ECO 420Y - Homework 2

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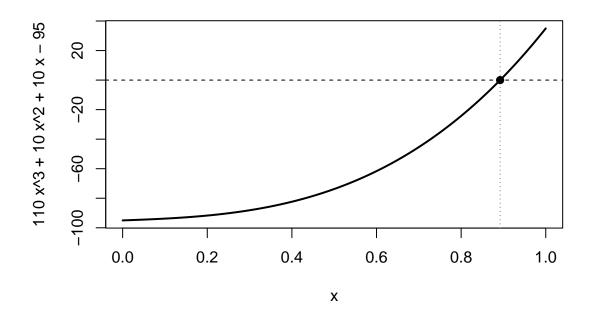
Question 1 — Solve $110x^3 + 10x^2 + 10x - 95 = 0$ by Bisection

```
d = function(x) \{ return(110*x^3 + 10*x^2 + 10*x - 95) \}
i = 0; smallx = 0; bigx = 1
while (i < 30) {
 root = (smallx + bigx)/2
 if (d(root) * d(bigx) >= 0) { bigx = root } else { smallx = root }
 cat("----", "\n")
 cat("Root is ", root, "\n")
 cat("d(root) is ", d(root), "\n")
 i = i + 1
}
## -----
## Root is 0.5
## d(root) is -73.75
## -----
## Root is 0.75
## d(root) is -35.46875
## -----
## Root is 0.875
## d(root) is -4.902344
## -----
## Root is 0.9375
## d(root) is 13.80127
## -----
## Root is 0.90625
## d(root) is 4.147644
## -----
## Root is 0.890625
## d(root) is -0.4515457
## -----
## Root is 0.8984375
## d(root) is 1.829343
## -----
## Root is 0.8945312
```

```
## d(root) is 0.6842417
## -----
## Root is 0.8925781
## d(root) is 0.1151862
## -----
## Root is 0.8916016
## d(root) is -0.1684699
## -----
## Root is 0.8920898
## d(root) is -0.02671442
## -----
## Root is 0.892334
## d(root) is 0.04421774
## -----
## Root is 0.8922119
## d(root) is 0.008747126
## -----
## Root is 0.8921509
## d(root) is -0.008984781
## -----
## Root is 0.8921814
## d(root) is -0.0001191111
## -----
## Root is 0.8921967
## d(root) is 0.004313936
## -----
## Root is 0.892189
## d(root) is 0.002097395
## -----
## Root is 0.8921852
## d(root) is 0.0009891375
## -----
## Root is 0.8921833
## d(root) is 0.0004350121
## -----
## Root is 0.8921824
## d(root) is 0.0001579502
## -----
## Root is 0.8921819
## d(root) is 1.941951e-05
## -----
## Root is 0.8921816
## d(root) is -4.98458e-05
## -----
## Root is 0.8921818
## d(root) is -1.521315e-05
## -----
## Root is 0.8921818
```

```
## d(root) is 2.10318e-06
## -----
## Root is 0.8921818
## d(root) is -6.554985e-06
## -----
## Root is 0.8921818
## d(root) is -2.225902e-06
## -----
## Root is 0.8921818
## d(root) is -6.136115e-08
## -----
## Root is 0.8921818
## d(root) is 1.020909e-06
## -----
## Root is 0.8921818
## d(root) is 4.797741e-07
## -----
## Root is 0.8921818
## d(root) is 2.092065e-07
```

Plot



Question 2 — Maximize $-x^2 + \log x$ using Newtons Method

```
f = function(x) \{ return(-x^2 + log(x)) \}
fprime = function(x) { return(-2*x + 1/x) }
fprime2 = function(x) { return(-2 - 1/x^2) }
tol = 0.001
x0 = 1
while (abs(fprime(x0)) > tol) {
  step = - fprime(x0) / fprime2(x0)
  x1 = x0 + step
  while ((x1 \le 0) || (f(x1) \le f(x0))) {
    step = step/10
    x1 = x0 + step
  }
  cat("-----
  cat("New value is ", x1, "\n")
  cat("Gradient is ", fprime(x1), "\n")
  cat("f(x) is ", f(x1), "\n")
  x0 = x1
}
```

```
## ------
## New value is 0.6666667
## Gradient is 0.1666667
## f(x) is -0.8499096
```

```
## New value is 0.7058824
## Gradient is 0.004901961
## f(x) is -0.8465766
## ------
## New value is 0.7071057
## Gradient is 4.2478e-06
## f(x) is -0.8465736
```

Plot

