

Arrays and Structures: The Polynomial Abstract Data Type

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Outline

1 Polynomial ADT

2 Structures



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Ordered or Linear Lists

- Months in a year.
 - January, February, March, April, May, June, July, August, September, October, November, December.
- Days of the week.
 - Sunday, Monday, Tuesday, Wednesday, Thursday, Friday, Saturday.
- Values in a deck of card.
 - Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, King.



Operations on an Ordered List

- **Finding** the length, n , of the list.
- **Reading** the items from left to right (or right to left).
- **Retrieving** the i th element.
- **Storing** a new value into the i th position.
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- $A(x) + B(x) = ?$
- $A(x) * B(x) = ?$



Array Representation (Approach #1)

Usage:

```
#define MAX_DEGREE 101
typedef struct {
    int degree;
    float coef[MAX_DEGREE];
    double salary;
} poly;
```

```
poly a;
a.degree = n;
for (i=0; i<n; i++) {
    scanf("%f", &a.coef[i]);
}
```



Array Representation (Approach #2)

Example:

```
#define MAX_TERMS 100
typedef struct {
    float coef;
    int expon;
} poly;
poly terms[MAX_TERMS];
int avail = 0; // available spaces
```

$$A(x) = 2x^{1000} + 1$$

$$B(x) = x^4 + 10x^3 + 3x^2 + 1$$

	start_A	finish_A	start_B			finish_B	avail
coef	2	1	1	10	3	1	
expon	1000	0	4	3	2	0	

- Storage: $\leq 2 \times$ Approach #1 when all the items are nonzero.
- n, m : # nonzeros in A and B , resp.



Function to Add Two Polynomials ($O(n + m)$ time)

```
void padd(int starta, int finisha, int startb, int finishb,
          int *startd, int *finishd) { /*add A(x) and B(x) to obtain D(x) */
    float coefficient;
    *startd = avail;
    while (starta <= finisha && startb <= finishb)
        switch(COMPARE(terms[starta].expon, terms[startb].expon)) {
            case -1: /* a expon < b expon */
                attach(terms[startb].coef, terms[startb].expon); startb++; break;
            case 0: /* equal exponents */
                coefficient = terms[starta].coef + terms[startb].coef;
                if (coefficient) attach(coefficient, terms[starta].expon);
                starta++; startb++; break;
            case 1: /* a expon > b expon */
                attach(terms[starta].coef, terms[starta].expon); starta++;
        }
    for (; starta <= finisha; starta++) /* add in remaining terms of A(x) */
        attach(terms[starta].coef, terms[starta].expon);
    for (; startb <= finishb; startb++) /* add in remaining terms of B(x) */
        attach(terms[startb].coef, terms[startb].expon);
    *finishd = avail-1;
}
```


Function to Add a New Term

```
void attach(float coefficient, int exponent) {  
    /* add a new term to the polynomial */  
    if (avail > MAX_TERMS) {  
        fprintf(stderr, "Too many terms in the polynomial\n");  
        exit(1); // exit(EXIT_FAILURE);  
    }  
    terms[avail].coef = coefficient;  
    terms[avail++].expon = exponent;  
}
```

- **Issue:** Compaction is required when polynomials are no longer needed.
 - Additional time for making data movement.



Exercise: Implement the Multiplication of Two Polynomials

```
void pmult(poly a[] , poly b[], poly c[], int na, int nb, int *nc)
{
    int i, j;
    *nc = 0;
    for (i = 0; i < na; i++)
        for (j = 0; j < nb; j++) {
            c[*nc].coef = a[i].coef * b[j].coef;
            c[( *nc )++].expon = a[i].expon + b[j].expon;
        }
    /*put simplification here*/
}
```



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Structures

- An array is a collection of data of **the same type**.
 - `int arr[] = { 0, 1, 2, 3, 4 };`
- A structure is a collection of **data items**, where each item is identified as to its type and name.

```
struct employee {  
    char name[10];  
    int age;  
    double salary;  
};  
struct employee person;
```

```
struct employee {  
    char name[10];  
    int age;  
    double salary;  
} person;
```



Discussions

