Basic Concepts

Overview & Algorithm Specification

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Outline

- System Life Cycle
- Algorithm Specification
 - Recursive Algorithms
- Oata Abstraction



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- System Life Cycle
- Algorithm SpecificationRecursive Algorithms
- 3 Data Abstraction



System Life Cycle

- Requirements.
- Analysis.
 - Bottom-up vs. top-down.
- Design.
 - Data objects.
 - · Operations.
- Refinement and coding.
- Verification.
 - Correctness proofs.
 - Testing.
 - Error removal (debugging).



Requirement

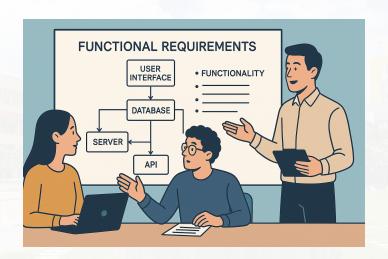
- Purpose of the project.
- We should rigorously define the input and the output.



Analysis

- Bottom-up:
 - Older and unstructured.
 - Due to not having a master plan for the project, the resulting program frequently has many loosely connected, error-ridden segments.
- Top-down:
 - Begin with the purpose.
 - Use the end (purpose) to divide the program into manageable segments.
 - Generate diagrams that are used to design the system.







Design

- The designer starts to approach the system...
- The data objects that the program needs and the operations performed on them.
- For example, consider a scheduling system for a university.
 - Data objects: students, courses, assistants, professors, etc.
 - Operations: inserting, removing, searching within each object or between them.
- We postpone the implementation decisions because the abstract data types and the algorithms specifications are language-independent.



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Algorithm Specification

Algorithm

An algorithm is a finite set of instructions that accomplishes a particular task.

Criteria of an algorithm

- Input.
- Output.
- Definiteness (clear & unambiguous).
- Finiteness* (terminate after a finite number of steps).
- Effectiveness (each instruction must be basic enough to be carried out).



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What's the issue/problem here?

- How the integers are initially stored?
- Where should we place the result?



Selection Sort

• Assume that the integers are stored in an array 'list', such that the *i*th integer is stored in the *i*th position list[i].

```
for (i = 0; i < n; i++) {
    Examine list[i] to list[n-1] and suppose that the smallest
    integer is at list[min];
    Interchange list[i] and list[min];
}</pre>
```

 \Rightarrow sample code.



```
#include <stdio.h>
                                         void sort(int list[], int n) {
#include <stdlib.h>
                                             int i, j, min, temp;
#define MAX SIZE 101
                                             for (i = 0; i < n; i++) {
                                                 min = i:
void SWAP(int *x, int *y) {
                                                 for (j = i+1; j < n; j++) {
    *x = *x^*y; *y = *x^*y; *x = *x^*y;
                                                     if (list[j] < list[min])</pre>
                                                         min = i:
void sort(int [], int ); /* 選擇排序 */
                                                 }
                                                 if (i != min) {
int main() {
                                                     SWAP(&list[i], &list[min])
    int i, n;
                                                 }
    int list[MAX SIZE];
                                            }
    scanf("%d", &n): /* 多少輸入值? */
   for (i = 0; i < n; i++) { /* 隨機產/}
        list[i] = rand() % 1000;
       printf("%d ", list[i]);
   printf("\n");
    sort(list. n):
   for (i = 0; i < n; i++) printf("%d ", list[i]);
   return 0:
```

Example: Binary Search

• Goal: Searching in a sorted list.

```
while (there are more integers to check) {
   middle = (left + right) / 2;
   if (searchnum < list[middle])
      right = middle - 1;
   else if (searchnum == list[middle])
      return middle;
   else
      left = middle + 1;
}</pre>
```



Example

i	[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]	[10]	[11]	[12]	[13]	[14]
	3	11	15	20	23	29	31	35	36	43	47	49	50	53	56
Dr.	3	11	15	20	23	29	31	35	36	43	47	49	50	53	56
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sample code



```
int binSearch(int list[], int target, int left, int right) {
    /* return its position if found. Otherwise return -1 */
    int middle;
    while (left <= right) {
        middle = (left + right)/2;
        if (list[middle] < target) {
              left = middle + 1;
        } else if (list[middle] == target)
              return middle;
        else
              right = middle - 1;
    }
    return -1;
}</pre>
```



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Recursion

- Direction recursion.
 - Functions can call themselves.
- Indirect recursion.
 - Functions may call other functions that invoke the calling function again.

```
void recurse() {
    ...
    recurse();
    ...
}
int main() {
    ...
    recurse();
    ...
}
```

Benefits of using recursion

- Extremely powerful/elegant
- It allow us to express an otherwise complex process in very clear term usually.

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Example:
$$\binom{n}{m} = \binom{n}{m-1} + \binom{n-1}{m-1}$$
.



Another Example: Fibonacci Sequence

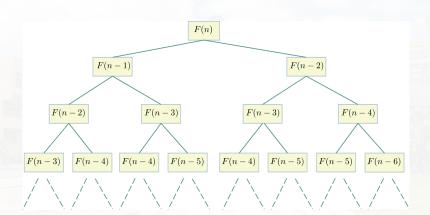
•
$$F(n) = F(n-1) + F(n-2)$$
, for $n \ge 2$.
 $F(0) = 0$, $F(1) = 1$: boundary conditions.



Another Example: Fibonacci Sequence

- F(n) = F(n-1) + F(n-2), for $n \ge 2$. F(0) = 0, F(1) = 1: boundary conditions.
- However, a recursive algorithm for computing F(n) given an arbitrary n is NOT a good idea. \odot





Recursive Binary Search

```
int binSearch(int list[], int target, int left, int right) {
/* return its position if found. Otherwise return -1 */
    int middle;
    while (left <= right) {
        middle = (left + right)/2;
        if (list[middle] < target) {
            return binSearch(list, target, middle+1, right);
        } else if (list[middle] == target)
            return middle;
        else
            return binSearch(list, target, left, middle-1);
    }
    return -1;
}</pre>
```



Outline

- Recursive Algorithms
- Data Abstraction



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A collection of

- objects.
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- The data types in C:
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 - Group data types: array, struct, ...,



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- The data types in C:
 - Basic types: char, int, float, double,
 - Group data types: array, struct, ..., Pointer data types.
 - User-defined types.



Example

```
struct student {
    char last_name;
    int student_id;
    float grade;
};
```



Abstract Data Type (ADT):

A data type that is organized in such a way that

the specification of the objects and the operations on the objects

is separated from

the representation of the objects and the implementation of the operations.

We know what it does, but not necessarily how it will do it.



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- We know what it does, but not necessarily how it will do it.
- Example in C++: class.
- The nature of an ADT argues that we avoid implementation details.
 Therefore, we will usually use a form of structured English to explain the meaning of the functions.

ADT in C

- struct.
- the functions that operate on the ADT defined separately from the struct.

```
struct Triangle {
    double a;
    double b;
    double c;
};

int main() {
    Triangle t1 = { 3, 4, 5 };
    Triangle t2 = { 3, 3, 3 };
}
```

ADT in C

```
double perimeter(const Triangle *tri) {
    return tri->a + tri->b + tri->c;
}
void scale(Triangle *tri, double s) {
    tri->a *= s;
    tri->b *= s;
    tri->c *= s;
int main() {
    Triangle t1 = { 3, 4, 5 };
    scale(&t1, 2);
    cout << perimeter(\&t1) << endl; // 6+8+10 = 24
}
```

Discussions

