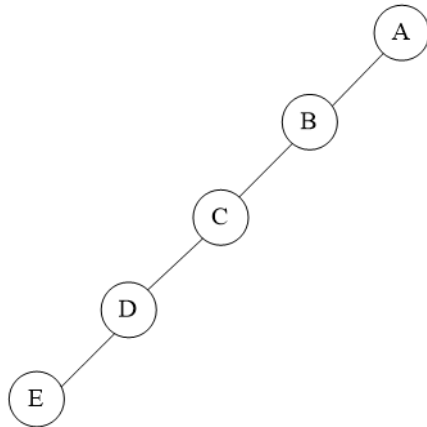


## Assignment 4

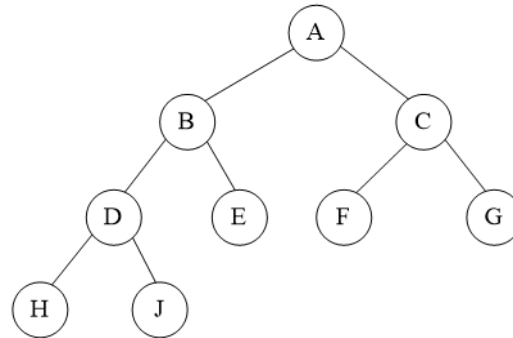
Due date: 18 December 2024

TA: 薛凱駿, 楊承霖, 吳奇軒 (ECG 706)

1. (20%) Write out the inorder, preorder, postorder, and level-order travels for the binary trees (a) and (b).



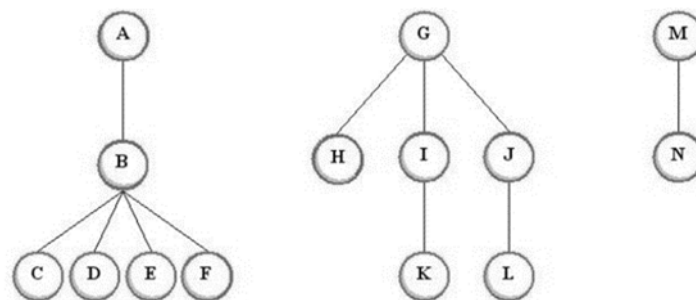
(a)



(b)

2. (20%) Transforming the forest into a binary tree using the rule:

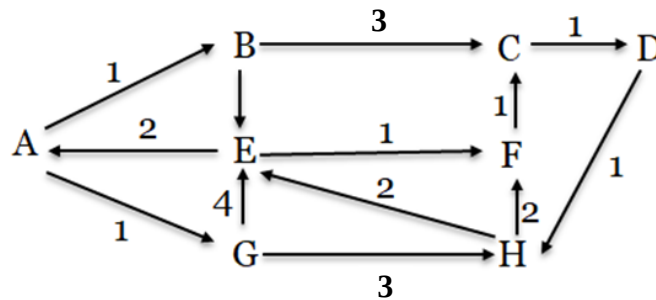
- If  $T_1, \dots, T_n$  is a forest of trees, then the binary tree corresponding to this forest, denoted by  $B(T_1, \dots, T_n)$
- Root equal to  $\text{root}(T_1)$
- Left subtree equal to  $B(T_{11}, T_{12}, \dots, T_{1m})$ , where  $T_{11}, T_{12}, \dots, T_{1m}$  are subtrees of  $\text{root}(T_1)$ ; and has right subtrees  $B(T_2, \dots, B_{T_n})$ .



3. (20%) Compute the generating function for the number of ways of computing multiplications of  $n$  square matrices of the same shape.

**Note:** You should only give the closed form of the function (e.g.,  $f(x) = 1/(x - 1)$ ).

4. (20%) A weighted directed graph  $G$  is given as follows. Filling in the given table using Dijkstra's algorithm to find shortest path from  $A$  to all nodes. If more than 1 vertices have the same minimum distance, choose the vertex with alphabet priority.



Iteration	Vertex Selected	Distance							
		A	B	C	D	E	F	G	H
Initial									
1									
2									
3									
4									
5									
6									
7									

5. (20%) Answer the questions with respect to the following graph.
- Show the result by the Kruskal's algorithm.
  - Starting from node  $A$ , show the result by the Prim's algorithm.
  - Starting from node  $D$ , give the sequence by depth-first-search. If you have multiple choices, just follow the alphabetical order.
  - Starting from node  $E$ , give the sequence by bread-first-search. If you have multiple choices, just follow the alphabetical order.

