



Tratamiento de Señales

Version 2024-I

Wavelets

[Capítulo 4]

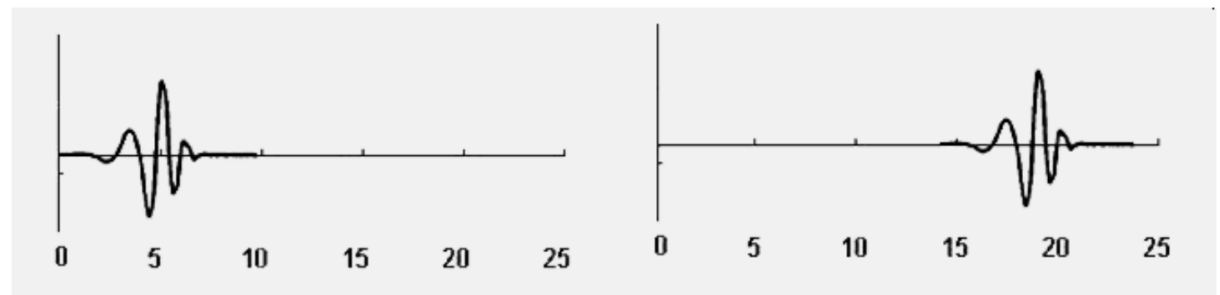
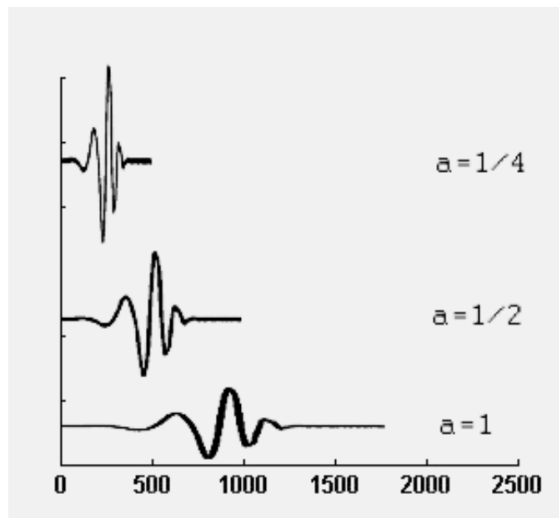
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Wavelets are functions in the set of real numbers to the set of real numbers, each of which is derived from the mother using translation and scaling:

$$\psi_{s,x}(t) = \psi(2^s * t + x)$$

where: s, x – real numbers, ψ – mother wavelet, $\psi_{s,x}$ – wavelet of scale s and translation x .

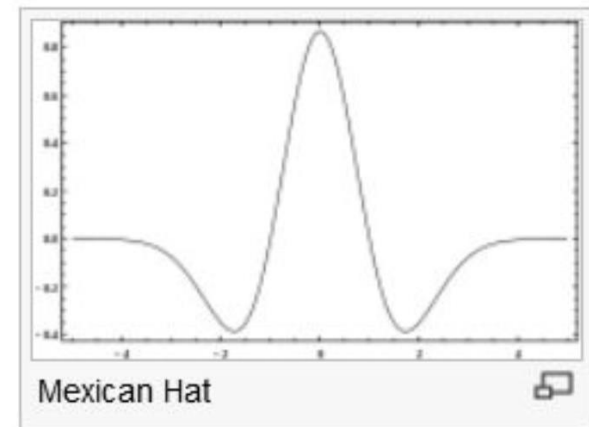
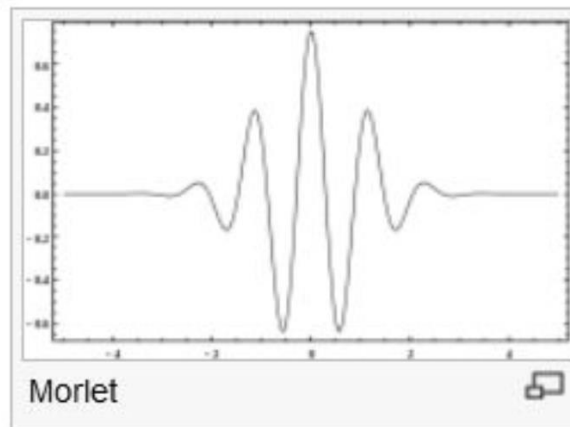
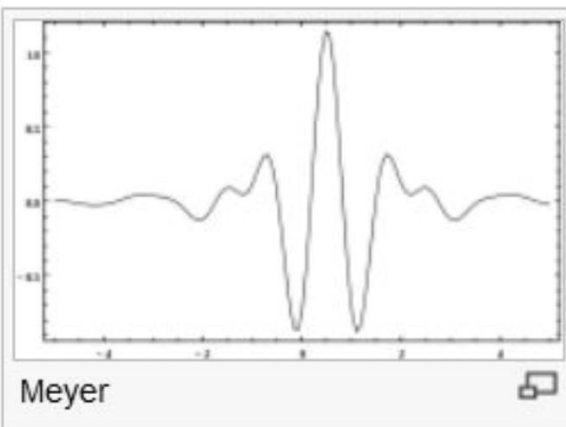


[wikipedia]

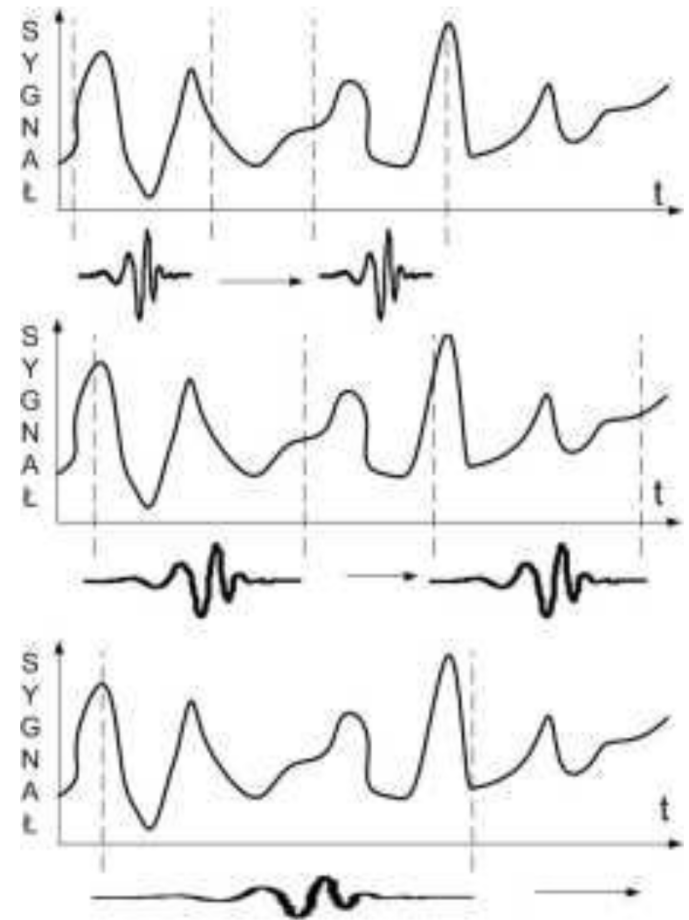
$$\psi^{s,x}(t) = \frac{1}{\sqrt{|s|}} \psi\left(\frac{t-x}{s}\right), \quad s \neq 0.$$

$\int \psi(t) dt = 0$ At least several oscillations of mother wavelet (basis function)

$f = \sum_{m,n \in \mathbb{C}} c_{m,n}(f) \psi_{m,n}$ Decomposition of f using base function



The sum of the weighted functions $\Psi_{s,x}$ can represent with any accuracy any continuous function like the cosine functions of different periods allow to represent any periodic function with arbitrary precision



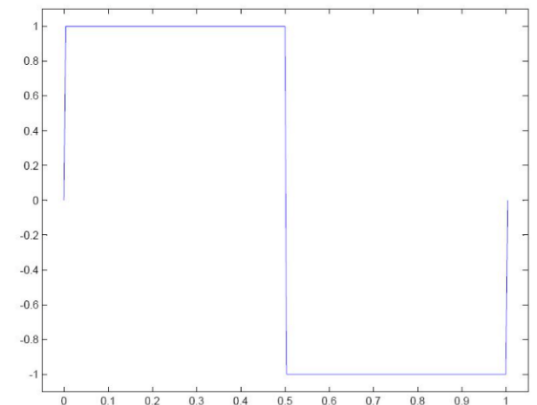
- Mean value = 0

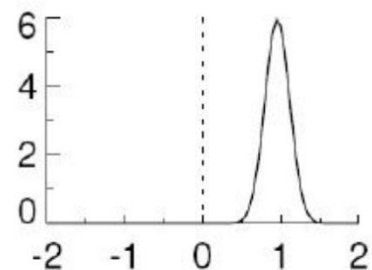
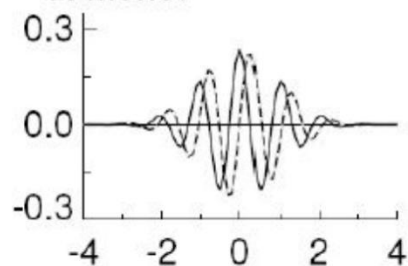
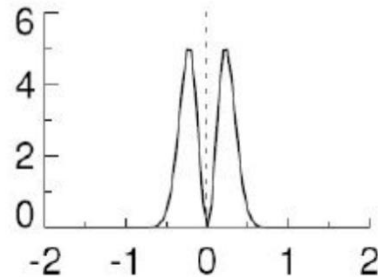
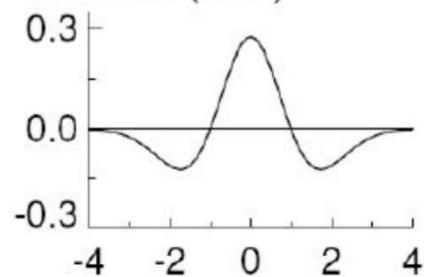
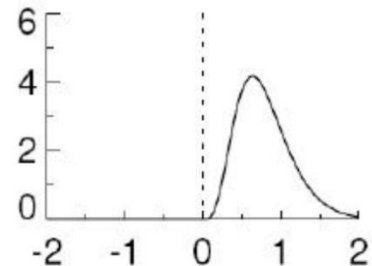
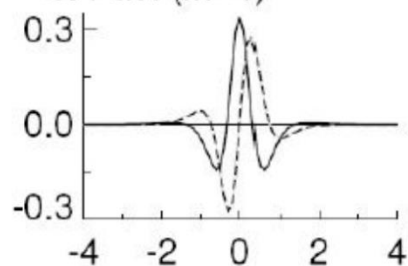
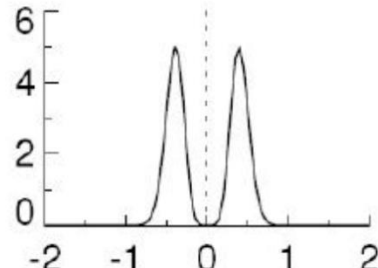
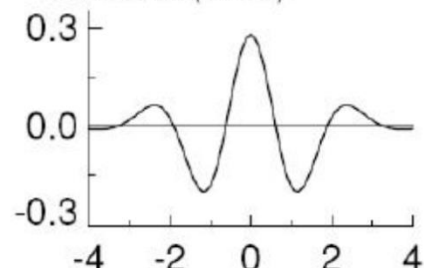
$$\int_{-\infty}^{+\infty} \psi(t) dt = 0$$

- normalization $\|\psi\| = 1$

- Set around $t=0$

- Finite range of transmission



$\psi(t/s)$ $\hat{\psi}(s\omega)$ $\psi(t/s)$ $\hat{\psi}(s\omega)$ **a. Morlet****c. DOG (m=2)****b. Paul (m=4)****d. DOG (m=6)** t/s $s\omega/(2\pi)$ t/s $s\omega/(2\pi)$

