

HW3

Friday, 4 February 2022 16:06

$$\mathcal{J} = -\ln(\sigma((2\gamma-1)z))$$

$$\frac{d\mathcal{J}}{dz} = \frac{-1}{\sigma} \cdot \sigma' \cdot (2\gamma-1)$$

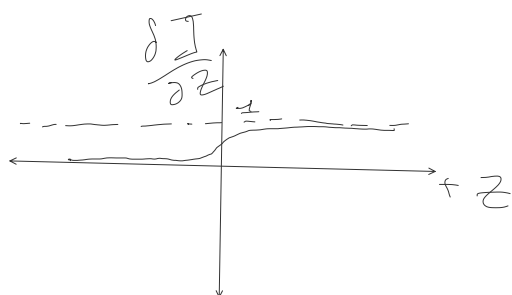
$$\begin{aligned} \frac{d\sigma(z)}{dz} &= ((1+e^{-z})^{-1})' \\ &= -1 \cdot (1+e^{-z})^{-2} \cdot -1 \cdot e^{-z} \\ &= \frac{e^{-z}}{(1+e^{-z})(1+e^{-z})} \\ &= \frac{1}{(1+e^z)(1+e^z)} = \sigma(z)\sigma(-z) \end{aligned}$$

$$\begin{aligned} \sigma(-z) &= \frac{1}{1+e^z} = \frac{e^{-z}}{1+e^{-z}} = \frac{(1+e^{-z})-1}{1+e^{-z}} \\ &= 1 - \sigma(z) \end{aligned}$$

$$\begin{aligned} \frac{d\mathcal{J}}{dz} &= \frac{-1}{\sigma} \cdot \sigma' \cdot (2\gamma-1) \\ &= \frac{-1 \cdot (2\gamma-1)}{\cancel{\sigma}} \cdot \cancel{\sigma} (1-\sigma) \\ &= (1-2\gamma)(1 - \sigma((2\gamma-1)z)) \\ &= (1-2\gamma)(\sigma((1-2\gamma)z)) \\ &= \frac{1-2\gamma}{1 + \exp((2\gamma-1)z)} \end{aligned}$$

for $y = 0$

$$\frac{\partial J}{\partial z} = \frac{1}{1 + \exp(-z)} = \sigma(z)$$

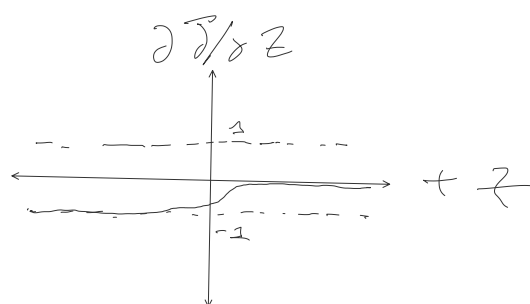


Vanishes for
negative large z

For $y = 0$ and large negative values of z the gradient vanishes and thus the model is unable to learn

for $y = 1$

$$\begin{aligned} \frac{\partial J}{\partial z} &= \frac{-1}{1 + \exp(z)} = -1 \cdot \sigma(-z) \\ &= -1(1 - \sigma(z)) \\ &= \sigma(z) - 1 \end{aligned}$$



Vanishes for
positive large z

For $y = 1$ and large positive values of z the gradient vanishes and thus the model is unable to learn

This activation function has these cases where the model cannot learn and thus minimize loss as well as possible