Lecture 7: Training Neural Networks

Dr. José Ramón Iglesias

DSP-ASIC BUILDER GROUP
Director Semillero TRIAC

Ingenieria Electronica

Universidad Popular del Cesar



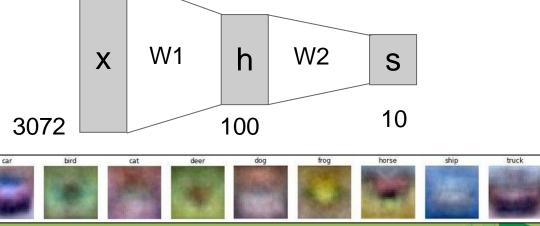
Neural Networks

Linear score function:

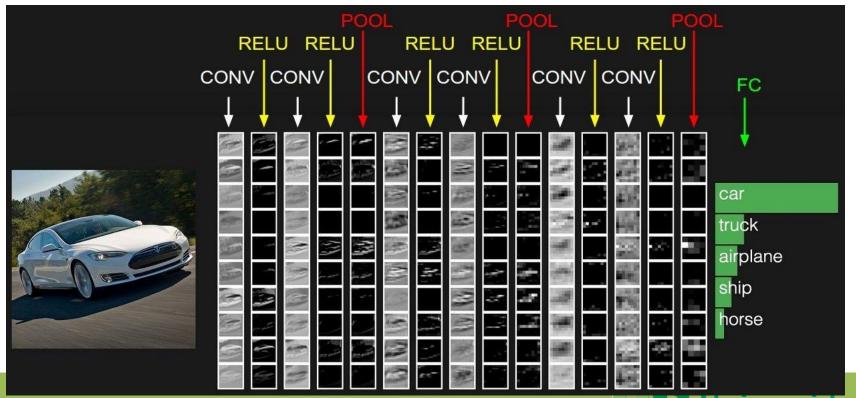
f = Wx

2-layer Neural Network

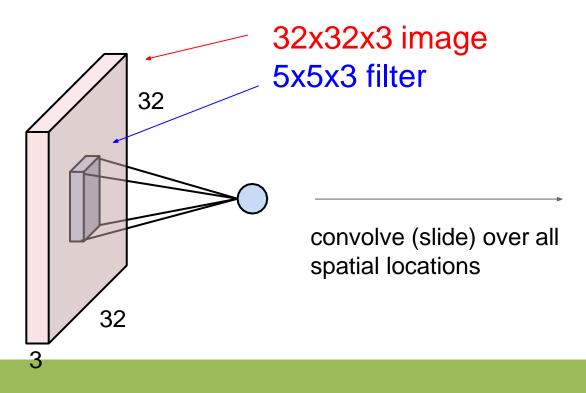
 $f = W_2 \max(0, W_1 x)$



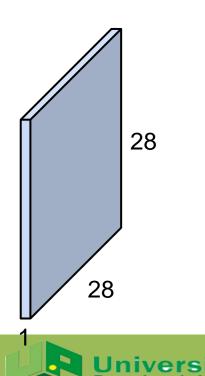
Convolutional Neural Networks



Convolutional Layer



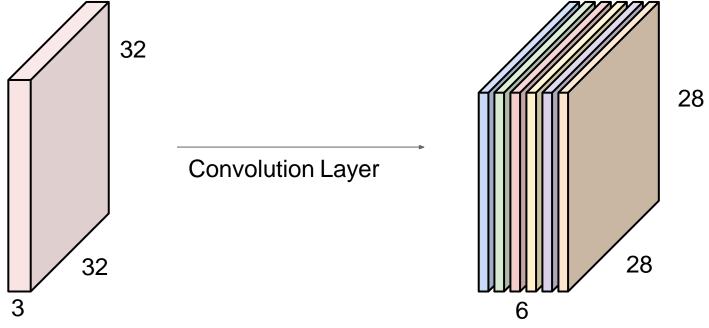
activation map



Convolutional Layer

For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:



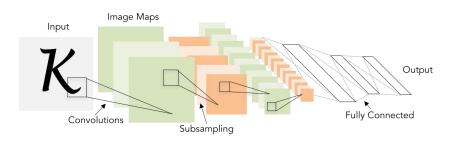


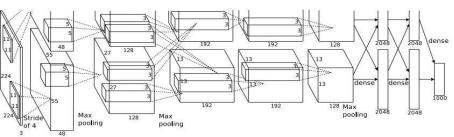
We stack these up to get a "new image" of size 28x28x6!

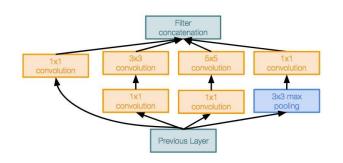
Training Neural Networks

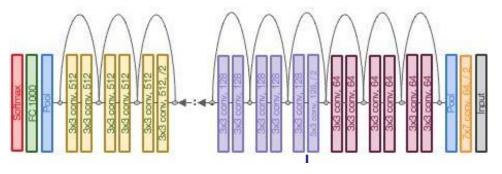


CNN Architectures



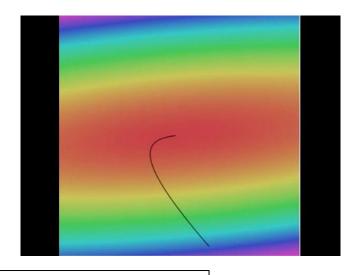






Learning network parameters through optimization





```
# Vanilla Gradient Descent
while True:
    weights_grad = evaluate_gradient(loss_fun, data, weights)
    weights += - step size * weights grad # perform parameter update
```

<u>Landscape image is CC0 1.0 public domain</u>

<u>Walking man image is CC0 1.0 public domain</u>



Mini-batch SGD

Loop:

- 1. Sample a batch of data
- 2. Forward prop it through the graph (network), get loss
- 3. Backprop to calculate the gradients
- 4. Update the parameters using the gradient



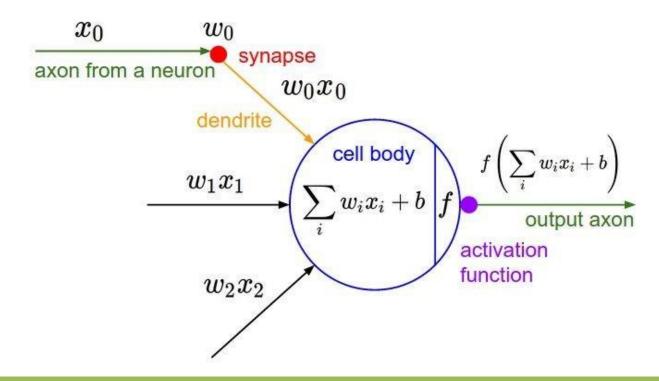
Today: Training Neural Networks



Overview

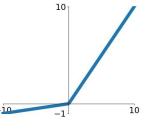
- 1. One time set up: activation functions, preprocessing, weight initialization, regularization, gradient checking
- 2. Training dynamics: babysitting the learning process, parameter updates, hyperparameter optimization
- 3. Evaluation: model ensembles, test-time augmentation, transfer learning





Sigmoid $\sigma(x) = \frac{1}{1 + e^{-x}}$

Leaky ReLU $\max(0.1x, x)$



tanh

$$\tanh(x)$$

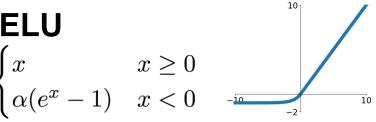
Maxout

 $\max(w_1^T x + b_1, w_2^T x + b_2)$

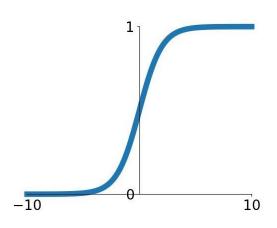
ReLU

ReLU
$$\max(0,x)$$

ELU



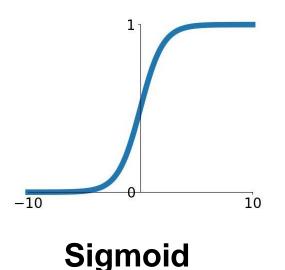




Sigmoid

$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

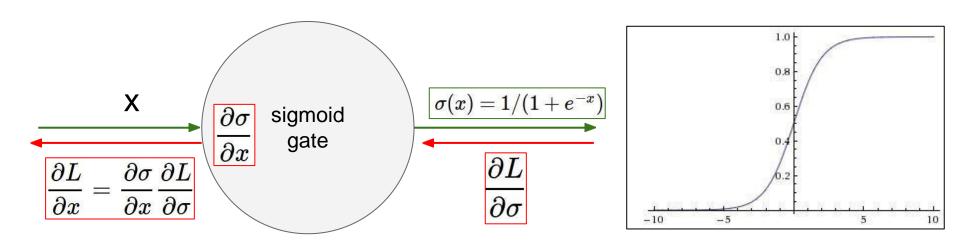


$$\sigma(x) = 1/(1 + e^{-x})$$

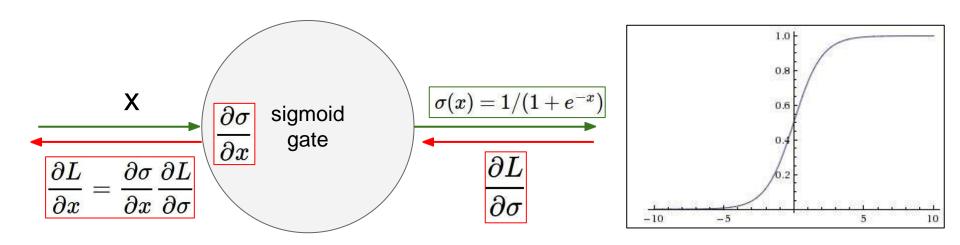
- Squashes numbers to range [0,1]
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3 problems:

Saturated neurons "kill" the gradients



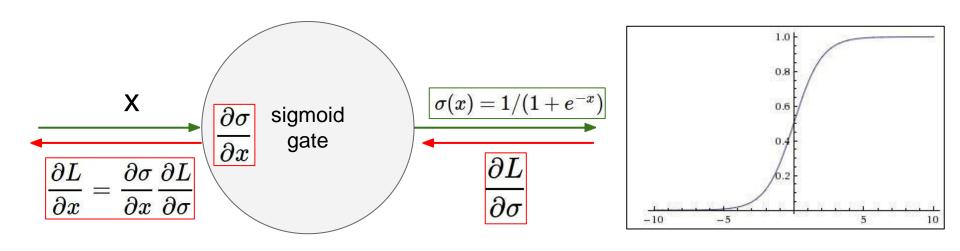
$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x) \right)$$



What happens when x = -10?

$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x) \right)$$





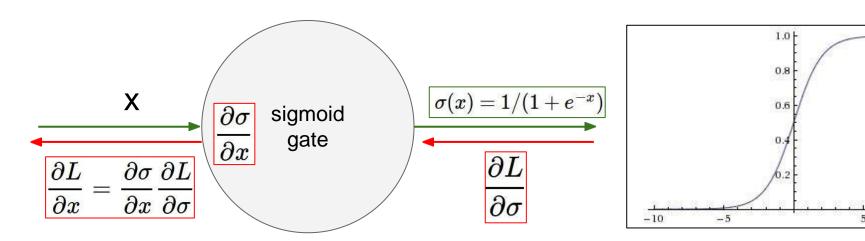
What happens when x = -10?

$$\sigma(x) = -0$$

$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x) \right) = 0 (1 - 0) = 0$$

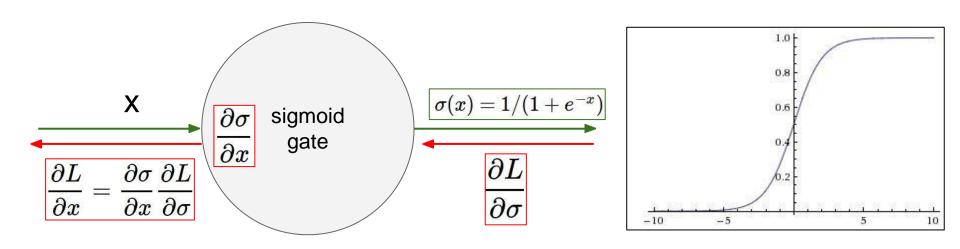
$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x) \right)$$





What happens when x = -10? What happens when x = 0?

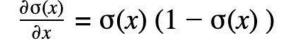
$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x) \right)$$



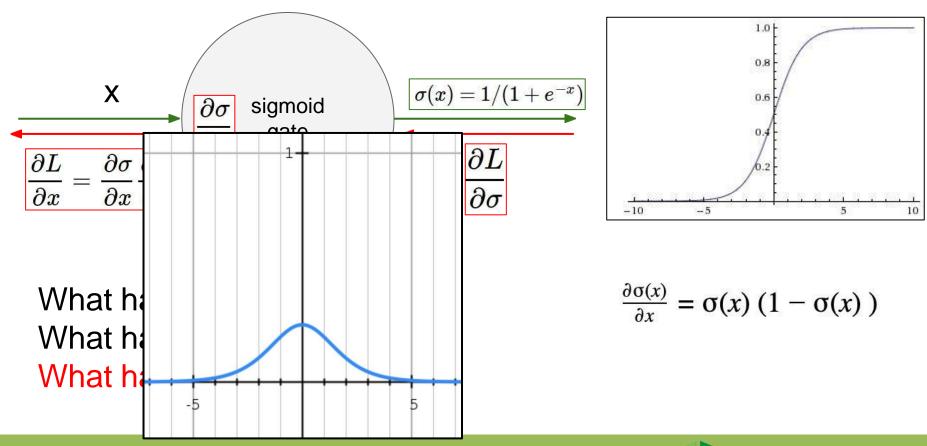
What happens when x = -10? What happens when x = 0? What happens when x = 10?

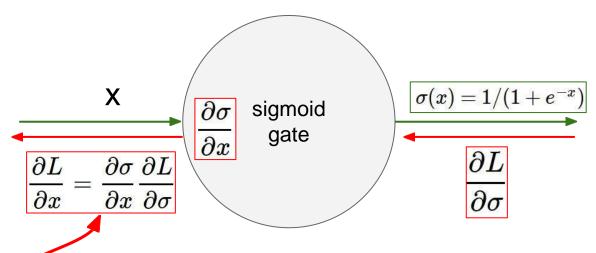
$$\sigma(x) = -1 \qquad \frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x)\right) = 1(1 - 1) = 0$$

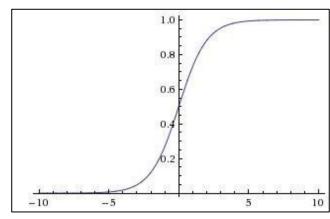
Training Neural Networks







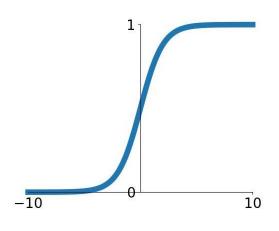




Why is this a problem?
If all the gradients flowing back will be zero and weights will never change

$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x) \right)$$





Sigmoid

$$\sigma(x) = 1/(1 + e^{-x})$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

- Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered

$$f\left(\sum_i w_i x_i + b\right)$$

What can we say about the gradients on **w**?



axon from a neuron

 w_1x_1

$$f\left(\sum_i w_i x_i + b
ight)$$

What can we say about the gradients on **w**?

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b))x imes upstream_gradient$$

$$f\left(\sum_i w_i x_i + b
ight)$$

What can we say about the gradients on $\overline{\mathbf{w}}$?

We know that local gradient of sigmoid is always positive

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b)) x imes upstream_gradient$$

Consider what happens when the input to a neuron is always positive... $\frac{x_0}{w_0}$

$$f\left(\sum_i w_i x_i + b
ight)$$

What can we say about the gradients on $\overline{\mathbf{w}}$?

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$$f\left(\sum_i w_i x_i + b
ight)$$

What can we say about the gradients on $\overline{\mathbf{w}}$?

We know that local gradient of sigmoid is always positive We are assuming x is always positive

So!! Sign of gradient for all w_i is the same as the sign of upstream scalar gradient!

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b))x imes upstream_gradient$$

$$f\left(\sum_i w_i x_i + b
ight)$$

What can we say about the gradients on **w**? Always all positive or all negative :(

allowed gradient update directions zig zag path allowed gradient update directions hypothetical optimal w vector

$$f\left(\sum_i w_i x_i + b
ight)$$

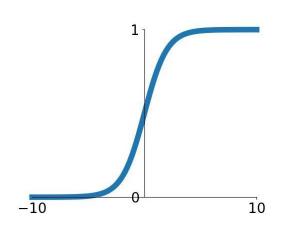
What can we say about the gradients on w?

Always all positive or all negative :(

(For a single element! Minibatches help)

gradient update directions zig zag path allowed gradient update directions hypothetical optimal w vector





Sigmoid

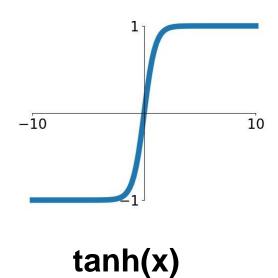
$\sigma(x) = 1/(1+e^{-x})$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

- Saturated neurons "kill" the gradients
- Sigmoid outputs are not zero-centered
- 3. exp() is a bit compute expensive





- Squashes numbers to range [-1,1]
- zero centered (nice)
- still kills gradients when saturated :(

[LeCun et al., 1991]
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Popular del Cesa

- Computes f(x) = max(0,x)
- Does not saturate (in +region)
 - Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)

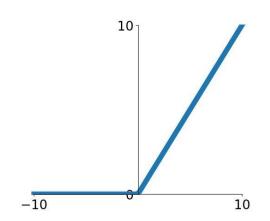
ReLU

-10

(Rectified Linear Unit)

[Krizhevsky et al., 2012]

10

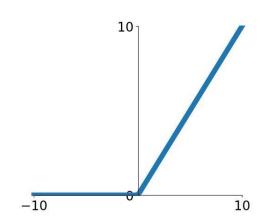


ReLU (Rectified Linear Unit)

- Computes f(x) = max(0,x)
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Not zero-centered output





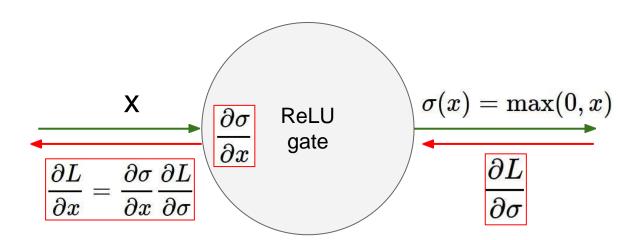
ReLU (Rectified Linear Unit)

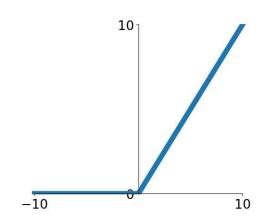
- Computes f(x) = max(0,x)
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- Not zero-centered output
- An annoyance:

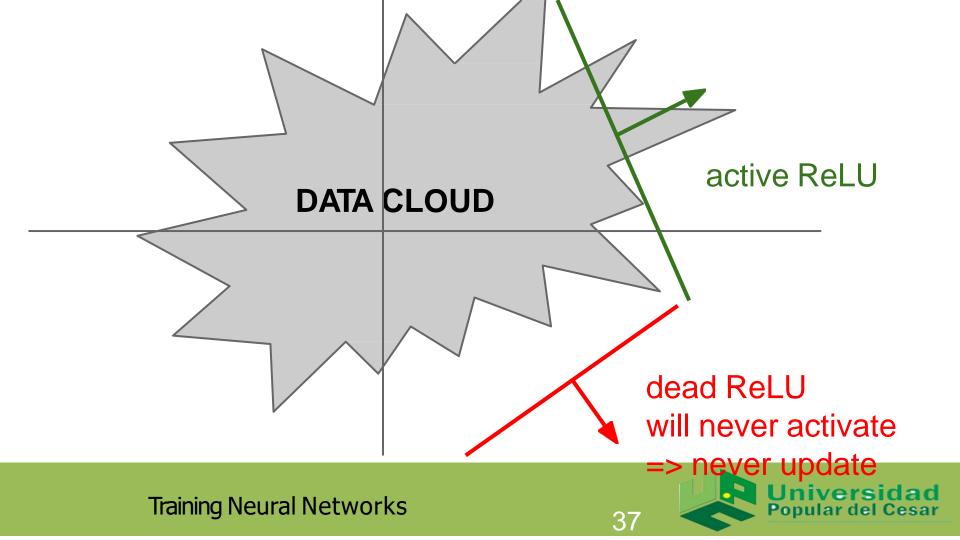
hint: what is the gradient when x < 0?

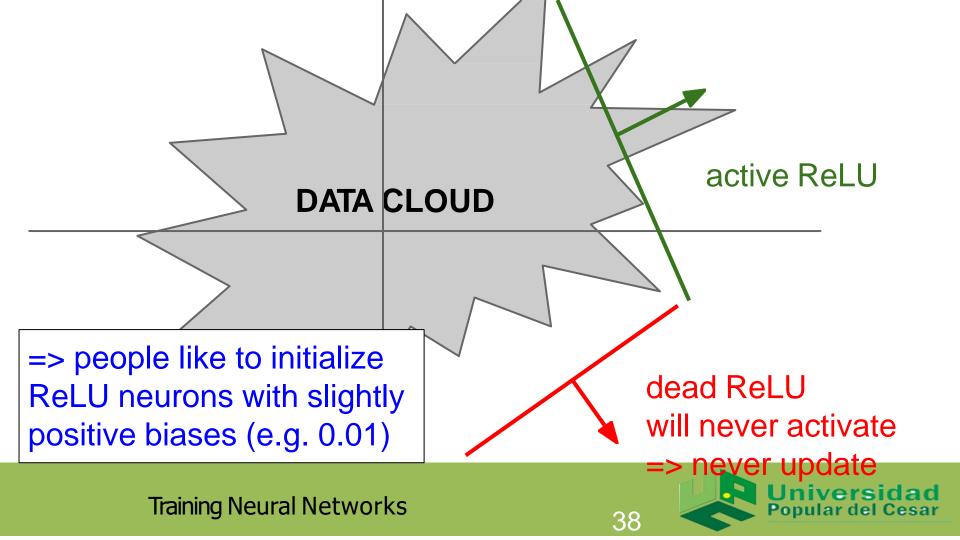






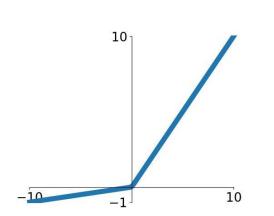
What happens when x = -10? What happens when x = 0? What happens when x = 10?





Activation Functions

[Mass et al., 2013] [He et al., 2015]



- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
- will not "die".

Leaky ReLU

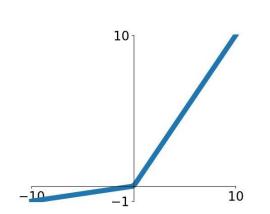
$$f(x) = \max(0.01x, x)$$



Activation Functions

[He et al., 2015] aturate

[Mass et al., 2013]



- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
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Leaky ReLU

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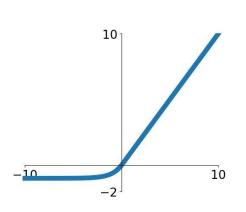
Parametric Rectifier (PReLU)

$$f(x) = \max(\alpha x, x)$$

backprop into α (parameter)



Exponential Linear Units (ELU)



$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha (\exp(x) - 1) & \text{if } x \le 0 \end{cases}$$

- All benefits of ReLU
- Closer to zero mean outputs
- Negative saturation regime compared with Leaky ReLU adds some robustness to noise

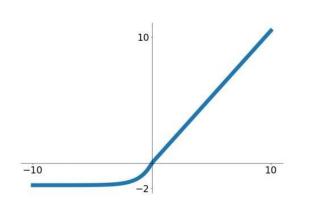
- Computation requires exp()

(Alpha default = 1)
Training Neural Networks



Activation Functions

Scaled Exponential Linear Units (SELU)



- "Self-normalizing" property;
- Can train deep SELU networks without BatchNorm

$$f(x) = \left\{ egin{array}{ll} \lambda x & ext{if } x > 0 \ \lambda lpha(e^x - 1) & ext{otherwise} \end{array}
ight.$$

$$\alpha = 1.6732632423543772848170429916717$$

 $\lambda = 1.0507009873554804934193349852946$ Training Neural Networks



Maxout "Neuron"

- Does not have the basic form of dot product -> nonlinearity
- Generalizes ReLU and Leaky ReLU
- Linear Regime! Does not saturate! Does not die!

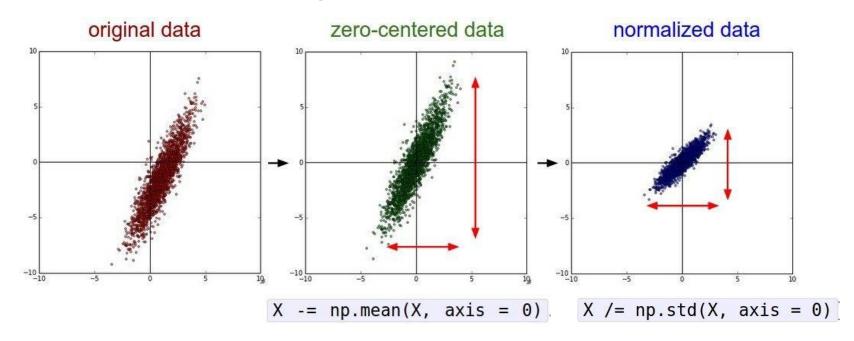
$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

Problem: doubles the number of parameters/neuron:(

TLDR: In practice:

- Use ReLU. Be careful with your learning rates
- Try out Leaky ReLU / Maxout / ELU / SELU
 - To squeeze out some marginal gains
- Don't use sigmoid or tanh





(Assume X [NxD] is data matrix, each example in a row)



Remember: Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_i w_i x_i + b
ight)$$

What can we say about the gradients on **w**? Always all positive or all negative :(

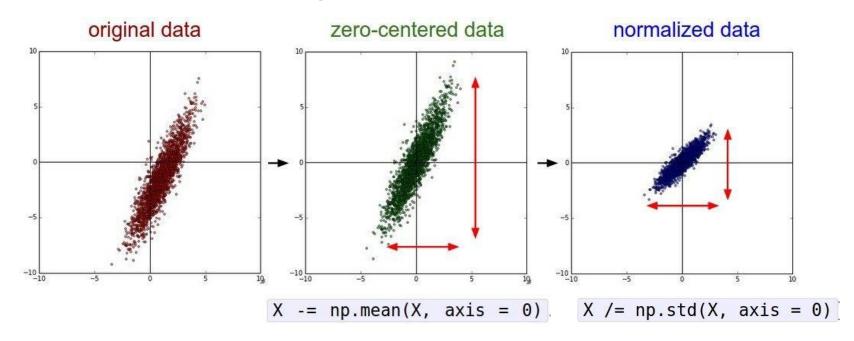
(this is also why you want zero-mean datal)

allowed gradient update directions zig zag path hypothetical optimal w



vector

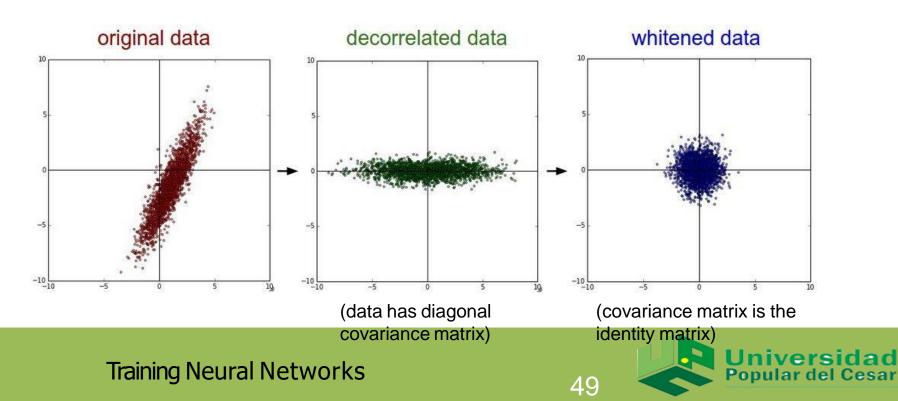
allowed gradient update directions



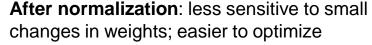
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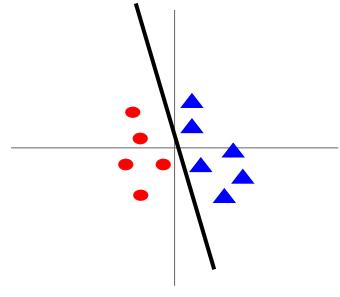


In practice, you may also see **PCA** and **Whitening** of the data



Before normalization: classification loss very sensitive to changes in weight matrix; hard to optimize









TLDR: In practice for Images: center only

- e.g. consider CIFAR-10 example with [32,32,3] images
- Subtract the mean image (e.g. AlexNet) (mean image = [32,32,3] array)
- Subtract per-channel mean (e.g. VGGNet)
 (mean along each channel = 3 numbers)
- Subtract per-channel mean and
 Divide by per-channel std (e.g. ResNet)
 (mean along each channel = 3 numbers)

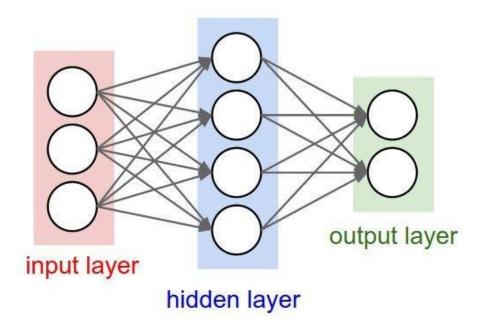
Not common to do PCA or whitening



Weight Initialization



- Q: what happens when W=constant init is used?



- First idea: **Small random numbers** (gaussian with zero mean and 1e-2 standard deviation)

W = 0.01 * np.random.randn(Din, Dout)

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Works ~okay for small networks, but problems with deeper networks.

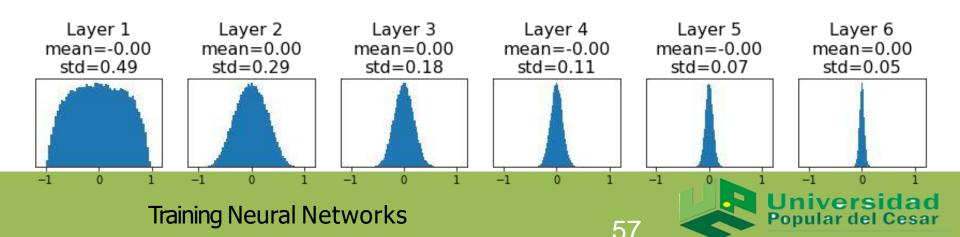
```
dims = [4096] * 7 Forward pass for a 6-layer
hs = [] net with hidden size 4096
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = 0.01 * np.random.randn(Din, Dout)
    x = np.tanh(x.dot(W))
    hs.append(x)
```

What will happen to the activations for the last layer?

```
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```

All activations tend to zero for deeper network layers

Q: What do the gradients dL/dW look like?

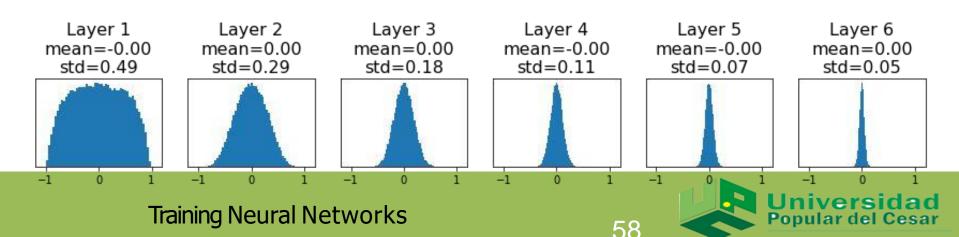


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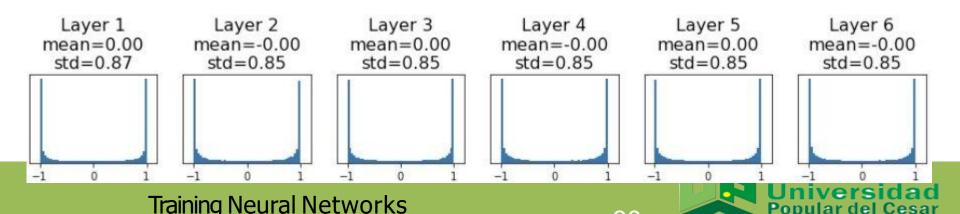
A: All zero, no learning =(



What will happen to the activations for the last layer?

All activations saturate

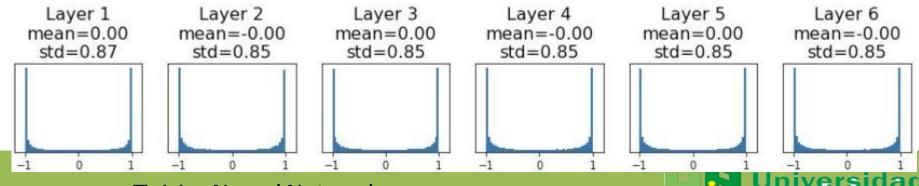
Q: What do the gradients look like?



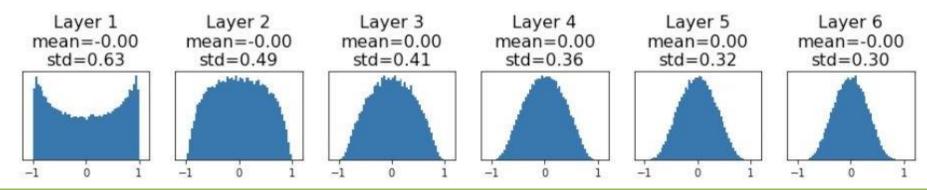
All activations saturate

Q: What do the gradients look like?

A: Local gradients all zero, no learning =(



"Just right": Activations are nicely scaled for all layers!

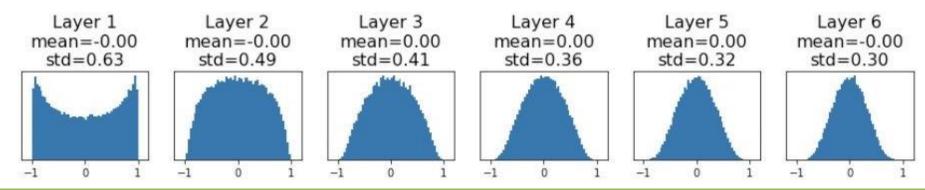


Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010



"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels



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"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels

Let:
$$y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}$$



"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels

Let:
$$y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}$$

Assume:
$$Var(x_1) = Var(x_2) = ... = Var(x_{Din})$$

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels

```
Let: y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}
```

Assume:
$$Var(x_1) = Var(x_2) = ... = Var(x_{Din})$$

We want: $Var(y) = Var(x_i)$

"Just right": Activations are nicely scaled for all layers!

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```
Let: y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}

Assume: Var(x_1) = Var(x_2) = ... = Var(x_{Din})
```

We want:
$$Var(y) = Var(x_i)$$

 $Var(y) = Var(x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din})$ [substituting value of y]



"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels

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Let: y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}

Assume: Var(x_1) = Var(x_2) = ... = Var(x_{Din})

We want: Var(y) = Var(x_i)
```

$$Var(y) = Var(x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din})$$

$$= Din Var(x_iw_i)$$
[Assume all x_i, w_i are iid]

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels

```
Let: y = x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din}

Assume: Var(x_1) = Var(x_2) = ... = Var(x_{Din})

We want: Var(y) = Var(x_i)
```

 $Var(y) = Var(x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din})$ $= Din Var(x_iw_i)$ $= Din Var(x_i) Var(w_i)$ [Assume all x_i, w_i are zero mean]

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels

```
Let: y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}

Assume: Var(x_1) = Var(x_2) = ... = Var(x_{Din})
```

x = np.tanh(x.dot(W))

We want: $Var(y) = Var(x_i)$

hs.append(x)

$$Var(y) = Var(x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din})$$

$$= Din Var(x_iw_i)$$

$$= Din Var(x_i) Var(w_i)$$
[Assume all x_i, w_i are iid]

So, $Var(y) = Var(x_i)$ only when $Var(w_i) = 1/Din$

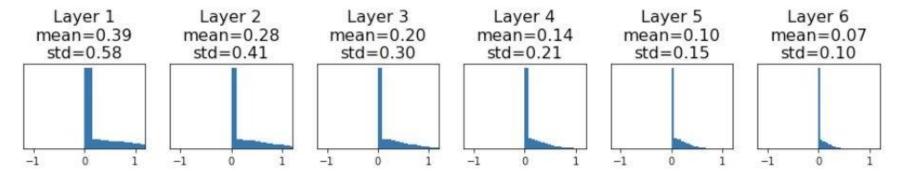


Weight Initialization: What about ReLU?

Weight Initialization: What about ReLU?

Xavier assumes zero centered activation function

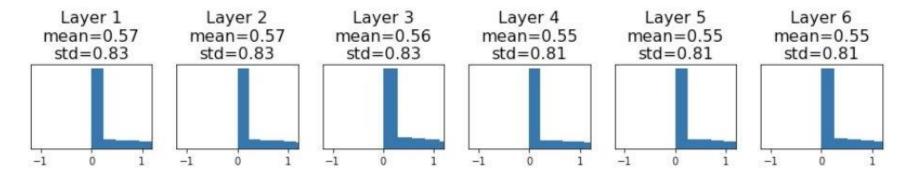
Activations collapse to zero again, no learning =(



Weight Initialization: Kaiming / MSRA Initialization

```
dims = [4096] * 7
hs = []
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = np.random.randn(Din, Dout) * np.sqrt(2/Din)
    x = np.maximum(0, x.dot(W))
    hs.append(x)
```

"Just right": Activations are nicely scaled for all layers!



He et al, "Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification", ICCV 2015



Proper initialization is an active area of research...

Understanding the difficulty of training deep feedforward neural networks by Glorot and Bengio, 2010

Exact solutions to the nonlinear dynamics of learning in deep linear neural networks by Saxe et al, 2013

Random walk initialization for training very deep feedforward networks by Sussillo and Abbott, 2014

Delving deep into rectifiers: Surpassing human-level performance on ImageNet classification by He et al., 2015

Data-dependent Initializations of Convolutional Neural Networks by Krähenbühl et al., 2015

All you need is a good init, Mishkin and Matas, 2015

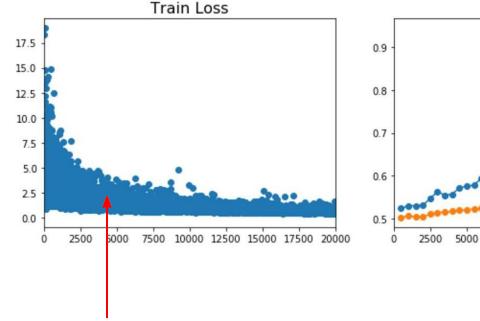
Fixup Initialization: Residual Learning Without Normalization, Zhang et al, 2019

The Lottery Ticket Hypothesis: Finding Sparse, Trainable Neural Networks, Frankle and Carbin, 2019



Training vs. Testing Error

Beyond Training Error



But we really care about error on new data - how to reduce the gap?

7500

10000

Accuracy

Better optimization algorithms help reduce training loss

Training Neural Networks

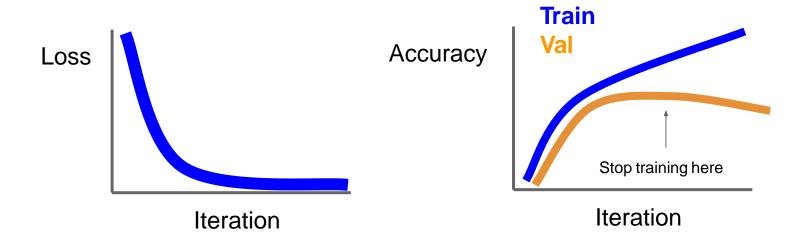


train

val

12500 15000 17500

Early Stopping: Always do this



Stop training the model when accuracy on the validation set decreases Or train for a long time, but always keep track of the model snapshot that worked best on val



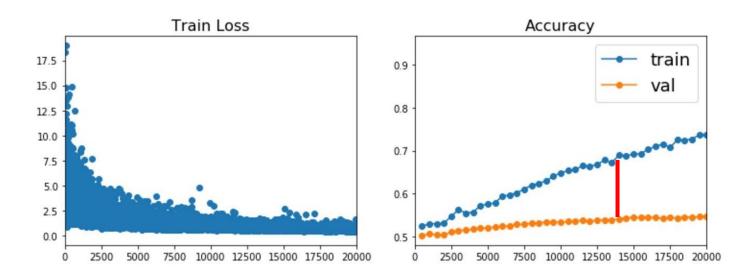
Model Ensembles

- 1. Train multiple independent models
- 2. At test time average their results
 (Take average of predicted probability distributions, then choose argmax)

Enjoy 2% extra performance



How to improve single-model performance?



Regularization



Regularization: Add term to loss

$$L=rac{1}{N}\sum_{i=1}^{N}\sum_{j
eq y_i}\max(0,f(x_i;W)_j-f(x_i;W)_{y_i}+1)+ \lambda R(W)$$

In common use:

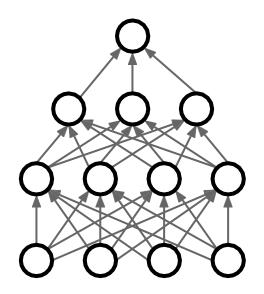
L2 regularization
$$R(W) = \sum_{k} \sum_{l} W_{k,l}^2$$
 (Weight decay)

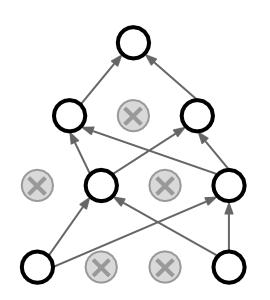
L1 regularization
$$R(W) = \sum_{k} \sum_{l} |W_{k,l}|$$

Elastic net (L1 + L2)
$$R(W) = \sum_{k} \sum_{l} \beta W_{k,l}^{2} + |W_{k,l}|$$



In each forward pass, randomly set some neurons to zero Probability of dropping is a hyperparameter; 0.5 is common

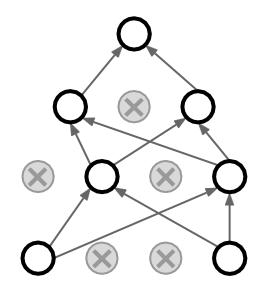






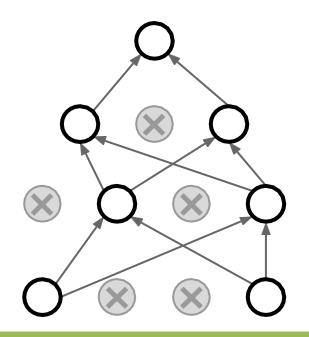
```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train step(X):
  """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) 
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
  # perform parameter update... (not shown)
```

Example forward pass with a 3-layer network using dropout





How can this possibly be a good idea?

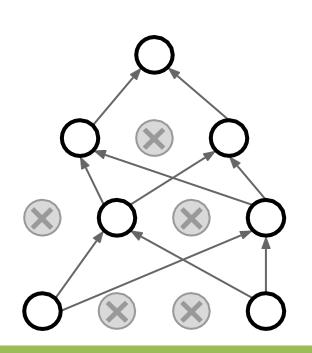


Forces the network to have a redundant representation; Prevents co-adaptation of features





How can this possibly be a good idea?



Another interpretation:

Dropout is training a large **ensemble** of models (that share parameters).

Each binary mask is one model

An FC layer with 4096 units has $2^{4096} \sim 10^{1233}$ possible masks!

Only ~ 1082 atoms in the universe...

Dropout makes our output random!

Output Input (label) (image)
$$y = f_W(x,z) \quad \text{Random} \quad \text{mask}$$

Want to "average out" the randomness at test-time

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

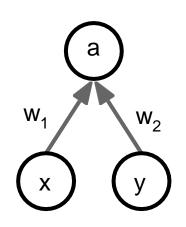
But this integral seems hard ...



Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

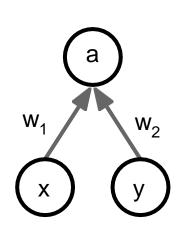
Consider a single neuron.





Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

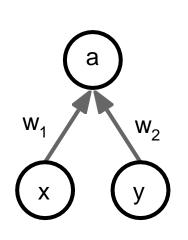


Consider a single neuron.

At test time we have: $E[a] = w_1x + w_2y$

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



Consider a single neuron.

At test time we have:
$$E[a] = w_1x + w_2y$$

During training we have:
$$E[a] = \frac{1}{4}(w_1x + w_2y) + \frac{1}{4}(w_1x + 0y)$$

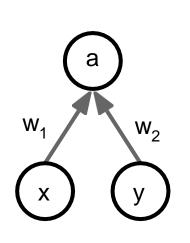
$$+\frac{1}{4}(0x+0y)+\frac{1}{4}(0x+w_2y)$$

$$= \frac{1}{2}(w_1 x + w_2 y)$$



Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



Consider a single neuron.

At test time we have: $E[a] = w_1x + w_2y$

During training we have:

 $E[a] = \frac{1}{4}(w_1x + w_2y) + \frac{1}{4}(w_1x + 0y) + \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2y)$

At test time, **multiply** by dropout probability

$$= \frac{1}{2}(w_1x + w_2y)$$



```
def predict(X):
    # ensembled forward pass
H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
out = np.dot(W3, H2) + b3
```

At test time all neurons are active always => We must scale the activations so that for each neuron: output at test time = expected output at training time



```
Vanilla Dropout: Not recommended implementation (see notes below)
p = 0.5 # probability of keeping a unit active, higher = less dropout
def train step(X):
  """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) < p # first dropout mask
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
 H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
 out = np.dot(W3, H2) + b3
```

Dropout Summary

drop in train time

scale at test time



More common: "Inverted dropout"

```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train step(X):
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = (np.random.rand(*H1.shape) < p) / p # first dropout mask. Notice /p!
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = (np.random.rand(*H2.shape) < p) / p # second dropout mask. Notice /p!
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
                                                                      test time is unchanged!
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(0, np.dot(W1, X) + b1) # no scaling necessary
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 out = np.dot(W3, H2) + b3
```

Regularization: A common pattern

Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



Regularization: A common pattern

Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

(sometimes approximate)
$$y = f(x) = E_z \big[f(x,z) \big] = \int p(z) f(x,z) dz$$

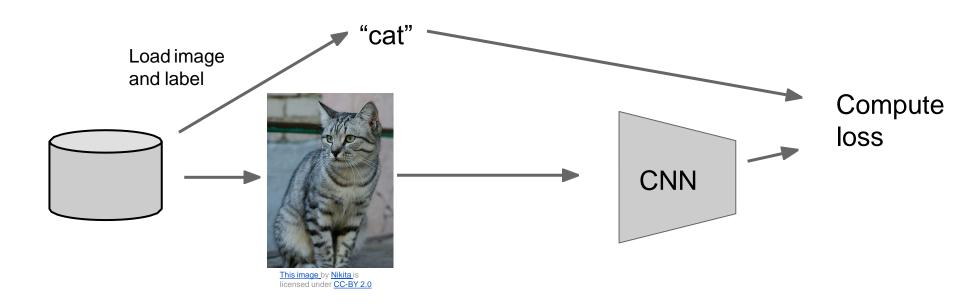
Example: Batch **Normalization**

Training: Normalize using stats from random minibatches

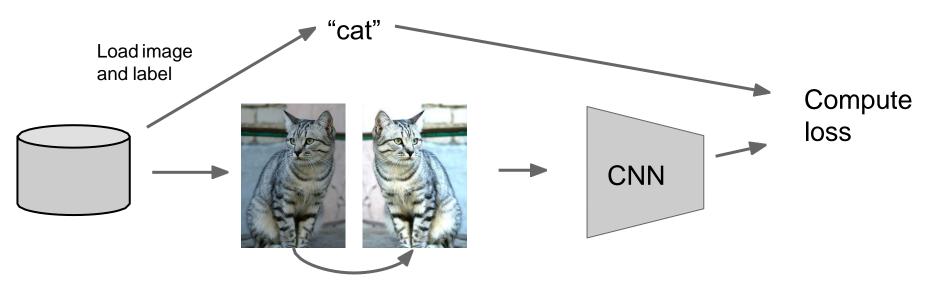
Testing: Use fixed stats to normalize

Training Neural Networks

Regularization: Data Augmentation



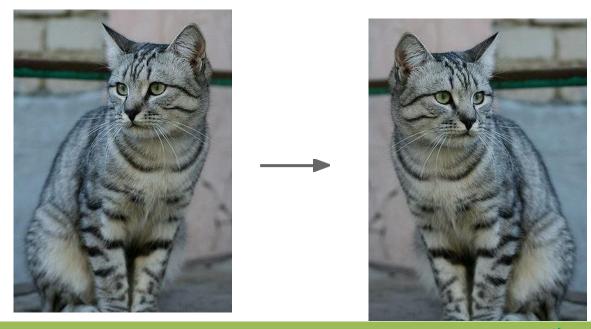
Regularization: Data Augmentation







Data Augmentation Horizontal Flips

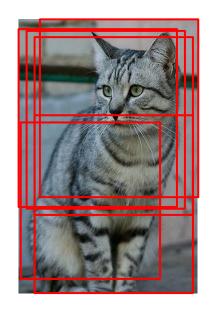




Data Augmentation Random crops and scales

Training: sample random crops / scales ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch

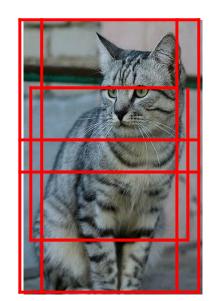


Data Augmentation Random crops and scales

Training: sample random crops / scales

ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



Testing: average a fixed set of crops

ResNet:

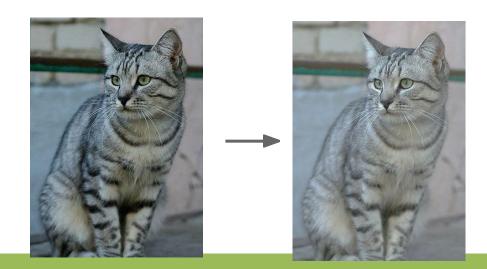
- 1. Resize image at 5 scales: {224, 256, 384, 480, 640}
- 2. For each size, use 10 224 x 224 crops: 4 corners + center, + flips

Training Neural Networks



Data Augmentation Color Jitter

Simple: Randomize contrast and brightness

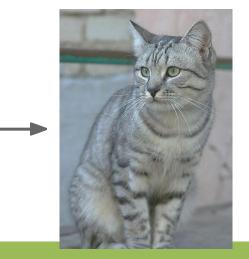




Data Augmentation Color Jitter

Simple: Randomize contrast and brightness





More Complex:

- 1. Apply PCA to all [R, G, B] pixels in training set
- 2. Sample a "color offset" along principal component directions
- 3. Add offset to all pixels of a training image

(As seen in [Krizhevsky et al. 2012], ResNet, etc)



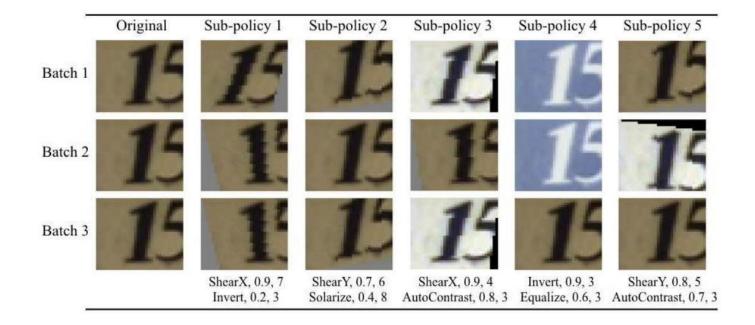
Data Augmentation Get creative for your problem!

Examples of data augmentations:

- translation
- rotation
- stretching
- shearing,
- lens distortions, ... (go crazy)



Automatic Data Augmentation



Cubuk et al., "AutoAugment: Learning Augmentation Strategies from Data", CVPR 2019





Regularization: A common pattern

Training: Add random noise

Testing: Marginalize over the noise

Examples:

Dropout

Batch Normalization

Data Augmentation



Regularization: DropConnect

Training: Drop connections between neurons (set weights to 0)

Testing: Use all the connections

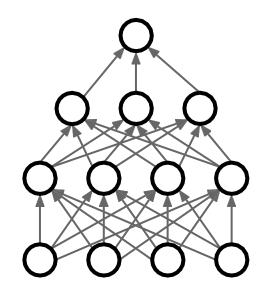
Examples:

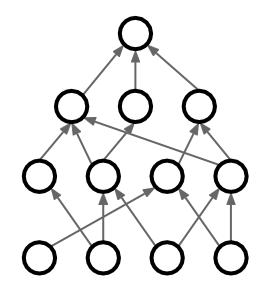
Dropout

Batch Normalization

Data Augmentation

DropConnect







Regularization: Fractional Pooling

Training: Use randomized pooling regions

Testing: Average predictions from several regions

Examples:

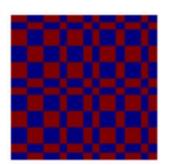
Dropout

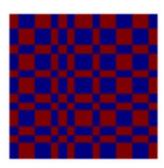
Batch Normalization

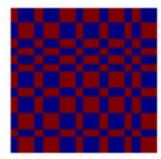
Data Augmentation

DropConnect

Fractional Max Pooling







Regularization: Stochastic Depth

Training: Skip some layers in the network

Testing: Use all the layer

Examples:

Dropout

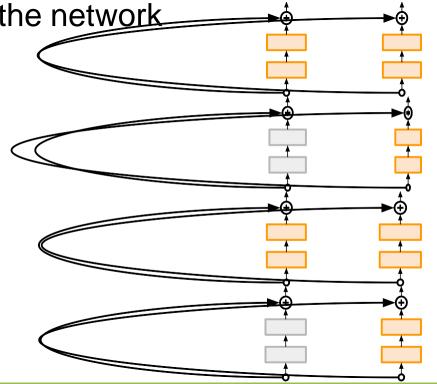
Batch Normalization

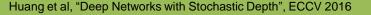
Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth





Regularization: Cutout

Training: Set random image regions to zero

Testing: Use full image

Examples:

Dropout

Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth

Cutout / Random Crop

DeVries and Taylor, "Improved Regularization of Convolutional Neural Networks with Cutout", arXiv 2017









Works very well for small datasets like CIFAR, less common for large datasets like ImageNet



Regularization: Mixup

Training: Train on random blends of images

Testing: Use original images

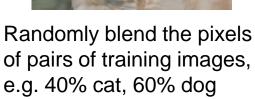


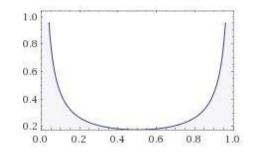
Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling
Stochastic Depth
Cutout / Random Crop
Mixup

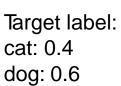


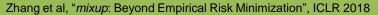
















CNN

Regularization - In practice

Training: Add random noise

Testing: Marginalize over the noise

Examples:

Dropout

Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth

Cutout / Random Crop

Mixup

- Consider dropout for large fully-connected layers
- Batch normalization and data augmentation almost always a good idea
- Try cutout and mixup especially for small classification datasets



(without tons of GPUs)



Step 1: Check initial loss

Turn off weight decay, sanity check loss at initialization e.g. log(C) for softmax with C classes



Step 1: Check initial loss

Step 2: Overfit a small sample

Try to train to 100% training accuracy on a small sample of training data (~5-10 minibatches); fiddle with architecture, learning rate, weight initialization

Loss not going down? LR too low, bad initialization Loss explodes to Inf or NaN? LR too high, bad initialization



Step 1: Check initial loss

Step 2: Overfit a small sample

Step 3: Find LR that makes loss go down

Use the architecture from the previous step, use all training data, turn on small weight decay, find a learning rate that makes the loss drop significantly within ~100 iterations

Good learning rates to try: 1e-1, 1e-2, 1e-3, 1e-4



Step 1: Check initial loss

Step 2: Overfit a small sample

Step 3: Find LR that makes loss go down

Step 4: Coarse grid, train for ~1-5 epochs

Choose a few values of learning rate and weight decay around what worked from Step 3, train a few models for ~1-5 epochs.

Good weight decay to try: 1e-4, 1e-5, 0



Step 1: Check initial loss

Step 2: Overfit a small sample

Step 3: Find LR that makes loss go down

Step 4: Coarse grid, train for ~1-5 epochs

Step 5: Refine grid, train longer

Pick best models from Step 4, train them for longer (~10-20 epochs) without learning rate decay



Step 1: Check initial loss

Step 2: Overfit a small sample

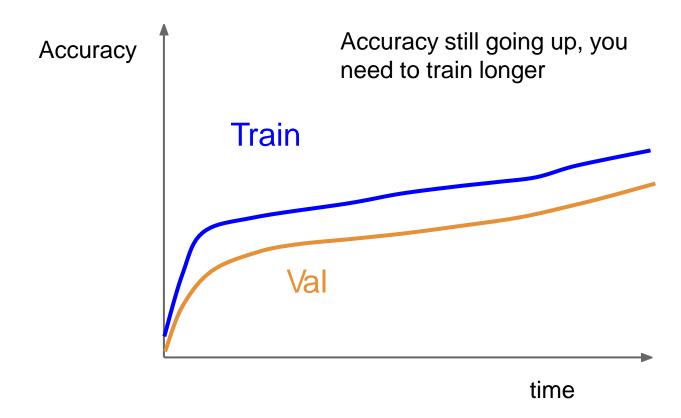
Step 3: Find LR that makes loss go down

Step 4: Coarse grid, train for ~1-5 epochs

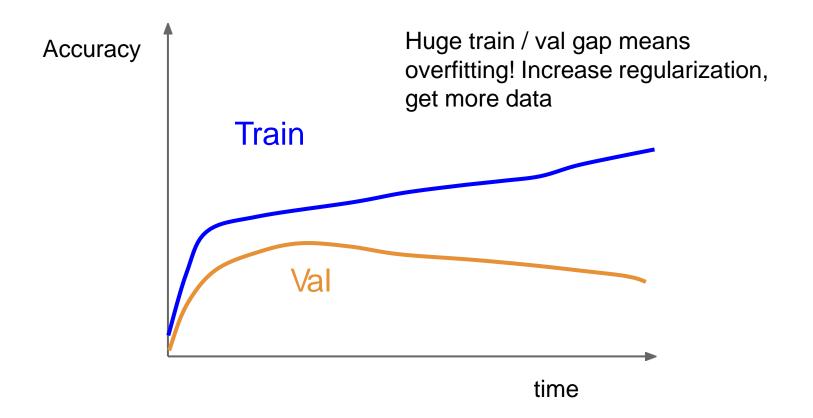
Step 5: Refine grid, train longer

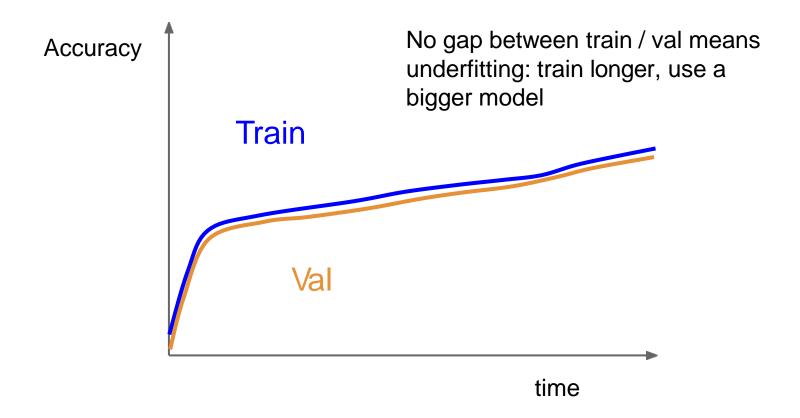
Step 6: Look at loss and accuracy curves



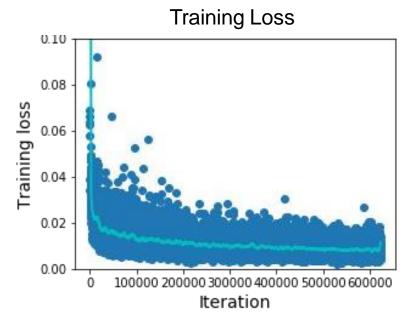








Look at learning curves!



96 -94 -92 -90 -88 0 100000 200000 300000 400000 500000 600000

Iteration

Train / Val Accuracy

train

Losses may be noisy, use a scatter plot and also plot moving average to see trends better

Training Neural Networks



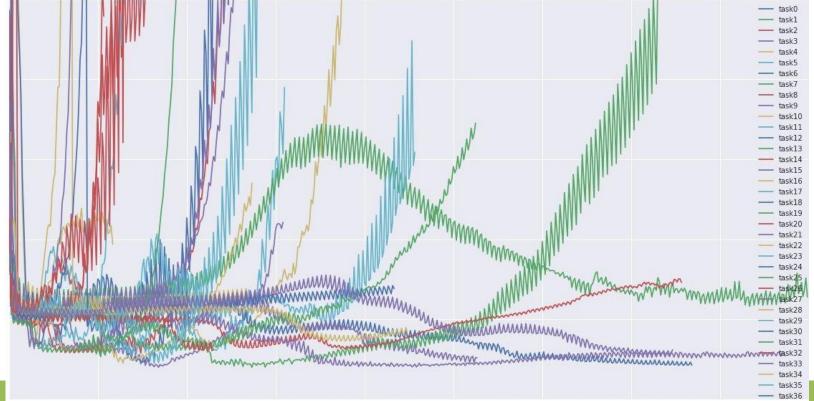
Cross-validation

We develop "command centers" to visualize all our models training with different hyperparameters

check out weights and biases



You can plot all your loss curves for different hyperparameters on a single plot



Don't look at accuracy or loss curves for too long!

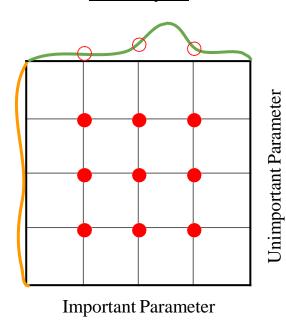


- Step 1: Check initial loss
- Step 2: Overfit a small sample
- Step 3: Find LR that makes loss go down
- Step 4: Coarse grid, train for ~1-5 epochs
- **Step 5**: Refine grid, train longer
- Step 6: Look at loss and accuracy curves
- Step 7: GOTO step 5

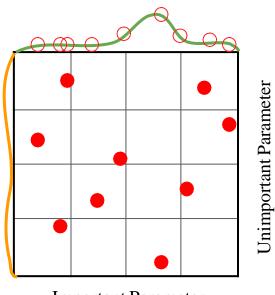
Random Search vs. Grid Search

Random Search for Hyper-Parameter Optimization Bergstra and Bengio, 2012





Random Lavout



Important Parameter

Illustration of Bergstra et al., 2012 by Shayne Longpre, copyright CS231n 2017

Summary

- Improve your training error:
 - Optimizers
 - Learning rate schedules
- Improve your test error:
 - Regularization
 - Choosing Hyperparameters

Summary

TLDRs

We looked in detail at:

- Activation Functions (use ReLU)
- Data Preprocessing (images: subtract mean)
- Weight Initialization (use Xavier/He init)
- Batch Normalization (use this!)
- Transfer learning (use this if you can!)

Next time: Visualizing and Understanding