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How to Operate the Code

Setup

Of course, ensure MATLAB is installed on your system.

1. Running the Script:

Open MATLAB

Navigate to the directory containing the script

Press the "Run" button or type the script name in the command window

2. Functionality:

The script performs forward kinematics

Visualizes the robot in 3D space

Calculates inverse kinematics

3. Outputs:

DH transformation matrix

3D visualization of the robot

Joint angles from inverse kinematics

4. Modifying Parameters:

Adjust link lengths (l_1 to l_6) for different robot configurations

Modify theta, d, a, and alpha arrays to change the DH parameters

5. Troubleshooting:

Ensure all required functions are in the same directory

Check for any error messages in the MATLAB command window

Documentation of Major Functions

Forward Kinematics

The forward kinematics function uses the Denavit-Hartenberg (DH) convention to calculate the end-effector position and orientation.

Mathematical Methods used in this project:

- DH Transformation Matrix

Tabulation of Transformation Matrices from the D-H table

$${}^{i-1}_iT = \begin{bmatrix} \cos(\theta_i) & -\sin(\theta_i) & 0 & a_{i-1} \\ \cos(\alpha_{i-1})\sin(\theta_i) & \cos(\alpha_{i-1})\cos(\theta_i) & -\sin(\alpha_{i-1}) & -d_i\sin(\alpha_{i-1}) \\ \sin(\alpha_{i-1})\sin(\theta_i) & \sin(\alpha_{i-1})\cos(\theta_i) & \cos(\alpha_{i-1}) & d_i\cos(\alpha_{i-1}) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\alpha_0 = 0, \quad a_0 = 0, \quad d_1 = 0$$

$${}^0_1T = \begin{bmatrix} \cos(\theta_1) & -\sin(\theta_1) & 0 & 0 \\ \sin(\theta_1) & \cos(\theta_1) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

● Chain Multiplication

The final transformation is computed by multiplying individual matrices

$$T_{06} = T_{01} \cdot T_{12} \cdot T_{23} \cdot T_{34} \cdot T_{45} \cdot T_{56}$$

Inverse Kinematics

The inverse kinematics function calculates joint angles for a desired end-effector position and orientation.

Using the Geometric Approach:

$$\text{Joint 1: } q_1 = \text{atan2}(p_y, p_x) \quad q_1 = \text{atan2}(p_y, p_x)$$

$$\text{Joint 2: } q_2 = \text{atan2}(p_z - l_1, r - l_2) + \text{offset}_2 \quad q_2 = \text{atan2}(p_z - l_1, r - l_2) + \text{offset}_2$$

Joint

$$3: q_3 = \text{atan2}(l_3 - p_z, l_2 - r) + \text{offset}_3 \quad q_3 = \text{atan2}(l_3 - p_z, l_2 - r) + \text{offset}_3$$

In order to calculate the wrist angles:

$$\text{Joint 4: } q_4 = \text{atan2}(R_{2,1}, R_{1,1}) \quad q_4 = \text{atan2}(R_{2,1}, R_{1,1})$$

$$\text{Joint 5: } q_5 = \text{atan2}(R_{3,12} + R_{3,22}, R_{3,3}) \quad q_5 = \text{atan2}(R_{3,12} + R_{3,22}, R_{3,3})$$

$$\text{Joint 6: } q_6 = \text{atan2}(R_{3,2}, -R_{3,1}) \quad q_6 = \text{atan2}(R_{3,2}, -R_{3,1})$$

Where R is the rotation matrix from the transformation matrix T₀₆.

Visualization

The visualization function plots the robot's links and joint frames in 3D space using MATLAB's plotting capabilities.

Notable Matlab Syntax:

- plot3() for drawing links
- quiver3() for representing joint frames
- Color coding for easy identification of links and axes