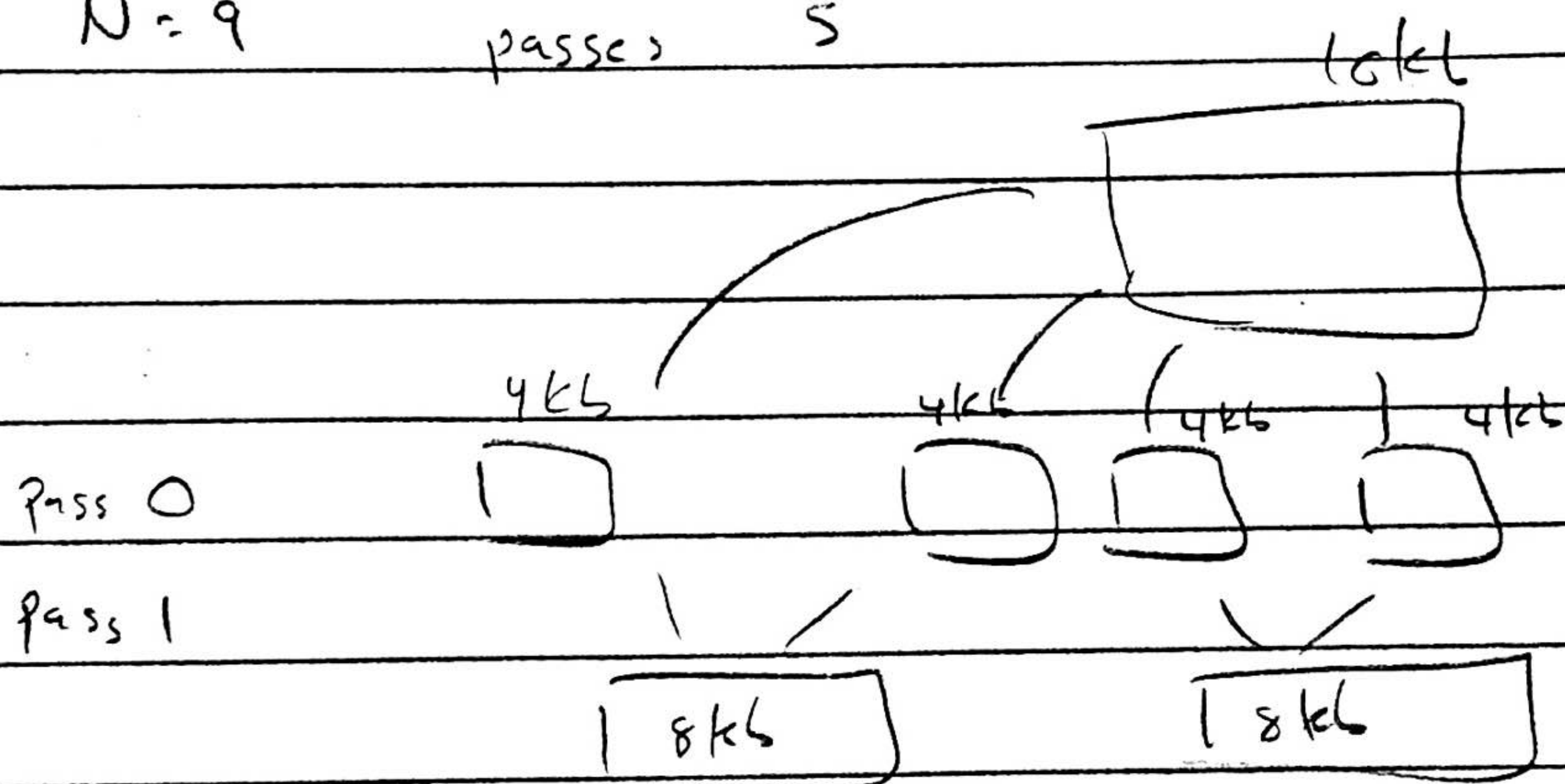


①

N=1	passes 1	1, 2, 3, 3, 4, 4, 4, 4, 5, 5, 5, 5
N=2	passes 2	5, 5, 5, 5
N=3	passes 3	
N=4	passes 3	# passes = $\lceil \log_2(n+1) \rceil + 1$
N=5	passes 4	or
N=6	passes 4	$\lceil \log_2(n+1) \rceil + 1$
N=7	passes 4	$\lceil \log_2(n+1) \rceil + 1$
N=8	passes 4	
N=9	passes 5	



$$T(n) = AT(n/B) + O(n^D)$$

master theorem

substitution

$$T(n) = 7T\left(\frac{n}{4}\right) + \log(n) + T\left(\frac{2(n+2)}{2}\right)$$

$$T(n) = 7T\left(\frac{n}{4}\right) + T\left(\frac{n}{2}\right)$$

$$8T(0) + \frac{17}{6}n + T'(0) + \frac{32}{72}n^2 + T''(0) + \frac{83n^3 + T'(0)}{1296} + \frac{193n^4 + T'(0)}{31104} + \dots$$

A = 7  
B = 2  
D = 2

$n \log n$

$O(n^5)$



2

Pseudo Code

Quicksort -  $O(n \log n)$

create datastructure of choice.  $\mathbb{E}$

1) fstream file, open file

file.open("filename", ios::in)

- while (file.good()) {

while file has lines

# of  
passes  
depends!

Sort everything and  
place into a data structure

sort(): quicksort

everything happens  
here range sort?

f.close  
f.open(name, output)

open file for  
output

```
for (auto x: "data structure") {
    file << x << endl;
}
```

Master Theorem

$$T(n) = 2n + n \log n + 6$$

$$A = 2, B = 1, D = 1$$

$$T(n) = aT\left(\frac{n}{b}\right) + f(n)$$

$$n \log n$$

3

datastructure +1

fstream file +1

open file +1

read file  $n$

buffer and sort

$n \log n$

close file +1

open file to write +1

write to file  $n$

close file +1

$$T(n) = 2n + n \log(n) + 6 \leftarrow \text{Time Complexity}$$

$$O(n \log n) \leftarrow \text{Space Complexity}$$