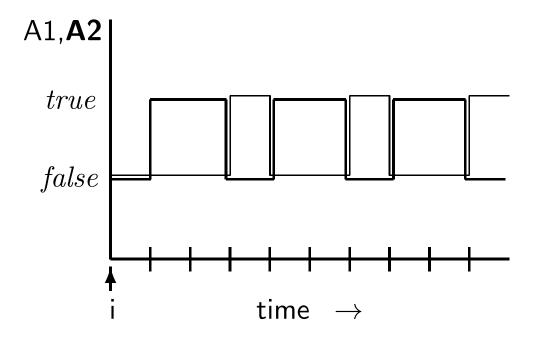




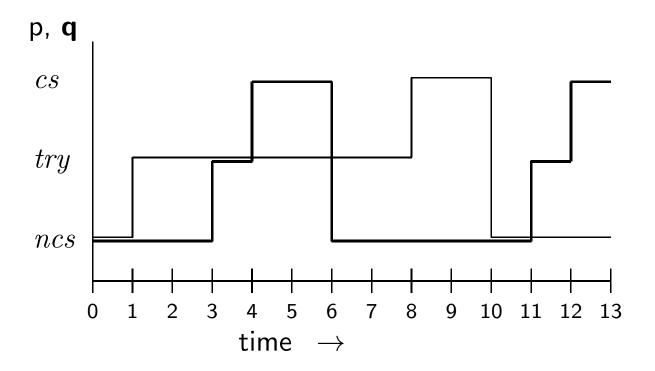








Overtaking: $try_p \rightarrow (\neg cs_q) \ \mathcal{W} \ (cs_q) \ \mathcal{W} \ (\neg cs_q) \ \mathcal{W} \ (cs_p)$



	Algorithm 4.2: Dekker's algorithm				
	boolean wantp \leftarrow false, wantq \leftarrow false				
	integer turn $\leftarrow 1$				
	р		q		
I	oop forever	I	oop forever		
p1:	non-critical section	q1:	non-critical section		
p2:	wantp \leftarrow true	q2:	wantq \leftarrow true		
p3:	while wantq	q3:	while wantp		
p4:	if $turn = 2$	q4:	$if\;turn=1$		
p5:	wantp ← false	q5:	$wantq \leftarrow false$		
p6:	await turn $=1$	q6:	await turn $= 2$		
p7:	$wantp \leftarrow true$	q7:	$wantq \leftarrow true$		
p8:	critical section	q8:	critical section		
p9:	$turn \leftarrow 2$	q9:	$turn \leftarrow 1$		
p10:	wantp ← false	q10:	$wantq \leftarrow false$		

Dekker's Algorithm in Promela

```
bool wantp = false, wantq = false;
    byte turn = 1;
3
    active proctype p() {
5
      do:: wantp = true;
        do :: !wantq -> break;
6
           :: else ->
              if :: (turn == 1)
8
                 :: (turn == 2) ->
9
                    wantp = false; (turn == 1); wantp = true
10
              fi
11
12
        od;
        printf ("MSC: p in CS\n");
13
        turn = 2; wantp = false
14
15
     od
16
```

Specifying Correctness in Promela

```
byte critical = 0;
3
    bool PinCS = false;
4
    #define nostarve PinCS /* LTL claim <> nostarve */
6
    active proctype p() {
     do ::
8
        /* preprotocol */
        critical ++;
10
   assert (critical \leq 1);
11
   PinCS = true;
12
   critical --;
13
     /* postprotocol */
14
15
    od
16
```

LTL Translation to Never Claims

```
never { /* !(<>nostarve) */
   accept_init :
   T0_init:
   if
  :: (! ((nostarve))) \rightarrow goto T0_init
   fi :
8
   never { /* !([]<>nostarve) */
    T0_init:
10
       if
11
:: (! ((nostarve))) \rightarrow goto accept_S4
13 :: (1) -> goto T0_init
   fi :
14
15
   accept_S4:
       if
16
:: (! ((nostarve))) \rightarrow goto accept\_S4
18 fi;
19 }
```

	Algorithm 5.1: Bakery algorithm (two processes)				
	integer np \leftarrow 0, nq \leftarrow 0				
p q					
loop forever		lo	oop forever		
p1:	non-critical section	q1:	non-critical section		
p2:	$np \leftarrow nq + 1$	q2:	$nq \leftarrow np + 1$		
p3:	await nq $=$ 0 or np \leq nq	q3:	await $np = 0$ or $nq < np$		
p4:	critical section	q4:	critical section		
p5:	$np \leftarrow 0$	q5:	nq ← 0		

```
Algorithm 5.2: Bakery algorithm (N processes)

integer array[1..n] number \leftarrow [0,...,0]

loop forever

p1: non-critical section

p2: number[i] \leftarrow 1 + max(number)

p3: for all other processes j

p4: await (number[j] = 0) or (number[i] \ll number[j])

p5: critical section

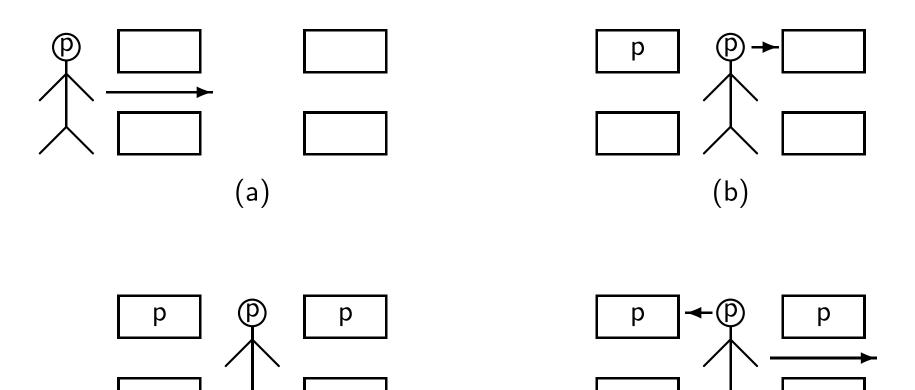
p6: number[i] \leftarrow 0
```

```
Algorithm 5.3: Bakery algorithm without atomic assignment
             boolean array[1..n] choosing \leftarrow [false,...,false]
             integer array[1..n] number \leftarrow [0,...,0]
     loop forever
       non-critical section
p1:
     choosing[i] \leftarrow true
p2:
    \mathsf{number[i]} \leftarrow 1 + \mathsf{max(number)}
p3:
    choosing[i] \leftarrow false
p4:
    for all other processes i
p5:
          await choosing[j] = false
p6:
          await (number[j] = 0) or (number[i] \ll number[j])
p7:
      critical section
p8:
       number[i] \leftarrow 0
p9:
```

	Algorithm 5.4: Fast algorithm for two processes (outline)			
	integer gate $1 \leftarrow 0$, gate $2 \leftarrow 0$			
	p	q		
	loop forever		loop forever	
	non-critical section		non-critical section	
p1:	$gate1 \leftarrow p$	q1:	$gate1 \leftarrow q$	
p2:	if $gate2 eq 0$ goto $p1$	q2:	if gate $2 eq 0$ goto q 1	
p3:	gate2 ← p	q3:	gate2 ← q	
p4:	if $gate1 \neq p$	q4:	if $gate1 \neq q$	
p5:	if gate2 \neq p goto p1	q5:	if gate $2 eq q$ goto $q1$	
	critical section		critical section	
p6:	gate2 ← 0	q6:	gate2 ← 0	

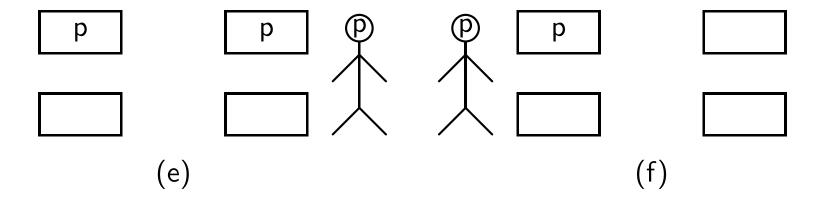
Fast Algorithm - No Contention (1)

(c)

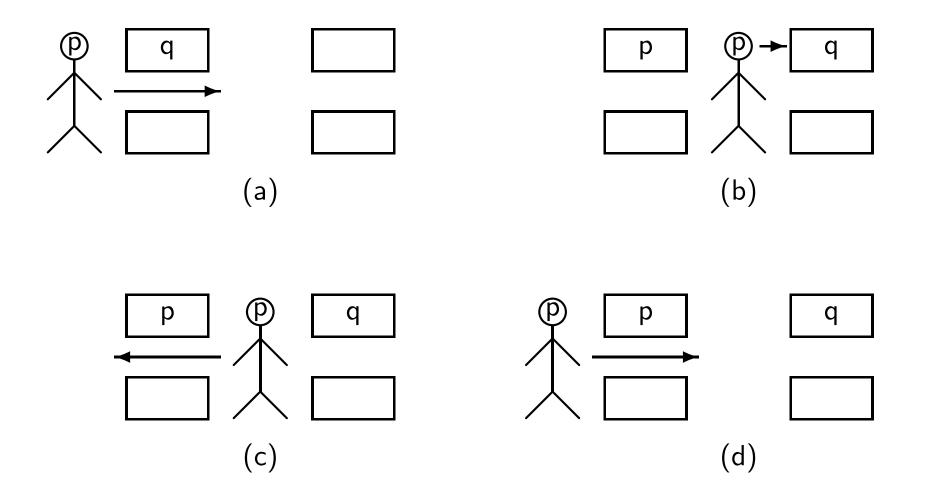


(d)

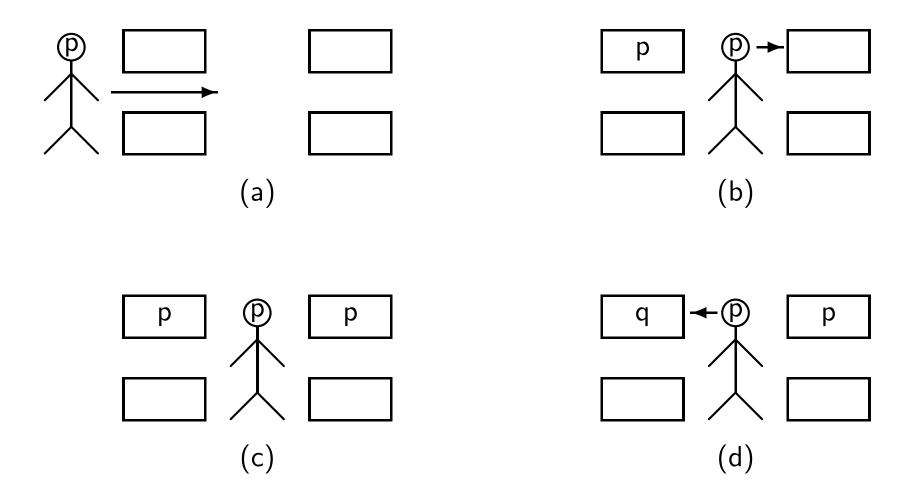
Fast Algorithm - No Contention (2)



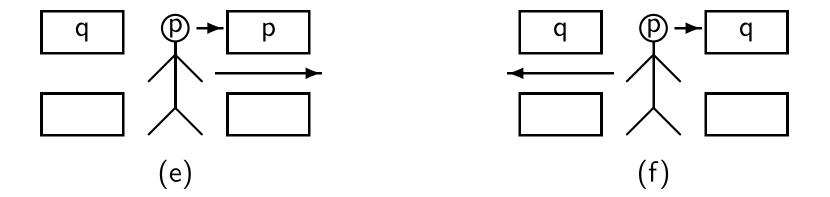
Fast Algorithm - Contention At Gate 2



Fast Algorithm - Contention At Gate 1 (1)



Fast Algorithm - Contention At Gate 1 (2)



	Algorithm 5.5: Fast algorithm for two processes (outline)			
	integer gate $1 \leftarrow 0$, gate $2 \leftarrow 0$			
	p	q		
	loop forever		loop forever	
	non-critical section		non-critical section	
p1:	$gate1 \leftarrow p$	q1:	$gate1 \leftarrow q$	
p2:	if $gate2 eq 0$ goto $p1$	q2:	if gate $2 eq 0$ goto q 1	
p3:	gate2 ← p	q3:	gate2 ← q	
p4:	if $gate1 \neq p$	q4:	if $gate1 \neq q$	
p5:	if gate2 \neq p goto p1	q5:	if gate $2 eq q$ goto $q1$	
	critical section		critical section	
p6:	gate2 ← 0	q6:	gate2 ← 0	

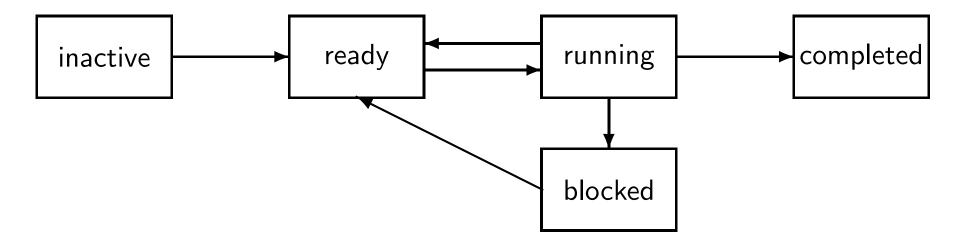
	Algorithm 5.6: Fast algorithm for two processes				
	integer gate $1 \leftarrow 0$, gate $2 \leftarrow 0$				
	boolean wantp \leftarrow	false, v	wantq ← false		
	p	q			
p1:	$gate1 \leftarrow p$	q1:	$gate1 \leftarrow q$		
	$wantp \leftarrow true$		wantq ← true		
p2:	if gate $2 \neq 0$	q2:	if gate $2 \neq 0$		
	wantp \leftarrow false		wantq ← false		
	goto p1		goto q1		
p3:	gate2 ← p	q3:	gate2 ← q		
p4:	if $gate1 eq p$	q4:	if $gate1 \neq q$		
	$wantp \leftarrow false$		wantq ← false		
	await wantq = false		await wantp = false		
p5:	if gate2 $ eq$ p goto p1	q5:	if gate2 \neq q goto q1		
	else wantp \leftarrow true		else wantq ← true		
	critical section		critical section		
p6:	$gate2 \leftarrow 0$	q6:	gate2 ← 0		
	wantp ← false		wantq ← false		

```
Algorithm 5.7: Fisher's algorithm
                           integer gate \leftarrow 0
    loop forever
       non-critical section
       loop
         await gate = 0
p1:
p2:
       gate ← i
       delay
p3:
       until gate = i
p4:
       critical section
       gate \leftarrow 0
p5:
```

```
Algorithm 5.8: Lamport's one-bit algorithm
              boolean array[1..n] want \leftarrow [false,...,false]
    loop forever
       non-critical section
    want[i] ← true
p1:
     for all processes j į i
p2:
      if want[j]
p3:
             want[i] \leftarrow false
p4:
             await not want[j]
p5:
             goto p1
       for all processes j į i
p6:
          await not want[j]
p7:
       critical section
       want[i] \leftarrow false
p8:
```

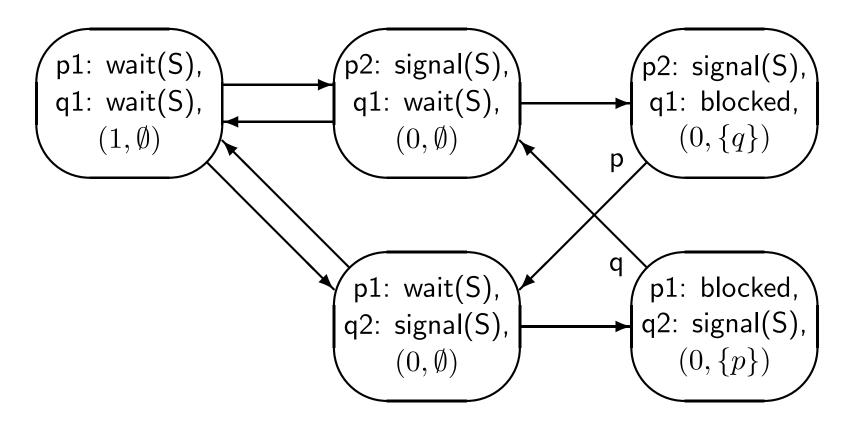
Algorithm 5.9: Manna-Pnueli central server algorithm integer request $\leftarrow 0$, respond $\leftarrow 0$ client process i loop forever non-critical section while respond \neq i p1: request \leftarrow i p2: critical section respond $\leftarrow 0$ p3: server process loop forever await request $\neq 0$ p4: $respond \leftarrow request$ p5: await respond = 0p6: request $\leftarrow 0$ p7:

State Changes of a Process



Α	Algorithm 6.1: Critical section with semaphores (two processes)			
	binary semaphore $S \leftarrow (1,\emptyset)$			
	p	q		
loop forever		loop forever		
p1:	non-critical section	q1:	non-critical section	
p2:	wait(S)	q2:	wait(S)	
p3:	critical section	q3:	critical section	
p4:	signal(S)	q4:	signal(S)	

State Diagram for the Semaphore Solution



Algorithm 6.3: Critical section with semaphores (N proc.)

binary semaphore $S \leftarrow (1, \emptyset)$

loop forever

p1: non-critical section

p2: wait(S)

p3: critical section

p4: signal(S)

Algorithm 6.4: Critical section with semaphores (N proc., abbrev.)

binary semaphore $S \leftarrow (1, \emptyset)$

loop forever

p1: wait(S)

p2: signal(S)

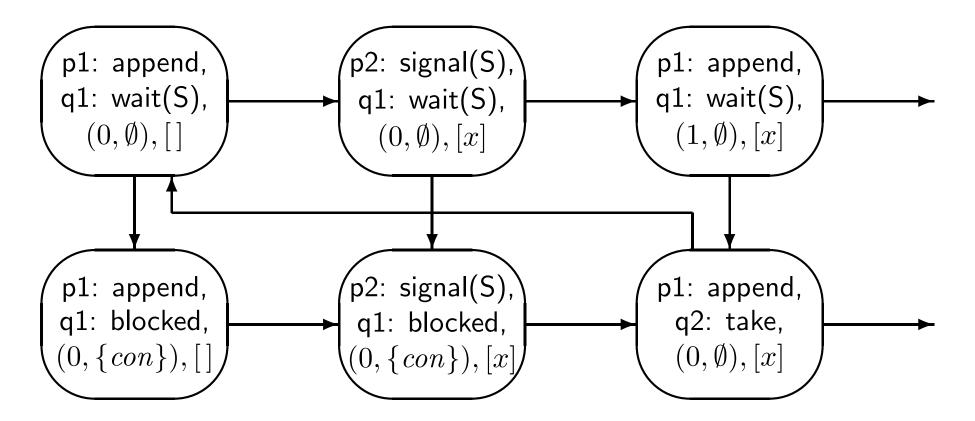
Scenario for Starvation

n	Process p	Process q	Process r	S
1	p1: wait(S)	q1: wait(S)	r1: wait(S)	$(1,\emptyset)$
2	p2: signal(S)	q1: wait(S)	r1: wait(S)	$(0,\emptyset)$
3	p2: signal(S)	q1: blocked	r1: wait(S)	$(0,\{q\})$
4	p1: signal(S)	q1: blocked	r1: blocked	$(0,\{q,r\})$
5	p1: wait(S)	q1: blocked	r2: signal(S)	$(0,\{q\})$
6	p1: blocked	q1: blocked	r2: signal(S)	$(0, \{p, q\})$
7	p2: signal(S)	q1: blocked	r1: wait(S)	$(0,\{q\})$

Algorithm 6.5: Mergesort				
integer array A				
binary semaphore $S1 \leftarrow (0,\emptyset)$				
binary semaphore S2 $\leftarrow (0, \emptyset)$				
sort1	sort2	merge		
p1: sort 1st half of A	q1: sort 2nd half of A	r1: wait(S1)		
p2: signal(S1)	q2: signal(S2)	r2: wait(S2)		
p3:	q3:	r3: merge halves of A		

Algorithm 6.6: Producer-consumer (infinite buffer)				
infinite queue of dataType buffer \leftarrow empty queue				
semaphore notEmpty $\leftarrow (0,\emptyset)$				
producer	consumer			
dataType d	dataType d			
loop forever	loop forever			
p1: d ← produce	q1: wait(notEmpty)			
p2: append(d, buffer)	q2: $d \leftarrow take(buffer)$			
p3: signal(notEmpty)	q3: consume(d)			

Partial State Diagram for Producer-Consumer with Infinite Buffer



Algorithm 6.7: Producer-consumer (infinite buffer, abbreviated)				
infinite queue of dataType buffer \leftarrow empty queue				
semaphore notEmpty $\leftarrow (0,\emptyset)$				
producer	consumer			
dataType d	dataType d			
loop forever	loop forever			
p1: append(d, buffer)	q1: wait(notEmpty)			
p2: signal(notEmpty)	q2: $d \leftarrow take(buffer)$			

Algorithm 6.8: Producer-consumer (finite buffer, semaphores)

finite queue of dataType buffer ← empty queue semaphore notEmpty $\leftarrow (0, \emptyset)$ semaphore notFull $\leftarrow (N, \emptyset)$

producer			consumer
dataType d		dataType d	
loop forever			loop forever
p1:	$d \leftarrow produce$	q1:	wait(notEmpty)
p2:	wait(notFull)	q2:	$d \leftarrow take(buffer)$
p3:	append(d, buffer)	q3:	signal(notFull)
p4:	signal(notEmpty)	q4:	consume(d)

Scenario with Busy Waiting

n	Process p	Process q	S
1	p1: wait(S)	q1: wait(S)	1
2	p2: signal(S)	q1: wait(S)	0
3	p2: signal(S)	q1: wait(S)	0
4	p1: wait(S)	q1: wait(S)	1

Algorithm 6.9: Dining philosophers (outline)

loop forever

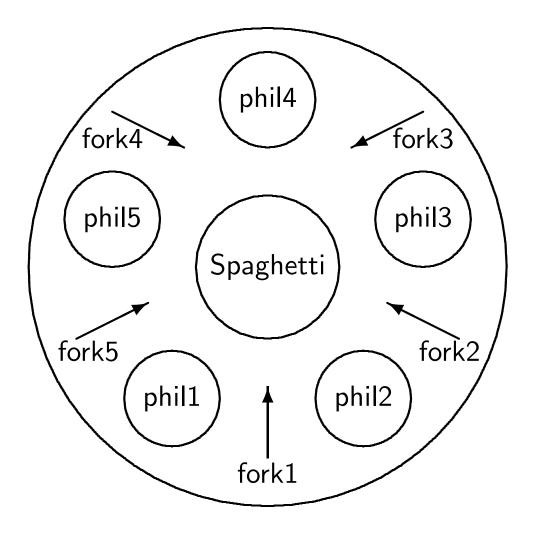
think p1:

preprotocol p2:

p3: eat

postprotocol p4:

The Dining Philosophers



```
Algorithm 6.11: Dining philosophers (second attempt)
              semaphore array [0..4] fork \leftarrow [1,1,1,1,1]
              semaphore room \leftarrow 4
    loop forever
      think
p1:
    wait(room)
p2:
   wait(fork[i])
p3:
   wait(fork[i+1])
p4:
    eat
p5:
   signal(fork[i])
p6:
   signal(fork[i+1])
p7:
```

signal(room)

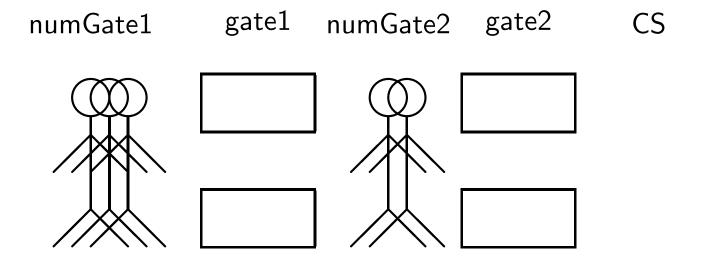
p8:

Algorithm 6.12: Dining philosophers (third attempt) semaphore array [0..4] fork $\leftarrow [1,1,1,1,1]$ philosopher 4 loop forever think p1: wait(fork[0]) p2: wait(fork[4]) p3: p4: eat signal(fork[0]) p5: signal(fork[4]) p6:

```
Algorithm 6.13: Barz's algorithm for simulating general semaphores
                         binary semaphore S \leftarrow 1
                         binary semaphore gate \leftarrow 1
                        integer count \leftarrow k
     loop forever
        non-critical section
       wait(gate)
p1:
     wait(S)
                                                // Simulated wait
p2:
    \mathsf{count} \leftarrow \mathsf{count} - 1
p3:
     if count > 0 then
p4:
       signal(gate)
p5:
       signal(S)
p6:
       critical section
      wait(S)
                                               // Simulated signal
p7:
      \mathsf{count} \leftarrow \mathsf{count} + 1
p8:
     if count = 1 then
p9:
       signal(gate)
p10:
       signal(S)
p11:
```

```
Algorithm 6.14: Udding's starvation-free algorithm
                    semaphore gate 1 \leftarrow 1, gate 2 \leftarrow 0
                    integer numGate1 \leftarrow 0, numGate2 \leftarrow 0
       wait(gate1)
p1:
       \mathsf{numGate1} \leftarrow \mathsf{numGate1} + 1
p2:
    signal(gate1)
p3:
    wait(gate1)
p4:
      \mathsf{numGate2} \leftarrow \mathsf{numGate2} + 1
p5:
        \mathsf{numGate1} \leftarrow \mathsf{numGate1} - 1
                                                  // Statement is missing in the
book
       if numGate1 ; 0
p6:
     signal(gate1)
p7:
    else signal(gate2)
p8:
      wait(gate2)
p9:
       numGate2 \leftarrow numGate2 - 1
p10:
        critical section
       if numGate2 ¿ 0
p11:
      signal(gate2)
p12:
       else signal(gate1)
p13:
```

Udding's Starvation-Free Algorithm



Scenario for Starvation in Udding's Algorithm

n	Process p	Process q	gate1	gate2	nGate1	nGate2
1	p4: wait(g1)	q4: wait(g1)	1	0	2	0
2	p9: wait(g2)	q9: wait(g2)	0	1	0	2
3	CS	q9: wait(g2)	0	0	0	1
4	p12: signal(g2)	q9: wait(g2)	0	0	0	1
5	p1: wait(g1)	CS	0	0	0	0
6	p1: wait(g1)	q13: signal(g1)	0	0	0	0
7	p1: blocked	q13: signal(g1)	0	0	0	0
8	p4: wait(g1)	q1: wait(g1)	1	0	1	0
9	p4: wait(g1)	q4: wait(g1)	1	0	2	0

Semaphores in Java

```
import java. util . concurrent. Semaphore;
    class CountSem extends Thread {
      static volatile int n = 0;
 3
      static Semaphore s = new Semaphore(1);
 4
 5
      public void run() {
 6
        int temp;
        for (int i = 0; i < 10; i++) {
8
9
          try {
            s.acquire();
10
11
12
          catch (InterruptedException e) {}
13
          temp = n;
          n = temp + 1;
14
          s. release ();
15
16
17
18
      public static void main(String[] args) {
19
          /* As before */
20
21
22
```

Semaphores in Ada

```
protected type Semaphore(Initial : Natural) is
      entry Wait;
2
      procedure Signal;
3
    private
4
5
      Count: Natural := Initial :
    end Semaphore;
6
7
    protected body Semaphore is
8
      entry Wait when Count > 0 is
9
10
      begin
11
        Count := Count - 1;
12
      end Wait;
13
      procedure Signal is
14
15
      begin
        Count := Count + 1;
16
        end Signal;
17
18
    end Semaphore;
```

Busy-Wait Semaphores in Promela

```
1 inline wait( s ) {
2     atomic { s > 0 ; s-- }
3  }
4
5 inline signal ( s ) { s++ }
```

Weak Semaphores in Promela (3 processes) (1)

```
typedef Semaphore {
           byte count;
           bool blocked[NPROCS];
4
5
   inline initSem(S, n) {
     S.count = n
8
```

Weak Semaphores in Promela (3 processes) (2)

```
inline wait(S) {
       atomic {
        if
        :: S.count >= 1 -> S.count --
   :: else ->
             S.blocked[\_pid -1] = true;
            !S.blocked[\_pid-1]
      fi
8
9
10
11
    inline signal (S) {
12
       atomic {
13
        if
14
        :: S.blocked[0] -> S.blocked[0] = false
15
        :: S.blocked[1] -> S.blocked[1] = false
        :: S.blocked[2] -> S.blocked[2] = false
17
:: else -> S.count++
19
        fi
20
21
```

Weak Semaphores in Promela (N processes) (1)

```
typedef Semaphore {
            byte count;
            bool blocked[NPROCS];
    byte i, choice;
4
 5
6
    inline initSem(S, n) {
      S.count = n
8
9
10
    inline wait(S) {
11
       atomic {
12
         if
13
         :: S.count >= 1 -> S.count --
14
         :: else ->
15
              S. blocked [-pid -1] = true;
16
              !S.blocked[\_pid-1]
17
18
         fi
19
20
```

Weak Semaphores in Promela (N processes) (2)

```
inline signal (S) {
       atomic {
        S.i = 0;
         S.choice = 255;
         do
         :: (S.i == NPROCS) \rightarrow break
         :: (S.i < NPROCS) && !S.blocked[S.i] -> S.i++
         :: else ->
             if
             :: (S.choice == 255) -> S.choice = S.i
10
             :: (S.choice != 255) -> S.choice = S.i
11
             :: (S.choice != 255) ->
12
13
             fi:
             S.i++
14
15
      od;
         if
16
         :: S.choice == 255 -> S.count++
17
         :: else -> S.blocked[S.choice] = false
18
         fi
19
20
21
```

Barz's Algorithm in Promela (N processes, K in CS)

```
byte gate = 1;
   int count = K;
3
    active [N] proctype P () {
5
      do ::
        atomic \{ \text{ gate} > 0; \text{ gate} --; \}
        d_step {
7
8
         count——;
9
     :: count > 0 -> gate++
10
         :: else
11
12
13
   /* Critical section */
14
15 d_step {
16
     count++;
         if
17
18
   :: count == 1 -> gate++
19
          :: else
         fi
20
21
22
      od
23
```

Algorithm 6.15: Semaphore algorithm A			
semaphore S \leftarrow 1, semaphore T \leftarrow 0			
p q			
p1: wait(S)	q1: $wait(T)$		
p2: write("p")	q1: wait(T) q2: write("q")		
p3: signal(T)	q3: signal(S)		

Algorithm 6.16: Semaphore algorithm B				
semaphore S1 \leftarrow 0, S2 \leftarrow 0				
p q r				
p1: write("p")	q1: wait(S1)	r1: wait(S2)		
p2: signal(S1)	q2: write("q")	r2: write("r")		
p3: signal(S2)	q3:	r3:		

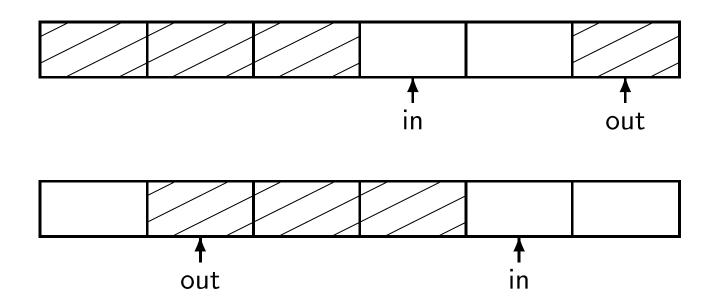
Algorithm 6.17: Semaphore algorithm with a loop			
semaphore $S \leftarrow 1$			
boolean B \leftarrow false			
p q			
p1: wait(S)	q1: wait(S)		
p2: B ← true	q2: while not B		
p3: signal(S)	q3: write("*")		
p4:	q4: signal(S)		

Algorithm 6.18: Critical section problem (k out of N processes)

binary semaphore $S \leftarrow 1$, delay $\leftarrow 0$ integer count $\leftarrow k$

```
integer m
     loop forever
        non-critical section
p1:
    wait(S)
p2:
    \mathsf{count} \leftarrow \mathsf{count} - 1
p3:
p4:
    \mathsf{m} \leftarrow \mathsf{count}
    signal(S)
p5:
    if \mathsf{m} \leq -1 wait(delay)
p6:
     critical section
p7:
    wait(S)
p8:
p9: count \leftarrow count + 1
p10: if count \leq 0 signal(delay)
       signal(S)
p11:
```

Circular Buffer



Algorithm 6.19: Producer-consumer (circular buffer)				
dataType array [0N] buffer				
integer in, out \leftarrow 0				
semaphore notEn	$npty \leftarrow (0,\emptyset)$			
semaphore notFull $\leftarrow (N, \emptyset)$				
producer	consumer			
dataType d	dataType d			
loop forever	loop forever			
p1: d ← produce	q1: wait(notEmpty)			
p2: wait(notFull)	q2: $d \leftarrow buffer[out]$			
p3: buffer[in] \leftarrow d	q3: out \leftarrow (out $+1$) modulo N			
p4: in \leftarrow (in+1) modulo N	q4: signal(notFull)			
p5: signal(notEmpty)	q5: consume(d)			

```
Algorithm 6.20: Simulating general semaphores
                  binary semaphore S \leftarrow 1, gate \leftarrow 0
                  integer count \leftarrow 0
    wait
p1: wait(S)
p2: count \leftarrow count -1
p3: if count < 0
p4: signal(S)
p5: wait(gate)
p6: else signal(S)
    signal
p7: wait(S)
p8: count \leftarrow count + 1
p9: if count \leq 0
p10: signal(gate)
p11: signal(S)
```

Weak Semaphores in Promela with Channels

```
typedef Semaphore {
             byte count;
             chan ch = [NPROCS] of \{ pid \};
             byte temp, i;
4
 5
    inline initSem(S, n) { S.count = n }
    inline wait(S) {
        atomic {
8
          :: S.count >= 1 -> S.count --;
          :: else -> S.ch!_pid; !(S.ch ?? [eval(_pid)])
11
12
13
14
    inline signal (S) {
15
        atomic {
16
         S.i = len(S.ch);
17
          if
18
          :: S.i == 0 -> S.count++ /*No blocked process, increment count*/
19
          :: else −>
20
                  do
21
            :: S.i == 1 -> S.ch? _; break /*Remove only blocked process*/
22
            :: else -> S.i--;
Principles of Concurrent and Distributed Programming. Slides © 2006 by M. Ben-Ari.
23
24
```

Algorithm 6.21: Readers and writers with semaphores

```
semaphore readerSem \leftarrow 0, writerSem \leftarrow 0
integer delayedReaders \leftarrow 0, delayedWriters \leftarrow 0
semaphore entry \leftarrow 1
integer readers \leftarrow 0, writers \leftarrow 0
```

SignalProcess

```
if writers = 0 or delayedReaders > 0
  delayedReaders \leftarrow delayedReaders - 1
  signal(readerSem)
else if readers = 0 and writers = 0 and delayedWriters > 0
  delayedWriters \leftarrow delayedWriters - 1
  signal(writerSem)
else signal(entry)
```

Algorithm 6.21: Readers and writers with semaphores

StartRead

```
wait(entry)
```

```
p2: if writers > 0
```

 $\mathsf{delayedReaders} \leftarrow \mathsf{delayedReaders} + 1$ p3:

signal(entry) p4:

wait(readerSem) p5:

p6: readers \leftarrow readers + 1

p7: SignalProcess

EndRead

```
p8: wait(entry)
```

p9: readers \leftarrow readers -1

p10: SignalProcess

Algorithm 6.21: Readers and writers with semaphores

StartWrite

```
p11: wait(entry)
p12: if writers > 0 or readers > 0
```

p13: $delayedWriters \leftarrow delayedWriters + 1$

```
p14: signal(entry)
```

p15: wait(writerSem)

p16: writers \leftarrow writers + 1

p17: SignalProcess

EndWrite

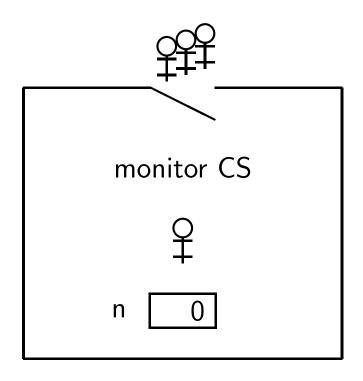
```
p18: wait(entry)
```

p19: writers \leftarrow writers -1

p20: SignalProcess

Algorithm 7.1: Atomicity of monitor operations		
monitor CS integer $n \leftarrow 0$		
operation increment integer temp temp \leftarrow n n \leftarrow temp $+$ 1		
р	q	
p1: CS.increment	q1: CS.increment	

Executing a Monitor Operation

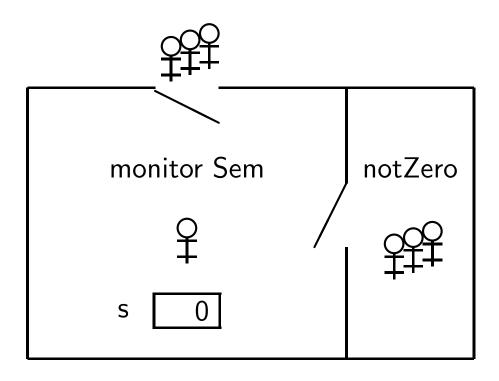


Algorithm 7.2: Semaphore simulated with a monitor

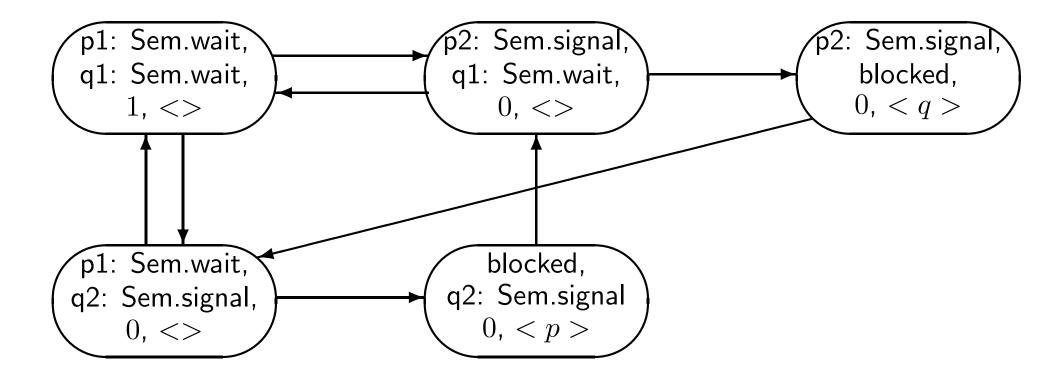
```
monitor Sem
   integer s \leftarrow k
   condition notZero
   operation wait
      if s = 0
          waitC(notZero)
      \mathsf{s} \leftarrow \mathsf{s} - \mathsf{1}
   operation signal
      s \leftarrow s + 1
      signalC(notZero)
```

р			q
	loop forever	loop forever	
	non-critical section	non-critical section	
p1:	Sem.wait	q1:	Sem.wait
	critical section		critical section
p2:	Sem.signal	q2:	Sem.signal

Condition Variable in a Monitor



State Diagram for the Semaphore Simulation



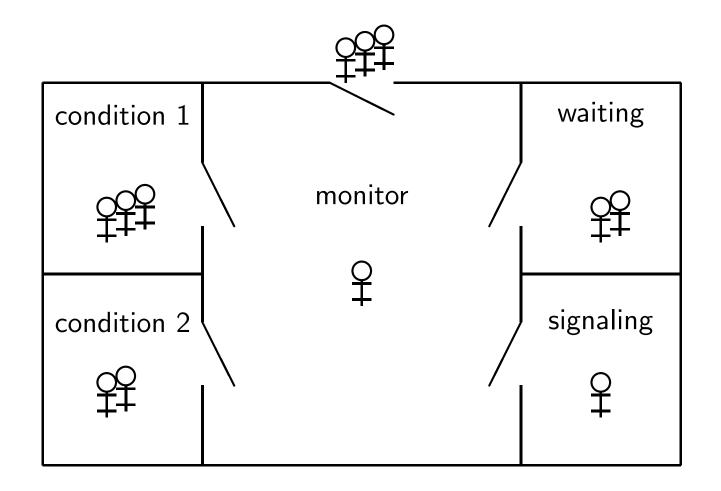
Algorithm 7.3: Producer-consumer (finite buffer, monitor)

```
monitor PC
  bufferType buffer ← empty
  condition notEmpty
  condition notFull
  operation append(datatype V)
     if buffer is full
       waitC(notFull)
     append(V, buffer)
     signalC(notEmpty)
  operation take()
     datatype W
     if buffer is empty
       waitC(notEmpty)
     W \leftarrow head(buffer)
     signalC(notFull)
     return W
```

Algorithm 7.3: Producer-consumer (finite buffer, monitor) (continued)

producer	consumer
datatype D	datatype D
loop forever	loop forever
p1: $D \leftarrow produce$	q1: $D \leftarrow PC.take$
p2: PC.append(D)	q2: consume(D)

The Immediate Resumption Requirement



Algorithm 7.4: Readers and writers with a monitor

```
monitor RW
  integer readers \leftarrow 0
  integer writers \leftarrow 0
  condition OKtoRead, OKtoWrite
  operation StartRead
     if writers \neq 0 or not empty(OKtoWrite)
        waitC(OKtoRead)
     readers \leftarrow readers + 1
     signalC(OKtoRead)
  operation EndRead
     readers \leftarrow readers -1
     if readers = 0
        signalC(OKtoWrite)
```

Algorithm 7.4: Readers and writers with a monitor (continued)

```
operation StartWrite
   if writers \neq 0 or readers \neq 0
      waitC(OKtoWrite)
   writers \leftarrow writers + 1
```

operation EndWrite writers \leftarrow writers -1if empty(OKtoRead) then signalC(OKtoWrite) else signalC(OKtoRead)

reader	writer
p1: RW.StartRead	q1: RW.StartWrite
p2: read the database	q2: write to the database
p3: RW.EndRead	q3: RW.EndWrite

Algorithm 7.5: Dining philosophers with a monitor

```
monitor ForkMonitor
   integer array[0..4] fork \leftarrow [2, ..., 2]
  condition array[0..4] OKtoEat
  operation takeForks(integer i)
     if fork[i] \neq 2
        waitC(OKtoEat[i])
     fork[i+1] \leftarrow fork[i+1] - 1
     fork[i-1] \leftarrow fork[i-1] - 1
  operation releaseForks(integer i)
     fork[i+1] \leftarrow fork[i+1] + 1
     fork[i-1] \leftarrow fork[i-1] + 1
     if fork[i+1] = 2
        signalC(OKtoEat[i+1])
     if fork[i-1] = 2
        signalC(OKtoEat[i-1])
```

Algorithm 7.5: Dining philosophers with a monitor (continued)

philosopher i

loop forever

p1: think

p2: takeForks(i)

p3: eat

p4: releaseForks(i)

Scenario for Starvation of Philosopher 2

n	phil1	phil2	phil3	f0	f1	f2	f3	f4
1	take(1)	take(2)	take(3)	2	2	2	2	2
2	release(1)	take(2)	take(3)	1	2	1	2	2
3	release(1)	take(2) and	release(3)	1	2	0	2	1
		waitC(OK[2])						
4	release(1)	(blocked)	release(3)	1	2	0	2	1
5	take(1)	(blocked)	release(3)	2	2	1	2	1
6	release(1)	(blocked)	release(3)	1	2	0	2	1
7	release(1)	(blocked)	take(3)	1	2	1	2	2

Readers and Writers in C

```
monitor RW {
      int readers = 0, writing = 1;
      condition OKtoRead, OKtoWrite;
 3
 4
      void StartRead() {
 5
        if (writing || !empty(OKtoWrite)) waitc(OKtoRead);
 6
        readers = readers + 1;
        signalc (OKtoRead);
8
9
      void EndRead() {
10
        readers = readers - 1;
11
        if (readers == 0) signalc (OKtoWrite);
12
13
14
      void StartWrite() {
15
        if (writing || (readers != 0)) waitc(OKtoWrite);
16
        writing = 1;
17
18
      void EndWrite() {
19
        writing = 0;
20
        if (empty(OKtoRead)) signalc(OKtoWrite);
21
        else
                             signalc (OKtoRead);
22
23
24
```

Algorithm 7.6: Readers and writers with a protected object

```
\begin{array}{l} \text{protected object RW} \\ \text{integer readers} \leftarrow 0 \\ \text{boolean writing} \leftarrow \text{false} \\ \text{operation StartRead when not writing} \\ \text{readers} \leftarrow \text{readers} + 1 \\ \text{operation EndRead} \\ \text{readers} \leftarrow \text{readers} - 1 \\ \text{operation StartWrite when not writing and readers} = 0 \\ \text{writing} \leftarrow \text{true} \end{array}
```

operation EndWrite writing ← false

reader			writer
loop forever			loop forever
p1:	RW. Start Read	q1:	RW.StartWrite
p2:	read the database	q2:	write to the database
p3:	RW.EndRead	q3:	RW.EndWrite

Context Switches in a Monitor

Process reader	Process writer
waitC(OKtoRead)	operation EndWrite
(blocked)	writing \leftarrow false
(blocked)	signalC(OKtoRead)
$ readers \leftarrow readers + 1 $	return from EndWrite
signalC(OKtoRead)	return from EndWrite
read the data	return from EndWrite
read the data	

Context Switches in a Protected Object

Process reader	Process writer
when not writing	operation EndWrite
(blocked)	writing \leftarrow false
(blocked)	when not writing
(blocked)	$readers \leftarrow readers + 1$
read the data	

Simple Readers and Writers in Ada

```
protected RW is
      procedure Write(I: Integer );
      function Read return Integer;
3
    private
4
      N: Integer := 0;
    end RW;
6
    protected body RW is
8
      procedure Write(I: Integer ) is
9
10
      begin
11
      N := I;
      end Write;
12
      function Read return Integer is
13
      begin
14
        return N;
15
      end Read;
16
    end RW;
17
```

Readers and Writers in Ada (1)

```
protected RW is
         entry StartRead;
2
         procedure EndRead;
3
         entry Startwrite ;
4
         procedure EndWrite;
5
      private
6
         Readers: Natural :=0;
7
         Writing: Boolean := false;
8
      end RW;
9
```

Readers and Writers in Ada (2)

```
protected body RW is
 1
 2
          entry StartRead
            when not Writing is
 3
          begin
4
             Readers = Readers + 1:
 5
          end StartRead;
 6
          procedure EndRead is
8
9
          begin
10
             Readers = Readers - 1;
          end EndRead;
11
12
          entry StartWrite
13
            when not Writing and Readers = 0 is
14
15
          begin
             Writing := true;
16
          end StartWrite;
17
18
          procedure EndWrite is
19
20
          begin
             Writing := false ;
21
          end EndWrite;
22
       end RW:
23
```

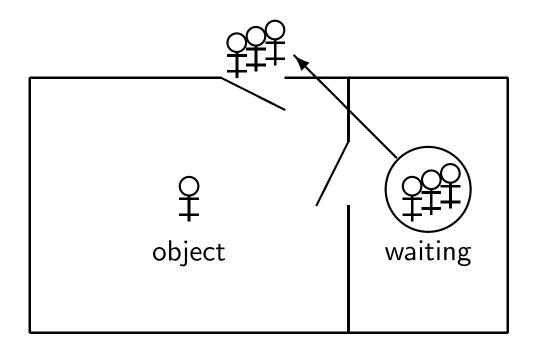
Producer-Consumer in Java (1)

```
class PCMonitor {
      final int N = 5;
      int Oldest = 0, Newest = 0;
      volatile int Count = 0;
      int Buffer[] = new int[N];
 6
      synchronized void Append(int V) {
 7
        while (Count == N)
8
9
          try {
             wait();
10
          } catch (InterruptedException e) {}
11
        Buffer [Newest] = V;
12
        Newest = (Newest + 1) \% N;
13
        Count = Count + 1;
14
        notifyAll ();
15
16
```

Producer-Consumer in Java (2)

```
synchronized int Take() {
        int temp;
        while (Count == 0)
4
          try {
             wait();
 5
          } catch (InterruptedException e) {}
6
        temp = Buffer[Oldest];
        Oldest = (Oldest + 1) \% N;
8
        Count = Count - 1;
9
        notifyAll ();
10
11
        return temp;
12
13
```

A Monitor in Java With notifyAll



Java Monitor for RW (try-catch omitted)

```
class RWMonitor {
      volatile int readers = 0;
      volatile boolean writing = false;
 4
 5
      synchronized void StartRead() {
        while (writing ) wait();
 6
        readers = readers + 1;
        notifyAll ();
8
9
      synchronized void EndRead() {
10
        readers = readers - 1;
11
        if (readers == 0) notifyAll();
12
13
14
      synchronized void StartWrite() {
15
        while (writing || (readers != 0)) wait();
16
        writing = true;
17
18
      }
19
      synchronized void EndWrite() {
20
        writing = false;
21
        notifyAll ();
22
23
24
```

Simulating Monitors in Promela (1)

```
bool lock = false;
    typedef Condition {
       bool gate;
4
       byte waiting;
 5
6
 7
    #define emptyC(C) (C.waiting == 0)
8
9
    inline enterMon() {
10
       atomic {
11
          !lock;
12
          lock = true;
13
14
15
16
    inline leaveMon() {
17
      lock = false;
18
19
```

Simulating Monitors in Promela (2)

```
inline waitC(C) {
      atomic {
2
         C.waiting ++;
         lock = false; /* Exit monitor */
     C.gate; /* Wait for gate */
   lock = true; /* IRR */
   C.gate = false; /* Reset gate */
   \mathsf{C.waiting} --;
9
10
11
    inline signalC(C) {
12
      atomic {
13
         if
14
            /* Signal only if waiting */
15
         :: (C.waiting > 0) \rightarrow
16
         C.gate = true;
17
           !lock; /* IRR - wait for released lock */
18
           lock = true; /* Take lock again */
19
         :: else
20
         fi ;
21
22
23
```

Readers and Writers in Ada (1)

```
protected RW is
1
        entry Start_Read;
        procedure End_Read;
3
        entry Start_Write;
4
        procedure End_Write;
5
6
      private
        Waiting_To_Read : integer := 0;
        Readers : Natural := 0;
8
        Writing: Boolean:= false;
9
      end RW;
10
```

Readers and Writers in Ada (2)

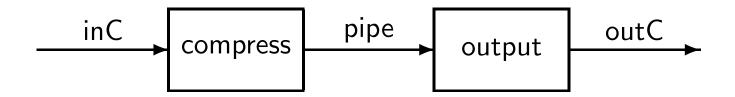
```
protected RW is
 1
        entry StartRead;
        procedure EndRead;
 3
        entry Startwrite ;
4
        procedure EndWrite;
 5
        function NumberReaders return Natural;
 6
 7
      private
        entry ReadGate;
8
        entry WriteGate;
9
        Readers: Natural :=0;
10
        Writing: Boolean := false;
11
      end RW;
12
```

Algorithm 8.1: Producer-consumer (channels)		
channel of integer ch		
producer	consumer	
integer x	integer y	
loop forever	loop forever	
p1: x ← produce	q1: $ch \Rightarrow y$	
p2: $ch \leftarrow x$	q2: consume(y)	

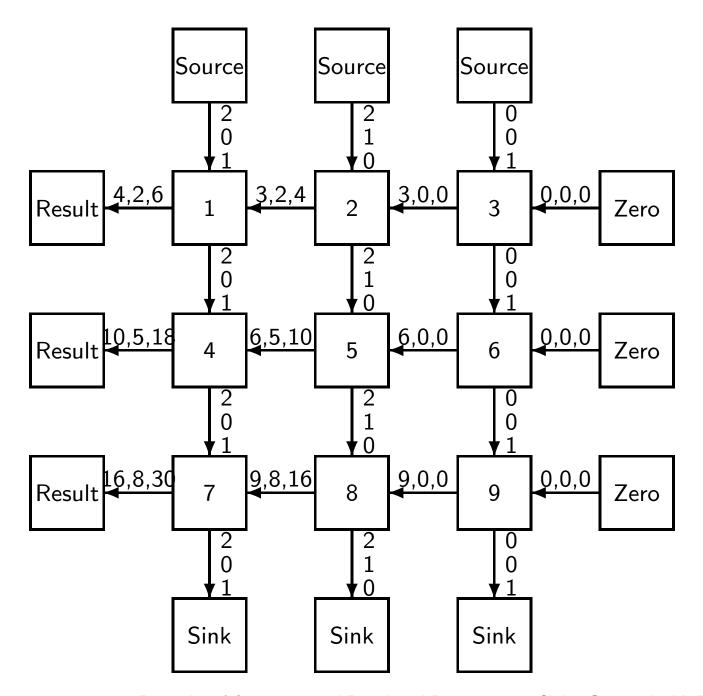
Algorithm 8.2: Conway's problem constant integer MAX \leftarrow 9 constant integer K \leftarrow 4 channel of integer inC, pipe, outC

compress	output
char c, previous ← 0	char c
integer $n \leftarrow 0$	integer m ← 0
$inC \Rightarrow previous$	
loop forever	loop forever
p1: inC \Rightarrow c	q1: $pipe \Rightarrow c$
p2: if $(c = previous)$ and	q2: out $C \Leftarrow c$
(n < MAX - 1)	
p3: $n \leftarrow n + 1$	q3: $m \leftarrow m + 1$
else	
p4: if $n > 0$	q4: if $m >= K$
p5: pipe \Leftarrow intToChar(n+1)	q5: outC ← newline
p6: n ← 0	q6:
p7: pipe \Leftarrow previous	q7:
p8: previous ← c	q8:

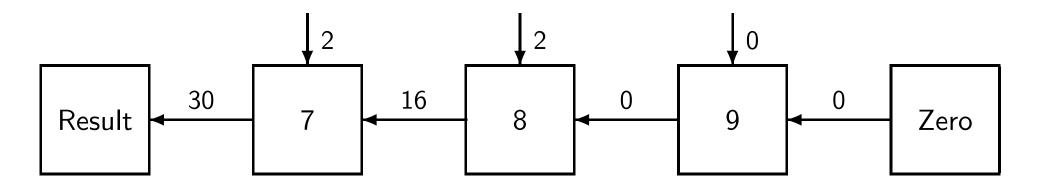
Conway's Problem



Process Array for Matrix Multiplication



Computation of One Element



Algorithm 8.3: Multiplier process with channels

integer FirstElement channel of integer North, East, South, West integer Sum, integer SecondElement

loop forever

p1: North \Rightarrow SecondElement

p2: East \Rightarrow Sum

p3: Sum \leftarrow Sum + FirstElement \cdot SecondElement

p4: South \Leftarrow SecondElement

p5: West \Leftarrow Sum

```
Algorithm 8.4: Multiplier with channels and selective input
                            integer FirstElement
                            channel of integer North, East, South, West
                            integer Sum, integer SecondElement
     loop forever
        either
           North \Rightarrow SecondElement
p1:
           \mathsf{East} \Rightarrow \mathsf{Sum}
p2:
        or
           \mathsf{East} \Rightarrow \mathsf{Sum}
p3:
           North \Rightarrow SecondElement
p4:
        South ← SecondElement
p5:
```

 $Sum \leftarrow Sum + FirstElement \cdot SecondElement$

p6:

p7:

West \Leftarrow Sum

	Algorithm 8.5: Dining philosophers with channels		
	channel of boolean forks[5]		
philosopher i		fork i	
	boolean dummy	boolean dummy	
	loop forever	loop forever	
p1:	think	q1: forks[i] \Leftarrow true	
p2:	$forks[i] \Rightarrow dummy$	q2: forks[i] \Rightarrow dummy	
p3:	$forks[i{+}1] \Rightarrow dummy$	q3:	
p4:	eat	q4:	
p5:	$forks[i] \Leftarrow true$	q5:	
p6:	$forks[i{+}1] \Leftarrow true$	q6:	

Conway's Problem in Promela (1)

```
#define N 9
    #define K 4
 3
    chan in C, pipe, out C = [0] of \{ byte \};
 5
    active proctype Compress() {
      byte previous, c, count = 0;
      inC ? previous;
8
      do
9
      :: inC ? c ->
10
         if
11
         :: (c == previous) \&\& (count < N-1) -> count++
12
         :: else ->
13
            if
14
            :: count > 0 ->
15
             pipe ! count+1;
16
              count = 0
17
18
            :: else
            fi :
19
            pipe! previous;
20
21
            previous = c;
         fi
22
      od
23
24
```

Conway's Problem in Promela (2)

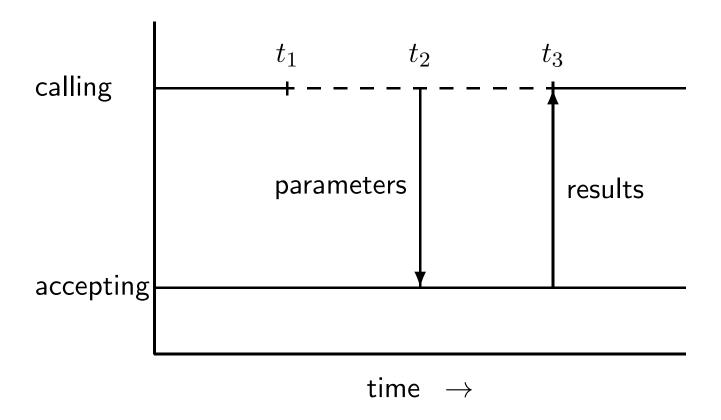
```
active proctype Output() {
      byte c, count = 0;
3
      do
      :: pipe ? c;
        outC ! c;
6
        count++;
     if
        :: count >= K ->
8
          outC ! '\n';
9
           count = 0
10
11
        :: else
12
13
      od
14
```

Multiplier Process in Promela

```
proctype Multiplier (byte Coeff;
        chan North; chan East; chan South; chan West) {
      byte Sum, X;
3
      for (i,0,SIZE-1)
        if :: North ? X \rightarrow East ? Sum;
           :: East ? Sum -> North ? X;
6
       fi;
        South! X;
8
        Sum = Sum + X*Coeff;
9
       West! Sum;
10
11
    rof (i)
12
```

Algorithm 8.6: Rendezvous			
	client		server
integer parm, result			integer p, r
loop forever			loop forever
p1:	parm ←	q1:	
p2: p3:	server.service(parm, result)	q2:	accept service(p, r)
p3:	use(result)	q3:	$r \leftarrow do \; the \; service(p)$

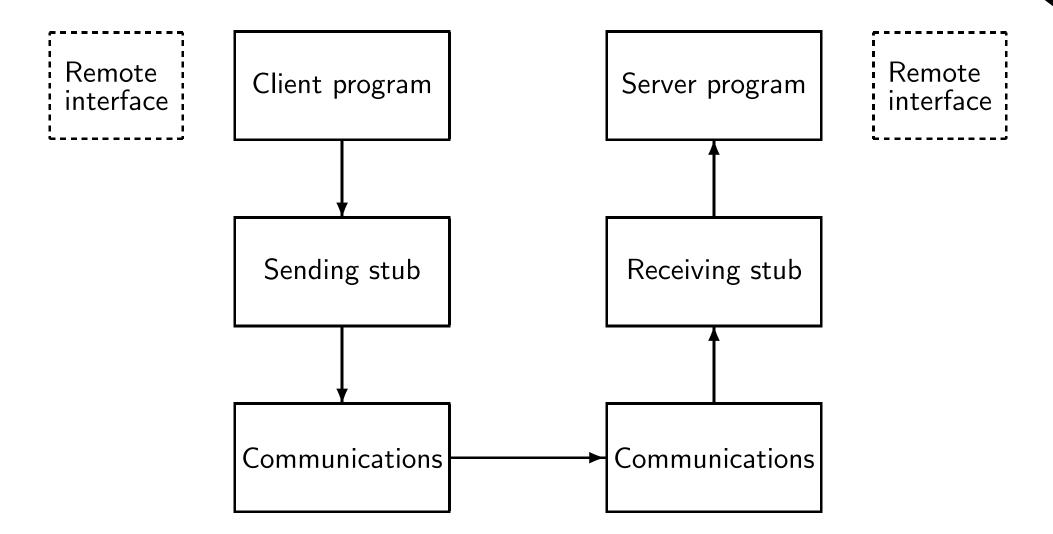
Timing Diagram for a Rendezvous



Bounded Buffer in Ada

```
task body Buffer is
      B: Buffer_Array;
      In_Ptr, Out_Ptr, Count: Index := 0;
 3
 4
 5
    begin
6
      loop
        select
 7
          when Count < Index'Last =>
8
            accept Append(I: in Integer ) do
9
                 B(In_Ptr) := I;
10
            end Append;
11
12
          Count := Count + 1; In_Ptr := In_Ptr + 1;
13
        or
          when Count > 0 =>
14
            accept Take(I: out Integer ) do
15
                 I := B(Out\_Ptr);
16
            end Take;
17
          Count := Count - 1; Out\_Ptr := Out\_Ptr + 1;
18
19
        or
            terminate;
20
        end select;
21
      end loop;
22
    end Buffer:
23
```

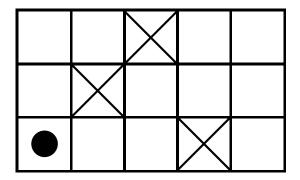
Remote Procedure Call



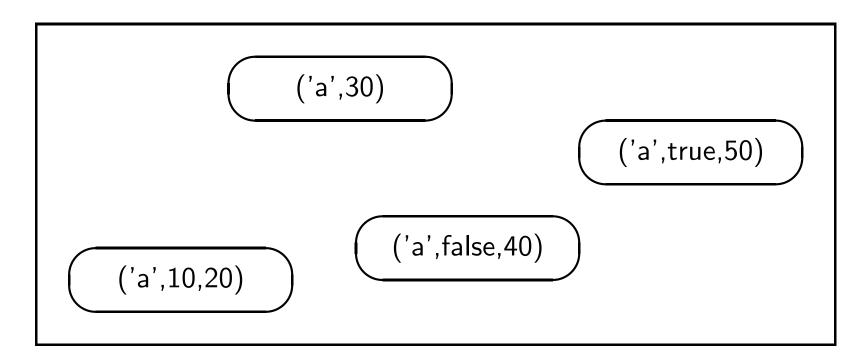
Pipeline Sort



Hoare's Game



A Space



Algorithm 9.1: Critical section problem in Linda

loop forever

p1: non-critical section

p2: removenote('s')

p3: critical section

p4: postnote('s')

Algorithm 9.2: Client-server algorithm in Linda				
	client server			
	constant integer me ←	integer client		
	serviceType service	serviceType s		
	dataType result, parm	dataType r, p		
p1:	service \leftarrow // Service requested	q1: removenote('S', client, s, p)		
p2:	postnote('S', me, service, parm)	q2: $r \leftarrow do(s, p)$		
p3:	removenote('R', me, result)	q3: postnote('R', client, r)		

	Algorithm 9.3: Specific service			
	client server			
	constant integer me ←	integer client		
	serviceType service	serviceType s		
	• •	ş.,		
	dataType result, parm	dataType r, p		
	$service \leftarrow // Service requested$	q1: $s \leftarrow //$ Service provided		
p2:	<pre>postnote('S', me, service, parm)</pre>	q2: removenote('S', client, s=, p)		
p3:		q3: $r \leftarrow do(s, p)$		
p4:	removenote('R', me, result)	q4: postnote('R', client, r)		

Algorithm 9.4: Buffering in a space			
producer consumer			
integer count \leftarrow 0	integer count ← 0		
integer v	integer v		
loop forever	loop forever		
p1: v ← produce	q1: removenote('B', count=, v)		
p2: postnote('B', count, v)	q2: consume(v)		
p3: count \leftarrow count $+$ 1	q3: $count \leftarrow count + 1$		

Algorithm 9.5: Multiplier process with channels in Linda			
	parameters: integer FirstElement		
parameters: integer North, East, South, West			
integer Sum, integer SecondElement			
integer Sum, integer SecondElement			
	loop forever		
p1:	removenote('E', North=, SecondElement)		
p2:	removenote('S', East $=$, Sum)		
p3:	$Sum \leftarrow Sum + FirstElement \cdot SecondElement$		
p4:	postnote('E', South, SecondElement)		
p5:	postnote('S', West, Sum)		

Algorithm 9.6: Matrix multiplication in Linda		
constant integer n $\leftarrow \dots$		
master	worker	
integer i, j, result	integer r, c, result	
integer r, c	integer array[1n] vec1, vec2	
	loop forever	
p1: for i from 1 to n	q1: removenote('T', r, c)	
p2: for j from 1 to n	q2: readnote('A', r=, vec1)	
p3: postnote('T', i, j)	q3: readnote('B', c=, vec2)	
p4: for i from 1 to n	q4: result \leftarrow vec1 \cdot vec2	
p5: for j from 1 to n	q5: postnote('R', r, c, result)	
p6: removenote('R', r, c, re-	q6:	
sult)		
p7: print r, c, result	q7:	

Algorithm 9.7: Matrix multiplication in Linda with granularity

constant integer $n \leftarrow \dots$ constant integer chunk $\leftarrow \dots$

master	worker
integer i, j, result	integer r, c, k, result
integer r, c	integer array[1n] vec1, vec2
	loop forever
p1: for i from 1 to n	q1: removenote('T', r, k)
p2: for j from 1 to n step by chunk	q2: readnote('A', r=, vec1)
p3: postnote('T', i, j)	q3: for c from k to k+chunk-1
p4: for i from 1 to n	q4: readnote('B', c=, vec2)
p5: for j from 1 to n	q5: $result \leftarrow vec1 \cdot vec2$
p6: removenote('R', r, c, re-	q6: postnote('R', r, c, result)
sult)	
p7: print r, c, result	q7:

Definition of Notes in Java

```
public class Note {
 2
        public String id;
        public Object[] p;
 3
 4
        // Constructor for an array of objects
 5
        public Note (String id, Object[] p) {
 6
             this \cdot id = id;
 7
            if (p != null) this p = p.clone();
8
9
10
        // Constructor for a single integer
11
        public Note (String id, int p1) {
12
             this (id, new Object[]{new Integer(p1)});
13
14
15
        // Accessor for a single integer value
16
        public int get(int i) {
17
             return ((Integer )p[i]). intValue();
18
19
20
```

Matrix Multiplication in Java

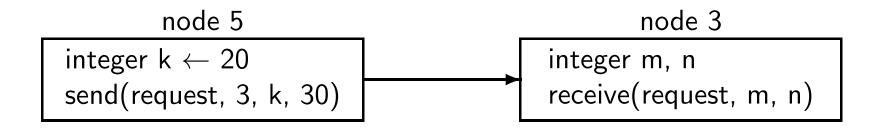
```
private class Worker extends Thread {
 2
         public void run() {
             Note task = new Note("task");
 3
             while (true) {
4
                 Note t = \text{space.removenote(task)};
 5
                 int row = t.get(0), col = t.get(1);
 6
                 Note r = space.readnote(match("a", row));
 7
                 Note c = \text{space.readnote}(\text{match}("b", col));
8
                 int ip = 0;
9
                 for (int i = 1; i \le SIZE; i++)
10
                     ip = ip + r.get(i)*c.get(i);
11
                 space. postnote(new Note("result", row, col, ip));
12
13
14
15
```

Matrix Multiplication in Promela

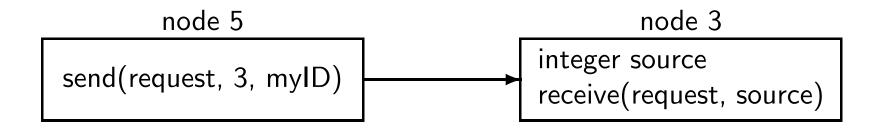
```
chan space = [25] of { byte, short, short, short, short };
2
3
    active[WORKERS] proctype Worker() {
        short row, col, ip, r1, r2, r3, c1, c2, c3;
4
5
        do
        :: space ?? 't', row, col, _, _;
6
          space ?? <'a', eval(row), r1, r2, r3>;
           space ?? <'b', eval(col), c1, c2, c3>;
8
          ip = r1*c1 + r2*c2 + r3*c3;
9
          space! 'r', row, col, ip, 0;
10
11
       od:
12 }
```

Algorithm 9.8: Matrix multiplication in Linda (exercise)			
constant integer n ←			
master	worker		
integer i, j, result	integer i, r, c, result		
integer r, c	integer array[1n] vec1, vec2		
	loop forever		
p1: postnote('T', 0)	q1: removenote('T' i)		
p2:	q2: if i j $(n \cdot n) - 1$		
p3:	q3: $postnote('T', i+1)$		
p4:	q4: $r \leftarrow (i / n) + 1$		
p5:	q5: $c \leftarrow (i \text{ modulo n}) + 1$		
p6: for i from 1 to n	q6: readnote('A', r=, vec1)		
p7: for j from 1 to n	q7: readnote('B', c=, vec2)		
p8: removenote('R', r, c, re-	q8: result \leftarrow vec1 \cdot vec2		
sult)			
p9: print r, c, result	q9: postnote('R', r, c, result)		

Sending and Receiving Messages

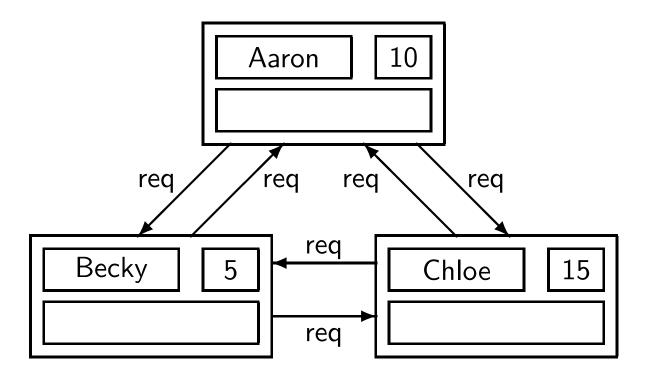


Sending a Message and Expecting a Reply

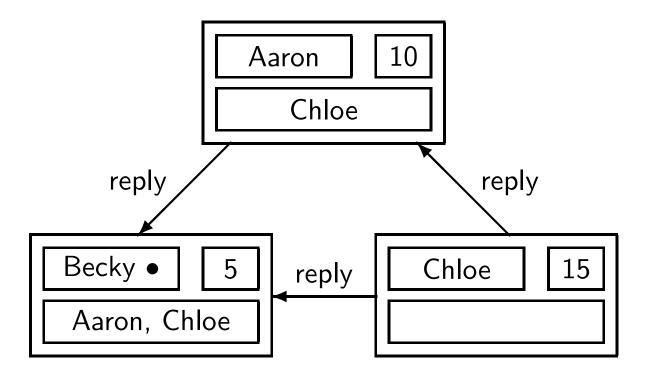


Algorithm 10.1: Ricart-Agrawala algorithm (outline) integer myNum $\leftarrow 0$ set of node IDs deferred ← empty set main non-critical section p1: $myNum \leftarrow chooseNumber$ p2: for all *other* nodes N p3: send(request, N, myID, myNum) p4: await reply's from all *other* nodes p5: critical section p6: for all nodes N in deferred p7: remove N from deferred p8: send(reply, N, myID) p9: receive integer source, reqNum receive(request, source, reqNum) p10: if regNum < myNump11: send(reply,source,myID) p12: else add source to deferred p13:

RA Algorithm (1)



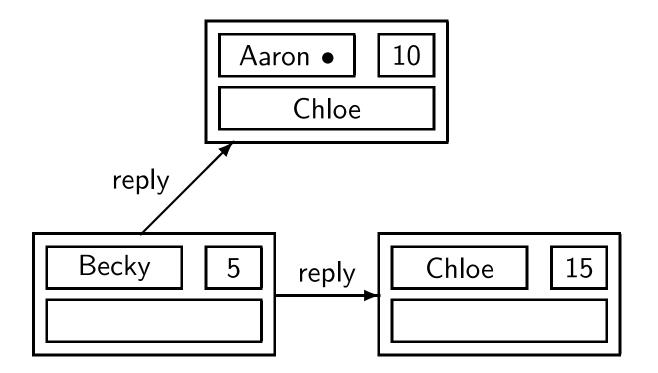
RA Algorithm (2)



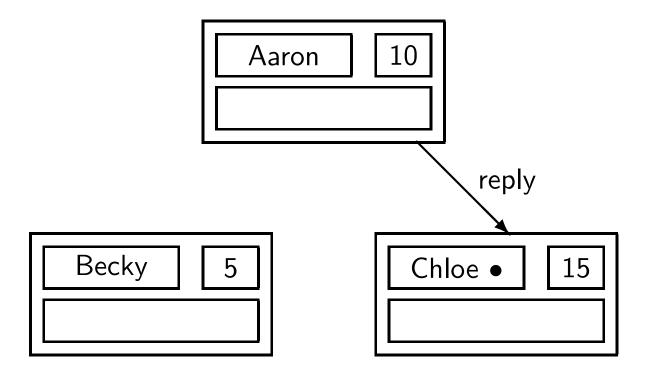
Virtual Queue in the RA Algorithm



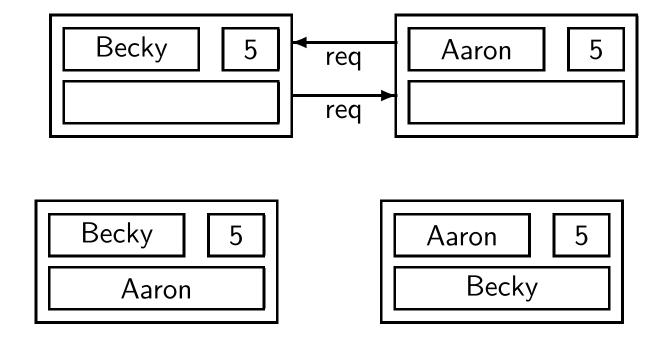
RA Algorithm (3)



RA Algorithm (4)

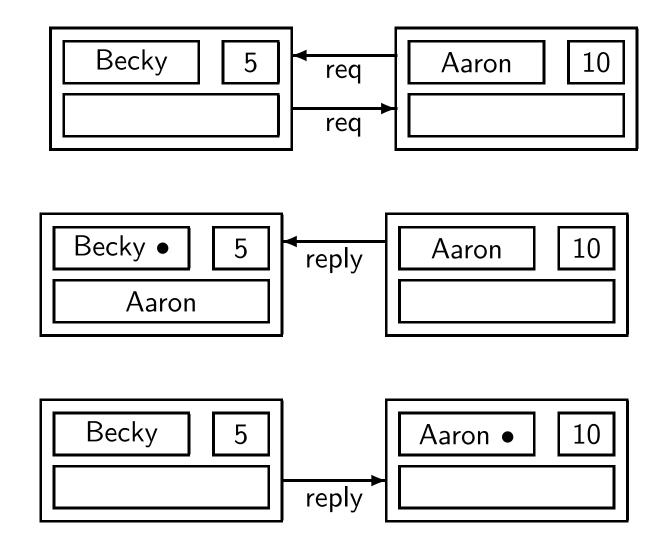


Equal Ticket Numbers

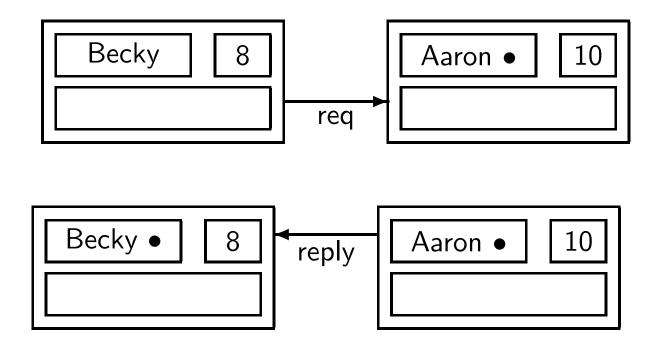


Note: This figure is not in the book.

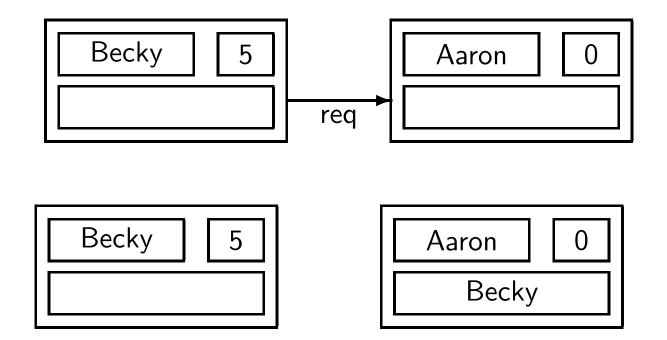
Choosing Ticket Numbers (1)



Choosing Ticket Numbers (2)



Quiescent Nodes



Algorithm 10.2: Ricart-Agrawala algorithm

integer myNum $\leftarrow 0$ set of node IDs deferred ← empty set integer highestNum $\leftarrow 0$ boolean requestCS \leftarrow false

Main

```
loop forever
       non-critical section
p1:
      requestCS \leftarrow true
p2:
       myNum \leftarrow highestNum + 1
p3:
      for all other nodes N
p4:
          send(request, N, myID, myNum)
p5:
       await reply's from all other nodes
p6:
       critical section
p7:
       requestCS \leftarrow false
:8q
       for all nodes N in deferred
p9:
          remove N from deferred
p10:
          send(reply, N, myID)
p11:
```

Algorithm 10.2: Ricart-Agrawala algorithm (continued)

Receive

integer source, requestedNum loop forever

p1: receive(request, source, requestedNum)

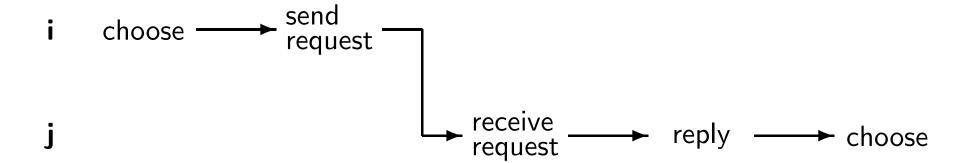
p2: highestNum \leftarrow max(highestNum, requestedNum)

p3: if not requestCS or requestedNum ≪ myNum

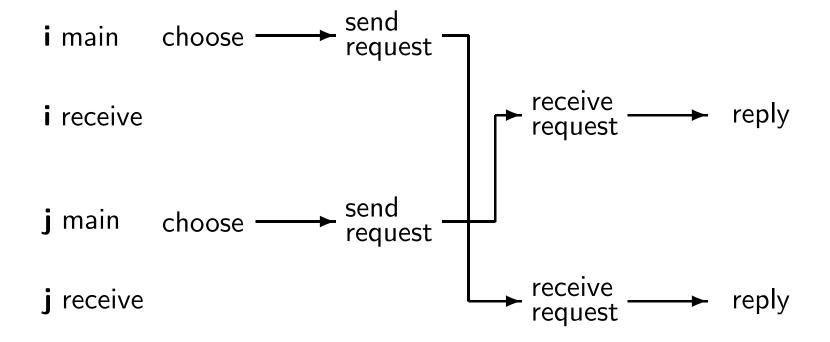
p4: send(reply, source, myID)

p5: else add source to deferred

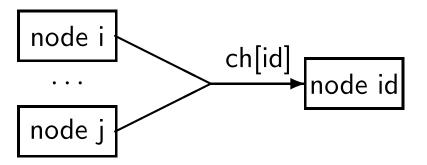
Correct of the RA Algorithm (Case 1)



Correct of the RA Algorithm (Case 2)



Channels in RA Algorithm in Promela



RA Algorithm in Promela – Main Process

25

```
proctype Main( byte myID ) {
       do ::
          atomic {
             requestCS[myID] = true;
4
             myNum[myID] = highestNum[myID] + 1;
 5
 6
          for (J,0, NPROCS-1)
             if
8
             :: J != myID ->
9
                ch[J] ! request, myID, myNum[myID];
10
             :: else
11
12
          rof (J);
13
          for (K,0,NPROCS-2)
14
             ch[myID] ?? reply, _ , _;
15
          rof(K);
16
          critical_section ();
17
          requestCS[myID] = false;
18
          byte N;
19
          do
20
             :: empty(deferred[myID]) -> break;
21
             :: deferred [myID] ? N \rightarrow ch[N]! reply, 0, 0
22
23
          od
       od
24
```

RA Algorithm in Promela – Receive Process

```
proctype Receive( byte myID ) {
        byte reqNum, source;
 2
 3
        do ::
            ch[myID] ?? request, source, reqNum;
 4
            highestNum[myID] =
 5
                ((reqNum > highestNum[myID]) ->
 6
                    reqNum : highestNum[myID]);
8
            atomic {
                if
9
                :: requestCS[myID] &&
10
                     ( (myNum[myID] < reqNum) ||
11
                     ( (myNum[myID] == reqNum) \&\&
12
                            (myID < source)
13
14
                        deferred [myID] ! source
15
                :: else ->
16
                    ch[source] ! reply, 0, 0
17
                fi
18
19
20
        od
21
```

Algorithm 10.3: Ricart-Agrawala token-passing algorithm

```
boolean haveToken \leftarrow true in node 0, false in others integer array[NODES] requested \leftarrow [0,...,0] integer array[NODES] granted \leftarrow [0,...,0] integer myNum \leftarrow 0 boolean inCS \leftarrow false
```

sendToken

```
if exists N such that requested[N] > granted[N] for some such N send(token, N, granted) haveToken \leftarrow false
```

Slide – 10.20

Algorithm 10.3: Ricart-Agrawala token-passing algorithm (continued)

Main

```
loop forever
       non-critical section
p1:
     if not haveToken
p2:
          myNum \leftarrow myNum + 1
p3:
         for all other nodes N
p4:
             send(request, N, myID, myNum)
p5:
          receive(token, granted)
p6:
       haveToken \leftarrow true
p7:
     inCS \leftarrow true
:8q
      critical section
p9:
      granted[myID] \leftarrow myNum
p10:
      inCS \leftarrow false
p11:
      sendToken
p12:
```

Algorithm 10.3: Ricart-Agrawala token-passing algorithm (continued)

Receive

integer source, reqNum loop forever

p13: receive(request, source, reqNum)

p14: requested[source] \leftarrow max(requested[source], reqNum)

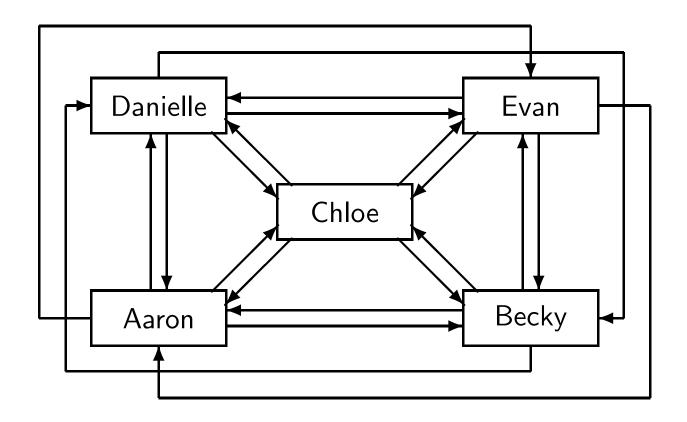
p15: if haveToken and not inCS

p16: sendToken

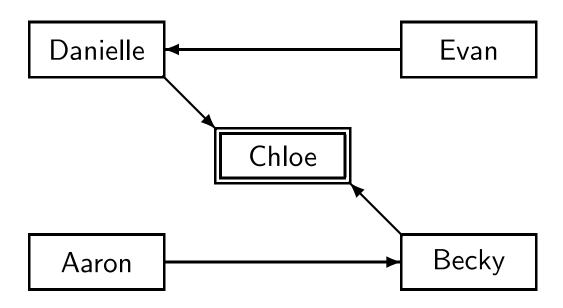
Data Structures for RA Token-Passing Algorithm

requested	4	3	0	5	1
granted	4	2	2	4	1
	Aaron	Becky	Chloe	Danielle	Evan

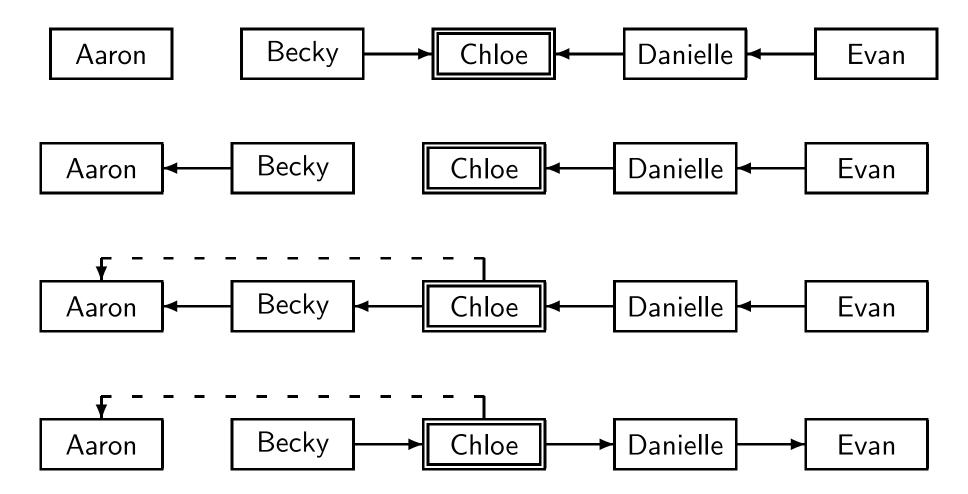
Distributed System for Neilsen-Mizuno Algorithm



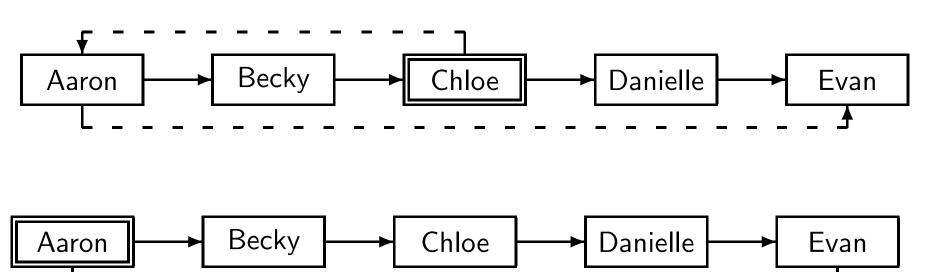
Spanning Tree in Neilsen-Mizuno Algorithm

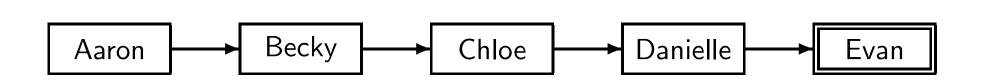


Neilsen-Mizuno Algorithm (1)



Neilsen-Mizuno Algorithm (2)





```
Algorithm 10.4: Neilsen-Mizuno token-passing algorithm
             integer parent \leftarrow (initialized to form a tree)
             integer deferred \leftarrow 0
             boolean holding ← true in the root, false in others
    Main
    loop forever
       non-critical section
p1:
    if not holding
p2:
          send(request, parent, myID, myID)
p3:
         parent \leftarrow 0
p4:
          receive(token)
p5:
     holding ← false
p6:
     critical section
p7:
       if deferred \neq 0
p8:
          send(token, deferred)
p9:
       deferred \leftarrow 0
p10:
       else holding ← true
p11:
```

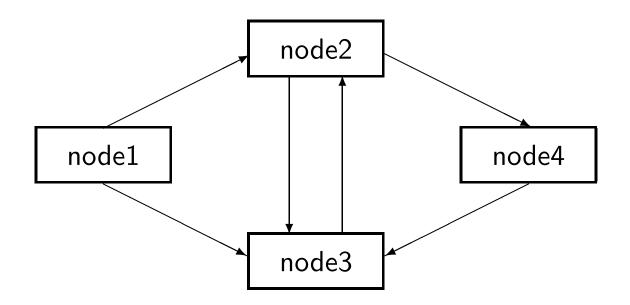
Algorithm 10.4: Neilsen-Mizuno token-passing algorithm (continued)

Receive

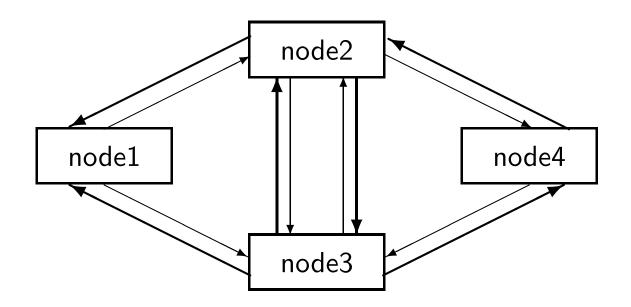
```
integer source, originator
    loop forever
      receive(request, source, originator)
p12:
     if parent = 0
p13:
p14: if holding
            send(token, originator)
p15:
            holding \leftarrow false
p16:
      else deferred ← originator
p17:
     else send(request, parent, myID, originator)
p18:
      parent ← source
p19:
```

Slide - 10.29

Distributed System with an Environment Node



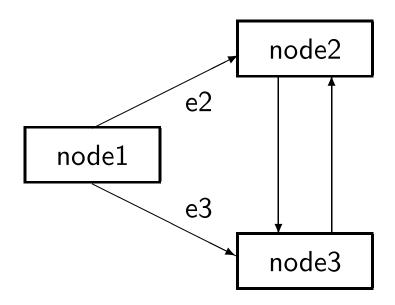
Back Edges



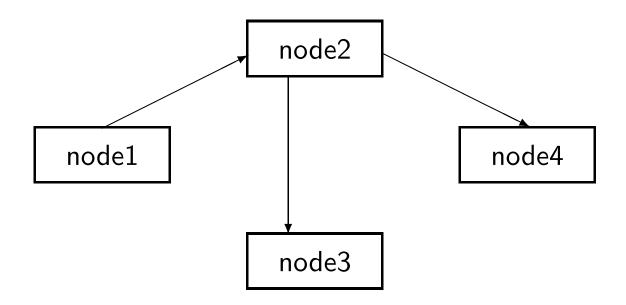
```
Algorithm 11.1: Dijkstra-Scholten algorithm (preliminary)
              integer array[incoming] inDeficit \leftarrow [0, ..., 0]
              integer inDeficit \leftarrow 0, integer outDeficit \leftarrow 0
     send message
p1: send(message, destination, myID)
    increment outDeficit
     receive message
p3: receive(message, source)
p4: increment inDeficit[source] and inDeficit
     send signal
p5: when inDeficit > 1 or
           (inDeficit = 1 and isTerminated and outDeficit = 0)
   \mathsf{E} \leftarrow \mathsf{some} \ \mathsf{edge} \ \mathsf{E} \ \mathsf{with} \ \mathsf{inDeficit}[\mathsf{E}] \neq \mathsf{0}
p6:
    send(signal, E, myID)
p7:
    decrement inDeficit[E] and inDeficit
:8q
     receive signal
p9: receive(signal, _)
p10: decrement outDeficit
```

Algorithm 11.2: Dijkstra-Scholten algorithm (env., preliminary) integer outDeficit ← 0 computation p1: for all outgoing edges E p2: send(message, E, myID) p3: increment outDeficit p4: await outDeficit = 0 p5: announce system termination receive signal p6: receive(signal, source) p7: decrement outDeficit

The Preliminary DS Algorithm is Unsafe



Spanning Tree



```
Algorithm 11.3: Dijkstra-Scholten algorithm
             integer array[incoming] inDeficit \leftarrow [0,...,0]
            integer in Deficit \leftarrow 0
            integer outDeficit \leftarrow 0
            integer parent \leftarrow -1
    send message
p1: when parent \neq -1 // Only active nodes send messages
       send(message, destination, myID)
p2:
       increment outDeficit
p3:
    receive message
    receive(message,source)
p5: if parent =-1
      parent ← source
p6:
   increment inDeficit[source] and inDeficit
```

Algorithm 11.3: Dijkstra-Scholten algorithm (continued)

send signal

```
when in Deficit > 1
        \mathsf{E} \leftarrow \mathsf{some} \ \mathsf{edge} \ \mathsf{E} \ \mathsf{for} \ \mathsf{which}
p9:
            (inDeficit[E] > 1) or (inDeficit[E] = 1 and E \neq parent)
       send(signal, E, myID)
p10:
       decrement inDeficit[E] and inDeficit
p11:
p12: or when inDeficit = 1 and isTerminated and outDeficit = 0
       send(signal, parent, myID)
p13:
p14: inDeficit[parent] \leftarrow 0
p15: inDeficit \leftarrow 0
      parent \leftarrow -1
p16:
```

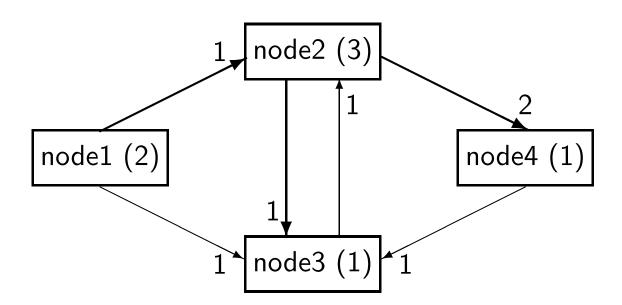
receive signal

```
p17: receive(signal, _)
p18: decrement outDeficit
```

Partial Scenario for DS Algorithm

Action	node1	node2	node3	node4
$1 \Rightarrow 2$	(-1,[],0)	(-1,[0,0],0)	(-1,[0,0,0],0)	(-1,[0],0)
$2 \Rightarrow 4$	(-1,[],1)	(1,[1,0],0)	(-1,[0,0,0],0)	(-1,[0],0)
$2 \Rightarrow 3$	(-1,[],1)	(1,[1,0],1)	(-1,[0,0,0],0)	(2,[1],0)
$2 \Rightarrow 4$	(-1,[],1)	(1,[1,0],2)	(2,[0,1,0],0)	(2,[1],0)
$1 \Rightarrow 3$	(-1,[],1)	(1,[1,0],3)	(2,[0,1,0],0)	(2,[2],0)
$3 \Rightarrow 2$	(-1,[],2)	(1,[1,0],3)	(2,[1,1,0],0)	(2,[2],0)
4 ⇒ 3	(-1,[],2)	(1,[1,1],3)	(2,[1,1,0],1)	(2,[2],0)
	(-1,[],2)	(1,[1,1],3)	(2,[1,1,1],1)	(2,[2],1)

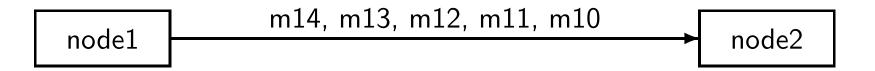
Data Structures After Partial Scenario



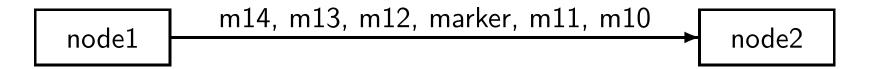
Algorithm 11.4: Credit-recovery algorithm (environment node) float weight $\leftarrow 1.0$ computation p1: for all outgoing edges E p2: weight \leftarrow weight / 2.0 p3: send(message, E, weight) p4: await weight = 1.0 p5: announce system termination receive signal p6: receive(signal, w) p7: weight \leftarrow weight + w

```
Algorithm 11.5: Credit-recovery algorithm (non-environment node)
          constant integer parent \leftarrow 0 // Environment node
          boolean active \leftarrow false
          float weight \leftarrow 0.0
    send message
p1: if active // Only active nodes send messages
    weight \leftarrow weight / 2.0
p2:
       send(message, destination, myID, weight)
p3:
    receive message
   receive(message, source, w)
p5: active \leftarrow true
p6: weight \leftarrow weight + w
    send signal
   when terminated
       send(signal, parent, weight)
:8q
p9: weight \leftarrow 0.0
p10: active \leftarrow false
```

Messages on a Channel



Sending a Marker



Algorithm 11.6: Chandy-Lamport algorithm for global snapshots integer array[outgoing] lastSent \leftarrow [0, ..., 0] integer array[incoming] lastReceived \leftarrow [0, ..., 0] integer array[outgoing] stateAtRecord \leftarrow [-1, ..., -1] integer array[incoming] messageAtRecord \leftarrow [-1, ..., -1] integer array[incoming] messageAtMarker \leftarrow [-1, ..., -1] send message p1: send(message, destination, myID) $lastSent[destination] \leftarrow message$ receive message p3: receive(message,source) p4: lastReceived[source] ← message

Algorithm 11.6: Chandy-Lamport algorithm (continued)

receive marker

```
p6: receive(marker, source)
```

p7: messageAtMarker[source] \leftarrow lastReceived[source]

p8: if stateAtRecord = [-1,...,-1] // Not yet recorded

p9: stateAtRecord \leftarrow lastSent

p10: $messageAtRecord \leftarrow IastReceived$

p11: for all outgoing edges E

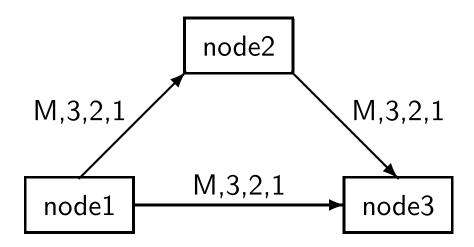
p12: send(marker, E, myID)

record state

p13: await markers received on all incoming edges

p14: recordState

Messages and Markers for a Scenario



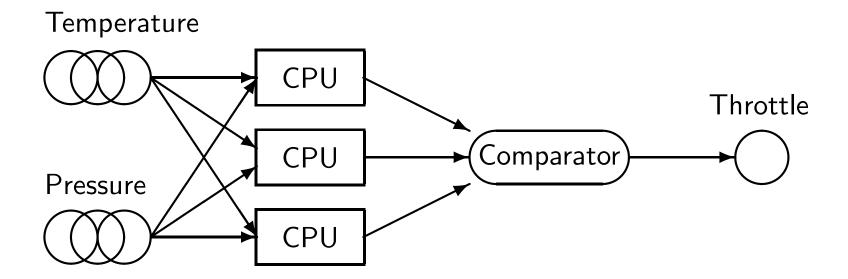
Scenario for CL Algorithm (1)

Action	node1			e1 node2						
	ls	lr	st	rc	mk	ls	lr	st	rc	mk
	[3,3]					[3]	[3]			
1M⇒2	[3,3]		[3,3]			[3]	[3]			
1M⇒3	[3,3]		[3,3]			[3]	[3]			
2 ← 1M	[3,3]		[3,3]			[3]	[3]			
2M⇒3	[3,3]		[3,3]			[3]	[3]	[3]	[3]	[3]

Scenario for CL Algorithm (2)

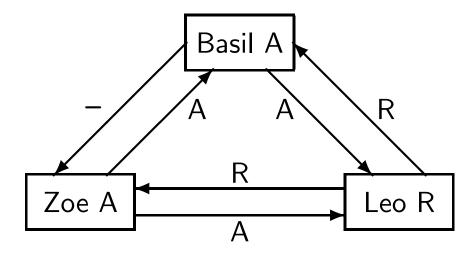
Action	node3					
	ls	lr	st	rc	mk	
3←2						
3 ← 2		[0,1]				
3←2		[0,2]				
3 ← 2M		[0,3]				
3←1		[0,3]		[0,3]	[0,3]	
3←1		[1,3]		[0,3]	[0,3]	
3←1		[2,3]		[0,3]	[0,3]	
3 ← 1M		[3,3]		[0,3]	[0,3]	
		[3,3]		[0,3]	[3,3]	

Architecture for a Reliable System



```
Algorithm 12.1: Consensus - one-round algorithm
                         planType finalPlan
                         planType array[generals] plan
    plan[myID] \leftarrow chooseAttackOrRetreat
p2: for all other generals G
      send(G, myID, plan[myID])
p3:
p4: for all other generals G
   receive(G, plan[G])
p5:
p6: finalPlan \leftarrow majority(plan)
```

Messages Sent in a One-Round Algorithm



Data Structures in a One-Round Algorithm

Leo				
general	plan			
Basil	Α			
Leo	R			
Zoe	Α			
majority	А			

Zoe				
general	plans			
Basil	_			
Leo	R			
Zoe	А			
majority	R			

```
Algorithm 12.2: Consensus - Byzantine Generals algorithm
                  planType finalPlan
                  planType array[generals] plan, majorityPlan
                  planType array[generals, generals] reportedPlan
p1: plan[mylD] \leftarrow chooseAttackOrRetreat
p2: for all other generals G
                                                 // First round
   send(G, myID, plan[myID])
p3:
p4: for all other generals G
    receive(G, plan[G])
   for all other generals G
                                                 // Second round
p7: for all other generals G' except G
         send(G', myID, G, plan[G])
p9: for all other generals G
p10: for all other generals G' except G
         receive(G, G', reportedPlan[G, G'])
p11:
p12: for all other generals G
                                                 // First vote
      majorityPlan[G] \leftarrow majority(plan[G] \cup reportedPlan[*, G])
p14: majorityPlan[myID] \leftarrow plan[myID]
                                                // Second vote
p15: finalPlan \leftarrow majority(majorityPlan)
```

Crash Failure - First Scenario (Leo)

Leo						
general	plan	report	ed by	majority		
		Basil Zoe				
Basil	А	_		А		
Leo	R			R		
Zoe	А	_		А		
majority				А		

Crash Failure - First Scenario (Zoe)

Zoe						
general	plan	report	ed by	majority		
		Basil Leo				
Basil	_	Α		А		
Leo	R	_		R		
Zoe	А			А		
majority				А		

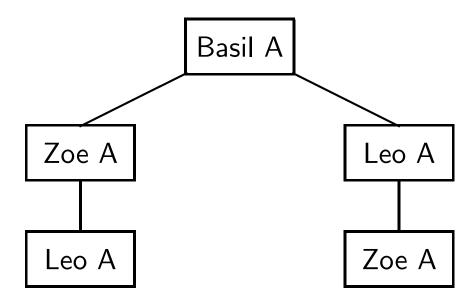
Crash Failure - Second Scenario (Leo)

Leo						
general	plan	report	ed by	majority		
		Basil Zoe				
Basil	А	А		А		
Leo	R			R		
Zoe	А	А		А		
majority				А		

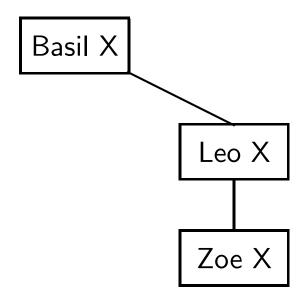
Crash Failure - Second Scenario (Zoe)

Zoe							
general	plan	report	ed by	majority			
		Basil Leo					
Basil	А	А		А			
Leo	R	_		R			
Zoe	А			А			
majority				А			

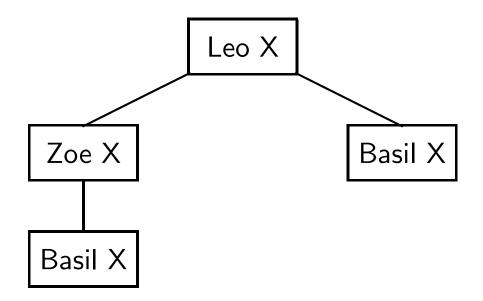
Knowledge Tree about Basil - First Scenario



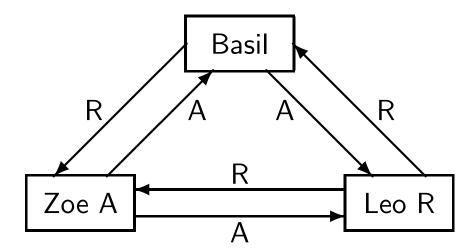
Knowledge Tree about Basil - Second Scenario



Knowledge Tree about Leo



Byzantine Failure with Three Generals



Data Stuctures for Leo and Zoe After First Round

Leo				
general	plans			
Basil	А			
Leo	R			
Zoe	А			
majority	А			

Zoe				
general	plans			
Basil	R			
Leo	R			
Zoe	А			
majority	R			

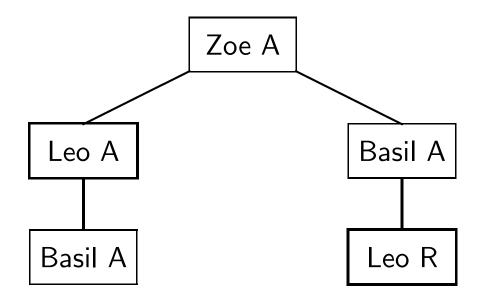
Data Stuctures for Leo After Second Round

Leo							
general	plans	report	ed by	majority			
		Basil Zoe					
Basil	А	Α		А			
Leo	R			R			
Zoe	А	R		R			
majority				R			

Data Stuctures for Zoe After Second Round

Zoe							
general	plans	report	ed by	majority			
		Basil Leo					
Basil	А	А		А			
Leo	R	R		R			
Zoe	А			А			
majority				А			

Knowledge Tree About Zoe



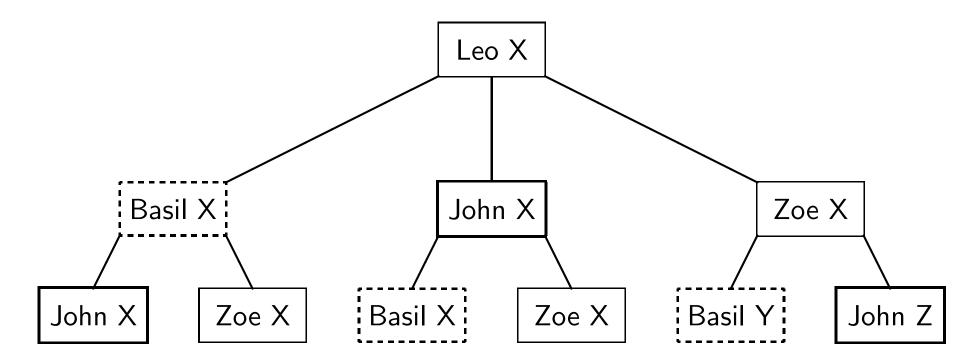
Four Generals: Data Structure of Basil (1)

Basil						
general	plan	rep	orted	by	majority	
		John	John Leo Zoe			
Basil	А					
John	Α		Α	?	А	
Leo	R	R		?	R	
Zoe	?	?	?		?	
majority					?	

Four Generals: Data Structure of Basil (2)

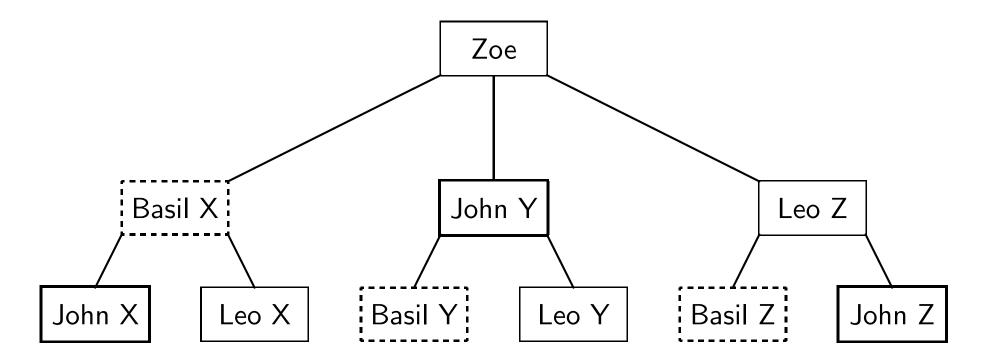
Basil						
general	plans	rep	orted	by	majority	
		John	Leo	Zoe		
Basil	А				А	
John	А		Α	?	А	
Leo	R	R		?	R	
Zoe	R	Α	R		R	
					R	

Knowledge Tree About Loyal General Leo



Slide - 12.20

Knowledge Tree About Traitor Zoe

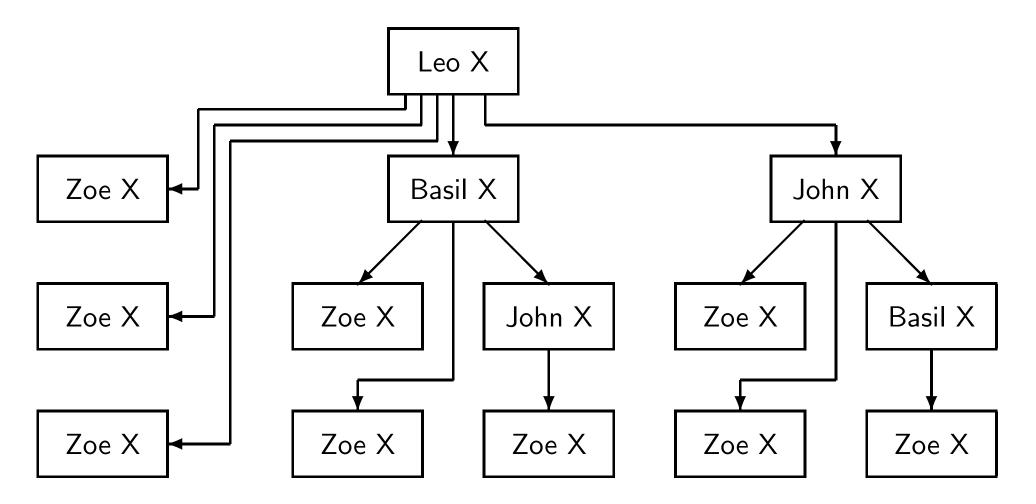


Complexity of the Byzantine Generals Algorithm

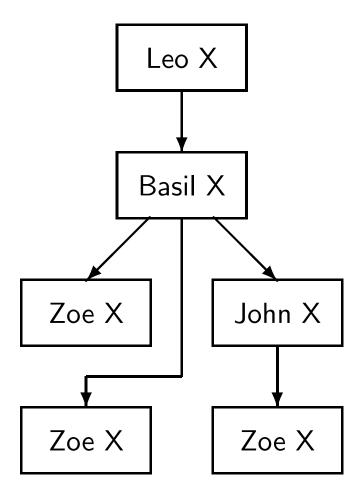
traitors	generals	messages
1	4	36
2	7	392
3	10	1790
4	13	5408

```
Algorithm 12.3: Consensus - flooding algorithm
                    planType finalPlan
                    set of planType plan \leftarrow { chooseAttackOrRetreat }
                    set of planType receivedPlan
    do t+1 times
       for all other generals G
p2:
          send(G, plan)
p3:
   for all other generals G
p4:
         receive(G, receivedPlan)
p5:
          plan \leftarrow plan \cup receivedPlan
p6:
    finalPlan \leftarrow majority(plan)
```

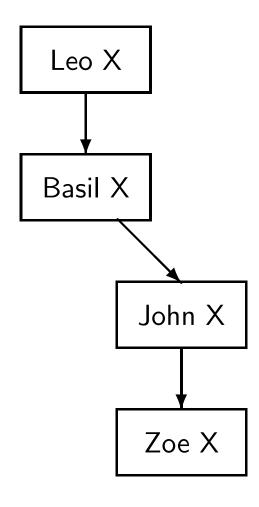
Flooding Algorithm with No Crash: Knowledge Tree About Leo



Flooding Algorithm with Crash: Knowledge Tree About Leo (1)



Flooding Algorithm with Crash: Knowledge Tree About Leo (2)



```
Algorithm 12.4: Consensus - King algorithm
              planType finalPlan, myMajority, kingPlan
              planType array[generals] plan
              integer votesMajority
   plan[myID] \leftarrow chooseAttackOrRetreat
    do two times
                                          // First and third rounds
      for all other generals G
p3:
         send(G, myID, plan[myID])
p4:
      for all other generals G
p5:
         receive(G, plan[G])
p6:
      myMajority \leftarrow majority(plan)
p7:
       votesMajority ← number of votes for myMajority
p8:
```

Algorithm 12.4: Consensus - King algorithm (continued)

```
if my turn to be king
                                          // Second and fourth rounds
p9:
         for all other generals G
p10:
             send(G, myID, myMajority)
p11:
          plan[myID] \leftarrow myMajority
p12:
       else
         receive(kingID, kingPlan)
p13:
      if votesMajority ¿ 3
p14:
             plan[myID] \leftarrow myMajority
p15:
          else
            plan[myID] ← kingPlan
p16:
p17: finalPlan \leftarrow plan[myID]
                                             Final decision
```

Scenario for King Algorithm: First King Loyal General Zoe (1)

Basil									
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
Α	А	R	R	R	R	3			
	John								
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
Α	А	R	Α	R	А	3			
<u> </u>				J					
					Leo				
Basil	John	Leo	Mike	Zoe	Leo myMajority	votesMajority	kingPlan		
Basil A	John A	Leo R	Mike A	Zoe R		votesMajority 3	kingPlan		
			_		myMajority	3 3	kingPlan		
			_		myMajority A	3 3	kingPlan		

Scenario for King Algorithm: First King Loyal General Zoe (2)

	Basil								
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
R							R		
	John								
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
	R						R		
					Leo				
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
		R					R		
					Zoe				
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
] 301111		'''''						

Scenario for King Algorithm: First King Loyal General Zoe (3)

Basil									
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
R	R	R	?	R	R	4–5			
	John								
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
R	R	R	?	R	R	4–5			
Leo									
					LCO				
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
Basil R	John R	Leo R	Mike ?	Zoe R	_	votesMajority 4–5	kingPlan		
					myMajority		kingPlan		
					myMajority R		kingPlan kingPlan		

Scenario for King Algorithm: First King Traitor Mike (1)

Basil									
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
R							R		
	John								
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
	А						А		
Leo									
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
Basil	John	Leo	Mike	Zoe		votesMajority	kingPlan A		
Basil	John		Mike	Zoe		votesMajority			
Basil	John		Mike Mike	Zoe	myMajority	votesMajority votesMajority			

Scenario for King Algorithm: First King Traitor Mike (2)

Basil									
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
R	А	А	?	R	?	3			
	John								
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
R	А	Α	?	R	?	3			
					Leo				
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
R	А	Α	?	R	?	3			
					Zoe				
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
R	Α	Α	2	R	2	3			

Scenario for King Algorithm: First King Traitor Mike (3)

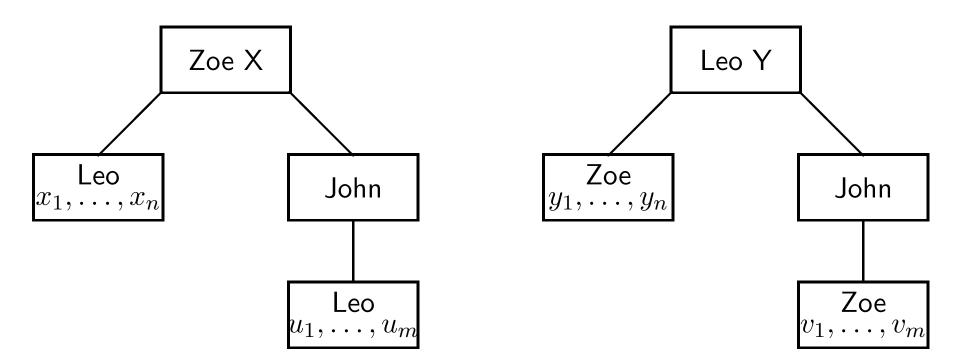
Basil									
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
А							А		
	John								
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
	А						А		
Leo									
Basil	John	Leo	Mike	Zoe	myMajority	votesMajority	kingPlan		
Basil	John	Leo A	Mike	Zoe	myMajority	votesMajority	kingPlan A		
Basil	John	_	Mike	Zoe	myMajority Zoe	votesMajority			
Basil	John	_	Mike Mike	Zoe	, J	votesMajority votesMajority			

Complexity of Byzantine Generals and King Algorithms

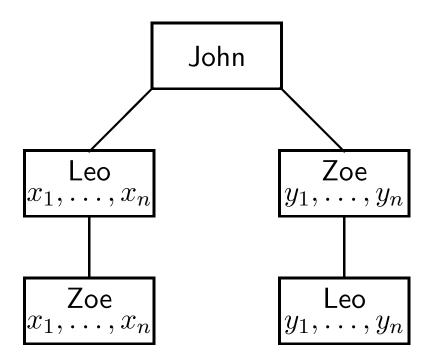
traitors	generals	messages
1	4	36
2	7	392
3	10	1790
4	13	5408

traitors	generals	messages
1	5	48
2	9	240
3	13	672
4	17	1440

Impossibility with Three Generals (1)



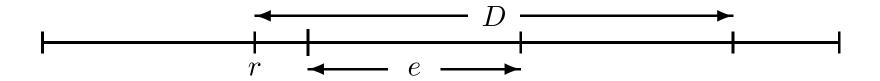
Impossibility with Three Generals (2)



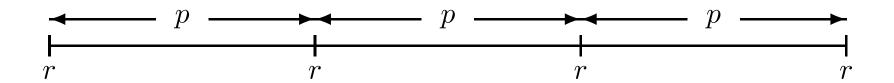
Exercise for Byzantine Generals Algorithm

Zoe								
general	plan	rep	majority					
		Basil	John	Leo				
Basil	R		А	R	?			
John	Α	R		Α	?			
Leo	R	R	R		?			
Zoe	Α				А			
					?			

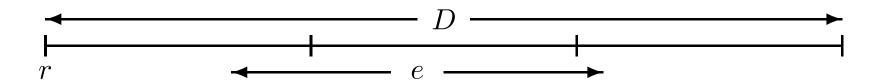
Release Time, Execution Time and Relative Deadline



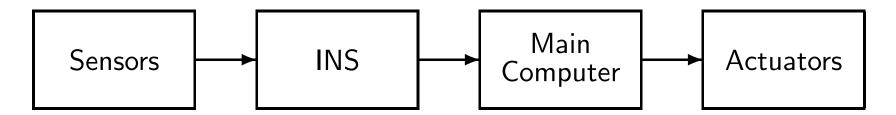
Periodic Task



Deadline is a Multiple of the Period

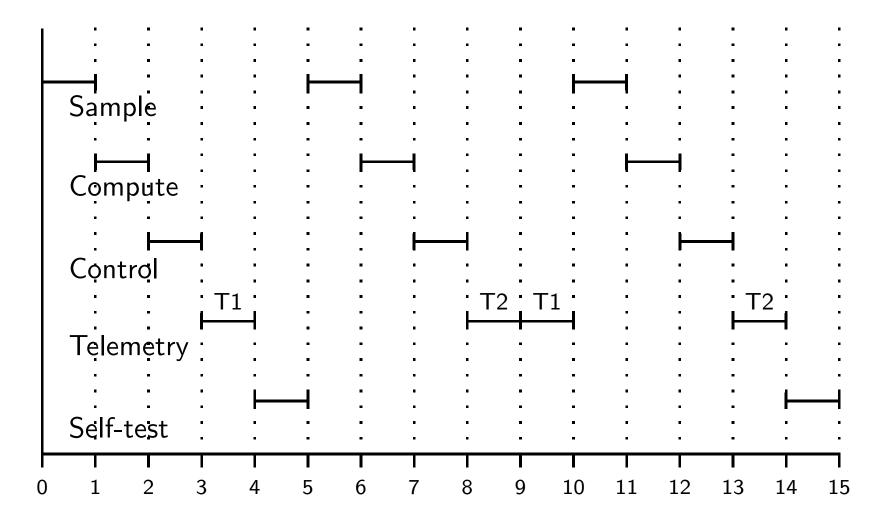


Architecture of Ariane Control System





Synchronous System



Synchronous System Scheduling Table

0	1	2	3	4
Sample	Compute	Control	Telemetry 1	Self-test
5	6	7	8	9
Sample	Compute	Control	Telemetry 2	Telemetry 1
Sample	Compute	Control	Telemetry 2	Telemetry 1
Sample 10	Compute 11	Control 12	Telemetry 2 13	Telemetry 1 14

Algorithm 13.1: Synchronous scheduler

 $taskAddressType array[0..numberFrames-1] tasks \leftarrow$ [task address,...,task address] integer currentFrame ← 0

loop p1:

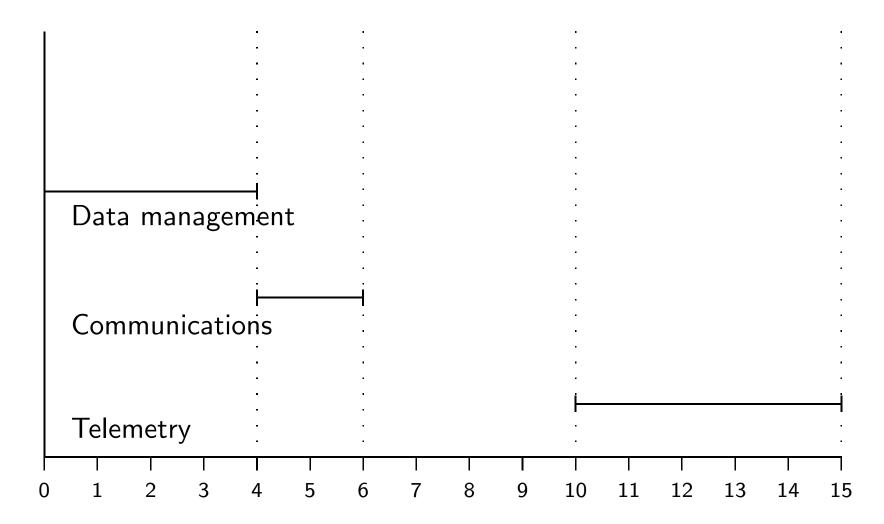
await beginning of frame p2:

invoke tasks[currentFrame] p3:

increment currentFrame modulo numberFrames p4:

Algorithm 13.2: Producer-consumer (synchronous system)			
queue of dataType buffer1, buffer2			
sample compute control		control	
dataType d	dataType d1, d2	dataType d	
p1: d ← sample	q1: $d1 \leftarrow take(buffer1)$	r1: $d \leftarrow take(buffer2)$	
p2: append(d, buffer1)	q2: $d2 \leftarrow compute(d1)$	r2: control(d)	
p3:	q3: append(d2,	r3:	
	buffer2)		

Asynchronous System



Algorithm 13.3: Asynchronous scheduler

queue of taskAddressType readyQueue $\leftarrow \dots$ taskAddressType currentTask

loop forever

p1: await readyQueue not empty

p2: currentTask \leftarrow take head of readyQueue

p3: invoke currentTask

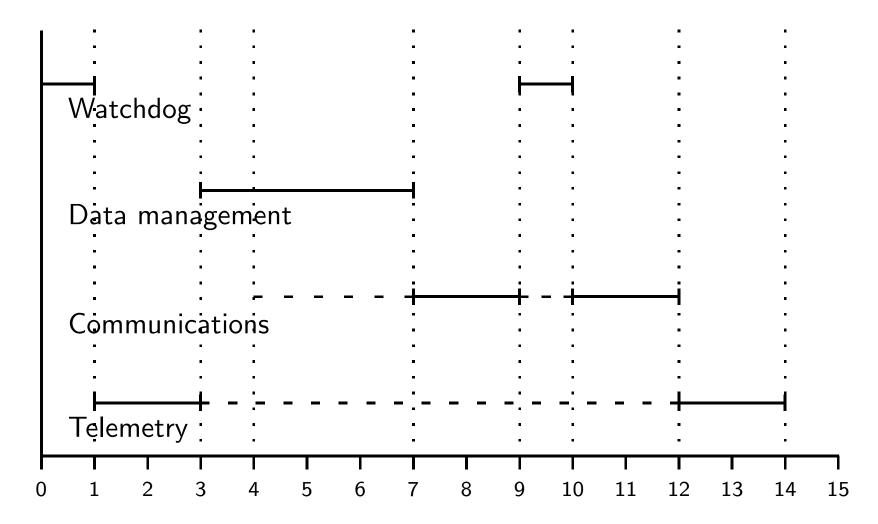
Algorithm 13.4: Preemptive scheduler

queue of taskAddressType readyQueue $\leftarrow \dots$ taskAddressType currentTask

loop forever

- p1: await a scheduling event
- p2: if currentTask.priority | highest priority of a task on readyQueue
- p3: save partial computation of currentTask and place on readyQueue
- p4: currentTask \leftarrow take task of highest priority from readyQueue
- p5: invoke currentTask
- p6: else if currentTask's timeslice is past and
 - currentTask.priority = priority of some task on readyQueue
- p7: save partial computation of currentTask and place on readyQueue
- p8: currentTask ← take a task of the same priority from readyQueue
- p9: invoke currentTask
- p10: else resume currentTask

Preemptive Scheduling

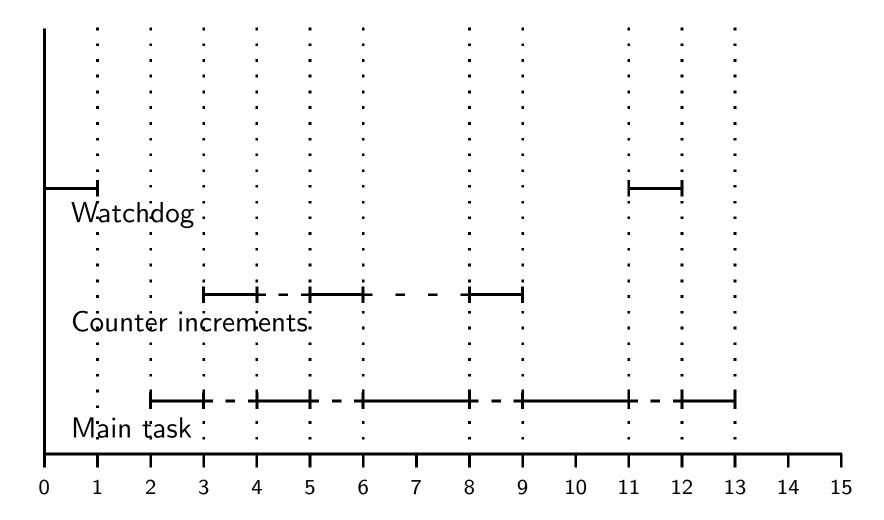


Algorithm 13.5: Watchdog supervision of response time				
	boolean ran ← false			
data management		watchdog		
loop forever		loop forever		
p1:	do data management	q1: await ninth frame		
p2:	$ran \leftarrow true$	q2: if ran is false		
p3:	rejoin readyQueue	q3: notify response-time over-		
		flow		
p4:		q4: ran ← false		
p5:		q5: rejoin readyQueue		

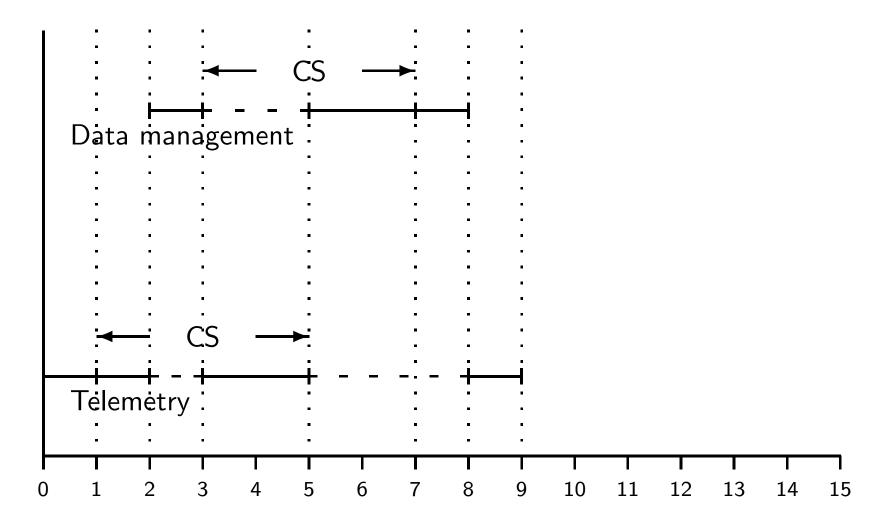
Algorithm 13.6: Real-time buffering - throw away new data				
	queue of dataType buffer \leftarrow empty queue			
sample			compute	
	dataType d		dataType d	
loop forever		loop forever		
p1:	$d \leftarrow sample$	q1:	await buffer not empty	
p2:	if buffer is full do nothing	q2:	$d \leftarrow take(buffer)$	
p3:	else append(d,buffer)	q3:	compute(d)	

Algorithm 13.7: Real-time buffering - overwrite old data			
queue of dataType buffer \leftarrow empty queue			
sample	compute		
dataType d	dataType d		
loop forever	loop forever		
p1: d ← sample	q1: await buffer not empty		
p2: append(d, buffer)	q2: $d \leftarrow take(buffer)$		
p3:	q3: compute(d)		

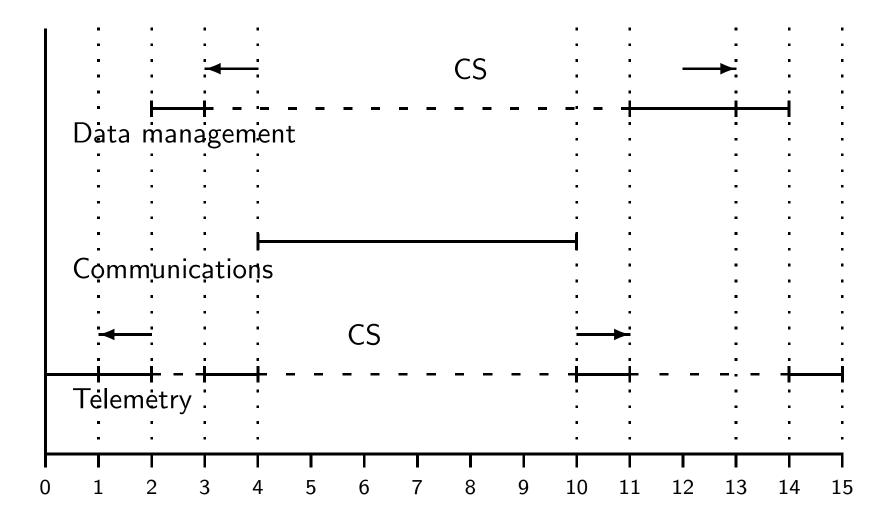
Interrupt Overflow on Apollo 11



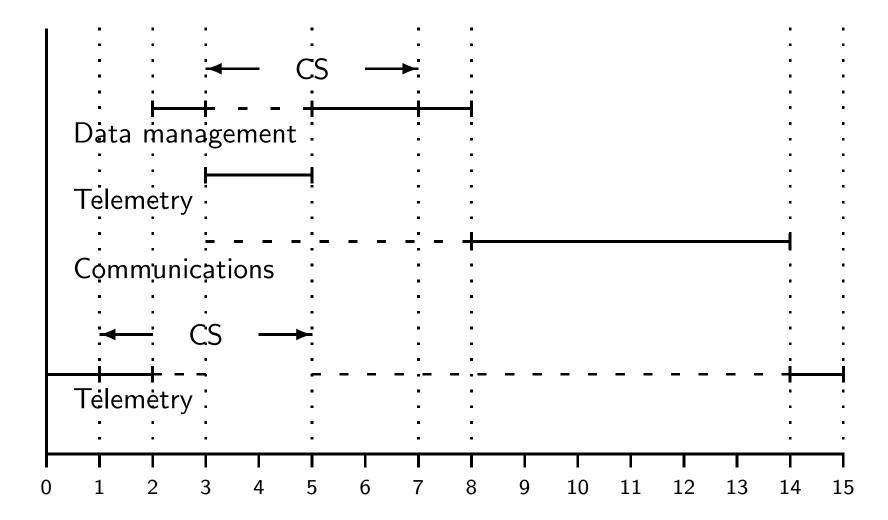
Priority Inversion (1)



Priority Inversion (2)



Priority Inheritance



Priority Inversion in Promela (1)

```
mtype = { idle, blocked, nonCS, CS, long };
 2
 3
    mtype data = idle, comm = idle, telem = idle;
4
    #define ready(p) (p != idle && p != blocked)
 5
6
    active proctype Data() {
 7
        do
8
           data = nonCS;
9
            enterCS(data);
10
            exitCS(data);
11
            data = idle;
12
13
        od
14
```

Priority Inversion in Promela (2)

```
active proctype Comm() provided (!ready(data)) {
        do
            comm = long;
            comm = idle;
4
 5
        od
6
 7
    active proctype Telem() provided (!ready(data) && !ready(comm)) {
8
        do
9
           telem = nonCS;
10
            enterCS(telem);
11
            exitCS(telem);
12
            telem = idle;
13
14
        od
15
```

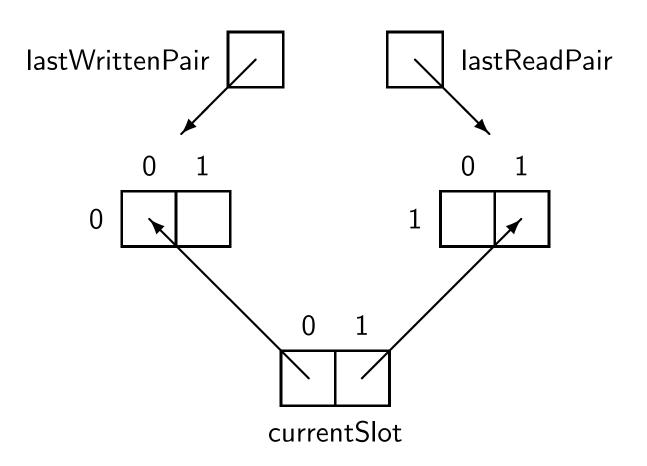
Priority Inversion in Promela (3)

```
bit sem = 1;
    inline enterCS(state) {
3
        atomic {
4
           if
5
            :: sem == 0 ->
6
             state = blocked;
                sem != 0;
8
9
           :: else ->
          fi;
10
       sem = 0;
11
           state = CS;
12
13
14
15
    inline exitCS(state) {
16
        atomic {
17
           sem = 1;
18
           state = idle
19
20
21
```

Priority Inheritance in Promela

```
#define inherit (p) (p == CS)
2
    active proctype Data() {
3
      do
4
5
      :: data = nonCS:
          assert(! (telem == CS \&\& comm == long));
6
          enterCS(data); exitCS(data);
          data = idle;
8
9
      od
10
11
12
    active proctype Comm()
      provided (! ready(data) && !inherit(telem))
13
       { ... }
14
15
    active proctype Telem()
16
      provided (! ready(data) && !ready(comm) || inherit(telem))
17
       { ... }
18
```

Data Structures in Simpson's Algorithm



```
Algorithm 13.8: Simpson's four-slot algorithm
```

```
dataType array[0..1,0..1] data \leftarrow default initial values bit array[0..1] currentSlot \leftarrow { 0, 0 } bit lastWrittenPair \leftarrow 1, lastReadPair \leftarrow 1
```

writer

```
bit writePair, writeSlot
dataType item
loop forever
```

```
p1: item \leftarrow produce
```

```
p2: writePair \leftarrow 1— lastReadPair
```

```
p3: writeSlot \leftarrow 1 - currentSlot[writePair]
```

```
p4: data[writePair, writeSlot] \leftarrow item
```

```
p5: currentSlot[writePair] \leftarrow writeSlot
```

p6: lastWrittenPair ← writePair

Algorithm 13.8: Simpson's four-slot algorithm (continued)

reader

```
bit readPair, readSlot
dataType item
loop forever
```

p7: readPair ← lastWrittenPair

p8: $lastReadPair \leftarrow readPair$

p9: $readSlot \leftarrow currentSlot[readPair]$

p10: item ← data[readPair, readSlot]

p11: consume(item)

Algorithm 13.9: Event signaling			
binary semaphore s \leftarrow 0			
p	q		
p1: if decision is to wait for event	q1: do something to cause event		
p2: wait(s)	q2: signal(s)		

Suspension Objects in Ada

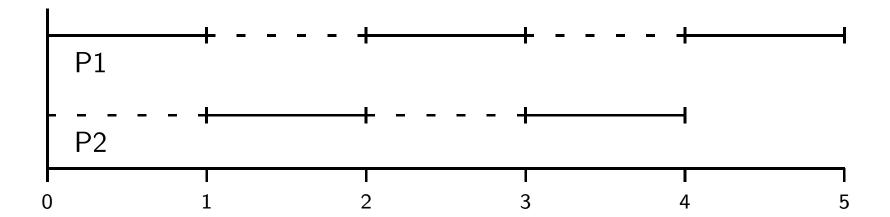
```
package Ada.Synchronous_Task_Control is
      type Suspension_Object is limited private;
      procedure Set_True(S : in out Suspension_Object);
3
      procedure Set_False(S: in out Suspension_Object);
4
      function Current_State(S : Suspension_Object)
5
        return Boolean;
6
      procedure Suspend_Until_True(
7
        S: in out Suspension_Object);
8
9
    private
10
      — not specified by the language
11
    end Ada.Synchronous_Task_Control;
```

Algorithm 13.10: Suspension object - event signaling			
Suspension_Object SO \leftarrow (false by default)			
p	q		
p1: if decision is to wait for event	q1: do something to cause event		
p2: Suspend_Until_True(SO)	q2: Set_True(SO)		

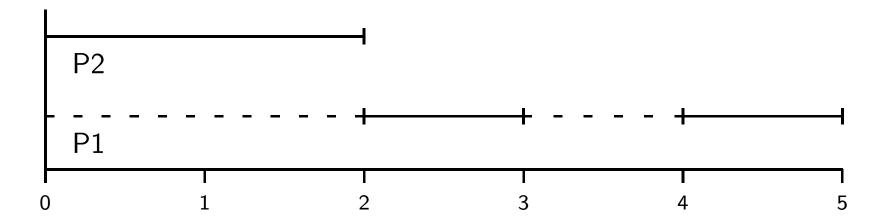
Transition in UPPAAL

$$clk >= 12, ch?, n := n + 1$$

Feasible Priority Assignment



Infeasible Priority Assignment



Algorithm 13.11: Periodic task

constant integer period ← ...

 $integer\ next \leftarrow currentTime$

loop forever

p1: delay next — currentTime

p2: compute

p3: $next \leftarrow next + period$

Semantics of Propositional Operators

A	$v(A_1)$	$v(A_2)$	v(A)
$\neg A_1$	T		F
$\neg A_1$	F		T
$A_1 \lor A_2$	F	F	F
$A_1 \vee A_2$	otherwise		T
$A_1 \wedge A_2$	T	T	T
$A_1 \wedge A_2$	otherwise		F
$A_1 \rightarrow A_2$	T	F	F
$A_1 \rightarrow A_2$	otherwise		T
$A_1 \leftrightarrow A_2$	$v(A_1) = v(A_2)$		T
$A_1 \leftrightarrow A_2$	$v(A_1) \neq v(A_2)$		F

Wason Selection Task

p3

p5

flag = 1

flag = 0

Algorithm 2.1: Verification example

```
integer x1, integer x2 integer y1 \leftarrow 0, integer y3 \leftarrow 0, integer y3 \leftarrow 0
```

```
p1: read(x1,x2)

p2: y3 \leftarrow x1

p3: while y3 \neq 0

p4: if y2+1 = x2

p5: y1 \leftarrow y1 + 1

p6: y2 \leftarrow 0

p7: else

p8: y2 \leftarrow y2 + 1

p9: y3 \leftarrow y3 - 1

p10: write(y1,y2)
```

Spark Program for Integer Division

```
1 \quad --\# main_program;
procedure Divide(X1,X2: in Integer; Q,R: out Integer)
3 --\# derives Q, R from X1,X2;
4 --\# pre (X1 >= 0) and (X2 > 0);
5 --\# post (X1 = Q * X2 + R) and (X2 > R) and (R >= 0);
6
   is
7
       N: Integer;
8
   begin
   Q := 0: R := 0: N := X1:
   while N /= 0
10
   --\# assert (X1 = Q*X2+R+N) and (X2 > R) and (R >= 0);
11
12
     loop
         if R+1 = X2 then
13
            Q := Q + 1: R := 0:
14
15
         else
            R := R + 1:
16
         end if:
17
         N := N - 1;
18
19
      end loop;
    end Divide;
20
```

Integer Division

```
procedure Divide(X1,X2: in Integer; Q,R: out Integer) is
2
        N: Integer;
3
    begin
       -- pre (X1 >= 0) and (X2 > 0);
      Q := 0; R := 0; N := X1;
     while N /= 0
6
       -- assert (X1 = Q*X2+R+N) and (X2 > R) and (R >= 0);
8
      loop
         if R+1 = X2 then Q := Q + 1; R := 0;
9
         else R := R + 1;
10
         end if;
11
         N := N - 1;
12
      end loop;
13
       -- post (X1 = Q * X2 + R) and (X2 > R) and (R >= 0);
14
    end Divide;
15
```

Verification Conditions for Integer Division

Precondition to assertion:

$$(X1 \ge 0) \land (X2 > 0) \to (X1 = Q \cdot X2 + R + N) \land (X2 > R) \land (R \ge 0).$$

Assertion to postcondition:

$$(X1 = Q \cdot X2 + R + N) \land (X2 > R) \land (R \ge 0) \land (N = 0) \rightarrow (X1 = Q \cdot X2 + R) \land (X2 > R) \land (R \ge 0).$$

Assertion to assertion by then branch:

$$(X1 = Q \cdot X2 + R + N) \land (X2 > R) \land (R \ge 0) \land (R + 1 = X2) \rightarrow (X1 = Q' \cdot X2 + R' + N') \land (X2 > R') \land (R' \ge 0).$$

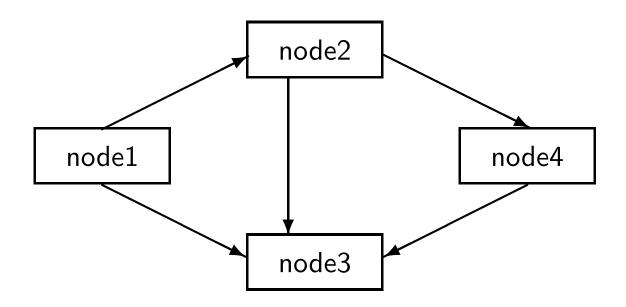
Assertion to assertion by else branch:

$$(X1 = Q \cdot X2 + R + N) \land (X2 > R) \land (R \ge 0) \land (R + 1 \ne X2) \rightarrow (X1 = Q' \cdot X2 + R' + N') \land (X2 > R') \land (R' \ge 0).$$

The Sleeping Barber

n	producer	consumer	Buffer	notEmpty
1	append(d, Buffer)	wait(notEmpty)	[]	0
2	signal(notEmpty)	wait(notEmpty)	[1]	0
3	append(d, Buffer)	wait(notEmpty)	[1]	1
4	append(d, Buffer)	$d \leftarrow take(Buffer)$	[1]	0
5	append(d, Buffer)	wait(notEmpty)	[]	0

Synchronizing Precedence



Algorithm 3.1: Barrier synchronization

global variables for synchronization

loop forever

p1: wait to be released

p2: computation

p3: wait for all processes to finish their computation

Slide - 3.3

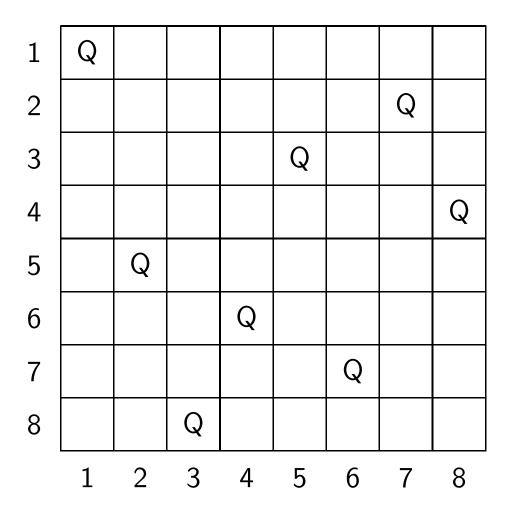
The Stable Marriage Problem

Man	List of women			
1	2	4	1	3
2	3	1	4	2
3	2	3	1	4
4	4	1	3	2

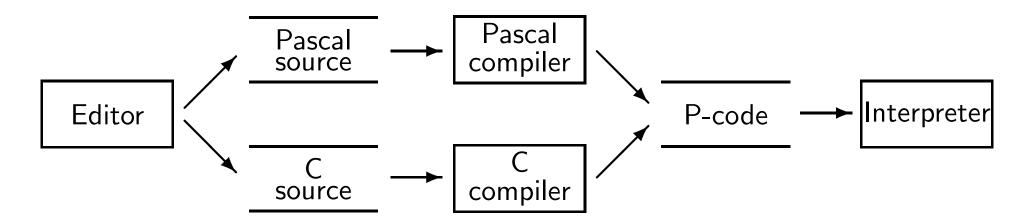
Woman	List of men			
1	2	1	4	3
2	4	3	1	2
3	1	4	3	2
4	2	1	4	3

```
Algorithm 3.2: Gale-Shapley algorithm for stable marriage
                    integer list freeMen \leftarrow \{1, \ldots, n\}
                    integer list freeWomen \leftarrow \{1, \dots, n\}
                    integer pair-list matched \leftarrow \emptyset
                    integer array[1..n, 1..n] menPrefs \leftarrow ...
                    integer array[1..n, 1..n] womenPrefs \leftarrow ...
                    integer array[1..n] next \leftarrow 1
    while freeMen \neq \emptyset, choose some m from freeMen
       w \leftarrow menPrefs[m, next[m]]
p2:
       next[m] \leftarrow next[m] + 1
p3:
      if w in freeWomen
p4:
          add (m,w) to matched, and remove w from freeWomen
p5:
       else if w prefers m to m' // where (m',w) in matched
p6:
          replace (m',w) in matched by (m,w), and remove m' from freeMen
p7:
       else // w rejects m, and nothing is changed
p8:
```

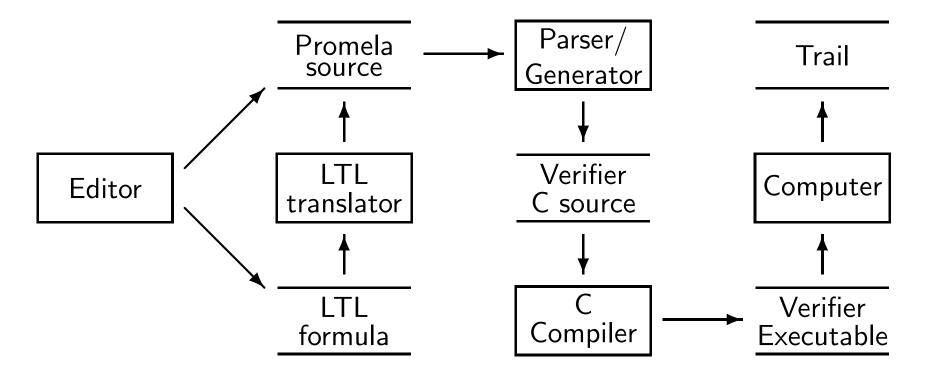
The n-Queens Problem



The Architecture of BACI



The Architecture of Spin



Cycles in a State Diagram

