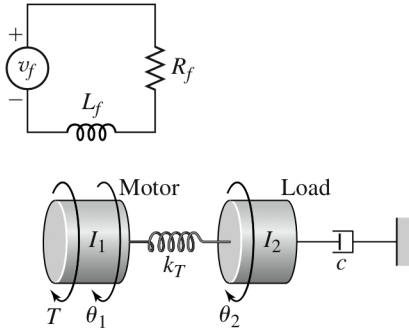


## System Dynamics Final, Fall 2015

1. Obtain the transfer function  $\Theta_2(s)/V_f(s)$  for the system shown below.



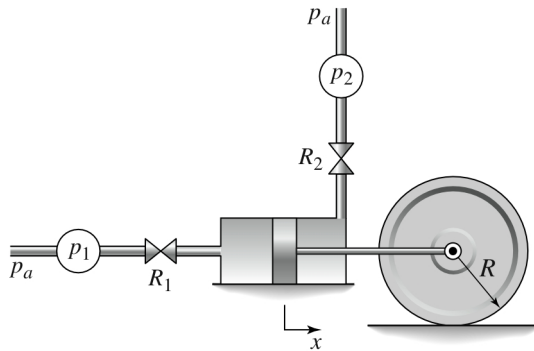
2. For the system below:

- (a) Draw a block diagram for the following system.
- (b) Is the system stable and why or how could you demonstrate this?

$$\begin{aligned} 2\ddot{x} + 6\dot{x} - 3x + y &= f_1(t) \\ 12\ddot{y} - y + 3x &= f_2(t) \end{aligned}$$

3. A piston of area  $A$  is connected to the axle of the cylinder with mass  $m$  and inertia  $I$  about its center.

- (a) Develop a dynamic model of the axle's translation with pressures  $p_1$  and  $p_2$  as inputs.
- (b) Write the governing equations in state-space form with  $x$  and the pressure on the left side of the cylinder as outputs.



$F(s)$	$F(t)$
$sX(s) - x(0)$	$\dot{x}(t)$
$s^2X(s) - sx(0) - v(0)$	$\ddot{x}(t)$
$\frac{a}{s^2+a^2}$	$\sin(at)$
$\frac{s}{s^2+a^2}$	$\cos(at)$
$\frac{1}{s}$	$\delta(t)$
$\frac{1}{s}$	$u(t)$
$\frac{1}{s^2}$	$t$
$\frac{1}{s-a}$	$e^{at}$
$\frac{1}{s^n}$	$\frac{t^{n-1}}{(n-1)!}$