Binary Search Trees & Forests

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Outline

Binary Search Trees

2 Forests



BSTs & Forests Binary Search Trees

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Binary Search Tree (BST) (1/2)

For searching, insertions and deletions...

Binary search tree provides a better performance then any of the data structures studied so far.



Binary Search Tree (BST) (2/2)

BST

A binary search tree (BST) is a binary tree which may be empty.

If it is not empty, then it satisfies the following properties:

- Each node has exactly one key and the keys in the tree are distinct.
- The keys (if any) in the left subtree are smaller than the key in the root.
- The keys (if any) in the right subtree are larger than the key in the root.
- The left and right subtrees are also binary search tree.



Binary Search Tree (BST) (2/2)

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- The left and right subtrees are also binary search tree.
 - a flavor of recursion?



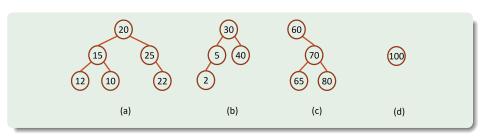
Examples of BST

• Which one of the following trees is BST? Which one is NOT?



Examples of BST

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Recursive Search of a BST

```
element* search(treePointer root, int key) {
/* return a pointer to the node that contains key,
   if there is no such node, return NULL. */
   if (!root) return NULL;
   if (k == root->data.key) return &(root->data);
   if (k < root->data.key)
      return search(root->leftChild, k);
   return search(root->rightChild, k);
}
```

• The time complexity of the search function is O(h), where h is the height of the binary search tree.

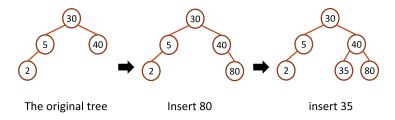


Iterative Search of a BST

```
element* iterSearch(treePointer tree, int k) {
/* return a pointer to the node that contains key,
   if there is no such node, return NULL. */
    while (tree) {
        if (k == tree->data.key) return &(tree→data);
        if (k < tree->data.key)
            tree = tree->leftChild:
        else
            tree = tree->rightChild;
    }
    return NULL;
```

• The time complexity of the search function is O(h), where h is the height of the binary search tree.

Inserting into a BST





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A Modified Searching Function

modifiedSearch(treePointer *node, int k)

- If the BST is empty, then return NULL.
- If the key *k* exists in the BST, return NULL.
- Otherwise, return the pointer of the last node in the BST.



Inserting a Dictionary Pair into a BST

```
void insert(treePointer *node, int k, iType theItem) {
/* If k is in the tree pointed at by "node", do nothing;
   otherwise, add a new node with data = (k, theItem) */
    treePointer ptr, temp = modifiedSearch(*node, k);
    if (temp || !(*node)) { /* k is not in the tree */
        malloc(ptr, sizeof(*ptr));
        ptr->data.key = k;
        ptr->data.item = theItem;
        ptr->leftChild = ptr->rightChild = NULL;
        if (*node) /* insert as child of temp */
            if (k < temp->data.key)
                temp->leftChild = ptr;
            else
                temp->rightChild = ptr;
        else
            *node = ptr;
```

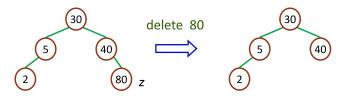
Deletion from a BST

- Case 1: leaf
 - delete the node and set the pointer from the parent node to NULL.
- Case 2: having only one child:
 - delete the node and change the pointer from the parent node to the single-child node.
- Case 3: having two children:
 - replaced by the largest element in its left subtree, or replaced by the smallest element in its right subtree.

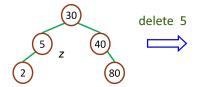


Illustraton (Case 1 & 2)

Case 1:



Case 2:



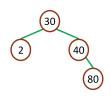
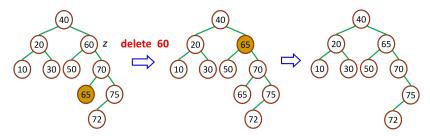




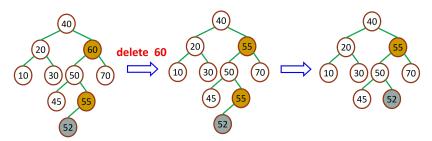
Illustration (Case 3)

Case 3:



Illustraton (Case 3)

Case 3:





Time Complexity Analysis of Deleting a Node in a BST

- The case: Deleting a nonleaf node that has two children.
- We can verify (Exercise) that, in both cases, it is originally in a node with a degree of at most one.
- The time complexity for case 3 is O(h) (h: the height of the BST).
- A deletion can be performed in O(h) time.



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Discussions

