Graph Algorithms for Engineering

Session 4







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Quick Recap

What we know so far:

- **V** Graph modeling (nodes, relationships)
- **V** Cypher queries (CREATE, MATCH, traversals)
- V Advanced patterns (properties, time-based, hierarchies)

Today: Use ALGORITHMS to solve real engineering problems!

The Story

A Crisis at LogisTech







Meet LogisTech Industries

Company: LogisTech Industries

Business: Supply chain for automotive parts across Europe

Crisis: A major supplier just went bankrupt!

Critical Questions:

- Which factories are affected?
- What's the fastest way to reroute shipments?
- Which suppliers are most critical to our operations?
- Can we find alternative supply chains?

Why They Need Graph Algorithms

Manual analysis would take weeks—they need answers NOW!

Graph algorithms can:

- Find optimal routes in seconds
- Identify critical nodes (suppliers, warehouses)
- Detect communities (clustered operations)
- Calculate impact of failures

Let's learn these algorithms!

Algorithm 1

Shortest Path (Dijkstra)







Shortest Path: What Is It?

Find the path with MINIMUM total cost between two points

Real-world applications:

- Logistics: Fastest delivery route
- Manufacturing: Shortest material flow path
- Robotics: Optimal robot navigation
- Network design: Minimum cable length

Cost can be: Distance, time, money, energy, risk...

How Dijkstra's Algorithm Works

Simple explanation:

- 1. Start at source node
- 2. Visit nearest unvisited neighbor
- 3. Calculate total cost to reach it
- 4. Keep track of best path found so far
- 5. Repeat until destination is reached

Always finds the optimal path!

X Hands-On: Build Logistics Network

Scenario: Build a distribution network with delivery times

```
CREATE (paris:City {name: "Paris"})
CREATE (lyon:City {name: "Lyon"})
CREATE (marseille:City {name: "Marseille"})
CREATE (toulouse:City {name: "Toulouse"})
CREATE (bordeaux:City {name: "Bordeaux"})
CREATE (strasbourg:City {name: "Strasbourg"})

CREATE (strasbourg:City {name: "Strasbourg"})

CREATE (paris)-[:ROAD {distance: 465, time_hours: 4.5}]->(lyon)
CREATE (lyon)-[:ROAD {distance: 315, time_hours: 3.0}]->(marseille)
CREATE (paris)-[:ROAD {distance: 679, time_hours: 6.5}]->(toulouse)
CREATE (toulouse)-[:ROAD {distance: 245, time_hours: 2.5}]->(bordeaux)
CREATE (bordeaux)-[:ROAD {distance: 584, time_hours: 5.5}]->(garis)
CREATE (paris)-[:ROAD {distance: 489, time_hours: 4.8}]->(strasbourg)
CREATE (lyon)-[:ROAD {distance: 505, time_hours: 5.0}]->(toulouse)
```

Find Shortest Path: Simple Method

Question: What's the shortest route from Paris to Marseille?

Result: Paris → Lyon → Marseille (780 km)



Breaking Down: shortestPath()

Let's understand how shortestPath works with reduce()

```
MATCH path = shortestPath(
  (start:City {name: "Paris"})
  -[:ROAD*]->
  (end:City {name: "Marseille"})
RETURN nodes(path) as cities,
      reduce(dist = 0, rel in relationships(path) |
              dist + rel.distance) as total distance
```

Step 1: Find Shortest Path

```
MATCH path = shortestPath(
  (start:City {name: "Paris"})
  -[:ROAD*]->
  (end:City {name: "Marseille"})
)
```

What this does:

- shortestPath() → Built-in Cypher function
- -[:ROAD*]-> → Follow ROAD relationships, any depth
- path = → Save the complete path
- Finds path with FEWEST hops (not necessarily shortest distance!)

Found path: Paris → Lyon → Marseille (2 hops)

Step 2: Calculate Total Distance

```
RETURN nodes(path) as cities,
reduce(dist = 0, rel in relationships(path) |
dist + rel.distance) as total_distance
```

Breaking it down:

- nodes(path) → Extract cities from path
- reduce(dist = 0, ...) → Start with distance 0
- rel in relationships(path) → Loop through road segments
- dist + rel.distance → Add each segment's distance

Calculation:

Start: dist = 0

+ Paris→Lyon: 465 km = 465

+ Lyon→Marseille: 315 km = **780 km total**

Important: Fewest Hops ≠ Shortest Distance

shortestPath() finds path with FEWEST relationships, NOT minimum total distance!

Example:

- Path A: Paris → Lyon → Marseille (2 hops, 780 km)
- **Path B:** Paris → Bordeaux → Toulouse → Lyon → Marseille (4 hops, 650 km)

shortestPath() chooses Path A (fewer hops), even though Path B is shorter distance!

Solution: Use reduce() to calculate actual distance, then sort manually (next slide!)

Shortest Path by TIME (not distance)

Challenge: Find fastest route, not shortest!

☑ Might find a longer route that's faster!

Find ALL Possible Paths

Use case: Find backup routes in case of road closure

✓ Shows top 5 routes sorted by distance!

Algorithm 2

Impact Analysis (Connected Components)







Impact Analysis: What Is It?

Find everything AFFECTED when a node fails

Critical business questions:

- "If Supplier X fails, which factories stop?"
- "If this part is recalled, which products are affected?"
- "If this server goes down, which services fail?"
- "If this road closes, which deliveries are delayed?"

Also called: Downstream impact, cascade analysis, dependency analysis

X Hands-On: Build Supply Chain

Scenario: Multi-tier supply chain

```
CREATE (raw:Supplier {name: "RawMaterials Co", tier: 3})

CREATE (parts1:Supplier {name: "PartsMaker GmbH", tier: 2})

CREATE (parts2:Supplier {name: "Components Ltd", tier: 2})

CREATE (assembly:Supplier {name: "AssemblyPro SA", tier: 1})

CREATE (factory:Factory {name: "AutoMeca Plant"})

CREATE (product:Product {name: "Electric Motor EM-1000"})

CREATE (raw)-[:SUPPLIES]->(parts1)

CREATE (raw)-[:SUPPLIES]->(parts2)

CREATE (parts1)-[:SUPPLIES]->(assembly)

CREATE (parts2)-[:SUPPLIES]->(assembly)

CREATE (assembly)-[:SUPPLIES]->(factory)

CREATE (factory)-[:PRODUCES]->(product)
```

✓ A realistic multi-tier supply chain!

Find Downstream Impact

Crisis: RawMaterials Co just failed! What's affected?

Result shows:

- 2 Tier-2 suppliers (PartsMaker, Components)
- 1 Tier-1 supplier (AssemblyPro)
- 1 Factory
- 1 Product

Complete production stops!

Quantify the Impact

```
MATCH (s:Supplier)

OPTIONAL MATCH (s)-[:SUPPLIES*]->(affected)

WITH s,

COUNT(DISTINCT affected) as impact_count

RETURN s.name as supplier,

s.tier as tier,

impact_count

ORDER BY impact_count DESC
```

Shows: Which suppliers are most critical!

Higher tier suppliers have bigger impact



Breaking Down: OPTIONAL MATCH

This query uses OPTIONAL MATCH to handle suppliers with no downstream!

```
MATCH (s:Supplier)
OPTIONAL MATCH (s)-[:SUPPLIES*]->(affected)
WITH s,
     COUNT(DISTINCT affected) as impact count
RETURN s.name as supplier,
       s.tier as tier,
       impact count
ORDER BY impact count DESC
```

Step 1: MATCH vs OPTIONAL MATCH

MATCH (s:Supplier)
OPTIONAL MATCH (s)-[:SUPPLIES*]->(affected)

Regular MATCH:

- Returns ONLY suppliers that have downstream
- Excludes end-of-chain suppliers
- Like SQL INNER JOIN

OPTIONAL MATCH:

- Returns ALL suppliers
- If no downstream, affected = null
- Like SQL LEFT JOIN

Use OPTIONAL MATCH when: Some nodes might not have the pattern, but you still want them in results

Step 2: COUNT(DISTINCT affected)

WITH s, COUNT(DISTINCT affected) as impact_count

Breaking it down:

- COUNT(affected) → Count how many downstream nodes
- DISTINCT → Don't count same node twice
- If affected = null (no downstream), COUNT = 0

Example results:

Supplier	Tier	Impact Count
RawMaterials Co	3	5
AssemblyPro SA	1	2



Why Use OPTIONAL MATCH Here?

Without OPTIONAL, we'd miss important suppliers!

Without OPTIONAL:

```
MATCH (s:Supplier)
MATCH (s)-[:SUPPLIES*]->(affected)
...
```

X Excludes Tier-1 suppliers who supply directly to factories!

With OPTIONAL:

```
MATCH (s:Supplier)
OPTIONAL MATCH (s)-[:SUPPLIES*]->(affected)
```

✓ Includes ALL suppliers, even those at end of chain!

Deep Dive

Understanding OPTIONAL MATCH







Let's Build a Simple Example

We'll create 3 suppliers with different downstream connections:

```
// Create simple supply chain
CREATE (s1:Supplier {name: "RawMat Inc", tier: 3})
CREATE (s2:Supplier {name: "PartsMaker", tier: 2})
CREATE (s3:Supplier {name: "EndSupplier", tier: 1})
CREATE (factory:Factory {name: "Plant A"})

// Create supply chain: s1 - s2 - factory
CREATE (s1)-[:SUPPLIES]->(s2)
CREATE (s2)-[:SUPPLIES]->(factory)

// Note: s3 has NO downstream connections!
```

Graph structure:

```
RawMat Inc (tier 3) → PartsMaker (tier 2) → Plant A EndSupplier (tier 1) → [nobody]
```

Test 1: Using Regular MATCH

Let's try to count downstream for ALL suppliers using regular MATCH:

Result: Regular MATCH

Problem: EndSupplier is MISSING!

Supplier	Tier	Impact
RawMat Inc	3	2
PartsMaker	2	1
EndSupplier	1	X NOT SHOWN

Why? Second MATCH requires pattern to exist. EndSupplier has no downstream, so it's excluded!

Test 2: Using OPTIONAL MATCH

Now let's try with OPTIONAL MATCH:

Notice: Only changed MATCH to OPTIONAL MATCH!

Result: OPTIONAL MATCH

Success: ALL suppliers included!

Supplier	Tier	Impact
RawMat Inc	3	2
PartsMaker	2	1
EndSupplier	1	v 0

Why? OPTIONAL MATCH returns NULL when pattern doesn't match. COUNT(NULL) = 0!

Side-by-Side: The Difference

MATCH (s:Supplier) MATCH (s)-[:SUPPLIES*]->(d) ... Acts like SQL INNER JOIN Result: 2 rows • RawMat Inc (2) • PartsMaker (1) • EndSupplier MISSING!

```
OPTIONAL MATCH

MATCH (s:Supplier)
OPTIONAL MATCH (s)-[:SUPPLIES*]->(d)
...

Acts like SQL LEFT JOIN

Result: 3 rows

• RawMat Inc (2)
• PartsMaker (1)
• EndSupplier (0) ✓
```

When to Use OPTIONAL MATCH?

Use OPTIONAL MATCH when some nodes might NOT have the pattern



- Counting connections (some may have 0)
- Finding all nodes even if isolated
- Calculating impact (includes zero impact)
- Left join scenarios

Use Regular MATCH for:

- Pattern MUST exist
- Only interested in connected nodes
- Inner join scenarios
- Filtering by relationship existence

X Practice: Try Both!

Exercise: Run both queries and compare results

Query 1 (Regular MATCH):

```
MATCH (s:Supplier)
MATCH (s)-[:SUPPLIES]->(customer)
RETURN s.name, COUNT(customer) as customers
ORDER BY customers DESC
```

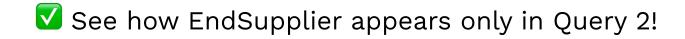
Query 2 (OPTIONAL MATCH):

```
MATCH (s:Supplier)

OPTIONAL MATCH (s)-[:SUPPLIES]->(customer)

RETURN s.name, COUNT(customer) as customers

ORDER BY customers DESC
```





OPTIONAL MATCH = "Try to find this pattern, but don't fail if it doesn't exist"

Think of it like this:

- MATCH: "Give me all students WHO have grades"
- OPTIONAL MATCH: "Give me all students, AND their grades IF they have any"

In SQL terms: OPTIONAL MATCH ≈ LEFT OUTER JOIN

Find Upstream Dependencies

Question: What does the factory depend on?

Shows: Complete dependency tree!

All suppliers the factory relies on, at all tiers

Algorithm 3 **Centrality Analysis**







Centrality: What Is It?

Measure how IMPORTANT a node is in the network

Degree Centrality

How many connections?

High → Hub node

Betweenness Centrality

How many paths pass through?

High → Bottleneck

Use cases: Find critical suppliers, bottleneck processes, key influencers

Degree Centrality (Simple)

Question: Which suppliers serve the most customers?

Shows: Hub suppliers with most connections

These are critical—their failure affects many!

Find Bottlenecks

Bottleneck: A node that many paths pass through

☑ Identifies single points of failure!

Algorithm 4

Community Detection







Community Detection: What Is It?

Find clusters of tightly connected nodes

Engineering applications:

- Supply chain: Regional supplier clusters
- Manufacturing: Coupled subsystems
- Organization: Team structures
- Products: Modular components

Why useful? Simplify complex systems, optimize operations, reduce risk



X Hands-On: Build Collaboration Network

```
CREATE (alice:Engineer {name: "Alice", dept: "Mech"})
CREATE (bob:Engineer {name: "Bob", dept: "Mech"})
CREATE (carol:Engineer {name: "Carol", dept: "Mech"})
CREATE (david:Engineer {name: "David", dept: "Elec"})
CREATE (emma:Engineer {name: "Emma", dept: "Elec"})
CREATE (frank:Engineer {name: "Frank", dept: "Elec"})
CREATE (alice)-[:COLLABORATES]->(bob)
CREATE (bob)-[:COLLABORATES]->(carol)
CREATE (carol)-[:COLLABORATES]->(alice)
CREATE (david)-[:COLLABORATES]->(emma)
CREATE (emma)-[:COLLABORATES]->(frank)
CREATE (frank)-[:COLLABORATES]->(david)
CREATE (carol)-[:COLLABORATES]->(david)
```

✓ Two tight teams with one bridge connection!

Find Connected Groups

Question: Who works closely together?

```
MATCH (e:Engineer)

OPTIONAL MATCH (e)-[:COLLABORATES*1..2]-(colleague:Engineer)

WITH e, COLLECT(DISTINCT colleague.name) as team

RETURN e.name as engineer,

e.dept as department,

SIZE(team) as team_size,

team

ORDER BY team_size DESC
```

☑ Shows collaboration network for each engineer!

Find Bridge Connections

Bridge: A person connecting two otherwise separate groups

```
MATCH (e:Engineer)-[:COLLABORATES]-(colleague1:Engineer)

MATCH (e)-[:COLLABORATES]-(colleague2:Engineer)

WHERE colleague1.dept <> colleague2.dept

AND colleague1 <> colleague2

RETURN DISTINCT e.name as bridge_person,

e.dept as department,

COUNT(DISTINCT colleague1) +

COUNT(DISTINCT colleague2) as connections

ORDER BY connections DESC
```

▼ These people are critical for cross-team communication!

Putting It All Together

Complete Supply Chain Analysis







Tinal Challenge

Crisis Simulation: Complete supply chain risk analysis

Your mission:

- 1. Build a realistic supply chain network
- 2. Find shortest delivery paths
- 3. Identify critical suppliers (centrality)
- 4. Analyze failure impact
- 5. Find alternative routes

Use ALL algorithms we learned!

Step 1: Build Complete Network

```
// Suppliers
CREATE (s1:Supplier {name: "Steel Inc", tier: 3, location: "Germany"})
CREATE (s2:Supplier {name: "Plastics Co", tier: 3, location: "Italy"})
CREATE (s3:Supplier {name: "Parts GmbH", tier: 2, location: "France"})
CREATE (s4:Supplier {name: "Components Ltd", tier: 2, location: "Spain"})
CREATE (s5:Supplier {name: "Assembly Pro", tier: 1, location: "France"})
// Factories
CREATE (f1:Factory {name: "Factory Paris", location: "France"})
CREATE (f2:Factory {name: "Factory Munich", location: "Germany"})
// Supply relationships with lead times
CREATE (s1)-[:SUPPLIES {leadTime: 5, cost: 1000}]->(s3)
CREATE (s1)-[:SUPPLIES {leadTime: 7, cost: 1200}]->(s4)
CREATE (s2)-[:SUPPLIES {leadTime: 4, cost: 800}]->(s3)
CREATE (s2)-[:SUPPLIES {leadTime: 6, cost: 900}]->(s4)
CREATE (s3)-[:SUPPLIES {leadTime: 3, cost: 2000}]->(s5)
CREATE (s4)-[:SUPPLIES {leadTime: 3, cost: 1800}]->(s5)
CREATE (s5)-[:SUPPLIES {leadTime: 2, cost: 5000}]->(f1)
CREATE (s5)-[:SUPPLIES {leadTime: 4, cost: 5500}]->(f2)
```

Analysis 1: Fastest Supply Route

Question: What's the fastest path from Steel Inc to Factory Paris?

Result: Steel Inc → Parts GmbH → Assembly Pro → Factory Paris (10 days)

Analysis 2: Find Critical Suppliers

Question: Which suppliers have highest impact?

```
MATCH (s:Supplier)

OPTIONAL MATCH (s)-[:SUPPLIES*]->(downstream)

WITH s,

COUNT(DISTINCT downstream) as impact,
s.tier as tier

RETURN s.name as supplier,
tier,
s.location as location,
impact as downstream_entities

ORDER BY impact DESC, tier DESC
```

☑ Shows which suppliers affect the most downstream entities!

Analysis 3: Simulate Supplier Failure

Simulation: What if Steel Inc fails?

Impact Assessment:

- 2 Tier-2 suppliers affected
- 1 Tier-1 supplier affected
- 2 Factories at risk

Analysis 4: Find Alternative Routes

Question: If Parts GmbH fails, what are backup routes?

☑ Shows backup routes avoiding the failed supplier!

Analysis 5: Cost vs Time Trade-off

Question: Compare routes by cost AND time

✓ Helps make informed business decisions!

Real-World Success Story

Company: Large automotive manufacturer

Challenge: COVID-19 chip shortage (2021)

Solution: Graph algorithms for supply chain analysis

Results:

- Identified alternative suppliers in 2 hours (vs 2 weeks)
- Found optimal rerouting saving €2M
- Prevented 3 factory shutdowns

Graph algorithms saved their business!

Summary: 4 Key Algorithms

1. Shortest Path (Dijkstra): Find optimal routes

Use: Logistics, navigation, optimization

2. Impact Analysis: Find downstream effects

Use: Risk assessment, failure analysis

3. Centrality: Identify critical nodes

Use: Find hubs, bottlenecks, key players

4. Community Detection: Find clusters

Use: Simplify systems, optimize organization

Key Takeaways



☑ Algorithms turn graphs into INSIGHTS!

Remember:

- Use shortest path for optimization
- Use **impact analysis** for risk
- Use **centrality** for importance
- Use community detection for structure

Pro tip: Combine multiple algorithms for deeper insights!

Quick Decision Guide

I need to...

- Find best route → Shortest Path
- Assess failure risk → Impact Analysis
- Identify critical nodes → **Centrality**
- Group related items → Community Detection
- Find all dependencies → Traversal (*)
- Find alternative paths → Multiple Shortest Paths
- Detect bottlenecks → Betweenness Centrality
- Find connection strength → Degree Centrality

Advanced Topics (Beyond This Course)

Graph Data Science Library (Neo4j GDS)

- PageRank (Google's algorithm)
- Louvain (community detection)
- Node similarity
- Link prediction
- Graph embeddings (ML)

These require additional installation but are VERY powerful!

Cypher Algorithm Cheat Sheet

Shortest Path: MATCH path = shortestPath((a)-[:REL*]->(b)) RETURN path **Impact (downstream):** MATCH (n)-[:REL*]->(affected) RETURN affected **Dependencies (upstream):** MATCH (n)<-[:REL*]-(dependency) RETURN dependency **Degree Centrality:** MATCH (n)-[r]->() RETURN n, COUNT(r) as degree **All Paths:** MATCH path = (a)-[:REL*1..5]->(b) RETURN path

Practice Exercises

Try these on your own:

- 1. Build your own supply chain and find critical paths
- 2. Model your university course prerequisites
- 3. Create a project dependency graph
- 4. Map your team's collaboration network
- 5. Design a manufacturing process flow

Goal: Apply algorithms to YOUR domain!

Learning Resources

Free Resources:

- Neo4j GraphAcademy: Free courses on algorithms
- Neo4j Sandbox: Try algorithms online
- Graph Data Science Playground: Interactive tutorials

Documentation:

neo4j.com/docs/cypher-manual → Path Functions

neo4j.com/docs/graph-data-science → Algorithms

Questions?







Thank you!

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Now go analyze some graphs! 🐬