Arrays and Structures: The Polynomial Abstract Data Type

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Arrays and Structures: Poly ADT

Outline

Polynomial ADT



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Polynomial ADT



Ordered or Linear Lists

- Months in a year.
 - January, February, March, April, May, June, July, August, September, October, November, December.
- Days of the week.
 - Sunday, Monday, Tuesday, Wednesday, Thursday, Friday, Saturday.
- Values in a deck of card.
 - Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, King.





- **Finding** the length, *n*, of the list.
- Reading the items from left to right (or right to left).
- Retrieving the ith element.
- Storing a new value into the ith position.
- **Inserting** a new element at the *i*th position.



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- > What's the problem if we implement the ordered list using an "array"?



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- A(x) + B(x) = ?
- A(x) * B(x) = ?





Array Representation (Approach #1)

```
#define MAX_DEGREE 101
typedef struct {
   int degree;
   float coef[MAX_DEGREE];
   double salary;
} poly;
```

Usage:

```
poly a;
a.degree = n;
for (i=0; i<n; i++) {
    scanf("%f", &a.coef[i]);
}
```





Array Representation (Approach #2)

#define MAX_TERMS 100 typedef struct { float coef; int expon; } poly; poly terms[MAX_TERMS];

int avail = 0; // available spaces

Example:

$$A(x) = 2x^{1000} + 1$$

$$B(x) = x^4 + 10x^3 + 3x^2 + 1$$

	start_A	finish_A	start_B			finish_B	avail
coef	2	1	1	10	3	1	
expon	1000	0	4	3	2	0	

- Storage: $< 2 \times$ Approach #1 when all the items are nonzero.
- n, m: # nonzeros in A and B, resp.



Function to Add Two Polynomials (O(n+m)) time

```
void padd(int starta, int finisha, int startb, int finishb,
         int *startd, int *finishd) { /*add A(x) and B(x) to obtain D(x) */
   float coefficient:
    *startd = avail:
   while (starta <= finisha && startb <= finishb)
        switch(COMPARE(terms[starta].expon, terms[startb].expon)) {
            case -1: /* a expon < b expon */
                attach(terms[startb].coef, terms[startb].expon); startb++; break;
            case 0: /* equal expontents */
                coefficient = terms[starta].coef + terms[startb].coef;
                if (coefficient) attach(coefficient, terms[starta].expon);
                starta++: startb++: break:
            case 1: /* a expon > b expon */
                attach(terms[starta].coef, terms[starta].expon); starta++;
   for (; starta <= finisha; starta++) /* add in remaining terms of A(x) */
        attach(terms[starta].coef, terms[starta].expon);
   for (; startb <= finishb; startb++) /* add in remaining terms of B(x) */
        attach(terms[startb].coef, terms[startb].expon);
    *finishd = avail-1;
```

Function to Add a New Term

```
void attach(float coefficient, int exponent) {
/* add a new term to the polynomial */
   if (avail > MAX_TERMS) {
      fprintf(stderr, "Too many terms in the polynomial\n");
      exit(1); // exit(EXIT_FAILURE);
   }
   terms[avail].coef = coefficient;
   terms[avail++].expon = exponent;
}
```

- Issue: Compaction is required when polynomials are no longer needed.
 - Additional time for making data movement.



Exercise: Implement the Multiplication of Two Polynomials

```
void pmult(poly a[] , poly b[], poly c[], int na, int nb, int *nc)
   int i, j;
   *nc = 0;
   for (i = 0; i < na; i++)
        for (j = 0; j < nb; j++) {
            c[*nc].coef = a[i].coef * b[j].coef;
            c[(*nc)++].expon = a[i].expon + b[j].expon;
        }
        /*put simplification here*/
}</pre>
```

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Discussions

