# Anexo IV. Analisis anat?mico-funcional

### August 27, 2018

## Anexo IV. Analisis anatómico-funcional José Pedro Manzano Lenguaje: Python

En este anexo se sigue el procedimiento necesario para, a partir de las matrices de conectividad obtenidas de cada dataset, construir una red binaria de la que extraer las principales propiedades, tanto globales como locales.

Para no hacer el anexo demasiado extenso, las principales conclusiones extraídas de los resultados pueden encontrarse en la memoria del trabajo.

### Importación de los datos

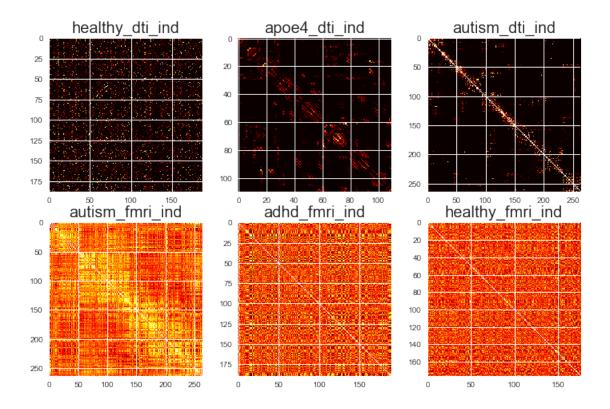
En esta primera parte, se cargarán las matrices de conectividad individuales de cada sujeto con el objetivo de obtener un promedio de 10 sujetos de cada modalidad. También mantendremos la matriz de un sujeto de cada modalidad para realizar algunas comparaciones:

- **Redes Anatómicos (DTI)** de sujetos sanos (healthy patients), con Alzheimer y Autismo.
- **Redes Funcionales (fMRI)** de sujetos sanos (healthy patients), con ADHD' y Autismo\*.

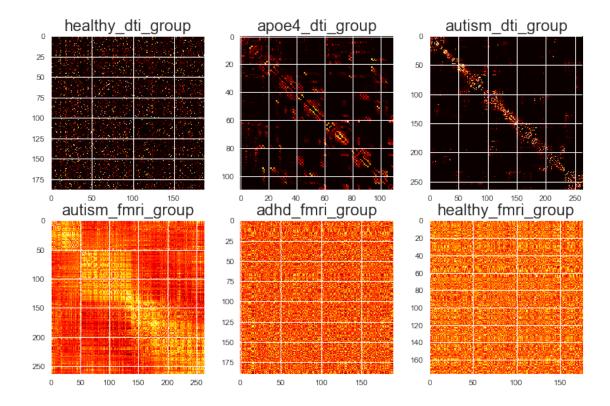
```
healthy_fmri_path = userpath + "/Datos/Seleccionados/fmri_sanos/datos/"
         pathfiles = [healthy_dti_path, apoe4_dti_path, autism_dti_path, autism_fmri_path, adhd_
         # NAME OF NODES
         hd_healthy_dti = pd.read_csv(userpath + "/Datos/Seleccionados/dti_sano/nodos/1013090_DT
         hd_apoe4_dti = pd.read_csv(userpath + "/Datos/Seleccionados/dti_alzheimer/nodos/APOE-4_
         hd_apoe4_dti = hd_apoe4_dti[0:110]
         hd_autism_dti = pd.read_csv(userpath + "/Datos/Seleccionados/dti_autism/nodos/ASD47B_DT
         hd_autism_fmri = pd.read_csv(userpath + "/Datos/Seleccionados/fmri_autismo/nodos/ASD83E
         hd_adhd_fmri = pd.read_csv(userpath + "/Datos/Seleccionados/fmri_adhd/nodos/KKI_1018959
         hd_healthy_fmri = pd.read_csv(userpath + "/Datos/Seleccionados/fmri_sanos/nodos/Baltimo
         node_names = [hd_healthy_dti, hd_apoe4_dti, hd_autism_dti, hd_autism_fmri, hd_adhd_fmri
         ## FOR THE SINGLE-SUBJECT LEVEL
         individuals = {}
         ind_names = ["healthy_dti_ind", "apoe4_dti_ind", "autism_dti_ind", "autism_fmri_ind", "
         ## FOR THE GROUP-LEVEL
         group_avg = {}
         groupnames = ["healthy_dti_group", "apoe4_dti_group", "autism_dti_group", "autism_fmri_
In [90]: # Load connectivity matrixes
        n = 0
         for i in pathfiles:
             files = os.listdir(i)
             aux = pd.read_csv(i+files[0], header=None, delim_whitespace=True)
             k = 0
             for j in files:
                 if k<1:
                     print("Individual subject of", ind_names[n], "is", j)
                     df = pd.read_csv(i+j, header=None, delim_whitespace=True)
                     np.fill_diagonal(df.values,1) # make sure diagonal = 0
                     normalized_df = preprocessing normalize(df, norm='max') # normalize
                     #normalized_df.columns = node_names[n]
                     newname = ind_names[n]
                     individuals[newname] = normalized_df
                 df = pd.read_csv(i+j, header=None, delim_whitespace=True)
                 np.fill_diagonal(df.values,1)
                 aux = aux + df
                 np.fill_diagonal(aux.values,1) # make sure diagonal = 0
                 k = k + 1
             avg_df = aux/len(files)
                                       # average matrix of groups subjects
             np.fill_diagonal(normalized_df,1)
             normalized_df = preprocessing.normalize(avg_df, norm='max') # normalize
             #normalized_df.columns = node_names[n]
```

Puede ser interesante representar las matrices de conectividad (normalizadas) para tener una primera idea del aspecto de nuestros datos.

```
In [91]: #BY SUBJECTS
         %matplotlib inline
         fig = plt.figure(figsize=(12, 12))
         plt.subplot(331)
         np.fill_diagonal(individuals[ind_names[0]],0)
         plt.imshow(individuals[ind_names[0]], cmap='hot', interpolation='nearest')
         plt.title(ind_names[0], fontsize=20)
         plt.subplot(332)
         np.fill_diagonal(individuals[ind_names[1]],0)
         plt.imshow(individuals[ind_names[1]], cmap='hot', interpolation='nearest')
         plt.title(ind_names[1], fontsize=20)
         plt.subplot(333)
         plt.imshow(individuals[ind_names[2]], cmap='hot', interpolation='nearest')
         plt.title(ind_names[2], fontsize=20)
         plt.subplot(334)
         plt.imshow(individuals[ind_names[3]], cmap='hot', interpolation='nearest')
         plt.title(ind_names[3], fontsize=20)
         plt.subplot(335)
         plt.imshow(individuals[ind_names[4]], cmap='hot', interpolation='nearest')
         plt.title(ind_names[4], fontsize=20)
         plt.subplot(336)
         plt.imshow(individuals[ind_names[5]], cmap='hot', interpolation='nearest')
         plt.title(ind_names[5], fontsize=20)
         plt.savefig('/Users/hose/Desktop/TFM_TECI/simulated_data/healthy_ill_ind')
```



```
In [92]: #BY AVERAGED GROUPS
         fig2 = plt.figure(figsize=(12, 12))
         plt.subplot(331)
         plt.imshow(group_avg[groupnames[0]], cmap='hot', interpolation='nearest')
         plt.title(groupnames[0], fontsize=20)
         plt.subplot(332)
         np.fill_diagonal(group_avg[groupnames[1]],0)
         plt.imshow(group_avg[groupnames[1]], cmap='hot', interpolation='nearest')
         plt.title(groupnames[1], fontsize=20)
         plt.subplot(333)
         plt.imshow(group_avg[groupnames[2]], cmap='hot', interpolation='nearest')
         plt.title(groupnames[2], fontsize=20)
         plt.subplot(334)
         plt.imshow(group_avg[groupnames[3]], cmap='hot', interpolation='nearest')
         plt.title(groupnames[3], fontsize=20)
         plt.subplot(335)
         plt.imshow(group_avg[groupnames[4]], cmap='hot', interpolation='nearest')
         plt.title(groupnames[4], fontsize=20)
         plt.subplot(336)
         plt.imshow(group_avg[groupnames[5]], cmap='hot', interpolation='nearest')
         plt.title(groupnames[5], fontsize=20)
         plt.savefig('/Users/hose/Desktop/TFM_TECI/simulated_data/healthy_ill_group')
```



Parece evidente que las matrices de conectividad promedio son capaces de filtrar gran parte de la variabilidad individual en las matrices funcionales, lo que revela de forma más evidente la estructura subyacente de la red.

En cuanto a las redes anatómicas parece no existir la misma variabilidad que en las funcionales, ya que el promedio grupal y las individuales se mantienen bastante similares.

### CONSTRUCCIÓN DEL GRAFO

El objetivo final es comparar las propiedades de las diferentes redes y discutir si la teoría de grafos puede ser una herramienta útil o complementaria para detectar singularidades entre patologías.

Recuerda que las redes pueden contener valores negativos de correlación. Dado que no existe consenso sobre lo que implica una correlación negativa en DTI o en fMRI, se trabajará con los valores positivos en este caso.

#### **DEFINE THE NULL-MODELS**

A continuación se definen como modelos nulos el modelo de Erdos-Renyi, una red en estrella y una red regular con propiedades similares a las de las redes construidas.

```
In [97]: n=110  # Erdos-Rengi nodes
    m=1200  # Erdos-Rengi links
    Grafos_ind = []
    Grafos_group = []

# Creation of random graphs to compare with the brain graphs
    Grandom=nx.gnm_random_graph(n,m,seed=123456789) #generador de grafo er, semilla fija
    Gregular=nx.grid_2d_graph(10,11) #generador de grafo regular
    Gstar=nx.star_graph(n-1) #generador de grafo en estrella

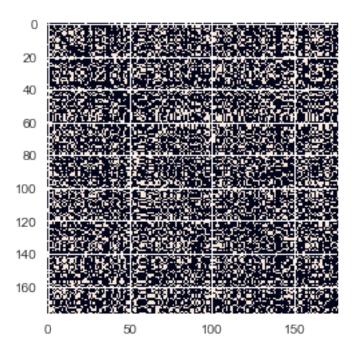
Grafos_ind.append(Grandom)
    Grafos_ind.append(Gregular)
    Grafos_group.append(Grandom)
    Grafos_group.append(Grandom)
    Grafos_group.append(Grandom)
    Grafos_group.append(Gregular)
    Grafos_group.append(Gregular)
    Grafos_group.append(Gregular)
```

Como se indicaba en la memoria, como cada matriz proviene de un dataset diferente, tienen un número de nodos y enlaces diferente. Se intentará solventar este problema lo máximo posible para cada modalidad, ajustando el umbral de modo que las redes de DTI tengan un número de enlaces y nodos lo más similar posible. Ídem para las de fMRI.

Y obtenemos las matrices de conectividad binarias tanto paras el promedio grupal como para el individual en cada modalidad:

```
n = 0
          for subject_i in individuals:
              x = individuals[subject_i]
              thr = 0.1
              print("Next subject!!!", subject_i)
              flag_error = 0
              flag_if = 0
              flag_else = 0
              while (abs(m - num_of_zeros(x,thr))>150 and (flag_error<2) and (thr<0.7)):
                  flag_error = flag_if + flag_else # to avoid starting to jump into the if and
                  if (m < num_of_zeros(x,thr)):</pre>
                      thr = thr + 0.03
                      flag_if = 1
                      thr = thr - 0.03
                      flag_else = 1
              x[x > thr] = 1
              x[x < thr] = 0
              matrizAdy = np.matrix(x)
              mat_ind.append(matrizAdy)
              thr_ind.append(thr)
              G_ind = nx.from_numpy_matrix(matrizAdy)
              G_ind.name = "Graph_" + subject_i
              nx.relabel_nodes(G_ind, dict_names(node_names[n]))
              Grafos_ind.append(G_ind)
              n = n + 1
Next subject!!! healthy_dti_ind
Next subject!!! apoe4_dti_ind
Next subject!!! autism_dti_ind
Next subject!!! autism_fmri_ind
Next subject!!! adhd_fmri_ind
Next subject!!! healthy_fmri_ind
In [102]: ## FOR THE GROUP LEVEL
          thr_group = []
          mat_group = []
          n = 0
          for group_i in group_avg:
              x = group_avg[group_i]
              thr = 0.1
              print("Next group average!!!", group_i)
              flag_error = 0
              flag_if = 0
              flag_else = 0
```

```
while (abs(m - num_of_zeros(x,thr))>150 and (flag_error<2) and (thr<0.7)):
                  flag_error = flag_if + flag_else # to avoid starting to jump into the if and
                  if (m < num_of_zeros(x,thr)):</pre>
                      thr = thr + 0.03
                      flag_if = 1
                  else:
                      thr = thr - 0.03
                      flag_else = 1
              x[x > thr] = 1
              x[x < thr] = 0
              matrizAdy = np.matrix(x)
              mat_group.append(matrizAdy)
              thr_group.append(thr)
              G_group = nx.from_numpy_matrix(matrizAdy)
              G_group.name = "Graph_" + group_i
              nx.relabel_nodes(G_group, dict_names(node_names[n]))
              Grafos_group.append(G_group)
              n = n + 1
Next group average!!! healthy_dti_group
Next group average!!! apoe4_dti_group
Next group average!!! autism_dti_group
Next group average!!! autism_fmri_group
Next group average!!! adhd_fmri_group
Next group average!!! healthy_fmri_group
In [103]: plt.imshow(group_avg[group_i])
Out[103]: <matplotlib.image.AxesImage at 0x1a21856668>
```



## ANÁLSIS I I - CARACTERÍSTICAS GLOBALES DE LA RED

```
In [105]: ## INDIVIDUAL SUBJECTS TABLE

    tabla1 = []
    tabla2 = []
    tabla3 = []
    for i in range(3,len(Grafos_ind)):
        tabla1.append(len(nx.nodes(Grafos_ind[i])))
        tabla2.append(len(nx.edges(Grafos_ind[i])))
        tabla3.append(thr_ind[i-3])

    columnas=['Healthy_DTI','Alzheimer_DTI','Autism_DTI','Autism_fMRI','ADHD_fMRI','Healthind = {0:'Nodes',1:'Edges',2:'Threshold'}
    tabla= pd.DataFrame([tabla1,tabla2,tabla3],columns=columnas)
    tabla.rename(index=ind)
```

```
ADHD_fMRI \
Out[105]:
                      Healthy_DTI
                                  Alzheimer_DTI Autism_DTI Autism_fMRI
          Nodes
                            188.0
                                          110.00
                                                        264.0
                                                                      264.0
                                                                                 190.0
                                                                                6459.0
                           2069.0
                                         5995.00
                                                       1646.0
                                                                    12820.0
          Edges
          Threshold
                              0.7
                                            0.04
                                                          0.7
                                                                        0.7
                                                                                   0.7
                      Healthy_fMRI
          Nodes
                             177.0
          Edges
                            5313.0
          Threshold
                               0.7
In [106]: ## GROUP TABLE
          tabla1 = []
          tabla2 = []
          tabla3 = []
          for i in range(3,len(Grafos_group)):
              tabla1.append(len(nx.nodes(Grafos_group[i])))
              tabla2.append(len(nx.edges(Grafos_group[i])))
              tabla3.append(thr_group[i-3])
          columnas=['Healthy_DTI', 'Alzheimer_DTI', 'Autism_DTI', 'Autism_fMRI', 'ADHD_fMRI', 'Health
          ind = {0:'Nodes',1:'Edges',2:'Threshold'}
          tabla= pd.DataFrame([tabla1,tabla2,tabla3],columns=columnas)
          tabla.rename(index=ind)
Out [106]:
                      Healthy_DTI
                                  Alzheimer_DTI
                                                  Autism_DTI Autism_fMRI
                                                                             ADHD_fMRI \
                            188.0
                                          110.00
                                                        264.0
                                                                      264.0
          Nodes
                                                                                 190.0
                           2224.0
                                                                    10649.0
          Edges
                                         5995.00
                                                       1873.0
                                                                                5880.0
          Threshold
                              0.7
                                            0.04
                                                          0.7
                                                                        0.7
                                                                                   0.7
                      Healthy_fMRI
          Nodes
                             177.0
          Edges
                            5440.0
          Threshold
                               0.7
In [107]: # CARACHTERISTICS OF INDIVIDUAL-SUBJECTS GRAPH
          Gcluster_ind=[]
          Gdegree_ind=[]
          Gbet_ind=[]
          Gclo_ind=[]
          Geff_ind=[]
          Gasor_ind=[]
          Gseg_ind=[]
          Gint_ind=[]
          Gpath_ind=[]
          for i in range(len(Grafos_ind)):
              aux_degree = 0
              for v in Grafos_ind[i].nodes():
```

```
Gbet_ind.append(st.mean(list(nx.betweenness_centrality(Grafos_ind[i]).values())))
                                            Gclo_ind.append(st.mean(list(nx.closeness_centrality(Grafos_ind[i]).values())))
                                            Geff_ind.append(nx.global_efficiency(Grafos_ind[i]))
                                            Gpath_ind.append(nx.average_shortest_path_length(Grafos_ind[i]))
                                            Gasor_ind.append(nx.degree_assortativity_coefficient(Grafos_ind[i]))
                                            Gseg_ind.append(Gcluster_ind[i]/Gcluster_ind[0]) #se considera el grafo e-r
                                            Gint_ind.append(Gpath_ind[i]/Gpath_ind[0])#integración con la eficiencia(en lugar
/Applications/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/li
      return (xy * (M - ab)).sum() / numpy.sqrt(vara * varb)
In [108]: # CARACHTERISTICS OF AVERAGE GROUPS GRAPH
                               Gcluster_group=[]
                               Gdegree_group=[]
                               Gbet_group=[]
                               Gclo_group=[]
                               Geff_group=[]
                               Gasor_group=[]
                               Gseg_group=[]
                               Gint_group=[]
                               Gpath_group=[]
                               for i in range(len(Grafos_group)):
                                            aux_degree = 0
                                           for v in Grafos_group[i].nodes():
                                                        aux_degree= aux_degree + Grafos_group[i].degree(v)
                                           Gcluster_group.append(nx.average_clustering(Grafos_group[i]))
                                           Gdegree_group.append((aux_degree)/(len(Grafos_group[i].nodes())))
                                           Gbet_group.append(st.mean(list(nx.betweenness_centrality(Grafos_group[i]).values()
                                           Gclo_group.append(st.mean(list(nx.closeness_centrality(Grafos_group[i]).values()))
                                            Geff_group.append(nx.global_efficiency(Grafos_group[i]))
                                            Gpath_group.append(nx.average_shortest_path_length(Grafos_group[i]))
                                           Gasor_group.append(nx.degree_assortativity_coefficient(Grafos_group[i]))
                                            Gseg_group.append(Gcluster_group[i]/Gcluster_group[0]) #se considera el grafo e-r
                                           Gint_group.append(Gpath_group[i]/Gpath_group[0])#integración con la eficiencia(en
/Applications/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3.6/site-packages/networkx/algorithms/assortativity/correlations/anaconda3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/lib/python3/li
      return (xy * (M - ab)).sum() / numpy.sqrt(vara * varb)
         Podemos mostrar las propiedades extraídas en una tabla para las redes individuales:
```

aux\_degree= aux\_degree + Grafos\_ind[i].degree(v)
Gcluster\_ind.append(nx.average\_clustering(Grafos\_ind[i]))
Gdegree\_ind.append((aux\_degree)/(len(Grafos\_ind[i].nodes())))

columnas=['Erdos-Renyi','Regular-Graph','Star-Graph','Sano\_DTI','Alzheimer\_DTI','Autis

In [109]: # SUMMARY TABLE OF INDIVIDUAL GRAPHS

ind = {0:'Clustering',1:'Grado Medio',2:'Betweenness Centrality',3:'Closeness Centralit
tabla= pd.DataFrame([Gcluster\_ind,Gdegree\_ind,Gbet\_ind,Gclo\_ind,Geff\_ind,Gpath\_ind,Gas
tabla.rename(index=ind)

| Out[109]: |                        | Erdos-Renyi  | Regular-Graph | Star-Graph   | Sano_DTI \ |   |
|-----------|------------------------|--------------|---------------|--------------|------------|---|
|           | Clustering             | 0.196564     | 0.000000      | 0.000000     | 0.551587   |   |
|           | Grado Medio            | 21.818182    | 3.618182      |              | 22.010638  |   |
|           | Betweenness Centrality | 0.007486     | 0.055556      | 0.009091     | 0.007207   |   |
|           | Closeness Centrality   | 0.553271     | 0.146311      | 0.506829     | 0.432862   |   |
|           | Global Efficiency      | 0.598638     | 0.208476      | 0.509091     | 0.486311   |   |
|           | Average Shortest Path  | 1.808507     | 7.000000      | 1.981818     | 2.340539   |   |
|           | Asortatividad          | -0.001453    | 0.575822      | -1.000000    | 0.097217   |   |
|           | Segregación(SW)        | 1.000000     | 0.000000      | 0.000000     | 2.806150   |   |
|           | Integración(SW)        | 1.000000     | 3.870596      | 1.095831     | 1.294183   |   |
|           |                        |              |               |              |            |   |
|           |                        | Alzheimer_DT | [ Autismo_DTI | Autismo_fMRI | ADHD_fMRI  | \ |
|           | Clustering             | 1.000000     | 0.427841      | 0.597563     | 0.605709   |   |
|           | Grado Medio            | 109.000000   | 12.469697     | 97.121212    | 67.989474  |   |
|           | Betweenness Centrality | 0.000000     | 0.008094      | 0.002417     | 0.003441   |   |
|           | Closeness Centrality   | 1.000000     | 0.324983      | 0.612688     | 0.607637   |   |
|           | Global Efficiency      | 1.000000     | 0.366363      | 0.684209     | 0.678752   |   |
|           | Average Shortest Path  | 1.000000     | 3.120607      | 1.633310     | 1.646951   |   |
|           | Asortatividad          | Nal          | 0.281060      | 0.138660     | 0.042546   |   |
|           | Segregación(SW)        | 5.087409     | 2.176601      | 3.040048     | 3.081489   |   |
|           | Integración(SW)        | 0.552942     | 2 1.725516    | 0.903126     | 0.910669   |   |
|           |                        |              |               |              |            |   |
|           |                        | Sano_fMRI    |               |              |            |   |
|           | Clustering             | 0.530262     |               |              |            |   |
|           | Grado Medio            | 60.033898    |               |              |            |   |
|           | Betweenness Centrality | 0.003789     |               |              |            |   |
|           | Closeness Centrality   | 0.602223     |               |              |            |   |
|           | Global Efficiency      | 0.669845     |               |              |            |   |
|           | Average Shortest Path  | 1.663136     |               |              |            |   |
|           | Asortatividad          | 0.221284     |               |              |            |   |
|           | Segregación(SW)        | 2.697657     |               |              |            |   |
|           | Integración(SW)        | 0.919618     |               |              |            |   |
|           | _                      |              |               |              |            |   |

## Y para las redes grupales:

### In [110]: # SUMMARY TABLE OF GROUP GRAPHS

columnas=['Erdos-Renyi', 'Regular-Graph', 'Star-Graph', 'Sano\_DTI', 'Alzheimer\_DTI', 'Autis
ind = {0:'Clustering',1:'Grado Medio',2:'Betweenness Centrality',3:'Closeness Centrali
tabla= pd.DataFrame([Gcluster\_group,Gdegree\_group,Gbet\_group,Gclo\_group,Geff\_group,Gpa
tabla.rename(index=ind)

| Out[110]: |                        | Erdos-Renyi | Regular-Graph | Star-Graph | Sano_DTI  | \ |
|-----------|------------------------|-------------|---------------|------------|-----------|---|
|           | Clustering             | 0.196564    | 0.000000      | 0.000000   | 0.576154  |   |
|           | Grado Medio            | 21.818182   | 3.618182      | 1.981818   | 23.659574 |   |
|           | Betweenness Centrality | 0.007486    | 0.055556      | 0.009091   | 0.006938  |   |

| Closeness Centrality        | 0.553271      | 0.146311    | 0.506829     | 0.442138  |   |
|-----------------------------|---------------|-------------|--------------|-----------|---|
| Global Efficiency           | 0.598638      | 0.208476    | 0.509091     | 0.497207  |   |
| Average Shortest Path       | 1.808507      | 7.000000    | 1.981818     | 2.290534  |   |
| Asortatividad               | -0.001453     | 0.575822    | -1.000000    | 0.040178  |   |
| Segregación(SW)             | 1.000000      | 0.000000    | 0.000000     | 2.931133  |   |
| Integración(SW)             | 1.000000      | 3.870596    | 1.095831     | 1.266533  |   |
|                             |               |             |              |           |   |
|                             | Alzheimer_DTI | Autismo_DTI | Autismo_fMRI | ADHD_fMRI | \ |
| Clustering                  | 1.000000      | 0.475642    | 0.568661     | 0.522363  |   |
| Grado Medio                 | 109.000000    | 14.189394   | 80.674242    | 61.894737 |   |
| Betweenness Centrality      | 0.000000      | 0.007950    | 0.002684     | 0.003592  |   |
| Closeness Centrality        | 1.000000      | 0.328346    | 0.587804     | 0.597662  |   |
| Global Efficiency           | 1.000000      | 0.373133    | 0.651731     | 0.663279  |   |
| Average Shortest Path       | 1.000000      | 3.082959    | 1.703105     | 1.675299  |   |
| Asortatividad               | NaN           | 0.269762    | 0.202035     | 0.162572  |   |
| Segregación(SW)             | 5.087409      | 2.419786    | 2.893010     | 2.657476  |   |
| Integración(SW)             | 0.552942      | 1.704698    | 0.941719     | 0.926344  |   |
|                             |               |             |              |           |   |
|                             | Sano_fMRI     |             |              |           |   |
| Clustering                  | 0.568543      |             |              |           |   |
| Grado Medio                 | 61.468927     |             |              |           |   |
| Betweenness Centrality      | 0.003765      |             |              |           |   |
| Closeness Centrality        | 0.604267      |             |              |           |   |
| Global Efficiency           | 0.673269      |             |              |           |   |
| Average Shortest Path       | 1.658898      |             |              |           |   |
| Asortatividad               | 0.395006      |             |              |           |   |
| ${	t Segregación}({	t SW})$ | 2.892411      |             |              |           |   |
| Integración(SW)             | 0.917275      |             |              |           |   |

### ANÁLISIS II - PROPIEDADES LOCALES DE LA RED

De manera similar, podemos extraer las mismas propiedades para cada nodo en lugar de para toda la red.

```
for i in range(0,len(Grafos_ind)):
              Local_prox_ind[i] = sorted(Local_prox_ind[i].items(),reverse=True,key=op.itemgette
              Local_bet_ind[i] = sorted(Local_bet_ind[i].items(),reverse=True,key=op.itemgetter(
              Local_clo_ind[i] = sorted(Local_clo_ind[i].items(),reverse=True,key=op.itemgetter(
              Local_cluster_ind[i] = sorted(Local_cluster_ind[i].items(),reverse=True,key=op.ite
              Grado_node_ind[i] = sorted(Grado_node_ind[i].items(),reverse=True,key=op.itemgette
In [112]: ## FOR GROUP AVERAGE SUBJECTS
         Local_prox_group = []
          Local_bet_group = []
          Local_clo_group = []
          Local_cluster_group = []
          Grado_node_group = []
          for i in range(0,len(Grafos_group)):
              Local_prox_group.append(nx.average_neighbor_degree(Grafos_group[i]))
              Local_bet_group.append(nx.betweenness_centrality(Grafos_group[i]))
              Local_clo_group.append(nx.closeness_centrality(Grafos_group[i]))
              Local_cluster_group.append(nx.clustering(Grafos_group[i]))
              grado_group={}
              for v in Grafos_group[i].nodes():
                      grado_group[v]=Grafos_group[i].degree(v)
              Grado_node_group.append(grado_group)
          for i in range(0,len(Grafos_group)):
              Local_prox_group[i] = sorted(Local_prox_group[i].items(),reverse=True,key=op.itemg
              Local_bet_group[i] = sorted(Local_bet_group[i].items(),reverse=True,key=op.itemget
              Local_clo_group[i] = sorted(Local_clo_group[i].items(),reverse=True,key=op.itemget
              Local_cluster_group[i] = sorted(Local_cluster_group[i].items(),reverse=True,key=op
              Grado_node_group[i] = sorted(Grado_node_group[i].items(),reverse=True,key=op.items
In [113]: ## SUMMARY TABLE
          def local_properties(graph_x, propertie_x):
              indc={0:'Erdos-Renyi',1:'Regular-Graph',2:'Star-Graph',3:'Healthy_DTI',4:'Alzheime
              lista=[]
              for i in range(0,len(graph_x)):
                  lista.append(itertools.islice(propertie_x[i],0,4))
              tabla_x= pd.DataFrame(lista)
              tabla_x.rename(index=indc)
              return(tabla_x)
  En este caso, resumir y mostrar la información es algo más complejo (como se vio antes,
son cientos de nodos). Por ello, mostraremos el valor de los 4 nodos más extremos para cada
```

propiedad, en forma de pares de valor (nodo, valor) para tener una idea:

### **SHORT PATH LENGHTS**

INDIVIDUAL SUBJECTS

```
In [61]: indc={0:'Erdos-Renyi',1:'Regular-Graph',2:'Star-Graph',3:'Healthy_DTI',4:'Alzheimer_DTI
         columns = {}
```

```
In [62]: local_properties(Grafos_ind, Local_prox_ind).rename(index=indc)
Out [62]:
                                        (47, 24.3)
         Erdos-Renyi
                                                      (67, 24.11764705882353)
         Regular-Graph
                                     ((2, 2), 4.0)
                                                                ((2, 3), 4.0)
         Star-Graph
                                        (1, 109.0)
                                                                   (2, 109.0)
         Healthy_DTI
                                                     (43, 35.6666666666664)
                            (3, 36.26315789473684)
         Alzheimer_DTI
                           (12, 15.76923076923077)
                                                      (8, 15.6666666666666)
         Autism_DTI
                                        (55, 20.4)
                                                     (51, 19.727272727272727)
         Autism_fMRI
                         (136, 105.63106796116504)
                                                      (87, 105.1304347826087)
         ADHD_fMRI
                          (163, 78.33333333333333)
                                                     (118, 78.02409638554217)
                                                      (58, 79.62790697674419)
         Healthy_fMRI
                            (68, 80.0657894736842)
                                                                              3
         Erdos-Renyi
                                                      (69, 23.6666666666668)
                          (92, 24.076923076923077)
         Regular-Graph
                                     ((2, 4), 4.0)
                                                                 ((2, 5), 4.0)
         Star-Graph
                                        (3, 109.0)
                                                                    (4, 109.0)
                                                                    (4, 33.35)
         Healthy_DTI
                         (186, 33.357142857142854)
         Alzheimer_DTI
                                        (7, 15.25)
                                                                 (73, 14.9375)
         Autism_DTI
                                       (97, 19.45)
                                                     (109, 19.357142857142858)
         Autism_fMRI
                          (68, 105.03658536585365)
                                                     (232, 104.76576576576576)
         ADHD_fMRI
                                        (96, 78.0)
                                                                   (159, 78.0)
         Healthy_fMRI
                            (85, 79.6067415730337)
                                                       (107, 79.4054054054054)
   GROUP AVERAGE
In [ ]: local_properties(Grafos_group, Local_prox_group).rename(index=indc)
   BETWENNESS
   INDIVIDUAL SUBJECTS
In [64]: local_properties(Grafos_ind, Local_bet_ind).rename(index=indc)
Out [64]:
                                                      0
                                                                                         \
                                                                                      1
                            (99, 0.014691107624638211)
                                                             (59, 0.01445917683048305)
         Erdos-Renyi
         Regular-Graph
                        ((4, 5), 0.12317750678824708)
                                                         ((5, 5), 0.12317750678824702)
         Star-Graph
                                               (0, 1.0)
                                                                               (1, 0.0)
         Healthy_DTI
                            (18, 0.060822427403918015)
                                                           (124, 0.052536864647576446)
         Alzheimer_DTI
                             (26, 0.09448485800450983)
                                                             (29, 0.08366961197166296)
         Autism_DTI
                              (61, 0.0738479674453349)
                                                             (94, 0.07131238961409556)
         Autism_fMRI
                           (230, 0.005618113772020311)
                                                           (257, 0.005394094206358545)
         ADHD_fMRI
                           (182, 0.009965574773996266)
                                                            (85, 0.009915206785946235)
         Healthy_fMRI
                            (50, 0.010623342630312749)
                                                            (40, 0.007367022246358978)
                                                      2
                                                                                      3
                            (19, 0.014047183900834929)
                                                               (42, 0.013750404203352)
         Erdos-Renyi
         Regular-Graph ((5, 4), 0.11884780954126385)
                                                         ((5, 6), 0.11884780954126385)
         Star-Graph
                                               (2, 0.0)
                                                                               (3, 0.0)
         Healthy_DTI
                             (28, 0.05178185478985241)
                                                             (32, 0.04439177829633221)
```

```
Alzheimer_DTI
                             (56, 0.06044706928717459)
                                                             (85, 0.05998581673615049)
         Autism_DTI
                           (195, 0.058677587257606724)
                                                             (63, 0.05333199200741908)
         Autism_fMRI
                             (91, 0.00536511674554631)
                                                            (62, 0.005095467814654273)
         ADHD_fMRI
                           (132, 0.007605799398216297)
                                                            (34, 0.007545934090884662)
         Healthy_fMRI
                          (117, 0.0068622504758469715)
                                                            (93, 0.006639537731329414)
   GROUP AVERAGE
In [65]: local_properties(Grafos_group, Local_bet_group).rename(index=indc)
Out [65]:
         Erdos-Renvi
                            (99, 0.014691107624638211)
                                                             (59, 0.01445917683048305)
         Regular-Graph
                         ((4, 5), 0.12317750678824708)
                                                         ((5, 5), 0.12317750678824702)
         Star-Graph
                                                                               (1, 0.0)
                                               (0, 1.0)
         Healthy_DTI
                            (137, 0.06044882035598517)
                                                            (18, 0.053623443064305935)
         Alzheimer_DTI
                                               (0, 0.0)
                                                                               (1, 0.0)
         Autism_DTI
                            (114, 0.07322392222561284)
                                                            (195, 0.06536875695098289)
         Autism_fMRI
                           (188, 0.007878824490298208)
                                                            (51, 0.007673799008738922)
         ADHD_fMRI
                           (128, 0.008170652790822923)
                                                            (74, 0.008076242711278757)
         Healthy_fMRI
                            (54, 0.015531810072773832)
                                                           (157, 0.010124987246980726)
                                                      2
                                                                                      3
         Erdos-Renyi
                            (19, 0.014047183900834929)
                                                               (42, 0.013750404203352)
                                                         ((5, 6), 0.11884780954126385)
         Regular-Graph
                         ((5, 4), 0.11884780954126385)
         Star-Graph
                                               (2, 0.0)
                                                                               (3, 0.0)
         Healthy_DTI
                            (19, 0.053025679068215474)
                                                             (32, 0.04528613953571924)
         Alzheimer_DTI
                                               (2, 0.0)
                                                                               (3, 0.0)
         Autism_DTI
                            (61, 0.058390637299586746)
                                                             (94, 0.05198298973216866)
         Autism_fMRI
                           (220, 0.007533870737179082)
                                                           (100, 0.007234018919107022)
         ADHD_fMRI
                            (79, 0.007670258763697202)
                                                           (122, 0.007482543374321487)
         Healthy_fMRI
                           (125, 0.009140547317157622)
                                                           (132, 0.008544249704405708)
   CLOSENESS
   INDIVIDUAL SUBJECTS
In [66]: local_properties(Grafos_ind, Local_clo_ind).rename(index=indc)
Out [66]:
                                                                                      1
         Erdos-Renyi
                              (42, 0.5828877005347594)
                                                              (19, 0.5797872340425532)
         Regular-Graph
                        ((4, 5), 0.18956521739130436)
                                                         ((5, 5), 0.18956521739130436)
         Star-Graph
                                                               (1, 0.5023041474654378)
                                               (0, 1.0)
         Healthy_DTI
                             (124, 0.5632530120481928)
                                                              (76, 0.5483870967741935)
         Alzheimer_DTI
                                                              (10, 0.4560669456066946)
                              (74, 0.4678111587982833)
         Autism_DTI
                             (94, 0.43543046357615894)
                                                              (61, 0.4332784184514003)
         Autism_fMRI
                             (135, 0.6658227848101266)
                                                             (138, 0.6641414141414141)
         ADHD_fMRI
                             (146, 0.6702127659574468)
                                                              (81, 0.6608391608391608)
         Healthy_fMRI
                              (50, 0.6984126984126984)
                                                             (125, 0.6956521739130435)
```

2

3

```
Erdos-Renyi
                             (99, 0.5767195767195767)
                                                             (59, 0.5736842105263158)
         Regular-Graph
                        ((4, 4), 0.18632478632478633)
                                                        ((4, 6), 0.18632478632478633)
         Star-Graph
                              (2, 0.5023041474654378)
                                                              (3, 0.5023041474654378)
         Healthy_DTI
                             (32, 0.5451895043731778)
                                                             (19, 0.5373563218390804)
         Alzheimer_DTI
                             (73, 0.4541666666666666)
                                                            (57, 0.45228215767634855)
         Autism_DTI
                             (114, 0.4228295819935691)
                                                             (63, 0.4161392405063291)
         Autism_fMRI
                             (147, 0.6624685138539043)
                                                             (84, 0.6493827160493827)
                                        (135, 0.65625)
         ADHD_fMRI
                                                              (1, 0.6539792387543253)
                             (26, 0.6929133858267716)
         Healthy_fMRI
                                                            (117, 0.6848249027237354)
   GROUP AVERAGE
In [67]: local_properties(Grafos_group, Local_clo_group).rename(index=indc)
Out [67]:
                                                     0
                                                                                     1
         Erdos-Renyi
                             (42, 0.5828877005347594)
                                                             (19, 0.5797872340425532)
         Regular-Graph
                        ((4, 5), 0.18956521739130436)
                                                        ((5, 5), 0.18956521739130436)
         Star-Graph
                                              (0, 1.0)
                                                              (1, 0.5023041474654378)
         Healthy_DTI
                             (19, 0.5683890577507599)
                                                             (32, 0.5683890577507599)
         Alzheimer_DTI
                                              (0, 1.0)
                                                                              (1, 1.0)
                                                            (94, 0.4383333333333333)
         Autism_DTI
                             (114, 0.4503424657534247)
         Autism_fMRI
                             (133, 0.6322115384615384)
                                                            (127, 0.6306954436450839)
         ADHD_fMRI
                             (122, 0.6472602739726028)
                                                            (146, 0.6472602739726028)
         Healthy_fMRI
                             (50, 0.6616541353383458)
                                                             (68, 0.6567164179104478)
                                                     2
                                                                                     3
         Erdos-Renyi
                             (99, 0.5767195767195767)
                                                             (59, 0.5736842105263158)
         Regular-Graph
                        ((4, 4), 0.18632478632478633)
                                                        ((4, 6), 0.18632478632478633)
         Star-Graph
                               (2, 0.5023041474654378)
                                                              (3, 0.5023041474654378)
         Healthy_DTI
                                           (123, 0.55)
                                                                           (124, 0.55)
                                              (2, 1.0)
                                                                              (3, 1.0)
         Alzheimer_DTI
         Autism_DTI
                             (195, 0.4228295819935691)
                                                            (61, 0.41878980891719747)
                             (130, 0.6306954436450839)
                                                            (113, 0.6291866028708134)
         Autism_fMRI
         ADHD_fMRI
                             (70, 0.6385135135135135)
                                                            (114, 0.6385135135135135)
         Healthy_fMRI
                             (98, 0.6567164179104478)
                                                            (163, 0.6567164179104478)
   CLUSTERING COEFFICIENT
   INDIVIDUAL SUBJECTS
In [68]: local_properties(Grafos_ind, Local_cluster_ind).rename(index=indc)
Out [68]:
                                                 0
         Erdos-Renyi
                         (73, 0.26143790849673204)
         Regular-Graph
                                       ((0, 0), 0)
                                                                   ((0, 1), 0)
         Star-Graph
                                            (0, 0)
                                                                        (1, 0)
         Healthy_DTI
                         (43, 0.8761904761904762)
                                                    (173, 0.8717948717948718)
         Alzheimer_DTI
                                         (35, 1.0)
                                                     (51, 0.86666666666667)
         Autism_DTI
                                         (23, 1.0)
                                                                   (213, 1.0)
```

(199, 0.7448453608247423)

(234, 0.7482900136798906)

Autism\_fMRI

```
ADHD_fMRI
                                                      (41, 0.7406103286384976)
                          (12, 0.7534246575342466)
         Healthy_fMRI
                         (156, 0.6938775510204082)
                                                      (71, 0.6848370927318296)
                                                  2
                                                                              3
         Erdos-Renyi
                                        (35, 0.25)
                                                     (55, 0.24333333333333333)
         Regular-Graph
                                       ((0, 2), 0)
                                                                    ((0, 3), 0)
         Star-Graph
                                             (2, 0)
                                                                         (3, 0)
                                                                     (135, 0.8)
         Healthy_DTI
                         (165, 0.86666666666667)
         Alzheimer_DTI
                          (87, 0.86666666666667)
                                                      (95, 0.86666666666667)
         Autism_DTI
                         (261, 0.8095238095238095)
                                                     (169, 0.7619047619047619)
                         (217, 0.7329292929292929)
                                                     (235, 0.7328178694158075)
         Autism_fMRI
         ADHD_fMRI
                          (30, 0.7405405405405405)
                                                     (183, 0.7330827067669173)
                                                     (120, 0.6689291101055806)
         Healthy_fMRI
                         (111, 0.6754300551768906)
   GROUP AVERAGE
In [69]: local_properties(Grafos_group, Local_cluster_group).rename(index=indc)
Out [69]:
                                                                              1
         Erdos-Renyi
                          (47, 0.3333333333333333)
                                                     (73, 0.26143790849673204)
         Regular-Graph
                                       ((0, 0), 0)
                                                                    ((0, 1), 0)
         Star-Graph
                                             (0, 0)
                                                                         (1, 0)
         Healthy_DTI
                          (38, 0.8333333333333333)
                                                     (135, 0.8333333333333333)
                                           (0, 1.0)
                                                                       (1, 1.0)
         Alzheimer_DTI
         Autism_DTI
                         (261, 0.866666666666667)
                                                      (34, 0.8214285714285714)
         Autism_fMRI
                          (65, 0.8069053708439897)
                                                      (60, 0.7718947718947718)
                                                     (177, 0.6338797814207651)
         ADHD_fMRI
                          (77, 0.6453900709219859)
         Healthy_fMRI
                          (37, 0.8369230769230769)
                                                     (124, 0.8022988505747126)
                                                                              3
                                                  2
         Erdos-Renyi
                                        (35, 0.25)
                                                     (55, 0.2433333333333333)
                                       ((0, 2), 0)
                                                                    ((0, 3), 0)
         Regular-Graph
                                             (2, 0)
         Star-Graph
                                                                         (3, 0)
         Healthy_DTI
                         (169, 0.8205128205128205)
                                                      (94, 0.8187134502923976)
         Alzheimer_DTI
                                           (2, 1.0)
                                                                       (3, 1.0)
         Autism_DTI
                          (51, 0.7636363636363637)
                                                     (124, 0.7454545454545455)
                          (61, 0.7616330114135206)
                                                       (71, 0.753746694093447)
         Autism_fMRI
         ADHD_fMRI
                         (101, 0.6308831306187203)
                                                     (123, 0.6265664160401002)
                                                      (89, 0.7318548387096774)
         Healthy_fMRI
                         (140, 0.7425287356321839)
   DEGREE NODE
   INDIVIDUAL SUBJECTS
In [70]: local_properties(Grafos_ind, Grado_node_ind).rename(index=indc)
Out [70]:
                                   0
                                                              2
                                                                            3
                                                 1
         Erdos-Renyi
                            (42, 31)
                                          (19, 30)
                                                       (99, 29)
                                                                     (59, 28)
         Regular-Graph
                        ((1, 1), 4)
                                      ((1, 2), 4)
                                                    ((1, 3), 4)
                                                                 ((1, 4), 4)
         Star-Graph
                                            (1, 1)
                                                         (2, 1)
                            (0, 109)
                                                                       (3, 1)
```

| Healthy_DTI   | (45, 53)   | (18, 52)   | (32, 51)   | (92, 51)   |
|---------------|------------|------------|------------|------------|
| Alzheimer_DTI | (29, 22)   | (9, 20)    | (74, 20)   | (15, 19)   |
| Autism_DTI    | (94, 34)   | (59, 28)   | (61, 27)   | (114, 27)  |
| Autism_fMRI   | (135, 132) | (138, 130) | (147, 129) | (220, 123) |
| ADHD_fMRI     | (146, 96)  | (81, 92)   | (135, 90)  | (1, 89)    |
| Healthy fMRT  | (50, 100)  | (125.99)   | (26.98)    | (117. 95)  |

## GROUP AVERAGE

In [71]: local\_properties(Grafos\_group, Grado\_node\_group).rename(index=indc)

| Out[71]: |                       | 0           | 1           | 2           | 3           |
|----------|-----------------------|-------------|-------------|-------------|-------------|
|          | Erdos-Renyi           | (42, 31)    | (19, 30)    | (99, 29)    | (59, 28)    |
|          | Regular-Graph         | ((1, 1), 4) | ((1, 2), 4) | ((1, 3), 4) | ((1, 4), 4) |
|          | Star-Graph            | (0, 109)    | (1, 1)      | (2, 1)      | (3, 1)      |
|          | Healthy_DTI           | (19, 61)    | (18, 58)    | (32, 58)    | (153, 57)   |
|          | Alzheimer_DTI         | (0, 109)    | (1, 109)    | (2, 109)    | (3, 109)    |
|          | Autism_DTI            | (190, 33)   | (61, 32)    | (114, 32)   | (59, 31)    |
|          | Autism_fMRI           | (96, 112)   | (133, 111)  | (135, 110)  | (113, 109)  |
|          | ADHD_fMRI             | (146, 87)   | (122, 86)   | (70, 82)    | (114, 82)   |
|          | ${\tt Healthv\_fMRI}$ | (50, 86)    | (98, 86)    | (104, 85)   | (29, 84)    |