

Assignment 1

The objective of this assignment is for you to gain familiarity with basic properties of univariate equity-index return series and standard test statistics gauging the existence of return dependence or weak-form predictability. A few useful technical tricks are also touched on in the exercises.

- 1) Provide a sketch of a proof for the Hausman Principle, given on page 11.
- 2) Derive the asymptotic distribution for the VD statistic on page 12.
- 3) Do the exercise on page 13 (on the VR statistic with overlapping returns). Hint: If it seems tricky, you can check the literature, e.g., Lo & MacKinlay publications, for inspiration.
- 4) Hong, Linton and Zhang (2017, JFEc) (HLZ) provide a correction and extension to the Variance Ratio statistic explored by Lo & MacKinlay (no formal proofs needed below).
 - a) Identify the changes in assumptions they introduce relative to Lo & MacKinlay.
 - b) What are the advantages of their proposed new assumptions?
 - c) State the limiting distribution result for the **univariate VR statistic** in their paper.
- 5) Apply the Spearman Correlation Test on page 4 of the notes to explore dependence for the daily S&P 500 index returns.
 - a) First, do the test as suggested for January 1991-December 2006 period.
 - b) Second, do the same test for the sample period 2007-2022.
 - c) Repeat the above, but using the absolute returns in lieu of the returns.
- 6) Implement the Lo & MacKinlay Variance Ratio test for the CRSP value-weighted and equal-weighted indices over their sample period, and for the periods 1991-2006 and 2007-2022. Try to assess significance according to the Lo & MacKinlay and HLZ robust limiting distributions.