

Pendulum

①

$$v_{\text{total}} = \sqrt{v_x^2 + v_y^2}$$

②

$$KE_{\text{total}} = \frac{1}{2} I \omega^2$$

③

$$m_c = \text{mass of cup} + \text{mass of plate} = 0.007 \text{ kg} + 0.002 \text{ kg} = 0.027 \text{ kg}$$

$$m_s = \text{mass of 1 skewer} = 0.001 \text{ kg}$$

$$L = \text{length of the skewer} = 0.203 \text{ m}$$

$$R = \text{distance of cup from axis of rotation} = 0.127 \text{ m}$$

$$I = \frac{1}{12} m_s L^2 + m_s \left(R - \frac{L}{2}\right)^2 + m_c (R)^2 \approx 0.00044$$

$$KE = \frac{1}{2} (0.00044) \omega^2 = \frac{1}{2} (0.00044) \frac{v^2}{R^2}$$

$$= (0.00022) \frac{v^2}{R^2} \rightarrow \text{calculated with LoggerPro}$$

(4)

$$KE_i = 0 \text{ since } v_i = 0$$

$$PE_i = KE + PE$$

(5)

$$PE = m_c gh = 0.265h$$

Sample Calcs:

(1)

At time $t = 1.979$:

$$x \text{ velocity} = 0.350 \text{ m/s} \quad y = 0.057 \text{ m}$$

$$y \text{ velocity} = -0.074 \text{ m/s}$$

$$v_{\text{total}} = \sqrt{(0.350)^2 + (-0.074)^2} = 0.358 \text{ m/s}$$

$$KE = \frac{1}{2} I \omega^2 = \frac{1}{2} (0.00044) \frac{(0.358)^2}{(0.127)} = \boxed{0.0017 \text{ J}}$$

(2)

$$PE = 0.265 (0.043) = \boxed{0.011 \text{ J}}$$

③

$$PE_{\max} = 0.265(y_{\max}) \quad \rightarrow \text{from Logger Pro}$$

$$= 0.265(0.08) = \boxed{0.021 \text{ J}}$$

$$KE_{\max} = 0.021 \text{ J}$$

$$\frac{1}{2} I \omega^2 = 0.021 \text{ J}$$

$$\frac{1}{2} (0.00044) \frac{v_{\max}^2}{(0.127)^2} = 0.021$$

$$v_{\max} = \boxed{1.241 \text{ m/s}}$$