



The Area lies between  $-Z$  and  $Z$  is 95%.

$$\text{Area Left of } -Z = \frac{1 - 0.95}{2} = 0.025$$

From the standard normal table value we get  $Z = -1.960$

$$P(Z \leq Z) = 0.025$$

98% of the area under the standard normal curve lies between the  $Z$  values  $-1.960$  and  $1.960$

2)  $\mu = 50$   $\sigma = 3$

$$P(X > 55) = P(Z > 1.66) = 0.0478$$

$$Z = \frac{X - \mu}{\sigma} = \frac{55 - 50}{3} = 1.66$$

3)  $\mu = 25$   $\sigma = 15$   $n = 49$

a)  $\mu_{\bar{X}} = \mu = 25$       b)  $\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}} = \frac{15}{\sqrt{49}} = \frac{15}{7} = 2.143$

$$c) P(24 \leq \bar{X} \leq 32) = P\left(\frac{24 - 25}{2.143} \leq Z \leq \frac{32 - 25}{2.143}\right)$$

$$= P(-0.4666 \leq Z \leq 3.266) = 0.9995 - 0.3204$$

$$= 0.6791$$

4) A) Yes it is appropriate to use normal approximation to the binomial because

$$600 \times 0.70 > 10$$

$$= 126 > 10$$

b)  $600 \times 0.70 = 420$

$$= \sqrt{600 \times 0.70 \times 0.3}$$

$$= 11.2250$$

$$= P(350 < X < 490)$$

$$= P\left(\frac{350 - 420}{11.2250} < \frac{X - \mu}{\sigma} < \frac{490 - 420}{11.2250}\right)$$

$$= P(-6.236 < Z < 6.236) = 0.0038$$

5)  $\bar{X} = 23,500$   $\sigma = 3,900$

$n = 100$   
Confidence = 99%

$$\frac{\alpha}{2} = \frac{1 - 99\%}{2} = 0.005$$

$$Z_{1 - \alpha/2} = Z_{0.995} = 2.5758$$

$$23500 - 2.5758 \times \frac{3900}{\sqrt{100}} < \mu < 23500 + 2.5758 \times \frac{3900}{\sqrt{100}}$$

$$23500 - 1004.573 < \mu < 23500 + 1004.573$$

$$= 22495.43 < \mu < 24504.57$$

6)  $E = 15$ ,  $Z = 1.96$ ,  $\sigma = 40$

$$n = \frac{Z^2 \sigma^2}{E^2}$$

$$n = \frac{(1.96)^2 (40)^2}{15^2}$$

$$= \frac{(3.8416)(1600)}{225}$$

$$= 27.31804$$

$$\approx 28$$