

Computational tools for problem solving
Lab list 4

Problem 1. Consider the RSA cryptosystem with public key

$$(n, e) = (135828482760150159223553231524924630769084223558056259571, 17).$$

Assume the following encoding of two letters into one number in \mathbb{Z}_n .

A	B	C	D	E	F	G	H	I	J	K	L	M
65	66	67	68	69	70	71	72	73	74	75	76	77
N	O	P	Q	R	S	T	U	V	W	X	Y	Z
78	79	80	81	82	83	84	85	86	87	88	89	90

- i) Use Fermat's factoring method to factor n as the product of two prime numbers.
- ii) Compute $\phi(n)$.
- iii) Using the extended Euclidean algorithm, compute the private key of this RSA cryptosystem.
- iv) The ciphertext $c = 94600282655101343031930533427672565665615053708288843906$ was obtained by encrypting the encoding sequence of a message m . Find m .