Summary of GMM Estimates

your old pal Jo
July 2, 2024

Joint GMM Estimation of Production and Demand - Preferred Specification

	ϵ_{\uparrow}	r,g	ϵ_x	H	δ	1	δ_2		
	$(\kappa = 0)$	$\kappa = 1$	$(\kappa = 0)$	$(\kappa = 1)$	$(\kappa = 0)$	$(\kappa = 1)$	$(\kappa = 0)$	$(\kappa = 1)$	
	0.20	0.20	0.49	0.49	0.08	0.12	0.93	0.93	
	(0.05)	(0.05)	(0.08)	(0.08)	(0.04)	(0.04)	(0.01)	(0.01)	
	ỗ· Moti	ner's Time	ỗ c∵ Fath	er's Time	ỗ-∴ Cŀ	ildcare	do:	TFP	
	$(\kappa = 0)$	$(\kappa = 1)$	$(\kappa = 0)$	$(\kappa = 1)$	$(\kappa = 0)$	$(\kappa = 1)$	$(\kappa = 0)$	$(\kappa = 1)$	
Const.	8.30	8.28	4.07	4.01	-1.19*	-1.19	-1.06	-1.46	
	(1.96)	(1.93)	(1.26)	(1.24)	(0.41)	(0.41)	(0.40)	(0.43)	
Single	-0.00*	0.03	-	-	0.57	0.56	-0.07	-0.10	
	(0.37)	(0.37)	-	-	(0.21)	(0.21)	(0.06)	(0.07)	
Type 2	-1.24	-1.24	-	-	0.08	0.10	0.23	0.13	
	(0.61)	(0.61)	-	-	(0.31)	(0.31)	(0.08)	(0.10)	
Type 3	-2.78*	-2.76	-	-	0.03	0.04	0.02	-0.16	
	(1.03)	(1.01)	-	-	(0.31)	(0.31)	(0.12)	(0.15)	
Mother: Some College	-0.33	-0.33	-	-	-0.01	-0.01	0.03	-0.02	
	(0.44)	(0.44)	-	-	(0.20)	(0.20)	(0.06)	(0.07)	
Mother: College+	-1.59	-1.57	-	-	-0.27	-0.26	0.01	-0.09	
	(0.72)	(0.71)	-	-	(0.19)	(0.19)	(0.10)	(0.11)	
Child Age	-0.58	-0.58	-0.47^{*}	-0.46	-0.06^*	-0.06	-0.02	-0.02	
	(0.17)	(0.17)	(0.17)	(0.17)	(0.03)	(0.03)	(0.01)	(0.02)	
Num. Children 0-5	0.52	0.48	0.64	0.62	0.10	0.10	0.15	0.14	
	(0.31)	(0.30)	(0.42)	(0.42)	(0.12)	(0.12)	(0.05)	(0.05)	
Father: College+	` - ´	` - ´	-1.03	-1.04	-0.00	-0.01	0.09	0.06	
	-	-	(0.73)	(0.72)	(0.25)	(0.25)	(0.08)	(0.08)	
Father: Some College	-	-	-0.70	-0.68	-0.67	-0.68	0.30	0.26	
9	-	_	(0.64)	(0.63)	(0.24)	(0.24)	(0.08)	(0.09)	
ind02	-	_	` - '	-	` -	` -	$0.14^{'}$	0.20	
	_	_	-	-	-	-	(0.06)	(0.07)	

Joint GMM Estimation of Demand - Preferred Specification

		$\epsilon_{ au,g}$	ϵ	x,H	Correl. residuals		
	(1)	(2)	(1)	(2)	(1)	(2)	
	0.20 (0.05)	0.37 (0.17)	0.52 (0.09)	0.77 (0.09)	0.88	0.88	
	$\tilde{\phi}_m$: Mo	ther's Time (2)	$\tilde{\phi}_f$: Fatl	ner's Time (2)	$\tilde{\phi}_x$: Cl (1)	nildcare (2)	
Const.	8.32	5.54	4.10	3.35	-1.19	-1.45	
	(1.95)	(1.67)	(1.27)	(0.76)	(0.40)	(0.28)	
Single	0.29	0.11	-	-	0.62	0.63	
	(0.38)	(0.21)	-	-	(0.21)	(0.14)	
Type 2	-1.14	-0.49	-	-	0.03	0.00	
	(0.59)	(0.46)	-	-	(0.29)	(0.20)	
Type 3	-2.46	-1.08	-	-	-0.04	-0.10	
	(0.95)	(0.86)	-	-	(0.30)	(0.21)	
Mother: Some College	-0.44	-0.13	-	-	-0.01	-0.06	
	(0.45)	(0.28)	-	-	(0.19)	(0.13)	
Mother: College+	-1.79	-0.76	-	-	-0.20	-0.28	
	(0.76)	(0.65)	-	-	(0.19)	(0.13)	
Child Age	-0.60	-0.34	-0.48	-0.24	-0.07	-0.04	
	(0.18)	(0.15)	(0.18)	(0.14)	(0.03)	(0.02)	
Num. Children 0-5	0.34	0.16	0.59	0.29	0.09	0.08	
	(0.29)	(0.18)	(0.41)	(0.26)	(0.12)	(0.08)	
Father: College+	-	-	-1.08	-0.41	0.06	0.01	
.0	_	_	(0.73)	(0.45)	(0.25)	(0.17)	
Father: Some College	_	_	-0.83	-0.22	-0.53	-0.41	
	_	_	(0.66)	(0.44)	(0.23)	(0.16)	

Table 1: Joint GMM Estimation - Fully Restricted Case, No Binding Constraints

	$\epsilon_{ au,g}$					ϵ_x	,H				δ_1				δ_2
-	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)	(1)	(2)	(3)
	0.32	0.26	0.20	0.18	0.52	0.44	0.49	0.50	0.06	0.08	0.08	0.07	0.93	0.93	0.9
	(0.05)	(0.05)	(0.05)	(0.05)	(0.08)	(0.08)	(0.08)	(0.08)	(0.04)	(0.04)	(0.04)	(0.04)	(0.01)	(0.01)	(0.0)
		ϕ_m : Mo	ther's Tim	e		ϕ_f : Fath	er's Time			/	hildcare			$\phi_{ heta}$:	TFP
_	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)	(1)	(2)	(3)
Constant	5.07	6.32	8.30	13.18	3.27^{+}	3.49^{+}	4.07	4.17	-1.17^{+}	-1.21^{+}	-1.19^{+}	-1.45^{+}	-0.78	-1.18	-1.0
	(0.68)	(1.02)	(1.96)	(3.97)	(0.74)	(0.90)	(1.26)	(1.41)	(0.32)	(0.44)	(0.41)	(0.61)	(0.46)	(0.49)	(0.40
Single	0.13	0.11^{+}	-0.00^{+}	0.08^{+}	-	-	-	-	0.52^{+}	0.52	0.57	0.60^{+}	-0.08	-0.07	-0.0
	(0.24)	(0.28)	(0.37)	(0.41)	-	-	-	-	(0.20)	(0.24)	(0.21)	(0.21)	(0.06)	(0.06)	(0.06)
Mother some coll.	-0.19	-	-0.33	-0.39	-	-	-	-	0.04	-	-0.01	0.04	0.07	-	0.0
	(0.27)	-	(0.44)	(0.50)	-	-	-	-	(0.19)	-	(0.20)	(0.20)	(0.06)	-	(0.06)
Mother coll+	-0.83	-	-1.59	-1.74	-	-	-	-	-0.22	-	-0.27	-0.23	0.06	-	0.0
	(0.35)	-	(0.72)	(0.83)	-	-	-	-	(0.18)	-	(0.19)	(0.19)	(0.08)	-	(0.10)
Child's age	-0.36	-0.45	-0.58	-0.65	-0.27^{+}	-0.34^{+}	-0.47^{+}	-0.51^{+}	-0.06^{+}	-0.06^{+}	-0.06^{+}	-0.06^{+}	-0.02	-0.02	-0.0
	(0.08)	(0.10)	(0.17)	(0.21)	(0.08)	(0.11)	(0.17)	(0.21)	(0.03)	(0.03)	(0.03)	(0.03)	(0.01)	(0.01)	(0.0]
Num. of children 0-5	0.35	0.44	0.52	0.65	0.41	0.46	0.64	0.80	0.10	0.13	0.10	0.10	0.14	0.16	0.15
	(0.18)	(0.23)	(0.31)	(0.36)	(0.25)	(0.30)	(0.42)	(0.49)	(0.12)	(0.14)	(0.12)	(0.13)	(0.05)	(0.05)	(0.05)
Type 2	-	-0.81	-1.24	-	-	-	-	-	-	0.12	0.08	-	-	0.23	0.23
	-	(0.41)	(0.61)	-	-	-	-	-	-	(0.34)	(0.31)	-	-	(0.08)	(0.08)
Type 3	-	-1.94	-2.78^{+}	-	-	-	-	-	-	0.08	0.03	-	-	0.01	0.03
	-	(0.61)	(1.03)	-	-	-	-	-	-	(0.34)	(0.31)	-	-	(0.12)	(0.12)
μ_k	-	-	-	-3.00^{+}	-	-	-	-	-	-	-	0.12^{+}	-	-	-
	-	-	-	(1.21)	-	-	-	-	-	-	-	(0.25)	-	-	-
Father some coll.	-	-	-	-	-0.46	-0.63	-1.03	-1.11	-0.00	0.05	-0.00	-0.03	0.12	0.10	0.09
	-	-	-	-	(0.41)	(0.50)	(0.73)	(0.82)	(0.24)	(0.29)	(0.25)	(0.25)	(0.08)	(0.08)	(0.08)
Father coll+	-	-	-	-	-0.17	-0.23	-0.70	-0.84	-0.66	-0.71	-0.67	-0.73	0.33	0.34	0.30
	-	-	-	-	(0.36)	(0.42)	(0.64)	(0.72)	(0.21)	(0.25)	(0.24)	(0.24)	(0.08)	(0.08)	(0.0)
Year = 2002	-	_	-	-	- ^	- 1	-	- 1	- 1		· - ´		0.14	0.16	0.1
	_	-	-	-	-	-	_	-	-	-	-	_	(0.06)	(0.06)	(0.0)

Table 2: Joint GMM Estimation - Fully Restricted Case, Unconstrained, Older Children

	ho				δ_1				δ_2			
	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)
	0.24 (0.06)	0.18 (0.06)	0.11 (0.07)	0.06 (0.07)	-0.02 (0.04)	$0.04 \\ (0.05)$	-0.02 (0.04)	-0.03 (0.04)	0.97 (0.02)	0.97 (0.02)	0.97 (0.02)	0.97 (0.02)
		ϕ_m : Mot	her's Tin	ne		ϕ_f : Fath	ner's Time	e		$\phi_{ heta}$:	TFP	
	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)	(1)	(2)	(3)	(4)
Const.	6.13 (2.16)	7.93 (3.17)	13.65 (8.64)	40.46 (47.99)	3.84 (2.36)	4.69 (3.21)	7.56 (6.41)	13.02 (16.64)	0.04 (0.47)	-0.46 (0.48)	0.04 (0.47)	0.22 (0.43)
Single	0.39 (0.45)	0.42 (0.60)	0.50 (1.02)	0.82 (2.07)	-	-	-	(10.04)	-0.10 (0.08)	-0.14 (0.09)	-0.11 (0.08)	-0.11 (0.08)
Mother: Some College	-0.56 (0.56)		-1.44 (1.55)	-2.58 (3.96)	-	-	-	-	-0.07 (0.09)	-	-0.07 (0.09)	-0.06 (0.09)
Mother: College+	-1.19 (0.71)	-	-3.35 (2.73)	-6.37 (8.46)	-	-	-	-	0.05 (0.12)	-	0.05 (0.13)	0.04 (0.13)
Child Age	-0.50 (0.21)	-0.63 (0.31)	-1.07 (0.77)	-1.99 (2.46)	-0.37 (0.24)	-0.54 (0.35)	-1.04 (0.84)	-2.04 (2.65)	-0.01 (0.04)	-0.03 (0.04)	-0.01 (0.04)	-0.01 (0.04)
Num. Children 0-5	0.55 (0.43)	0.95 (0.61)	1.24 (1.14)	2.80 (3.64)	0.56 (0.52)	0.74 (0.70)	1.22 (1.34)	2.24 (3.32)	-0.00 (0.11)	0.01 (0.11)	0.00 (0.10)	0.01 (0.10)
Type 2	-	-1.55 (1.02)	-3.11 (2.51)	-	-	-	-	-	-	0.00 (0.11)	0.11 (0.12)	-
Type 3	-	-3.17 (1.62)	-5.72 (4.27)	-	-	-	-	-	-	-0.16 (0.19)	0.07 (0.17)	-
μ_k	-	-	-	-12.10 (15.53)	-	-	-	-	-	-	-	-0.01 (0.20)
Father: College+	-	-	-	-	-1.26 (0.85)	-1.76 (1.19)	-3.72 (3.12)	-7.77 (10.35)	-0.01 (0.14)	-0.10 (0.14)	-0.01 (0.14)	-0.00 (0.14)
Father: Some College	-	-	-	-	-0.94 (0.73)	-1.59 (1.07)	-3.44 (2.96)	-7.51 (10.08)	0.33 (0.13)	0.27 (0.14)	0.37 (0.13)	0.38 (0.14)
ind02	-	-	-	-	-	-	-	-	0.22 (0.08)	0.23 (0.08)	0.22 (0.08)	0.22 (0.08)

Table 3: Joint GMM Estimation - Unrestricted, No Binding Constraints

	$\epsilon_{ au,g}$			$\epsilon_{x,H}$	δ_1	δ_2	$2N(Q_N- ilde{Q})$
	Rel. Dem.	Prod.	Rel. Dem.	Prod.	-	-	-
	0.18	-	0.51	-	0.12	0.92	6.52
	(0.05)	-	(0.08)	-	(0.05)	(0.04)	(0.26)
	ϕ_m : Mother	's Time	φ _f : Fa	ather's Time	ϕ_V :	Childcare	ϕ_{θ} : TFP
	Rel. Dem.	Prod.	Rel. Dem.	Prod.	Rel. Dem.	Prod.	-
Const.	8.87	_	4.19	_	-1.19	180.32	-1.71
	(2.23)		(1.38)		(0.40)	(43037845.96)	(0.75)
Single	0.02	3.09	` -	-	0.60	-	0.08
	(0.40)	(7.21)			(0.20)		(0.21)
Type 2	-1.36	-	-	-	0.08	-	0.20
	(0.67)				(0.29)		(0.13)
Type 3	-3.01	0.64	-	-	$0.04^{'}$	-	0.13
* -	(1.15)	(5.37)			(0.30)		(0.26)
Mother: Some College	-0.39	-	-	-	-0.02	-	0.03
	(0.48)				(0.19)		(0.09)
Mother: College+	-1.76	_	-	-	-0.30	-	-0.01
	(0.81)				(0.18)		(0.14)
Child Age	-0.64	_	-0.50	-2.15	-0.07	-14.94	-0.00
	(0.20)		(0.20)	(876691433.57)	(0.03)	(3599435.10)	(0.03)
Num. Children 0-5	$0.52^{'}$	_	0.69	-	0.09	-	0.16
	(0.33)		(0.46)		(0.12)		(0.07)
Father: College+	-	_	-1.13	-	-0.02	-	0.06
<u> </u>			(0.79)		(0.24)		(0.09)
Father: Some College	_	-	-0.78	-	-0.65	-	$0.27^{'}$
O .			(0.70)		(0.23)		(0.11)
ind02	_	_	- /	-	-	-	$0.17^{'}$
							(0.10)

Note: the distance metric, $2N(Q_N - \tilde{Q}_N)$, is the difference between the optimally weighted gmm criterion at the restricted estimates and its value at the relaxed estimates. It has a χ^2 distribution with degrees of freedom equal to the number of constraints that are relaxed. Standard errors are indicated in parentheses *except* for the distance metric, which reports a p-value.

Table 4: Joint GMM Estimation - Mother's Share Unrestricted, No Borrowing or Saving

	$\epsilon_{\tau,g}$ Rel. Dem. Prod.		$\epsilon_{x,H}$ Rel. Dem.	Prod.	$rac{\delta_1}{\cdot}$	δ_2 -	$2N(Q_N - \tilde{Q}_N)$
	0.20 (0.05)	-	0.49 (0.08)	-	0.13 (0.05)	0.92 (0.02)	0.34 (0.56)
	ϕ_m : Mother Rel. Dem.	r's Time Prod.	ϕ_f : Father' Rel. Dem.	s Time Prod.	ϕ_Y : Chil Rel. Dem.	dcare Prod.	$\phi_{ heta}$: TFP
Const.	8.32	10.40	4.02	_	-1.19	_	-1.69
	(1.96)	(4.98)	(1.26)		(0.41)		(0.69)
Single	$0.02^{'}$	` - ´	` - ′	-	$0.56^{'}$	-	-0.07
	(0.37)				(0.21)		(0.07)
Type 2	-1.25	-	-	-	0.10	-	0.19
	(0.61)				(0.31)		(0.15)
Type 3	-2.75	-	-	-	0.04	-	-0.04
	(1.02)				(0.31)		(0.26)
Mother: Some College	-0.33	-	-	-	-0.01	-	0.00
	(0.44)				(0.20)		(0.08)
Mother: College+	-1.58	-	-	-	-0.26	-	-0.01
	(0.72)				(0.19)		(0.17)
Child Age	-0.58	-	-0.46	-	-0.06	-	-0.00
	(0.17)		(0.17)		(0.03)		(0.05)
Num. Children 0-5	0.47	-	0.62	-	0.10	-	0.13
	(0.30)		(0.41)		(0.12)		(0.05)
Father: College+	-	-	-1.05	-	-0.01	-	0.06
			(0.73)		(0.25)		(0.09)
Father: Some College	-	-	-0.70	-	-0.68	-	0.24
			(0.64)		(0.24)		(0.10)
ind02	-	-	-	-	-	-	0.19
							(0.07)

Note: the distance metric, $2N(Q_N - \tilde{Q}_N)$, is the difference between the optimally weighted gmm criterion at the restricted estimates and its value at the relaxed estimates. It has a χ^2 distribution with degrees of freedom equal to the number of constraints that are relaxed. Standard errors are indicated in parentheses *except* for the distance metric, which reports a p-value.

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Table 5: Joint GMM Estimation - Mother's Share Unrestricted, No Binding Constraints

	$\epsilon_{ au,g}$ Rel. Dem. Prod.		$\epsilon_{x,H}$ Rel. Dem.	Prod.	δ_1	δ_2 -	$2N(Q_N - \tilde{Q}_N)$
	0.20 (0.05)	-	0.49 (0.08)	- -	0.08 (0.04)	0.93 (0.01)	0.26 (0.61)
	ϕ_m : Mother Rel. Dem.	s's Time Prod.	ϕ_f : Father Rel. Dem.	's Time Prod.	ϕ_Y : Chil Rel. Dem.	dcare Prod.	ϕ_{θ} : TFP
Const.	8.40	10.05	4.08	_	-1.19	_	-1.18
	(2.00)	(7.40)	(1.28)		(0.41)		(0.64)
Single	-0.00	- '	- '	-	$0.57^{'}$	-	-0.05
	(0.38)				(0.21)		(0.07)
Type 2	-1.27	-	-	-	0.08	-	0.26
	(0.62)				(0.31)		(0.16)
Type 3	-2.81	-	-	-	0.03	-	0.07
	(1.04)				(0.31)		(0.29)
Mother: Some College	-0.34	-	-	-	-0.01	-	0.04
	(0.45)				(0.20)		(0.08)
Mother: College+	-1.62	-	-	-	-0.27	-	0.05
	(0.73)				(0.19)		(0.19)
Child Age	-0.59	-	-0.47	-	-0.06	-	-0.01
	(0.18)		(0.18)		(0.03)		(0.05)
Num. Children 0-5	0.52	-	0.65	-	0.10	-	0.15
	(0.31)		(0.42)		(0.12)		(0.05)
Father: College+	-	-	-1.05	-	-0.00	-	0.08
			(0.74)		(0.25)		(0.08)
Father: Some College	-	-	-0.73	-	-0.67	-	0.29
			(0.65)		(0.24)		(0.09)
ind02	-	-	-	-	-	-	0.14
							(0.06)

Note: the distance metric, $2N(Q_N - \tilde{Q}_N)$, is the difference between the optimally weighted gmm criterion at the restricted estimates and its value at the relaxed estimates. It has a χ^2 distribution with degrees of freedom equal to the number of constraints that are relaxed. Standard errors are indicated in parentheses *except* for the distance metric, which reports a p-value.