

Objekt test 1 ordinal test 3 distance between 1,3

1.	A	excellent	45
2.	B	fair	22
3.	C	good	64
4.	A	excellent	28

$$A, C = 1$$

$$test 3 + 2 = |3 - 2| = 1$$

$$test 3 + 45; 64 - |45 - 64| = 19$$

Manhattan Distance

$$D = 1 + 1 + 19 = 21$$

Euclidean Distance

$$D = \sqrt{(1)^2 + (1)^2 + (19)^2}$$

$$D = \sqrt{1 + 1 + 361} = \sqrt{363} = 19.05$$

ordinal value	range
excellent	3
good	2
fair	1

Object	test 1	test 3
1	A	3
3	C	2

	Passed	Failed	Total
Attempted	$\frac{31 \times 33}{54} = 18.94$	$\frac{31 \times 21}{54} = 12.06$	31
Skipped	$\frac{23 \times 33}{54} = 14.06$	$\frac{23 \times 21}{54} = 8.94$	23
Total	33	21	54

computing chi square statistic  $\chi^2 = \sum \frac{(O - E)^2}{E}$

$$1. \frac{(25 - 18.94)^2}{18.94} = \frac{6.06^2}{18.94} = \frac{36.72}{18.94} = 1.94$$

$$2. \frac{(6 - 12.06)^2}{12.06} = \frac{(-6.06)^2}{12.06} = \frac{36.72}{12.06} = 3.04$$

$$3. \frac{(8 - 14.06)^2}{14.06} = \frac{(-6.06)^2}{14.06} = \frac{36.72}{14.06} = 2.61$$

$$4. \frac{(15 - 8.94)^2}{8.94} = \frac{(6.06)^2}{8.94} = \frac{36.72}{8.94} = 4.11$$

students who attend are more likely to pass

$$\chi^2 = 1.94 + 3.04 + 2.61 + 4.11 = 11.7$$

$$df = (2 - 1) \times (2 - 1) = 1$$

$$\alpha = 0.05, df = 1 \Rightarrow 3.84$$

$$11.7 > 3.84$$

3. Senior count:  $30 + 5 + 3 + 10 + 4 = 52$

Junior count:  $40 + 40 + 20 + 3 + 4 + 6 = 113$

Total count:  $30 + 40 + 40 + 20 + 5 + 3 + 10 + 4 + 4 + 6 = 165$

$P_{\text{Junior}} = \frac{113}{165}$   $H(S) = -\left(\frac{113}{165} \log_2 \frac{113}{165} + \frac{52}{165} \log_2 \frac{52}{165}\right)$

$P_{\text{Senior}} = \frac{52}{165}$   $= 0.89903087$

	Juniors	Seniors	Total
Sales:	80	30	110
Systems:	23	8	31
Marketing:	4	10	14
Secretary:	6	4	10

$H(\text{Sales}) = -\left(\frac{80}{110} \log_2 \frac{80}{110} + \frac{30}{110} \log_2 \frac{30}{110}\right)$   
 $= 0.8453509$

$H(\text{Systems}) = -\left(\frac{23}{31} \log_2 \frac{23}{31} + \frac{8}{31} \log_2 \frac{8}{31}\right)$   
 $= 0.8238116$

$H(\text{Secretary}) = -\left(\frac{6}{10} \log_2 \frac{6}{10} + \frac{4}{10} \log_2 \frac{4}{10}\right) = 0.9182956$

$H(\text{Marketing}) = -\left(\frac{4}{14} \log_2 \frac{4}{14} + \frac{10}{14} \log_2 \frac{10}{14}\right) = 0.9182956$

$H(\text{Department}) = \sum_{i=1}^5 \frac{15v_i}{151} H(Sv_i) = 0.650924$

$I_G(\text{Department}) = H(S) - H(\text{Department}) = 0.89903087 - 0.650924 = 0.24810687$

	Junior	Senior	Total
21-25	20	0	20
26-30	49	0	49
31-35	40	35	75
36-40	0	10	10
41-45	0	3	3
46-50	4	4	8

$$H(21-25) = -\left(\frac{20}{20} \log_2 \frac{20}{20} + \frac{0}{20} \log_2 \frac{0}{20}\right)$$

$$= 0$$

$$H(26-30) = -\left(\frac{49}{49} \log_2 \frac{49}{49} + \frac{0}{49} \log_2 \frac{0}{49}\right)$$

$$= 0$$

$$H(31-35) = -\left(\frac{40}{75} \log_2 \frac{40}{75} + \frac{35}{75} \log_2 \frac{35}{75}\right)$$

$$= 0.9906175$$

$$H(36-40) = -\left(\frac{0}{10} \log_2 \frac{0}{10} + \frac{10}{10} \log_2 \frac{10}{10}\right)$$

$$= 0$$

$$H(41-45) = -\left(\frac{0}{3} \log_2 \frac{0}{3} + \frac{3}{3} \log_2 \frac{3}{3}\right)$$

$$= 0$$

$$H(46-50) = -\left(\frac{4}{8} \log_2 \frac{4}{8} + \frac{4}{8} \log_2 \frac{4}{8}\right)$$

$$= 0$$

$$H(\text{age}) = 0.4742957$$

$$I_g(\text{age} = \text{HCS}) - H(\text{age}) = 0.894380 - 0.474295$$

$$= 0.420085$$



Salary	Junior	Senior	Total
26k-30k	46	0	46
31k-35k	40	0	40
36k-40k	0	4	4
41k-45k	4	0	4
46k-50k	23	40	63
66k-70k	0	8	8

$$H(26-30) = -\left(\frac{46}{46} \log_2 \frac{46}{46} + \frac{0}{46} \log_2 \frac{0}{46}\right)$$

$$= 0$$

$$H(31-35) = -\left(\frac{40}{40} \log_2 \frac{40}{40} + \frac{0}{40} \log_2 \frac{0}{40}\right)$$

$$= 0$$

$$H(36-40) = -\left(\frac{0}{4} \log_2 \frac{0}{4} + \frac{4}{4} \log_2 \frac{4}{4}\right)$$

$$= 0$$

$$H(41-45) = -\left(\frac{4}{4} \log_2 \frac{4}{4} + \frac{0}{4} \log_2 \frac{0}{4}\right)$$

$$= 0$$

$$H(46-50) = -\left(\frac{23}{63} \log_2 \frac{23}{63} + \frac{40}{63} \log_2 \frac{40}{63}\right)$$

$$= 0.9468188$$

$$H(66-70) = -\left(\frac{0}{8} \log_2 \frac{0}{8} + \frac{8}{8} \log_2 \frac{8}{8}\right)$$

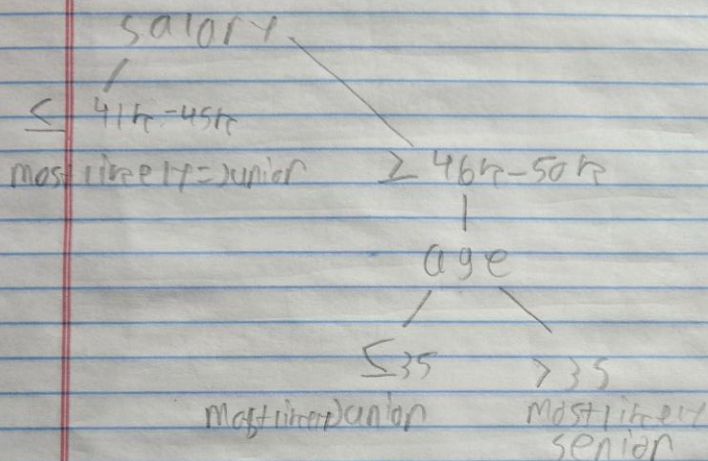
$$= 0$$

$$H(\text{Salary}) = 0.3615126$$

$$IQC(\text{Salary}) = H(S) - H(\text{Salary}) = 0.8409802615226$$

$$= 0.57937181$$

## Decision Tree



- 4.
- If salary is  $\leq 41k-45k$ , then they are junior
  - If salary is  $\geq 46k-50k$  and age  $\leq 35$ , then they are junior
  - If salary is  $\geq 46k-50k$  and age  $> 35$ , then they are senior