PHYS1406: Physics of Sound and Music

Spring 2021

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Topics we'll cover this semester

- Preliminaries: Basic math, music, and physics terminology
- Physics of oscillations and waves
- Production of sound (instruments and voice)
- Perception of sound (hearing, loudness, pitch & timbre)
- Auditorium and room acoustics; electrical reproduction of sound
- Musical scales and tuning systems (standardization of musical notes)

Why are you in this class?

What questions about sound & music would you like to know the answer to?

What is sound? What differentiates speech, music, & noise?

- Sound is a **pressure wave** in air (or some other medium, which could be a liquid or solid).
- The pressure wave consists of alternating regions of **compression** and **expansion** of the air molecules.
- **Energy is transferred** from the source of sound to our ears, while the individual air molecules just oscillate back-and-forth in place.
- noise: chaotic, unorganized sound
- speech & music: organized sound
- musical notes have a definite pitch (low or high), while noise does not

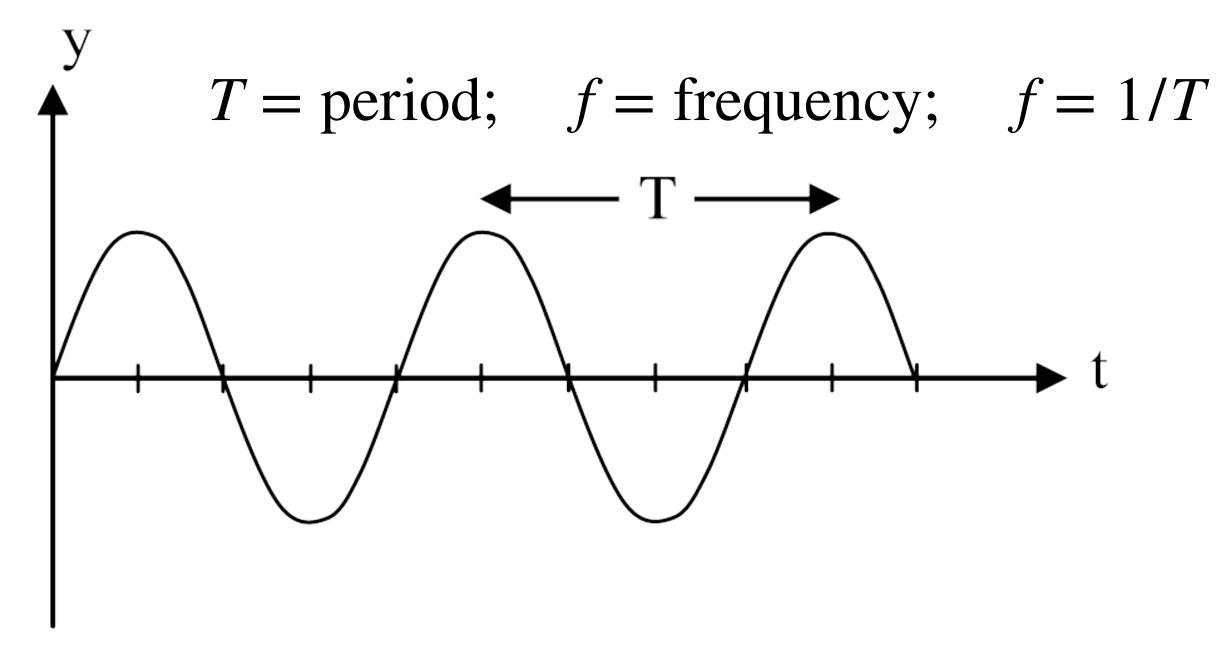
Demos: sound measuring devices & musical instruments

- Measuring devices
 - oscilloscope: shows how the sound pressure wave changes in time
 - FFT analyzer: shows how much sound energy is associated with different pitch components
 - spectrogram: shows how the pitch content of a sound changes in time
- Musical instruments and sound-making devices:
 - whistle, singing, speaking
 - penny whistle, recorder, funny plastic recorder, train whistle, other wind instruments
 - plucked guitar string, bowed violin string
 - bell, drum, shakers, marimba bar, other percussion instruments
 - ratchet, crumpled paper, applause

Range of human hearing

https://www.szynalski.com/tone-generator/

- Normal range: 20 Hz 20,000 Hz
- What is frequency? Number of repetitions (oscillations, cycles, ...) in a given time interval
- Example: Heart rate: 70 beats/1 minute = 1.14 beats/sec
- Hertz (Hz): 1 Hz = 1 cycle/sec



1. Preliminaries

Basic math review

- Entering numbers on a calculator: What's the value of $1/2\pi$? **Ans:** $1 \div (2 \times \pi) = 0.16$ not $1 \div 2 \times \pi = 1.57$
- Fractions: What's the value of 2 divided by 3/2? **Ans:** $2 \div (3/2) = 2 \times (2/3) = 4/3 = 1.33$
- Powers (exponential notation): What's the value of 2^4 ? 10^3 ? 10^{-2} ?

Ans:
$$2^4 = 2 \times 2 \times 2 \times 2 = 16$$
; $10^3 = 100$; $10^{-2} = 1/10^2 = 0.01$

Prefixes:

nano	micro	milli	centi	kilo	mega	giga	tera
10^{-9}	10^{-6}	10^{-3}	10^{-2}	10^{3}	10^{6}	10^{9}	10^{12}

• Comparing two numbers: Compare the heights of two people, one who is 5.5 ft tall versus another who is 72 inches all.

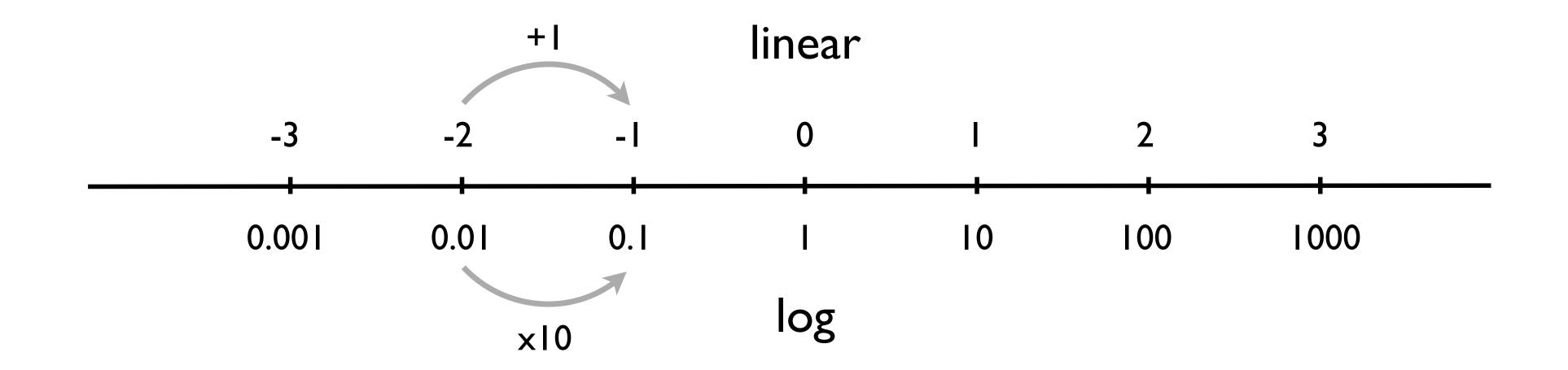
Ans: First convert 5.5 ft to 66 inches. Then subtract (72 in – 66 in = 6 in) or divide (72 in/66 in = 1.09) or calculate percent difference $(100 \times (72 - 66)/66 = 9\%)$. For music applications, taking ratios or percent differences are most convenient and useful

• Converting units: The speed of sound in air at room temperature (25 celsius) is 346 m/s. What is its value in ft/s? miles/s?

Ans: Using the conversion factors (1 m = 3.28 ft and 1 mi = 5280 ft), we find:

$$346 \frac{\text{m}}{\text{s}} \times \frac{3.28 \text{ ft}}{\text{m}} = 1135 \frac{\text{ft}}{\text{s}} \approx 1000 \frac{\text{ft}}{\text{s}} \text{ and } 1135 \frac{\text{ft}}{\text{s}} \times \frac{1 \text{ mi}}{5280 \text{ ft}} = 0.21 \frac{\text{mi}}{s} \approx \frac{1 \text{ mi}}{5 \text{ s}}$$

Linear vs logarithmic scales

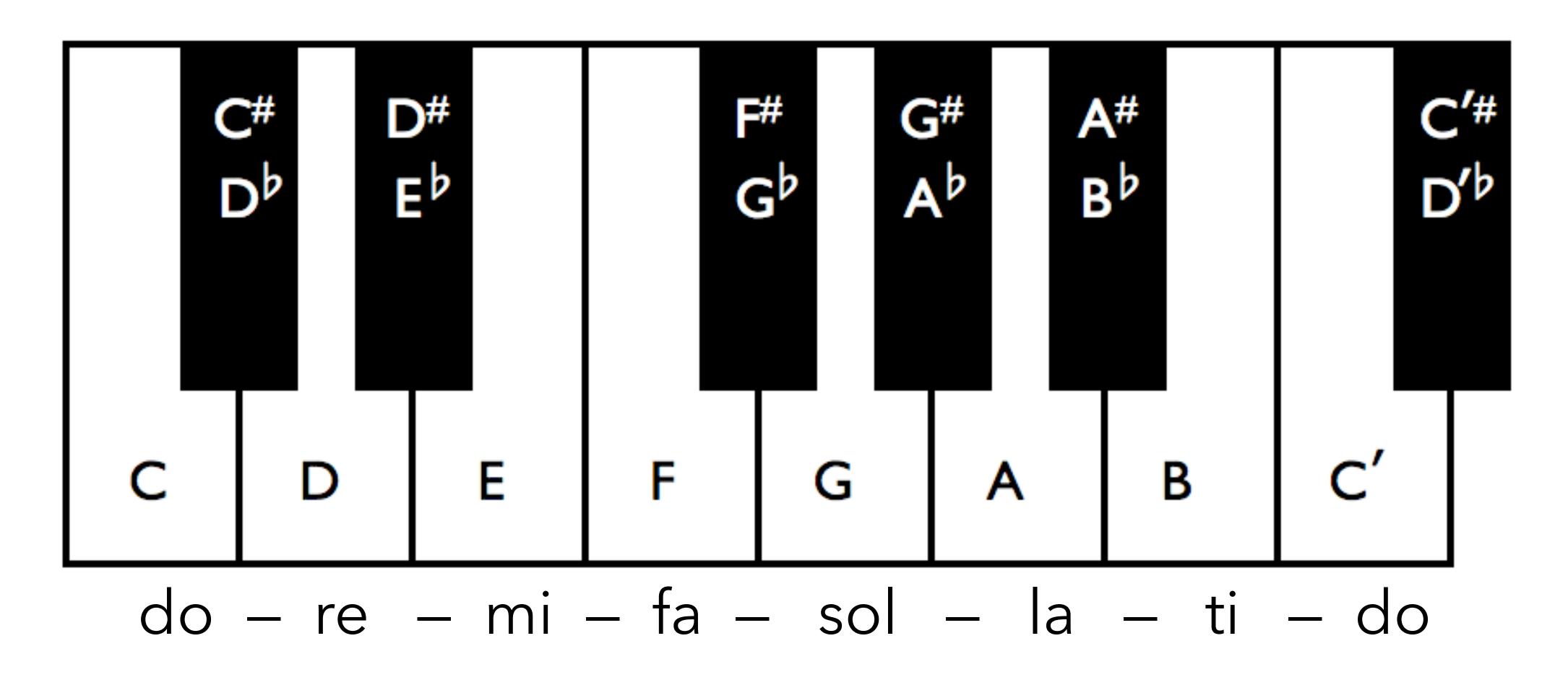


Music terminology

- Pitch: fundamental frequency
- Timbre: richness of a sound, associated with contributions from higher harmonics. It's what makes a guitar sound different from a flute, etc., even though they are all playing the same musical note.
- Octave: Factor of 2 in frequency (e.g., C3 to C4)
- Chromatic, diatonic, and pentatonic scales: divide the octave into 12, 7, and 5 pieces (intervals)
 - https://www.youtube.com/watch?v=jaMA8LWW3C0 (pentatonic scale; all black keys in C-major scale)
- Equal temperament: musical scale where all semitone intervals are equal to one another (6% higher in frequency)
- Musical intervals:
 - **fifth** (C to G; 7 semitones; frequency ratio = 3/2), **fourth** (C to F; 5 semitones; frequency ratio = 4/3), **major third** (C to E; 4 semitones; frequency ratio = 5/4), **minor third** (E to G; 3 semitones; frequency ratio = 6/5)
- Chord: Major chord C-E-G

Chromatic and diatonic scales

C - C# - D- Eb - E - F - F# - G - Ab - A- Bb - B - C'



Physics terminology

- Position, displacement: position = location of an object in space, specified by its distance from a reference point and its direction relative to reference axes; displacement = change in position Δx ; units for both are m, in, ft, mi, ...
- Time, duration: time = reading on a clock; duration = difference in times Δt ; units for both are s, min, hr, year, ...
- Velocity, speed, acceleration: velocity = displacement/duration; speed = distance traveled/duration; acceleration = change in velocity/duration; velocity and acceleration have both magnitude and direction; units of velocity and speed are m/s, mi/hr, ...; units of acceleration are m/s², mph/s, ...
 - (i) uniform circular motion: changing position, velocity, and acceleration even though speed = constant
 - (ii) mass on a spring: changing position, velocity, and acceleration; velocity = 0 at the turning points of the motion; acceleration = 0 at the equilibrium position where the speed is greatest
- Force, mass, Newton's 2nd law: force = that which produces an acceleration; mass = resistance that an object offers to changes in its state of motion; a = F/m or F = ma (units of force are Newtons or lbs; units of mass are grams or kilograms)
- Density, pressure, atmospheric pressure: density = mass/volume or mass/length; pressure = force/area; units of pressure are N/m² or lb/in² = psi; 1 atm = 10^5 N/m² = 14.5 psi

Exercise

- Calculate the pressure exerted by a 120 lb woman standing on the floor, wearing stilettos having approximately circular heels with radius 0.25 in. Compare to the pressure exerted by a 10,000 lb elephant whose four feet are approximately circles with radius 10 in.
- Ans: Recall that the area of a circle is πr^2 , where r is the radius.

Woman: $P = F/A = 120 \text{ lb}/(2 \times \pi (0.25 \text{ in})^2) \approx 300 \text{ lb/in}^2$

Elephant: $P = F/A = 10000 \text{ lb/}(4 \times \pi (10 \text{ in})^2) \approx 8 \text{ lb/in}^2$

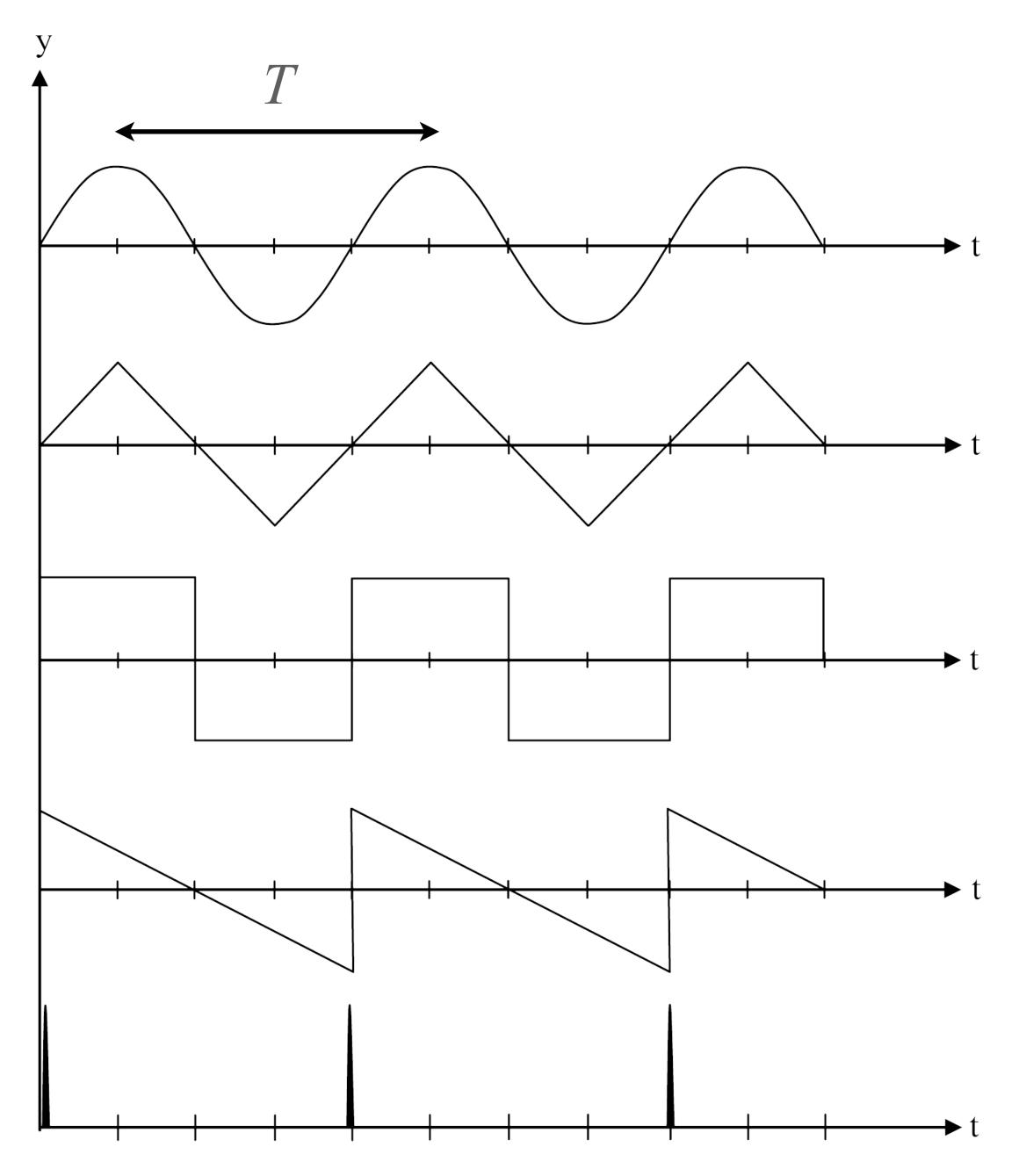
2. Oscillations

Periodic motion

- Oscillation: any motion that repeats
- Examples: vibrating guitar string; vibrating reed of a bassoon; swinging pendulum bob; mass on a spring; yearly orbital motion of Earth around the Sun; beating heart; ...
- Period (T), frequency (f): period is the time for one complete oscillation; frequency is the number of oscillations in a given interval of time; f = 1/T or T = 1/f. Pitch corresponds to the fundamental frequency of a musical note.
 - Ques: What are the periods of sound waves corresponding to the range of human hearing?
 - **Ans:** f = 20 Hz has T = 50 msec; f = 20,000 Hz has T = 50 microsec
- Amplitude: 1/2 the peak-to-peak displacement of an oscillation (related to the loudness of a sound)
- Waveform: the shape of a wave. Different waveforms having the same period (or frequency) sound differently. So the waveform of a sound corresponds to its timbre.

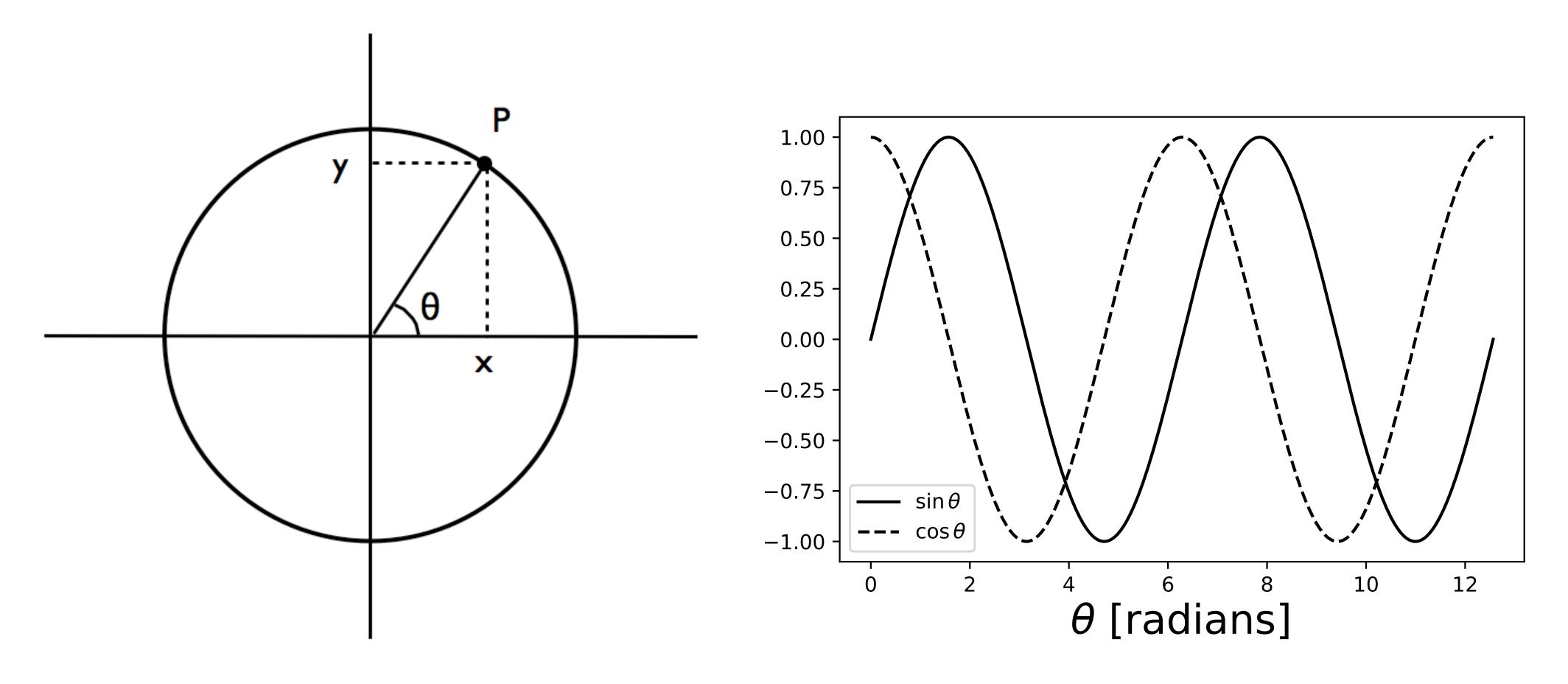
Different waveforms

- Demo: Compare sounds
- Although the pitch is the same, the timbre (i.e., sound quality) is different



Simple harmonic motion (SHM)

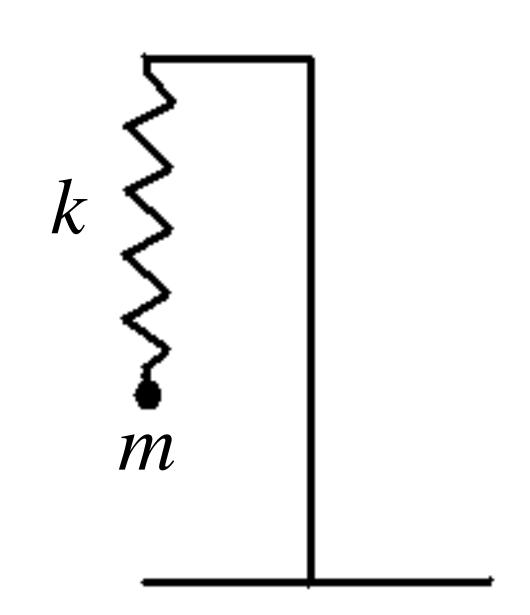
• Produced whenever you have a **linear restoring force** acting on a system that has a **stable equilibrium**. (Linear means the restoring force is twice is great if the displacement from equilibrium is twice as large.)



Examples of SHM

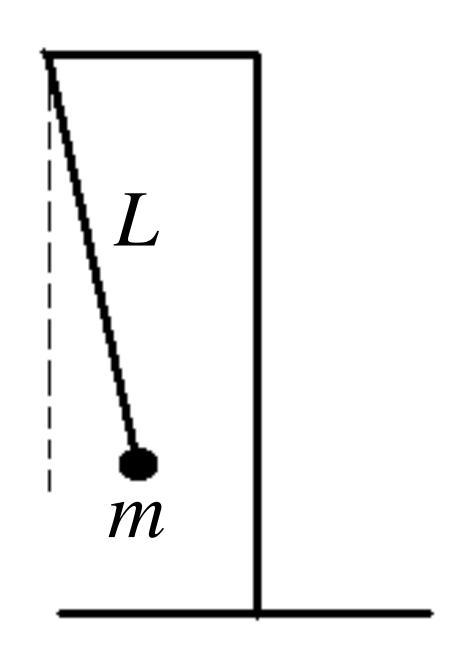
Mass on a spring

$$T = 2\pi \sqrt{\frac{m}{k}}, \qquad f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$



Swinging pendulum bob

$$T = 2\pi \sqrt{\frac{L}{g}}, \qquad f = \frac{1}{2\pi} \sqrt{\frac{g}{L}}$$



Damping and resonance

- Demo with swinging pendulum
- Friction, air resistance, ... cause oscillations to die out. Need to apply a driving force to keep them going.
- Natural frequency of a swinging pendulum: $f_0 = \frac{1}{2\pi} \sqrt{\frac{g}{L}}$
- Compare to **driving frequency** f:
 - $f \ll f_0$: the pendulum bob follows the motion of the driving force
 - $f \gg f_0$: the pendulum bob oscillates back and forth, with a very small amplitude, 180 degrees out of phase with the driving motion
 - $f = f_0$: the amplitude of the swinging motion of the pendulum bob **increases** as the driving force is applied, even for small driving amplitudes. This is called **resonance**.

3. Waves & sound

Topics (for lab 2, this week):

- Part 2 of Course Guide; Sec 4 of Supplemental Notes
- wave velocity: the speed of a wave as it travels from one location to another
- reflection, refraction: the change of direction of a wave when it encounters another medium
- interference: two waves can combine with one another to form another wave
- diffraction: the "spreading" out of a wave as it passes through an opening or around a barrier

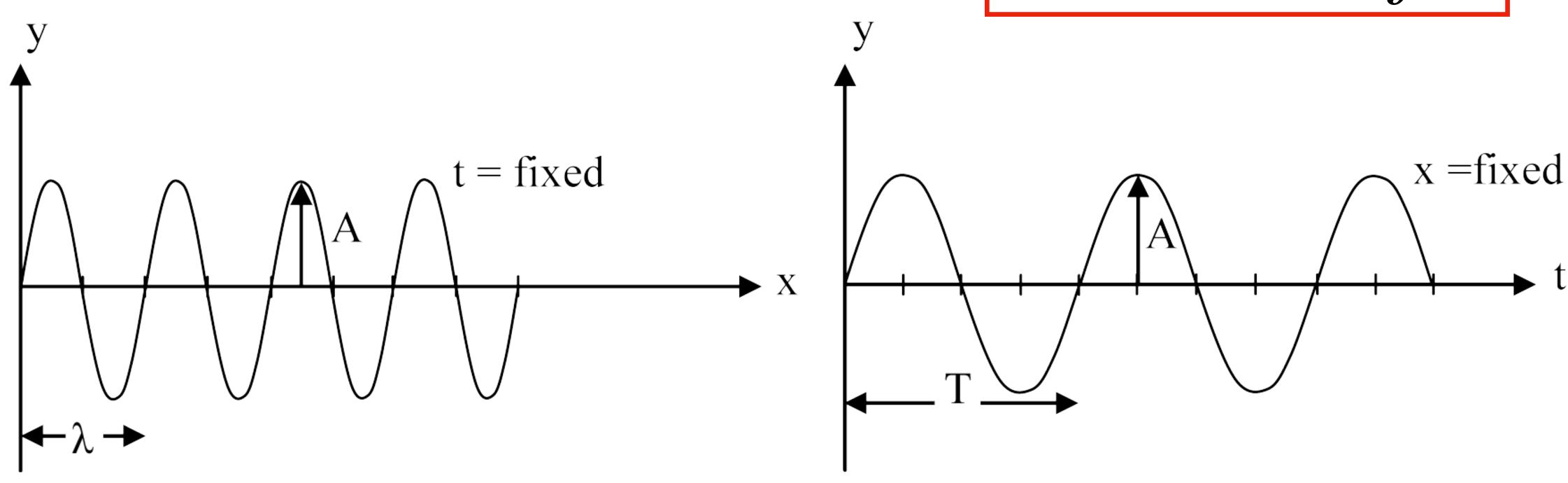
Wave motion, wave velocity

- wave: any "disturbance" that transports energy from one location to another without the transport of matter
- Examples: sound waves in air; light (example of an electromagnetic wave, which can travel through empty space); water waves on the surface of a pond; "wave" at a football game
- transverse vs longitudinal waves
- wave pulse vs period waves
- wave velocity: $v = \Delta x/\Delta t$
- v = 346 m/s (speed of sound in air at room temp, 25 Celsius or 77 Farenheit)
- $v = 331 \frac{\text{m}}{\text{s}} \sqrt{1 + \frac{T_C}{273.15}}$ (speed of sound in air increases with increasing temperature)

Periodic waves, wavelength

• Produced by **periodic sources**; λ is the **wavelength**

$$v = \lambda/T = f\lambda$$



"snap shot" at a fixed time, showing how the displacement varies with position **fixed location**, showing how the displacement varies with time

Exercise

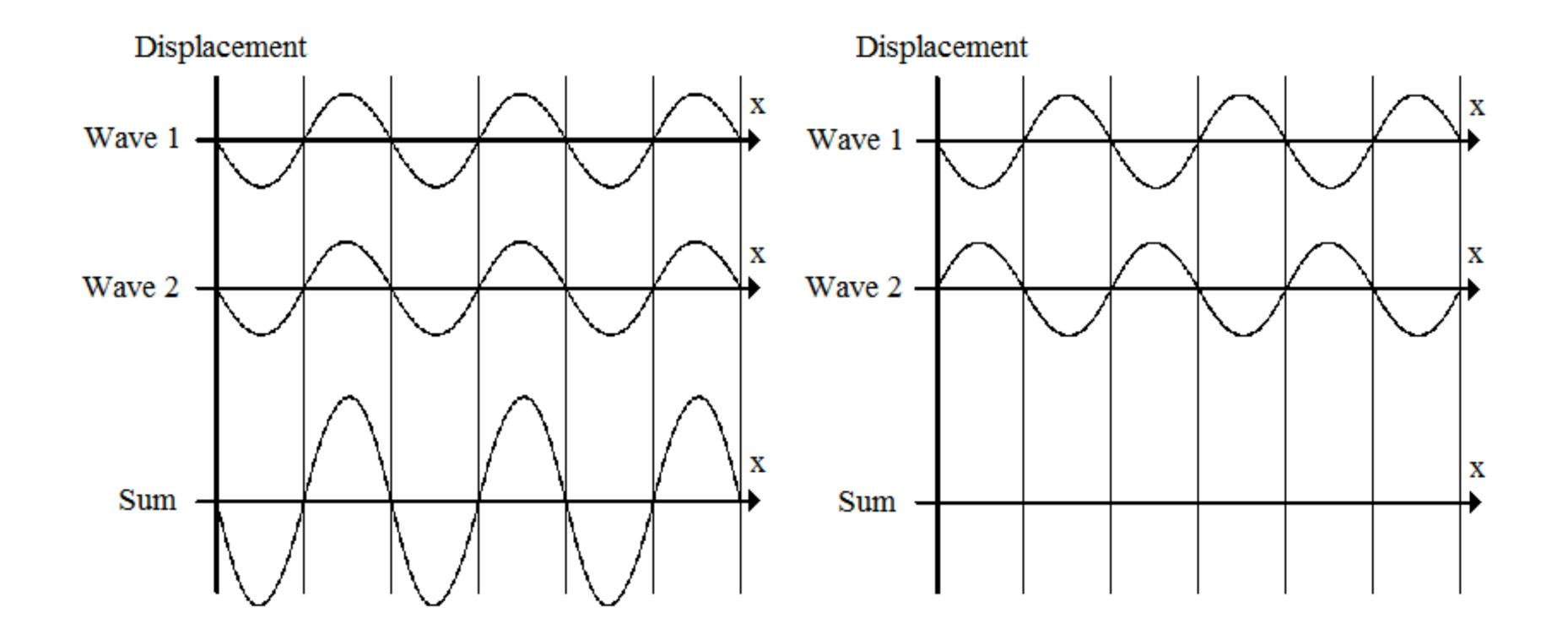
• Calculate the wavelengths of sound corresponding to the range of human hearing. Use v = 346 m/s for the speed of sound in air at room temperature.

Ans:

- For f = 20 Hz:
- For f = 20,000 Hz:

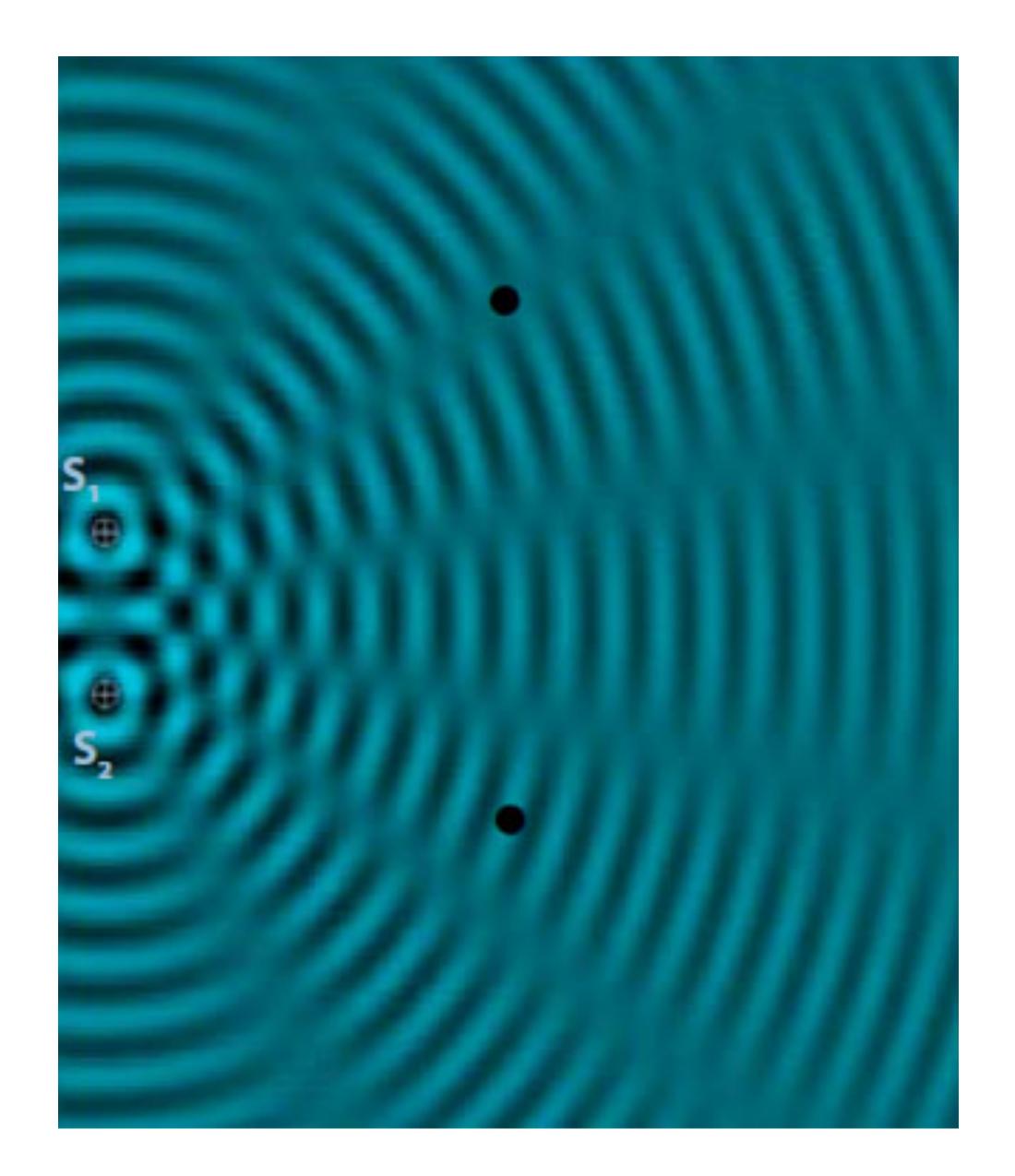
Superposition / interference

- the combination of two waves is another wave
- constructive & destructive interference depends on the phase difference (matlab demo)



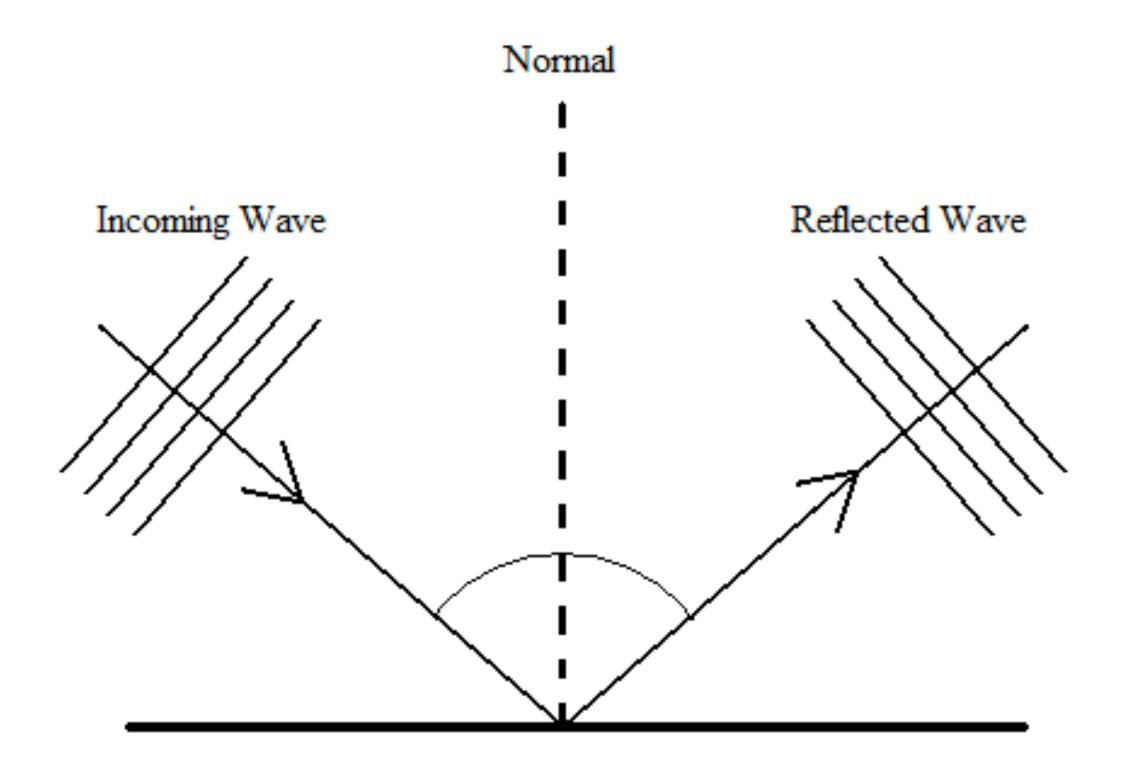
Examples

- Waves on a pond (interference in space)
- Beats (interference in time; matlab demo, and using signal generators)

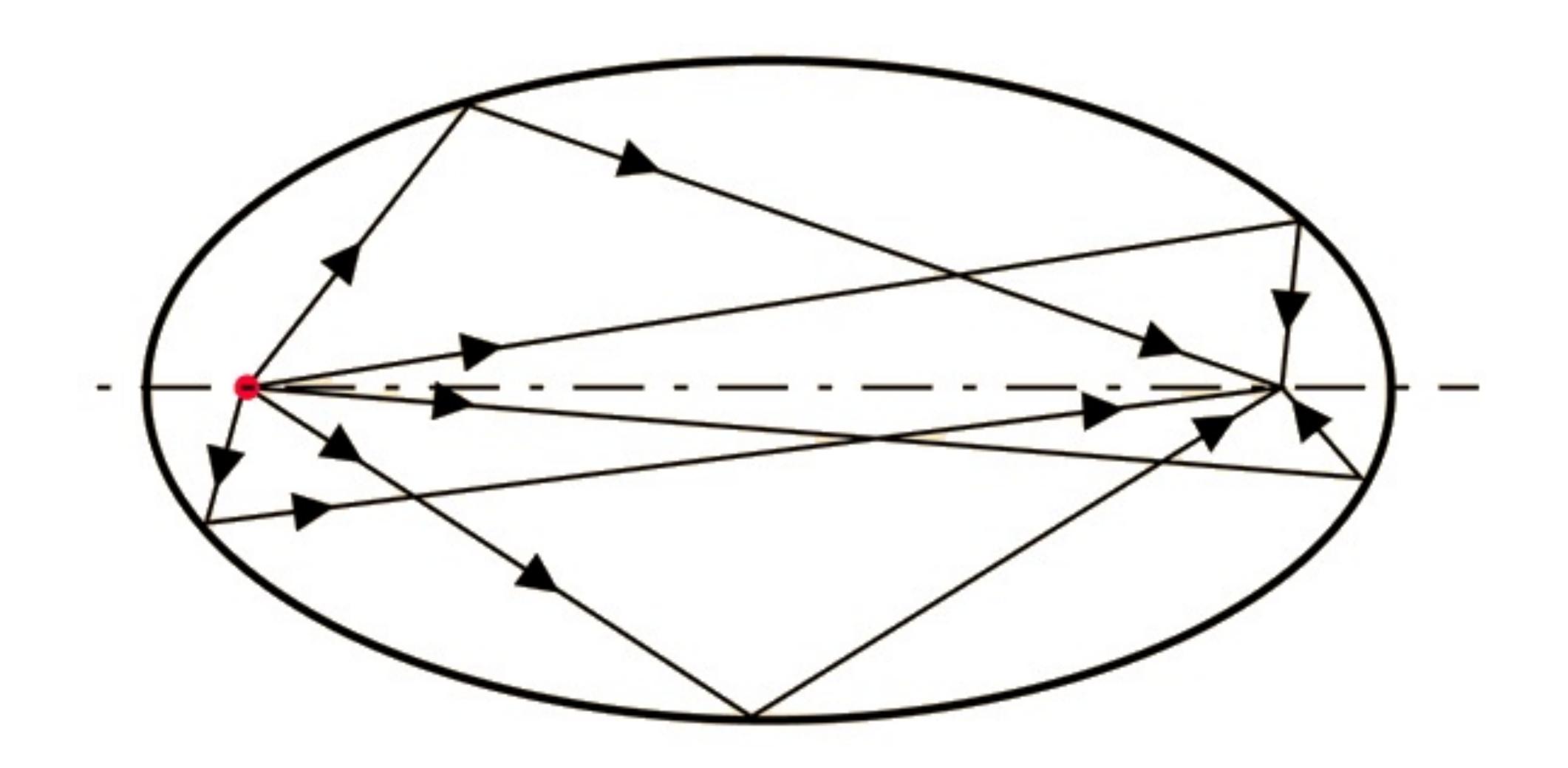


Reflection

- Change in direction of a wave when it encounters an interface between two media
- Demos with plane, concave, and convex mirrors



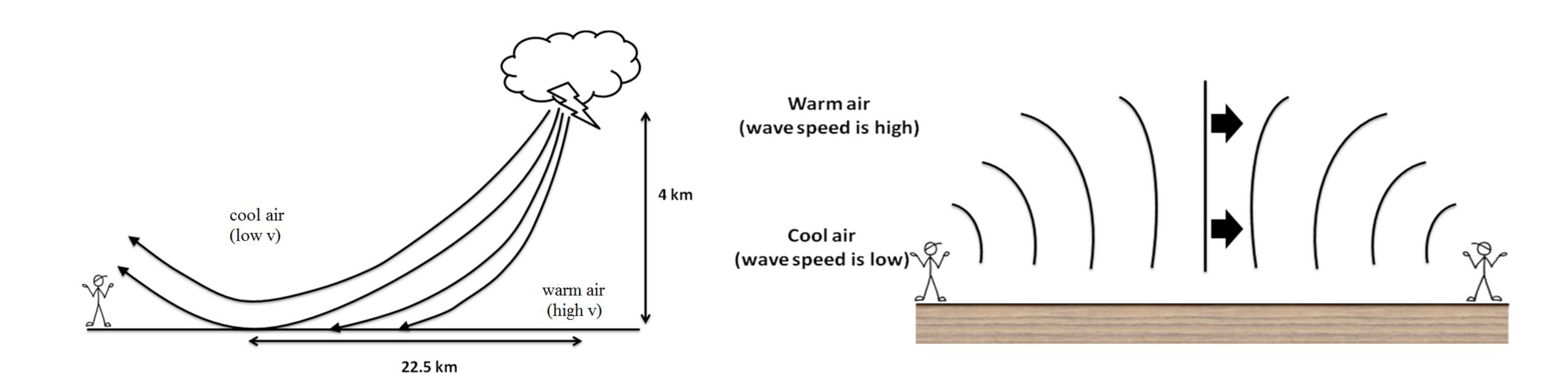
Reflections - whispering chamber



Refraction

• Change in direction of a wave Normal due to a change in its velocity Demos with light (stick, prism, medium 1 and laser) Incoming Wave medium 2 $(v_2 < v_1)$ Refracted Wave

Examples of refraction of sound

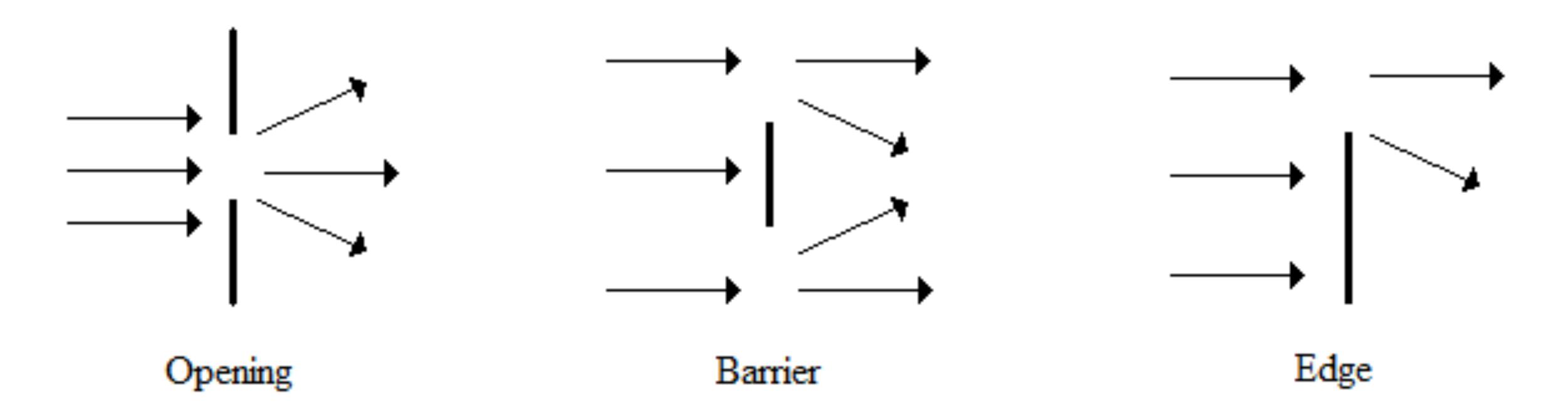


Usual temperature distribution

Temperature inversion

Diffraction

- "spreading" of a wave as it passes through openings or around barriers ...
- amount of spreading depends on relative size of wavelength and opening, barrier, ...

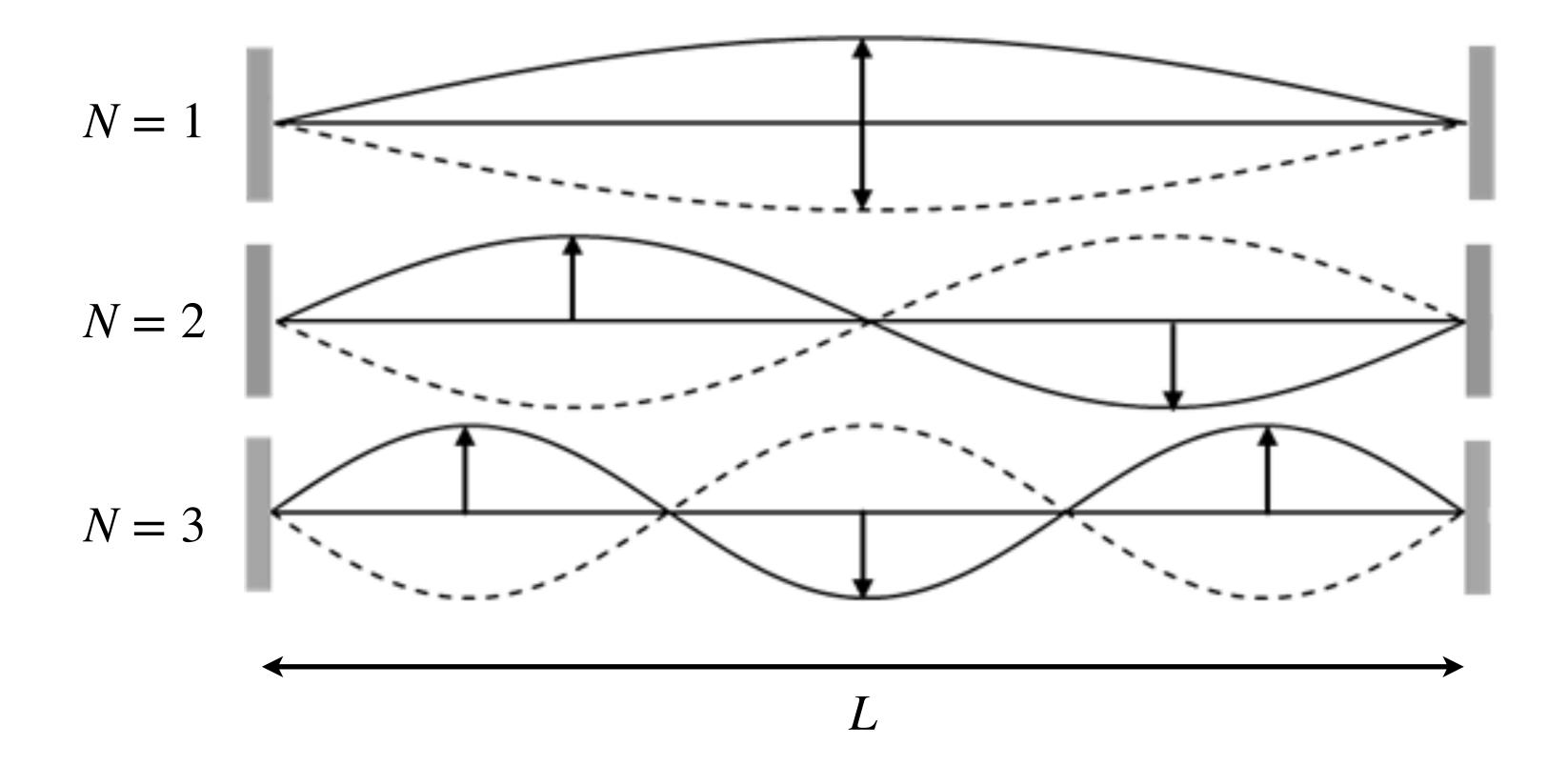


Doppler effect

- Change in frequency due to the motion of the observer or source (e.g., for sound, light, ...)
- Examples?
- Demo with nerf ball

Standing waves

- Demo: superposition of right-moving and left-moving waves on a string
- occurs only for certain frequencies (resonance phenomenon)



Air molecule displacement vs pressure deviation

