

Queues

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Outline

- 1 Definition
- 2 Implementation
- 3 Sequential Queue & Circular Queue

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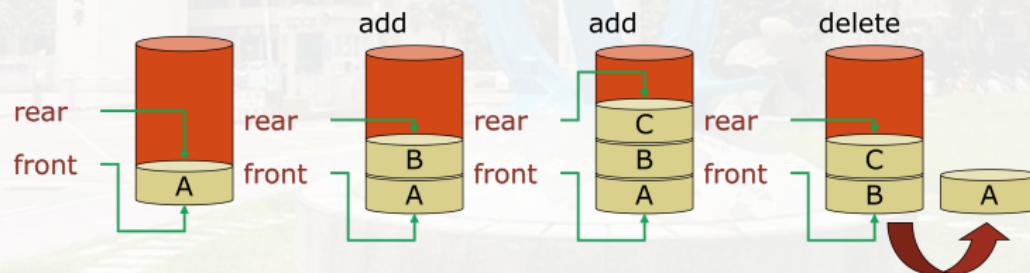
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Definition

- A queue is an ordered list in which **insertions** take place at one end (i.e., **front**) and deletions take place at the opposite end (i.e., **rear**).
 - insertions: push/add
 - deletions: pop/remove
- First-In-First-Out (FIFO).



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Functions for Queues

- Create a queue (implemented by an **array**).
 - Create an empty queue with maximum size MAX_QUEUE_SIZE.

```
#define MAX_QUEUE_SIZE 100

typedef struct {
    int key; // can be of other types...
    /* other fields? */
} element;

element queue a[MAX_QUEUE_SIZE];
int front = -1; // initially no element
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```

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 - Insert the element into the `rear` of the queue.

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If the queue is not full, `queue[++rear] = element;`
- Dequeue (or DeleteQ)
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- Dequeue (or DeleteQ)
 - Remove and return the item at the front of the queue.
If the queue is not empty, `return stack[++front];`



addQ or Enqueue

```
void Enqueue(element item) { // add item to the queue
    if (rear == MAX_QUEUE_SIZE - 1) {
        queueFull();
    }
    queue[++rear] = item;
}

void queueFull() {
    fprintf(stderr, "Queue is FULL!!");
    exit(EXIT_FAILURE);
}
```

delteQ or Dequeue

```
element Dequeue() { // no argument is required!
    if (front == rear) {
        return queueEmpty(); // return an error
    }
    return queue[++front];
}

element queueEmpty() {
    element errKey; // depending the struct of element
    errKey.key = -99;
    fprintf(stderr, "Queue is EMPTY!!!");
    return errorKey;
}
```

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Job Scheduling

| front | rear | Q[0] | Q[1] | Q[2] | Q[3] | comments |
|-------|------|-------|-------|-------|------|----------------------|
| -1 | -1 | | | | | queue is empty |
| -1 | 0 | J_1 | | | | Job J_1 is added |
| -1 | 1 | J_1 | J_2 | | | Job J_2 is added |
| -1 | 2 | J_1 | J_2 | J_3 | | Job J_3 is added |
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- We should move the ENTIRE queue to the left. $\Rightarrow O(MAX_QUEUE_SIZE)$ (very time consuming!)

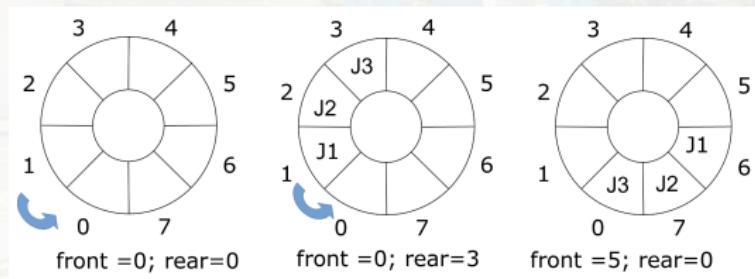


Solution: Circular Queue

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- Initially, $\text{front} = \text{rear} = 0$;
- front : one position counterclockwise from the first element in the queue.
- rear : current end of the queue.



Circular Queue (2/2)

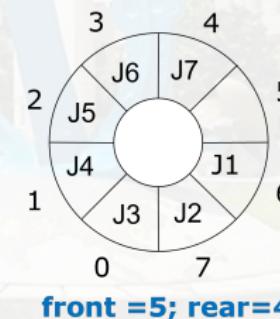
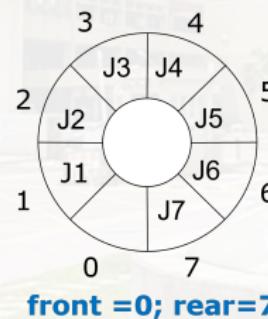
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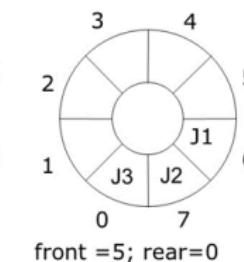
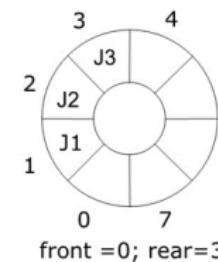
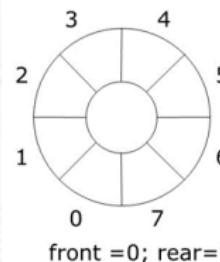
Circular Queue (2/2)

- Such a circular queue is permitted to hold at most `MAX_QUEUE_SIZE - 1` elements.
- The addition of an element such that `front == rear`: the queue is empty (?) or full (?).



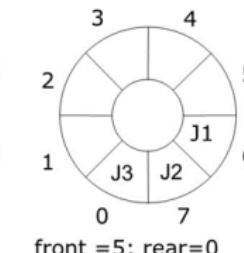
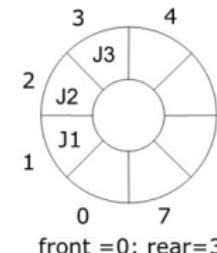
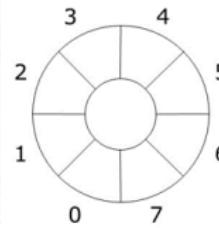
Adding an Element to a Circular Queue

```
void Enqueue(element item) {  
    rear = (rear+1) % MAX_QUEUE_SIZE;  
    if (front == rear) {  
        queueFull(); // reset rear and print error!  
    }  
    queue[rear] = item;  
}
```



Deleting an Element from a Circular Queue

```
element Dequeue() {  
    element item;  
    if (front == rear) {  
        return queueEmpty();  
    }  
    front = (front+1) % MAX_QUEUE_SIZE;  
    return queue[front];  
}
```



Discussions