Joseph Morgan Homework 3

CISP440



Section 2.1

In Exercises 1-16, let the universe be the set $U = \{1, 2, 3, ..., 10\}$. Let $A = \{1, 4, 7, 10\}$, $B = \{1, 2, 3, 4, 5\}$, and $C = \{2, 4, 6, 8\}$. List the elements of each.

6: U - C

 $U-C = \{1, 3, 5, 9, 10\}$

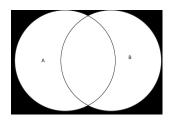
12: $A \cap (B \cup C)$

 $B \cup C = \{1, 2, 3, 4, 5, 6, 8\}$

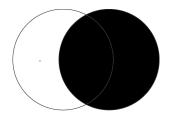
 $A \cap (B \cup C) = \{1, 4, 10\}$

In exercises 17-24, draw a Venn diagram and shade the given set.

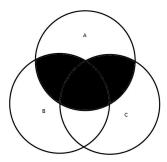
18: $\overline{A} - B$



19: $B \cup (B - A)$



24: $(B - \overline{C}) \cup ((B - \overline{A}) \cap (C \cup B))$



30: A television poll of 151 persons found that 68 watched "M*E*S*S"; 61 watched "Leave It to Seaver" (a base-ball show), 52 watched "The Yuppie Hour"; 16 watched both "M*E*S*S" and "Leave It to Seaver"; 25 watched both "M*E*S*S" and "The Yuppie Hour"; 19 watched both "Leave It to Seaver" and "The Yuppie Hour"; and 26 watched none of these shows. How many persons watched all 3 shows?

Total Number of People: 151

People who didn't watch any of these shows: 26

MESS only: 68 - (16 + 25) = 27LITS only: 61 - (16 + 19) = 26TYH only: 52 - (25 + 19) = 8

Total people who only watched one show: 8 + 26 + 27 = 61

Total people who watched exactly two shows: 16 + 19 + 25 = 60

People who watched 3 shows: (Total People) - {(No Shows) + (Only One) + (Exactly Two)}

$$151 - (26 + 61 60) = 4$$

List all partitions of each set

40: {1, 2}

- {{1},{2}}
- {{1,2}}

Determine weather each pair of sets is equal

48: {1, 2, 2, 3}, {1, 2, 3}

Yes, they are equal, because they contain the same elements. Duplicates don't matter.

49: {1, 1, 3}, {3, 3, 1}

Yes, they are equal. They both contain only a 1 and a 3

53: List the members of $\mathcal{P}(\{a,b,c,d\})$. Which are proper subsets of $\{a,b\}$

 $\mathcal{P}(\{a,b,c,d\})$:

• {Ø}

• {a,b}

• {a}

• {a,c}

• {b}

• $\{a,d\}$

• {c}

 $\bullet \ \{b,c\}$

• {*d*}

• {b,d}

• $\{c,d\}$

• $\{a,b,c\}$

• {*a*, *b*, *d*}

• $\{a, c, d\}$

• $\{b, c, d\}$

• $\{a,b,c,d\}$

Proper Subsets of $\{a, b\}$:

- {a}
- {b}

54: If X has 10 members, how many members does $\mathcal{P}(X)$ have? How many proper subsets does X have?

The powerset of X has 2^{10} , or 1024 members. X has 1023 proper subsets

Write true if statement is true; otherwise, give a counterexample. The sets X, Y and Z are subsets of a universal set U. Assume that the universe for Cartesians products is U*U

58: $X \cap (Y - Z) = (X \cap Y) - (X \cap Z)$ for all sets X, Y and Z.

True

For each condition in Exercises 71–74, what relation must hold between sets A and B?

72: $A \cup B = A$

B = A

73: $\overline{A} \cap U = \emptyset$

A = U