

Summary of the EM Algorithm for the Gaussian case:

$$D_1^i = \mu_2^{\text{old}} + \frac{\sigma_2^{\text{old}}}{1 - \Phi\left(\frac{s_i - \mu_2^{\text{old}}}{\sigma_2^{\text{old}}}\right)} \phi\left(\frac{s_i - \mu_2^{\text{old}}}{\sigma_2^{\text{old}}}\right)$$

$$D_2^i = (\mu_2^{\text{old}})^2 + (\sigma_2^{\text{old}})^2 + \frac{\mu_2^{\text{old}} \sigma_2^{\text{old}}}{1 - \Phi\left(\frac{s_i - \mu_2^{\text{old}}}{\sigma_2^{\text{old}}}\right)} \phi\left(\frac{s_i - \mu_2^{\text{old}}}{\sigma_2^{\text{old}}}\right)$$

$$+ \frac{(\sigma_2^{\text{old}})^2}{1 - \Phi\left(\frac{s_i - \mu_2^{\text{old}}}{\sigma_2^{\text{old}}}\right)} \phi\left(\frac{s_i - \mu_2^{\text{old}}}{\sigma_2^{\text{old}}}\right) s_i$$

$$X_1^i = \mu_1^{\text{old}} + \frac{\sigma_1^{\text{old}}}{1 - \Phi\left(\frac{s_i - \mu_1^{\text{old}}}{\sigma_1^{\text{old}}}\right)} \phi\left(\frac{s_i - \mu_1^{\text{old}}}{\sigma_1^{\text{old}}}\right)$$

$$X_2^i = (\mu_1^{\text{old}})^2 + (\sigma_1^{\text{old}})^2 + \frac{\mu_1^{\text{old}} \sigma_1^{\text{old}}}{1 - \Phi\left(\frac{s_i - \mu_1^{\text{old}}}{\sigma_1^{\text{old}}}\right)} \phi\left(\frac{s_i - \mu_1^{\text{old}}}{\sigma_1^{\text{old}}}\right)$$

$$+ \frac{(\sigma_1^{\text{old}})^2}{1 - \Phi\left(\frac{s_i - \mu_1^{\text{old}}}{\sigma_1^{\text{old}}}\right)} \phi\left(\frac{s_i - \mu_1^{\text{old}}}{\sigma_1^{\text{old}}}\right) s_i$$

$$\mu_1^{\text{new}} = \frac{1}{2N} \sum_{i=1}^N (x_1^i + s_i)$$

$$(\sigma_1^2)^{\text{new}} = \frac{1}{2N} \sum_{i=1}^N (x_1^i + s_i^2) - \left[\frac{1}{2N} \sum_{i=1}^N (x_1^i + s_i) \right]^2$$

$$\mu_2^{\text{new}} = \frac{1}{2N} \sum_{i=1}^N (D_1^i + s_i)$$

$$(\sigma_2^2)^{\text{new}} = \frac{1}{2N} \sum_{i=1}^N (D_2^i + s_i^2) - \left(\frac{1}{2N} \sum_{i=1}^N (D_1^i + s_i) \right)^2$$

Iterate until convergence.