Basic Concepts
Performance Analysis & Measurement

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Outline

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1 Performance Analysis

2 Performance Measurement

Criteria for judging a program:

- Meet the original specification?
- Work correctly?
- The documentation.
- Does the program effectively use functions to create logic units?
- Code readability.
- Efficient usage of storage?
- Acceptable running time?

Performance Analysis

machine independent

- Space complexity
  - The amount of memory that it needs to run to completion.

- Time complexity
  - Computing time

Space complexity

$$S(P) = c + S_P(I),$$

P: the program; I: the input.

- ⋆ $S_P(I)$ can be represented by $S_P(n)$ if n is the only instance characteristic.

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- ⋆ $S_P(I)$ can be represented by $S_P(n)$ if n is the only instance characteristic.

- Fixed space requirement: c.
  - Independent of the characteristics of the inputs and outputs.
    - Instruction space.
    - Space for simple variables, fixed-size structured variable and constants.

- **Variable** Space Requirement ($S_P(I)$)
  - depend on the instance characteristic I.
    - For instance, additional space when the program uses recursion.
  - values of inputs and outputs associated with I.

Example

- Assume that the integers are stored in an array 'list', such that the ith integer is stored in the ith position list[i].

```
float abc(float a, float b, float c) {
    return a + b + b * c + (a + b - c) / (a + b) + 4.00;
}
```

- Fixed space requirement (c): 16.
  - Three float numbers: a, b, c and one return float number.
- $S_{abc}(I) = 0$. (for only fixed space requirements)

Example

```
float sum(float list[ ], int n) {
    float temp = 0;
    int i;
    for (i=0; i<n; i++)
        temp += list[i];
    return temp;
}
```

- In this program, $S_{\mathrm{sum}}(I) = 0$.
- C Programming Language: passing the address of the first element of list[] (instead of copying).

Example (recursive)

```
float rsum(float list[ ], int n) {
    if (n) return list[n] + rsum(list, n-1);
    return list[0];
}
```

- Total variable space: $S_{\mathrm{rsum}}(l) = 12n$.
    - parameter list []: array pointer: 4 bytes.
    - parameter n: integer: 4 bytes
    - return address (internally used): 4 bytes.
- The recursive version has a far greater overhead than its iterative counterpart.

Time Complexity: $T(P) = c + T_P(I)$

- Compile time: c
  - Independent of the characteristics of the input and output.
  - Once the correctness of the program is verified, it can run without recompilation.

- Run time: $T_P(I)$ (what we are really concerned about)
  - E.g., $T_P(n) = c_a \cdot \mathrm{ADD}(n) + c_s \cdot \mathrm{SUB}(n) + c_l \cdot \mathrm{LDA}(n) + c_{st} \cdot \mathrm{STA}(n)$.
  - ADD, SUB, LDA, STA: the number of additions, subtractions, loads and stores.
  - c_a, c_s, c_l, c_{st}: the time needed to perform each operation (constants).

Time Complexity - Program Step (1/2)

⋆ machine independent

Program Step

a syntactically or semantically meaningful program segment whose execution time is independent of the instance characteristics.

- Example of ONE program step
    - `a = 2;`
    - `a = 2*b + 3*c/d - e + f/g/a/b/c;`

- In complexity analysis, we do not break down a statement into individual machine-level operations.

Time Complexity - Program Step (1/2)

Methods to compute the number of program steps

- Creating a global variable, say, count.
- Tabular method:
  - Compute the contribution of a statement:
    # program steps per execution $\times$ frequency.
  - Add up the contribution of all statements.

Example

```c
float sum(float list[ ], int n) {
    float tempSum = 0; count++; /* for assignment */
    int i;
    for (i = 0; i < n; i++) {
        count++; /* for the "for" loop */
        tempSum += list[i]; count++; /* for assignment */
    }
    count++; /* last execution of "for" */
    count++; /* for return */
    return tempSum;
}
```

- count $= 2n + 3$ (steps).

Example (Tabular Method)

s/e: steps per execution.

Statements	s/e	Frequency	Total Steps
`float sum(float list[ ], int n) {`	0	0	0
`float tempsum = 0;`	1	1	1
`int i;`	0	0	0
`for(i=0; i <n; i++)`	1	n+1	n+1
`tempsum += list[i];`	1	n	n
`return tempsum;`	1	1	1
`}`	0	0	0
Total			$2n + 3$

Asymptotic Notation

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- A motivating example:
- $c_3 n < c_1 n^2 + c_2 n$ when n is sufficiently large.
  - For $c_1 = 1$, $c_2 = 2$, $c_3 = 100$, $c_1 n^2 + c_2 n \leq c_3 n$ for $n \leq 98$.
  - For $c_1 = 1$, $c_2 = 2$, $c_3 = 1000$, $c_1 n^2 + c_2 n \leq c_3 n$ for $n \leq 998$.

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    - For $c_1 = 1$, $c_2 = 2$, $c_3 = 1000$, $c_1 n^2 + c_2 n \leq c_3 n$ for $n \leq 998$.
    - ⋆ For small values of n, either one could be faster.
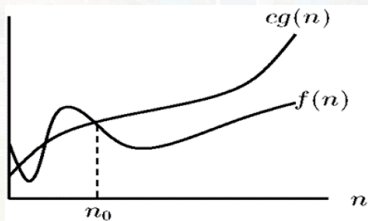
Big-O Notation

Definition ($O(\cdot)$)

$f(n) = O(g(n))$ (or write $f(n) \in O(g(n))$) iff there exist positive constants c and $n_0 \in \mathbb{N}$ such that $f(n) \leq cg(n)$ for all $n \geq n_0$.

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- $g(n)$ serves as an upper bound on $f(n)$.
  - The smaller $g(n)$ is, the more informative it would be!

Big-Ω Notation

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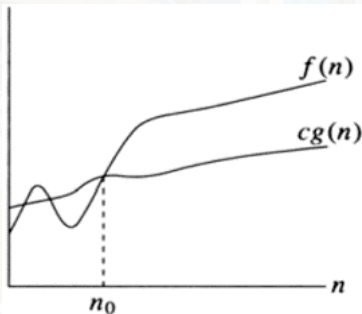
- $g(n)$ serves as an lower bound on $f(n)$.
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    - $6 \cdot 2^n + n^2 \leq 7 \cdot 2^n$ for $n \geq 4$.

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A Disproof Example

- **Claim:** $3n + 2$ is NOT $\Omega(n^2)$.

Proof (by contradiction). Assume $3n + 2 \in \Omega(n^2)$. Then there exist constants $c > 0$ and $n_0 \in \mathbb{N}$ such that

$$\forall n \geq n_0 : \quad 3n + 2 \; \geq \; c\,n^2. \qquad (*)$$

However, for all $n \geq 1$, we have $3n + 2 \; < \; 3n + 2n \; = \; 5n$. Moreover, if $n \geq \frac{5}{c}$, then $5n \leq c\,n^2$. Hence for

$$\text{for all } \; n \geq \max\left\{ 1, \; \left\lceil \tfrac{5}{c} \right\rceil, \; n_0 \right\}, \text{ we have } \; 3n + 2 \; < \; c\,n^2,$$

which contradicts $(*)$. Therefore $3n + 2 \notin \Omega(n^2)$. $\qquad \square$

Polynomial

Theorem 1.2

If $f(n) = a_k n^k + a_{k-1} n^{k-1} + \cdots + a_1 n + a_0$, then $f(n) = O(n^k)$.

Polynomial

Theorem 1.2

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Note that $n^{i-k} \leq 1$ if $i \leq k$ and $\sum_{i=0}^{k} |a_i|$ is a constant.

Most often seen big-O complexities

* with respect to the input of size n.
  - $O(1)$: constant.
  - $O(n)$: linear.
  - $O(n^2)$: quadratic.
  - $O(n^3)$: cubic.
  - $O(2^n)$: exponential.

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- $O(\log n)$: logarithmic.

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- $O(2^{\sqrt{n}})$: sub-exponential.
- $O(\log n)$: logarithmic.
    - $O(\lg n)$?
- $O(n \log n)$: log linear.

Polynomial (Lower Bound)

Theorem 1.3

If $f(n) = a_k n^k + a_{k-1} n^{k-1} + \cdots + a_1 n + a_0$ and $a_k > 0$, then $f(n) = \Omega(n^k)$.

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Proof:

- Skipped and left as an exercise.

Polynomial (Lower Bound)

Theorem 1.3

If $f(n) = a_k n^k + a_{k-1} n^{k-1} + \cdots + a_1 n + a_0$ and $a_k > 0$, then $f(n) = \Omega(n^k)$.

Proof:

- Skipped and left as an exercise.
- **Note:** a_i might be negative for $0 \leq i < k$.

Theta Notation (Θ)

Definition (Θ)

$f(n) = \Theta(g(n))$ iff $f(n) = O(g(n))$ and $f(n) = \Theta(g(n))$.

- More precise than simply using big-O or big-Ω notations.

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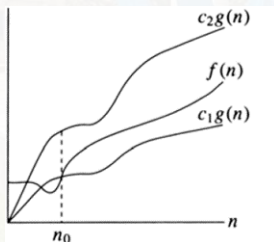
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Theorem 1.4

If $f(n) = a_k n^k + a_{k-1} n^{k-1} + \cdots + a_1 n + a_0$ and $a_k > 0$, then $f(n) = \Theta(n^k)$

Little "oh" and little "omega"

Definition (o)

The function $f(n) = o(g(n))$ iff

$$\lim_{n \to \infty} \frac{f(n)}{g(n)} = 0.$$

Definition (ω)

The function $f(n) = \omega(g(n))$ iff

$$\lim_{n \to \infty} \frac{g(n)}{f(n)} = 0.$$

Examples

- $3n + 2 = o(n^2)$ (i.e., $n^2 = \omega(n)$).
- $3n + 2 = o(n \log n)$.
- $3n + 2 = o(n \log \log n)$.
- $6 \cdot 2^n + n^2 \neq o(2^n)$.
- $6 \cdot 2^n + n^2 \neq o(2^n)$.
- $6 \cdot 2^n + n^2 = o(2^n \log n)$.

Example (Tabular Method)

| Statements	s/e	Frequency	Total Steps	Asymptotic Complexity
void add (int a[ ][MAX_SIZE],...) {	0	0	0	0
int i, j;	0	0	0	0
for (i = 0; i < row; i++)	1	rows+1	rows+1	$\Theta(\text{rows})$
for (j=0; j< cols; j++)	1	rows*(cols+1)	rows*(cols+1)	$\Theta(\text{rows} \cdot \text{cols})$
c[i][j] = a[i][j]+b[i][j];	1	rows*cols	rows*cols	$\Theta(\text{rows} \cdot \text{cols})$
}	0	0	0	0
Total		$2 \cdot \text{rows} \cdot \text{cols} + 2 \cdot \text{rows} + 1$		$\Theta(\text{rows} \cdot \text{cols})$

Function Values & Plots

Refer to Fig. 1.7 & 1.8 in the textbook.

Instance characteristic n							
Time	Name	1	2	4	8	16	32
1	Constant	1	1	1	1	1	1
$\log n$	Logarithmic	0	1	2	3	4	5
n	Linear	1	2	4	8	16	32
$n \log n$	Log linear	0	2	8	24	64	160
n^2	Quadratic	1	4	16	64	256	1024
n^3	Cubic	1	8	64	512	4096	32768
2^n	Exponential	2	4	16	256	65536	4294967296
$n!$	Factorial	1	2	24	40326	20922789888000	26313 x 10^{33}

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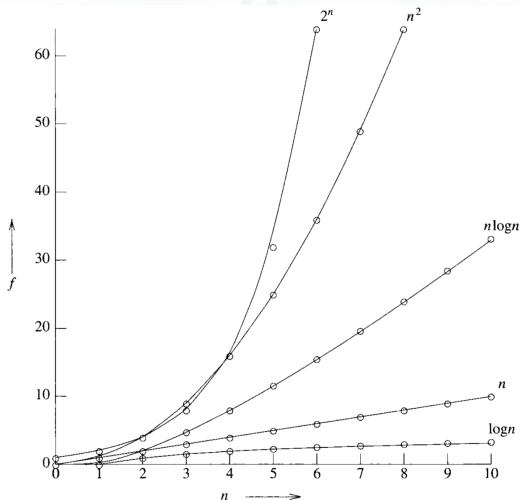
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2 Performance Measurement

Motivations

- Sometimes we still need to consider how long an algorithm executes **on our machine**.

- In order to obtain accurate times, we can repeatedly run the programs for several times (and take the average running time).

The Tricks

#include<time.h>

	1st Method	2nd Method
start timing	start = clock();	start = time(NULL);
stop timing	end = clock();	end = time(NUL);
type returned	clock_t	time_t

Result (in seconds):

- 1st Method: duration = (double)(stop-start))/(CLOCKS_PER_SEC);
- 2nd Method: duration = (double)difftime(stop, start);

The Tricks (Example)

```
...  // previous code omitted
    clock_t start, stop;
    double duration;
    printf("n time\n");
    for(i=0; i< ITERATIONS; i++) {
        for(j=0; j<sizeList[i]; j++)
            list[j] = sizeList[i]-j; /* worst case */
            start = clock();
            sort(list, sizeList[i]);
            stop = clock();
            /* number of clock ticks per second */
            duration = ((double) (stop-start));
            printf("%6d %f\n", sizeList[i], duration);
    }
}
```

⇒ sample code.

Discussions