

Lecture 9:

Attention and Transformers

Dr. José Ramón Iglesias

DSP-ASIC BUILDER GROUP

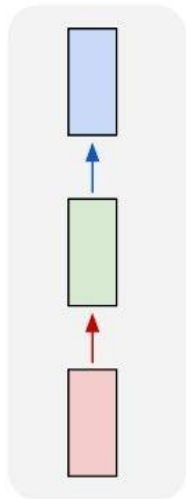
Director Semillero TRIAC

Ingeniería Electronica

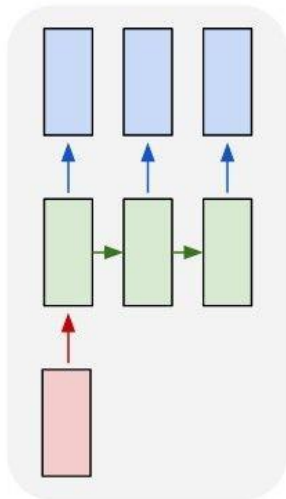
Universidad Popular del Cesar

Last Time: Recurrent Neural Networks

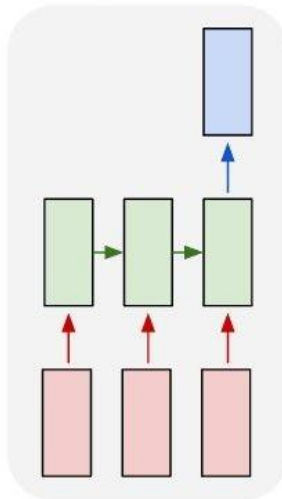
one to one



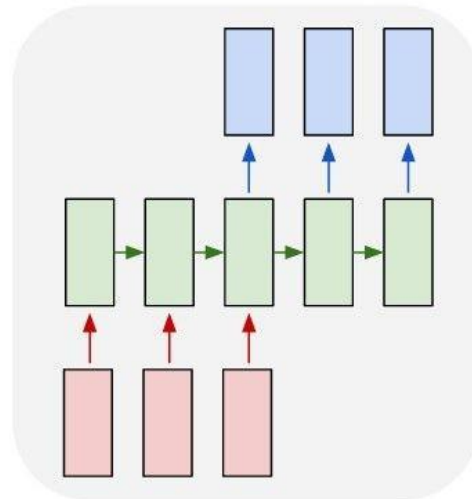
one to many



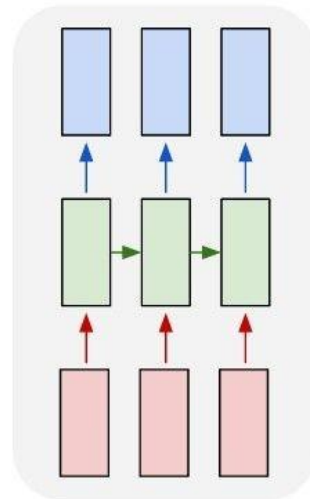
many to one



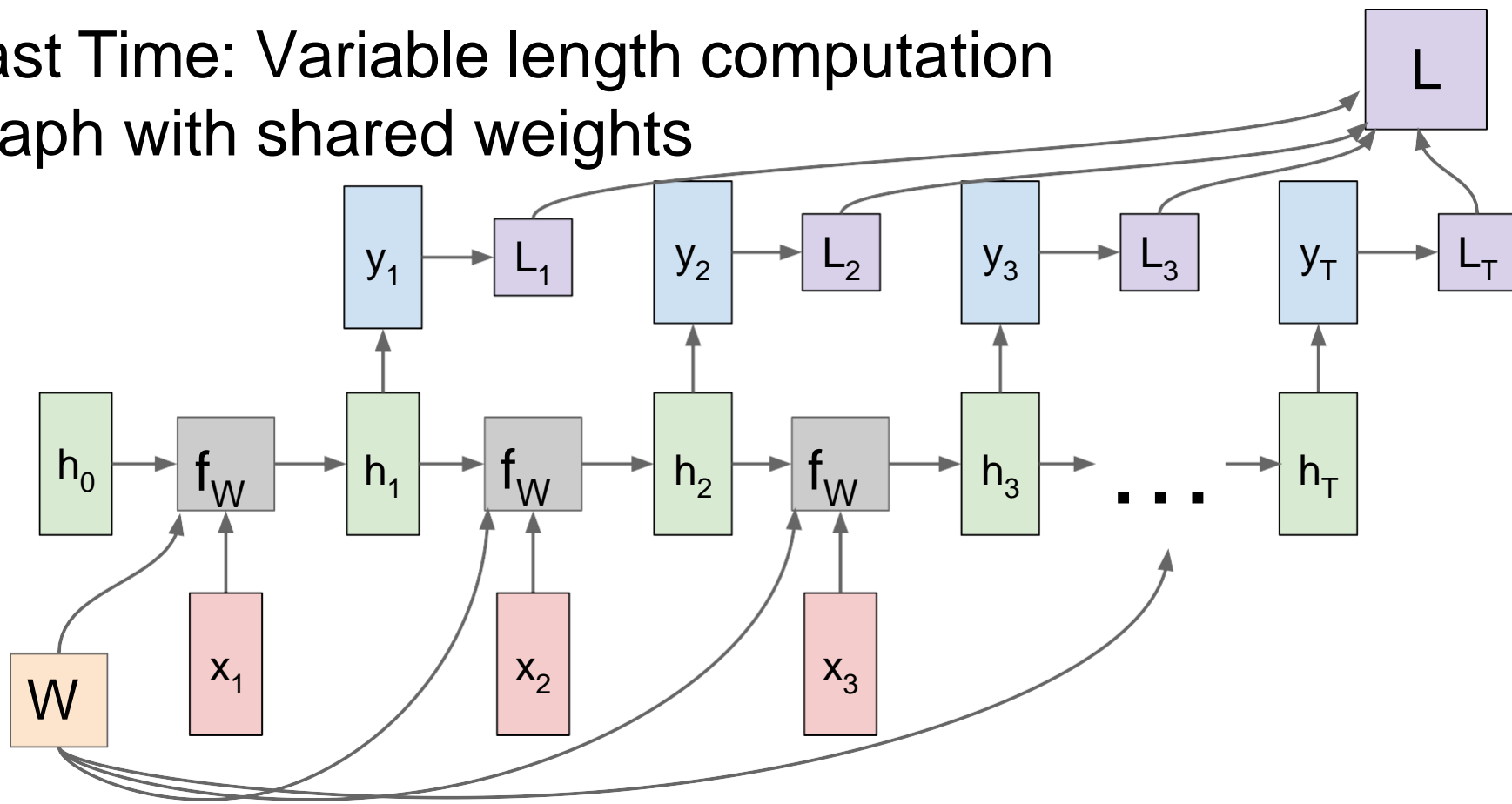
many to many



many to many



Last Time: Variable length computation graph with shared weights

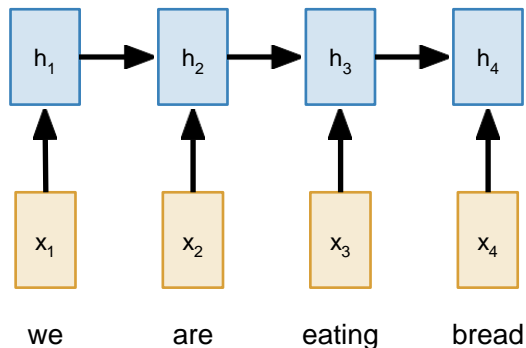


Sequence to Sequence with RNNs

Input: Sequence x_1, \dots, x_T

Output: Sequence y_1, \dots, y_T

Encoder: $h_t = f_W(x_t, h_{t-1})$



Sequence to Sequence with RNNs

Input: Sequence x_1, \dots, x_T

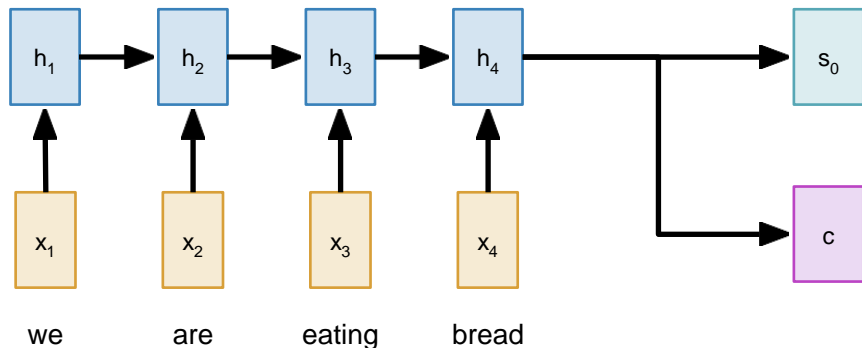
Output: Sequence y_1, \dots, y_T

From final hidden state predict:

Encoder: $h_t = f_W(x_t, h_{t-1})$

Initial decoder state s_0

Context vector c (often $c=h_T$)



Sequence to Sequence with RNNs

Input: Sequence x_1, \dots, x_T

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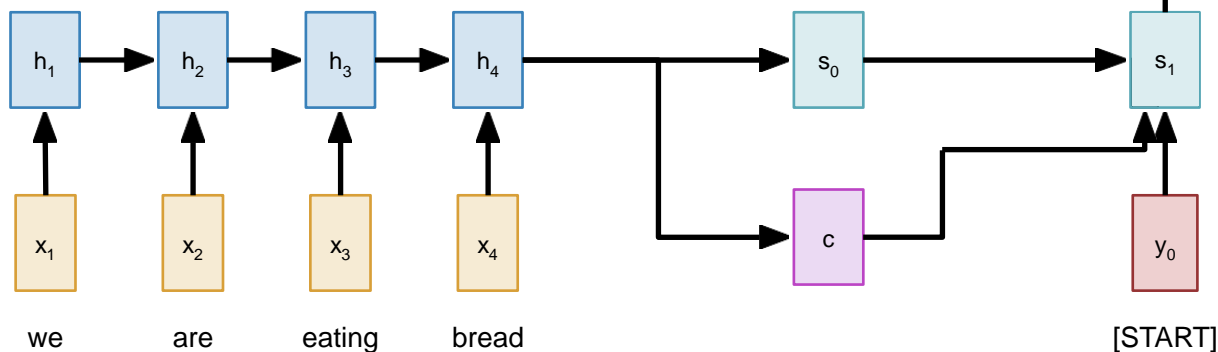
Decoder: $s_t = g_U(y_{t-1}, s_{t-1}, c)$

Encoder: $h_t = f_W(x_t, h_{t-1})$

From final hidden state predict:

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Context vector c (often $c=h_T$)



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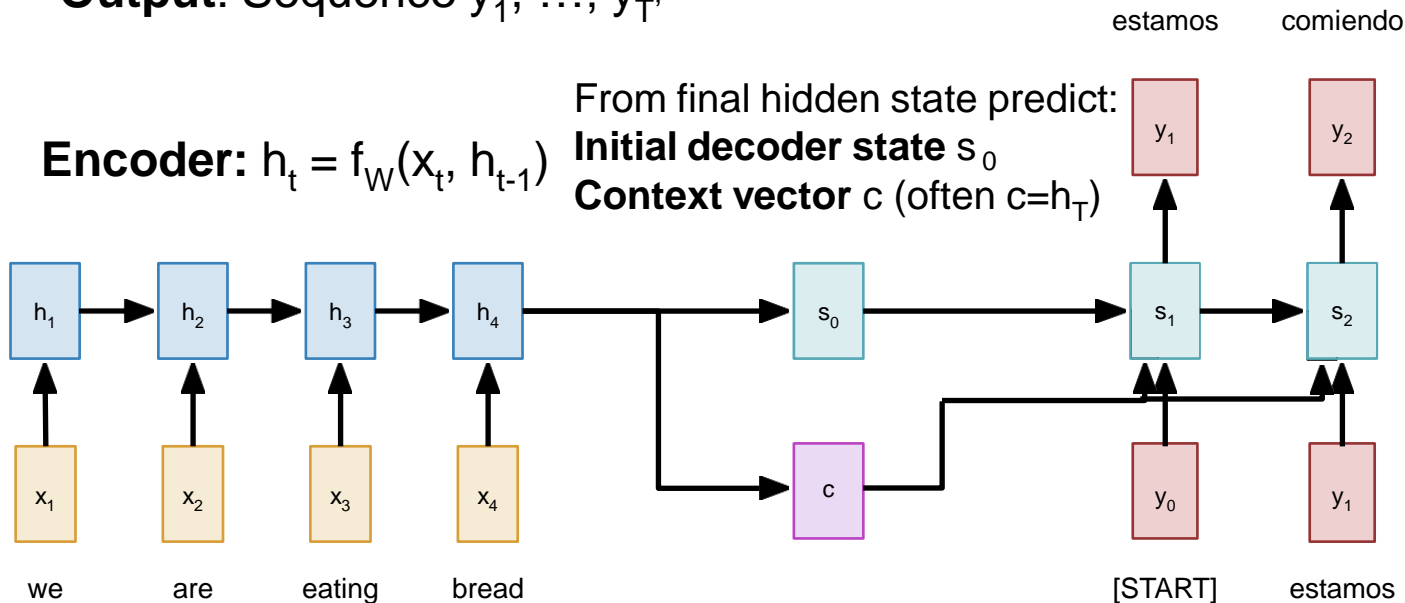
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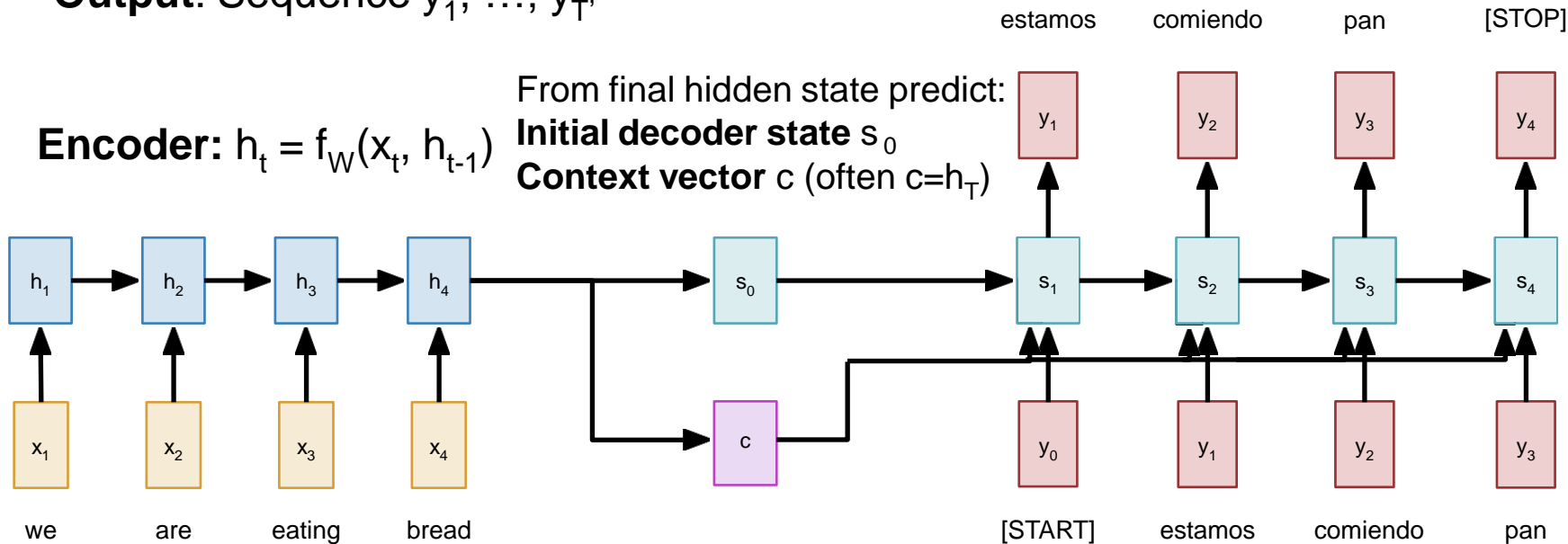
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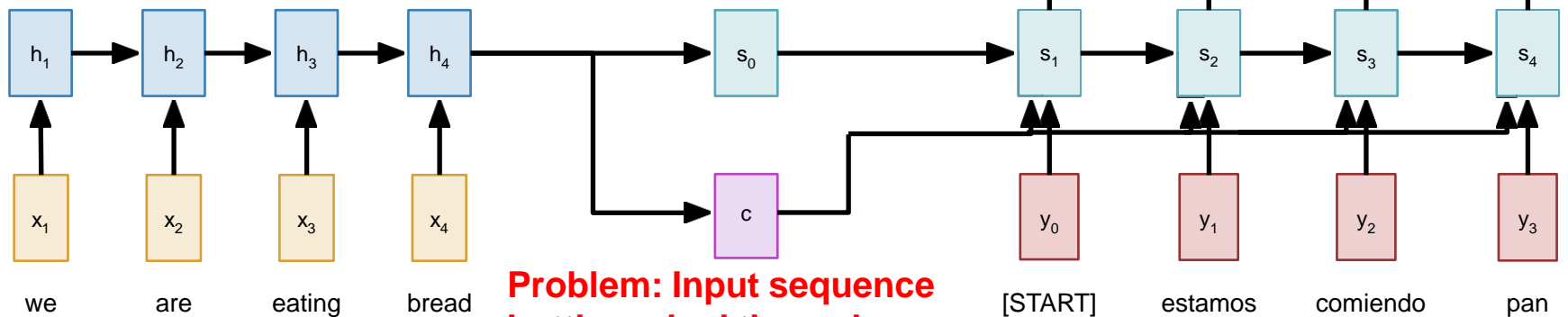
Decoder: $s_t = g_U(y_{t-1}, s_{t-1}, c)$

Encoder: $h_t = f_W(x_t, h_{t-1})$

From final hidden state predict:

Initial decoder state s_0

Context vector c (often $c=h_T$)



Problem: Input sequence bottlenecked through fixed-sized vector. What if

$T=1000?$

Attention and Transformers

Sequence to Sequence with RNNs

Input: Sequence x_1, \dots, x_T

Output: Sequence y_1, \dots, y_T

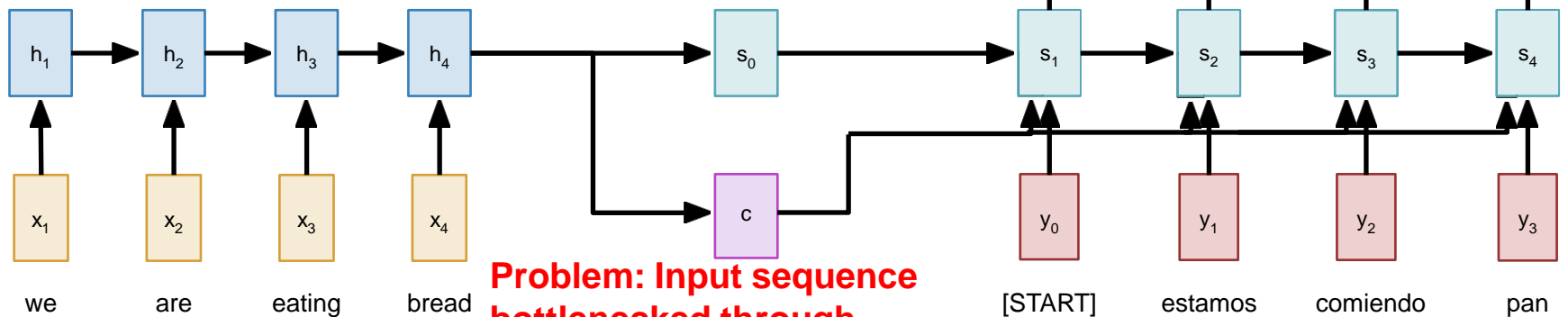
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From final hidden state predict:

Initial decoder state s_0

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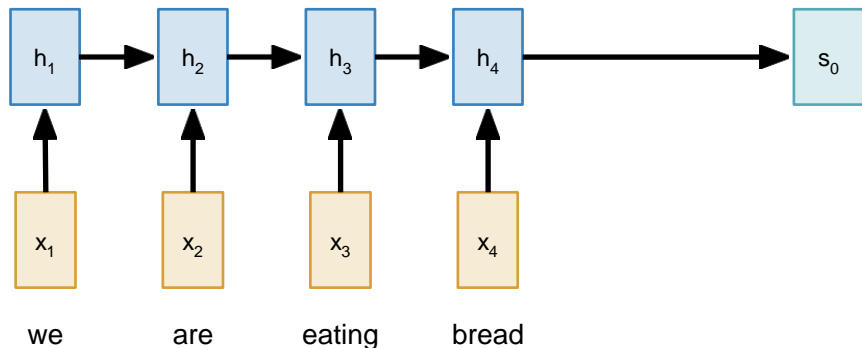
Idea: use new context vector at each step of decoder!

Sequence to Sequence with RNNs and Attention

Input: Sequence x_1, \dots, x_T

Output: Sequence y_1, \dots, y_T

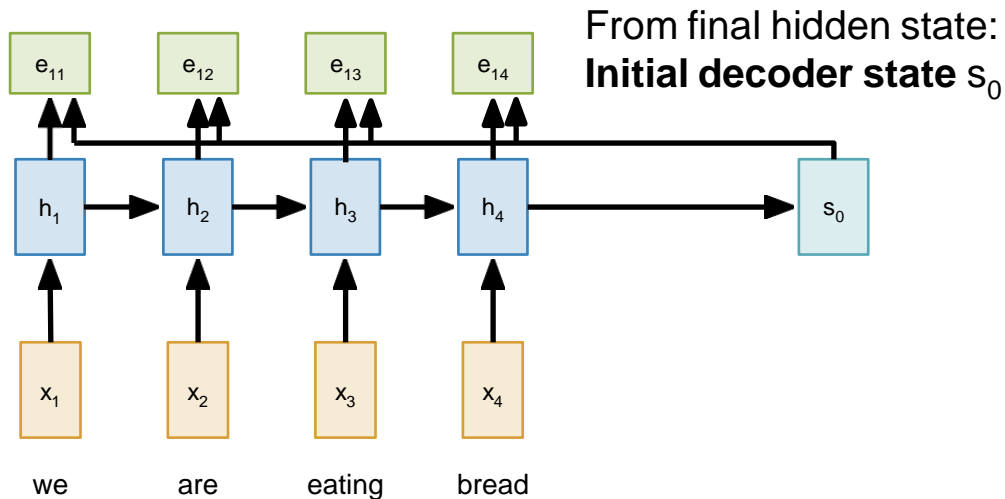
Encoder: $h_t = f_W(x_t, h_{t-1})$ From final hidden state:
Initial decoder state s_0



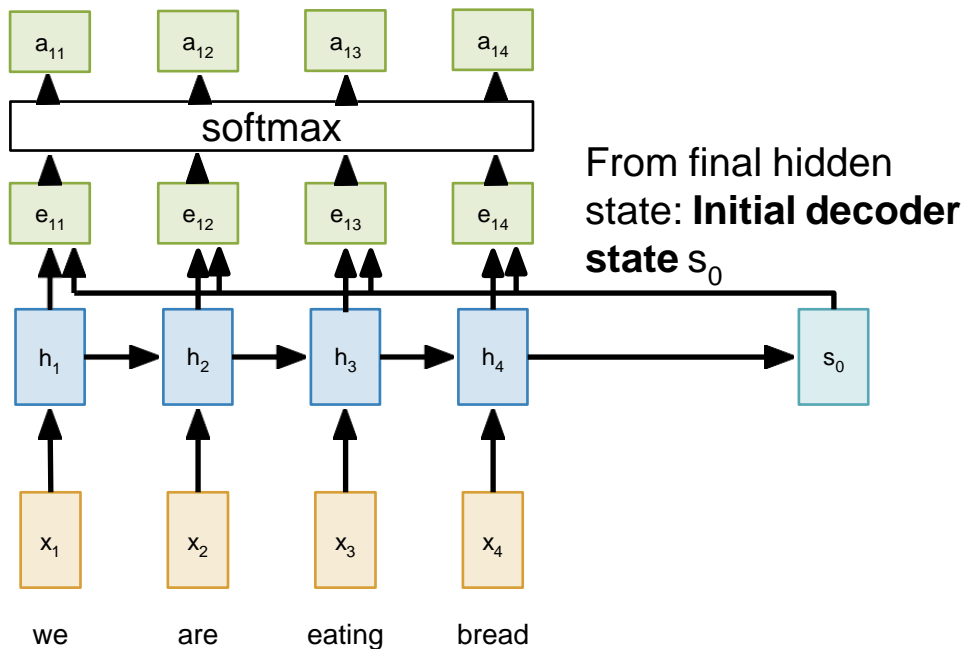
Sequence to Sequence with RNNs and **Attention**

Compute (scalar) **alignment scores**

$$e_{t,i} = f_{\text{att}}(s_{t-1}, h_i) \quad (f_{\text{att}} \text{ is an MLP})$$



Sequence to Sequence with RNNs and Attention



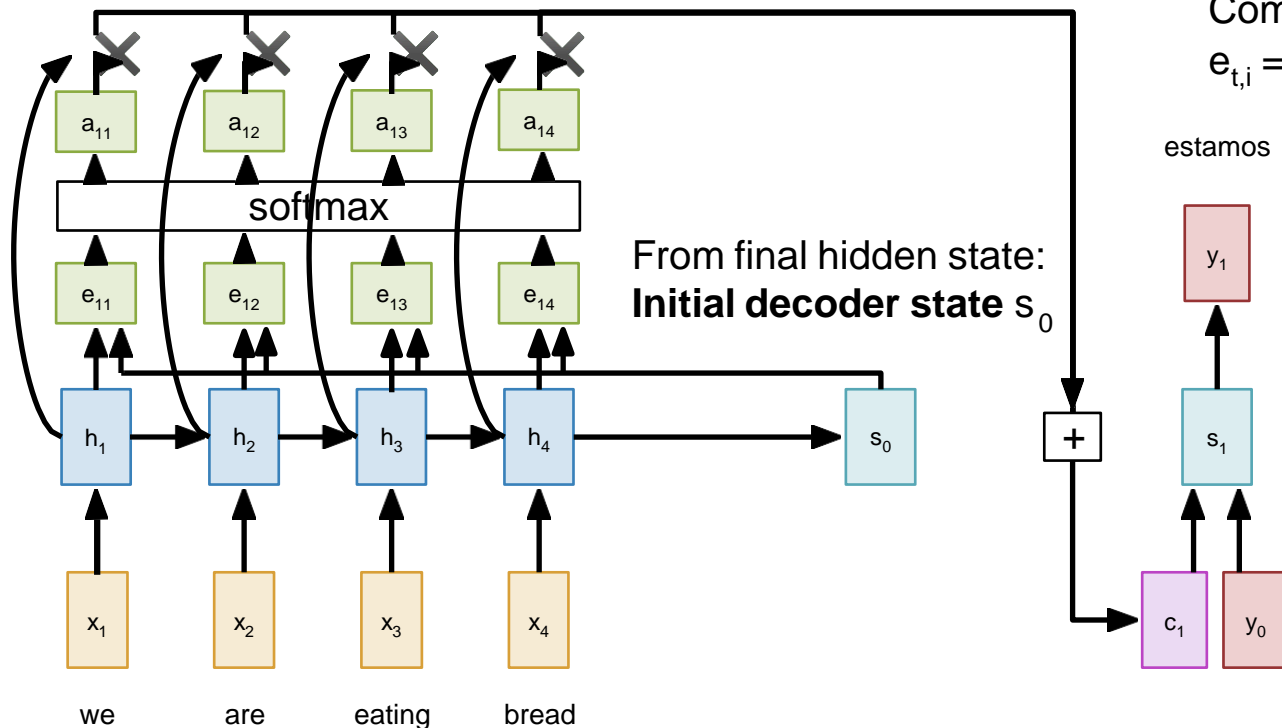
Compute (scalar) **alignment scores**

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Normalize alignment scores
to get **attention weights**

$$0 < a_{t,i} < 1 \quad \sum_i a_{t,i} = 1$$

Sequence to Sequence with RNNs and Attention



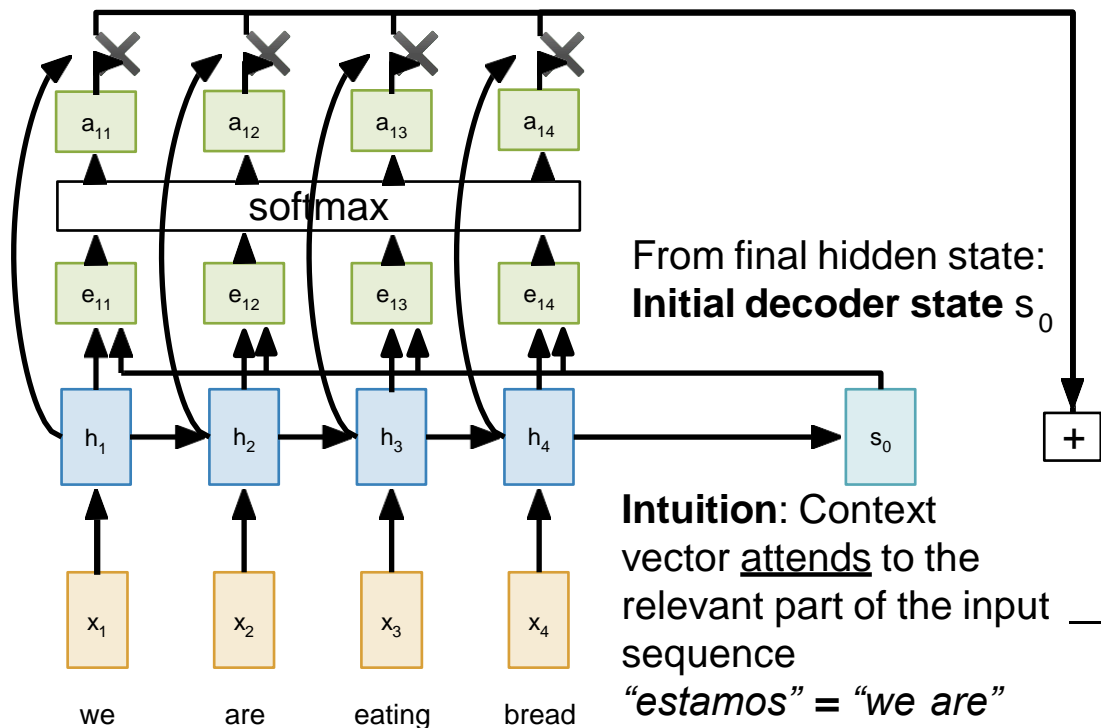
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 $e_{t,i} = f_{\text{att}}(s_{t-1}, h_i)$ (f_{att} is an MLP)

Normalize alignment scores to get **attention weights**
 $0 < a_{t,i} < 1 \quad \sum_i a_{t,i} = 1$

Compute context vector as linear combination of hidden states
 $c_t = \sum_i a_{t,i} h_i$

[START]

Sequence to Sequence with RNNs and Attention



From final hidden state:
Initial decoder state s_0

Intuition: Context vector attends to the relevant part of the input sequence

"estamos" = "we are"
so maybe $a_{11}=a_{12}=0.45$,

$a_{13}=a_{14}=0.05$

Compute (scalar) **alignment scores**
 $e_{t,i} = f_{\text{att}}(s_{t-1}, h_i)$ (f_{att} is an MLP)

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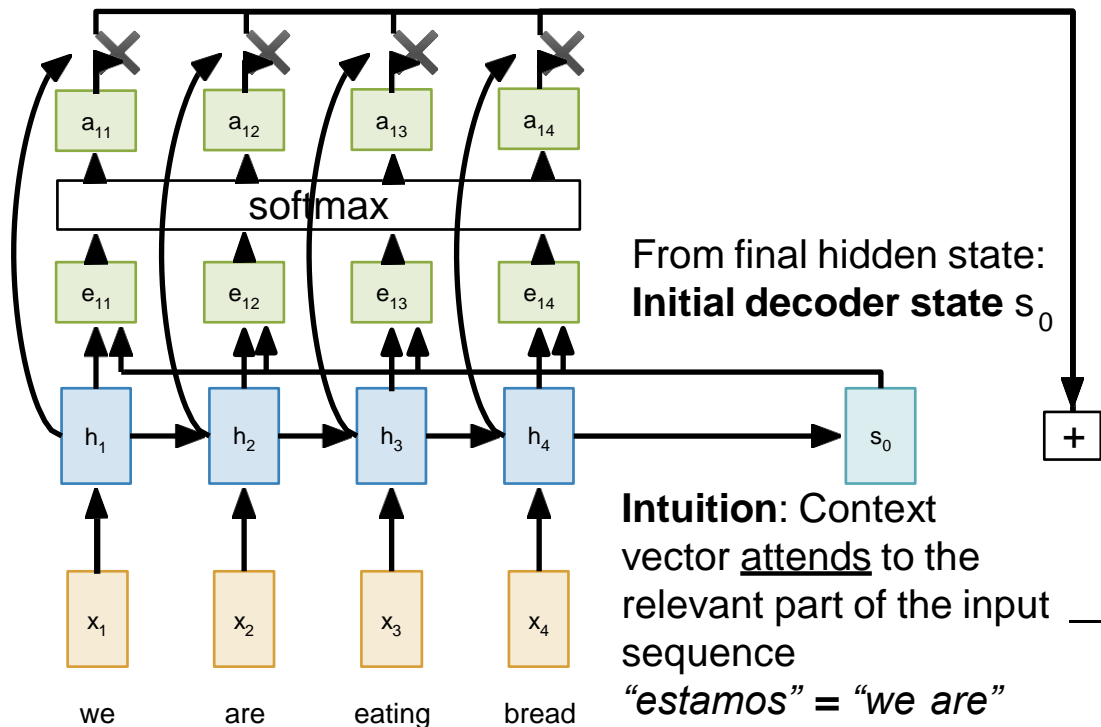
Compute context vector as linear combination of hidden states

$$c_t = \sum_i a_{t,i} h_i$$

Use context vector in decoder: $s_t = g_U(y_{t-1}, s_{t-1}, c_t)$

[START]

Sequence to Sequence with RNNs and Attention



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Initial decoder state s_0

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Compute context vector as linear combination of hidden states

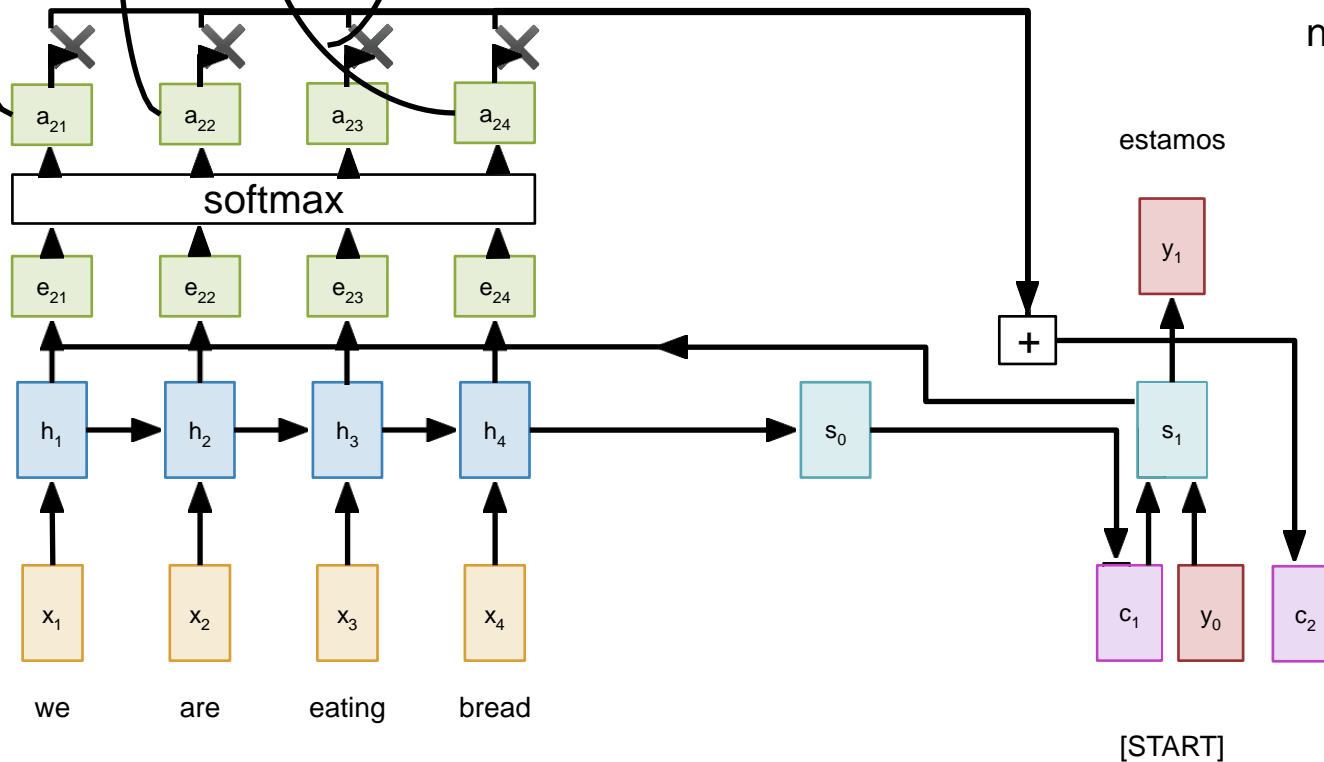
$$c_t = \sum_i a_{t,i} h_i$$

Use context vector in decoder: $s_t = g_U(y_{t-1}, s_{t-1}, c_t)$

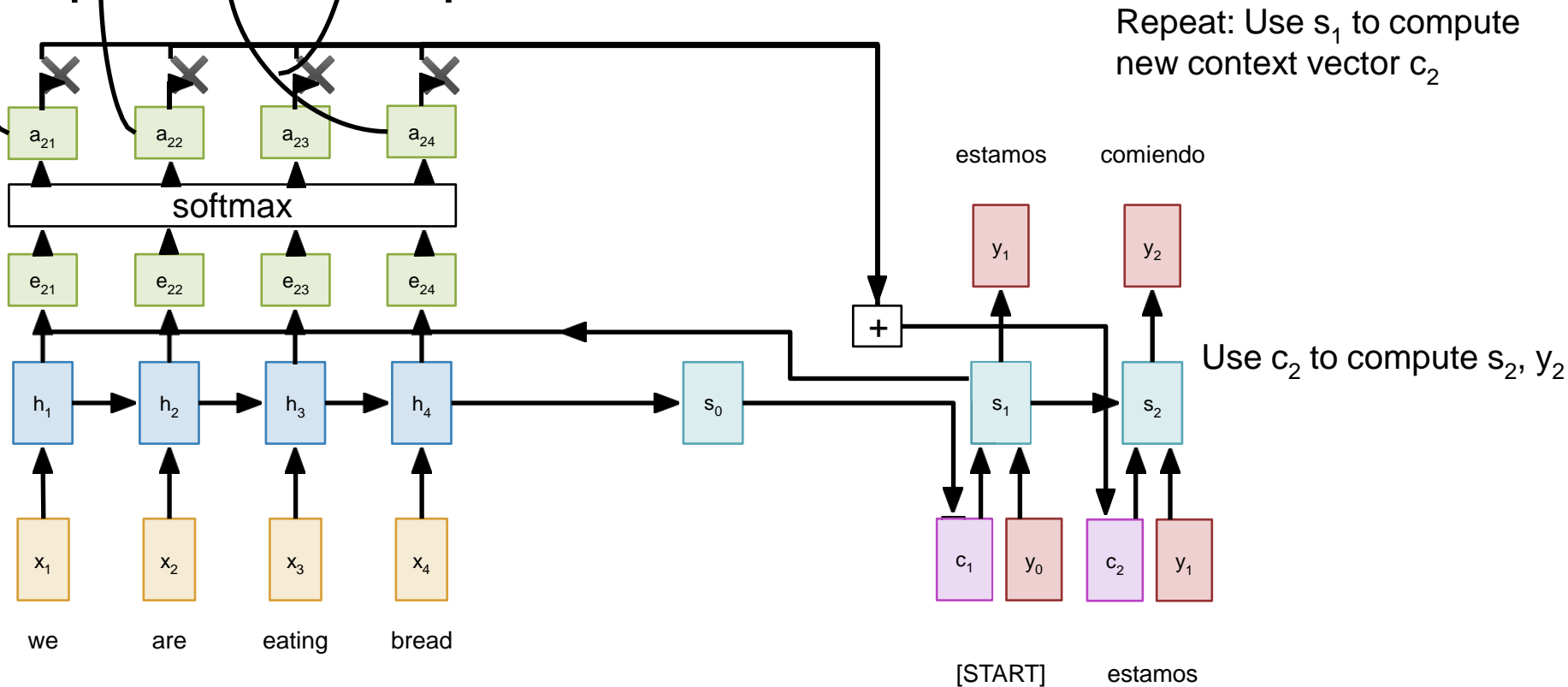
This is all differentiable! No supervision on attention weights – backprop through everything

Sequence to Sequence with RNNs and Attention

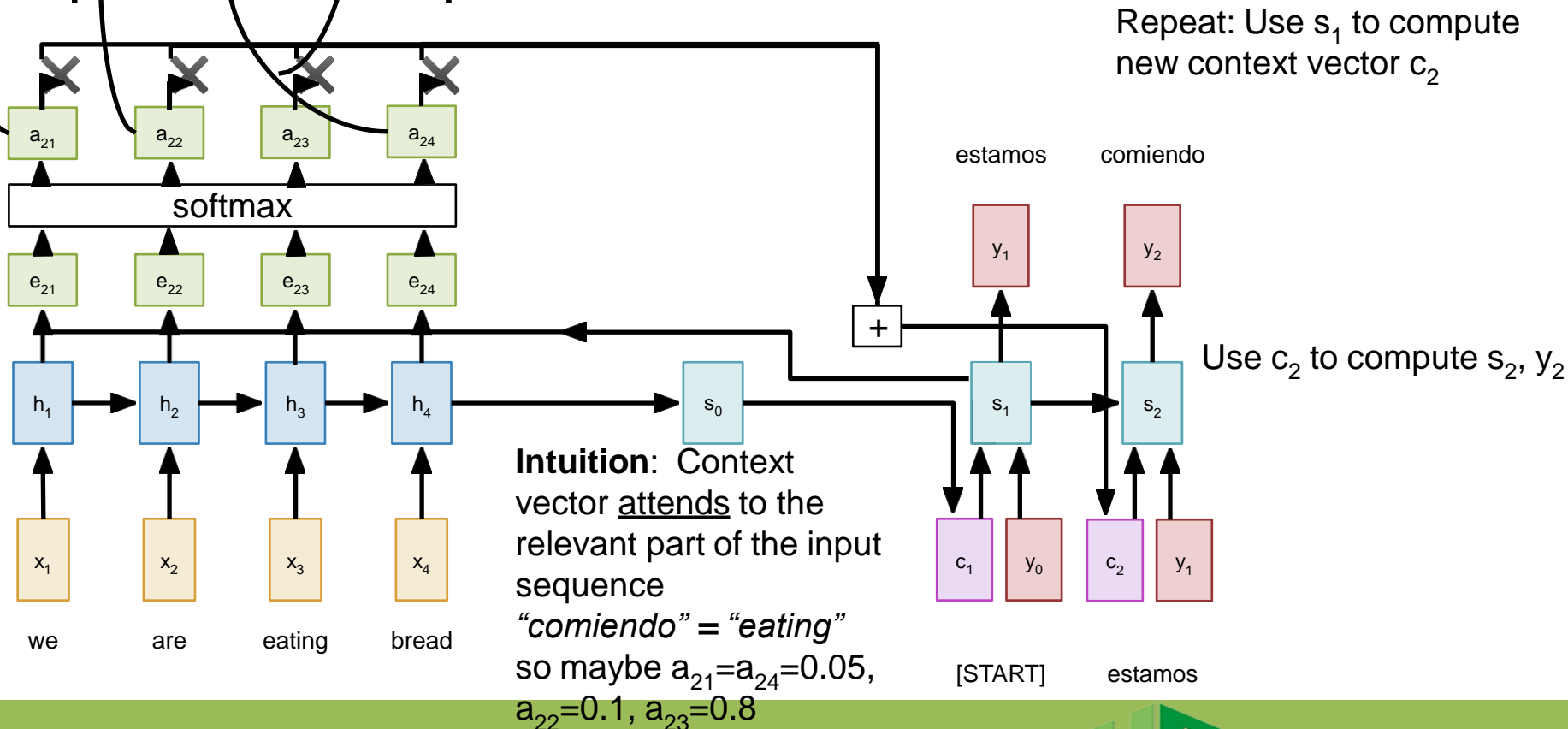
Repeat: Use s_1 to compute new context vector c_2



Sequence to Sequence with RNNs and Attention



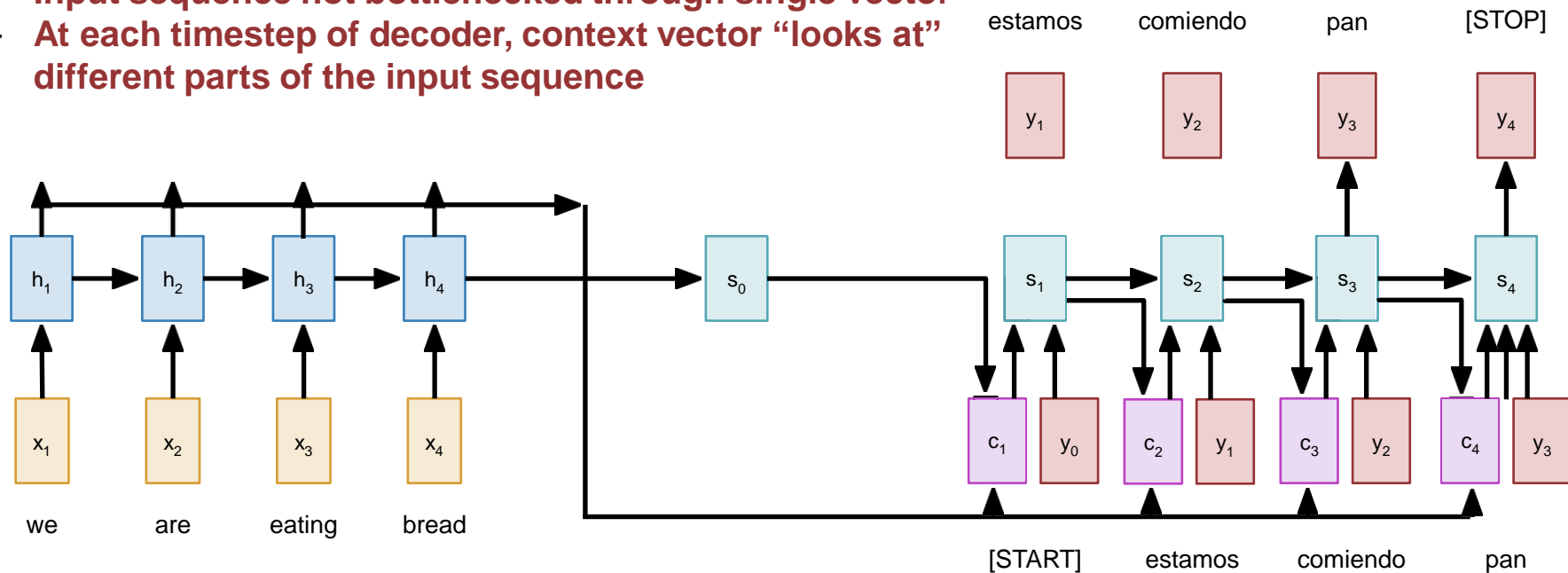
Sequence to Sequence with RNNs and Attention



Sequence to Sequence with RNNs and Attention

Use a different context vector in each timestep of decoder

- Input sequence not bottlenecked through single vector
- At each timestep of decoder, context vector “looks at” different parts of the input sequence



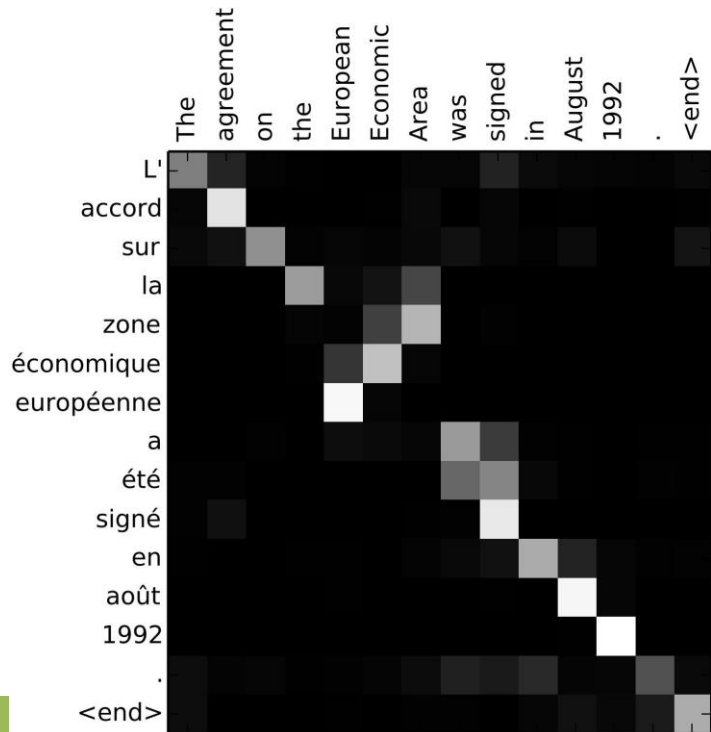
Sequence to Sequence with RNNs and Attention

Example: English to French translation

Input: “The agreement on the European Economic Area was signed in August 1992.”

Output: “L'accord sur la zone économique européenne a été signé en août 1992.”

Visualize attention weights $a_{t,i}$



Sequence to Sequence with RNNs and Attention

Example: English to French translation

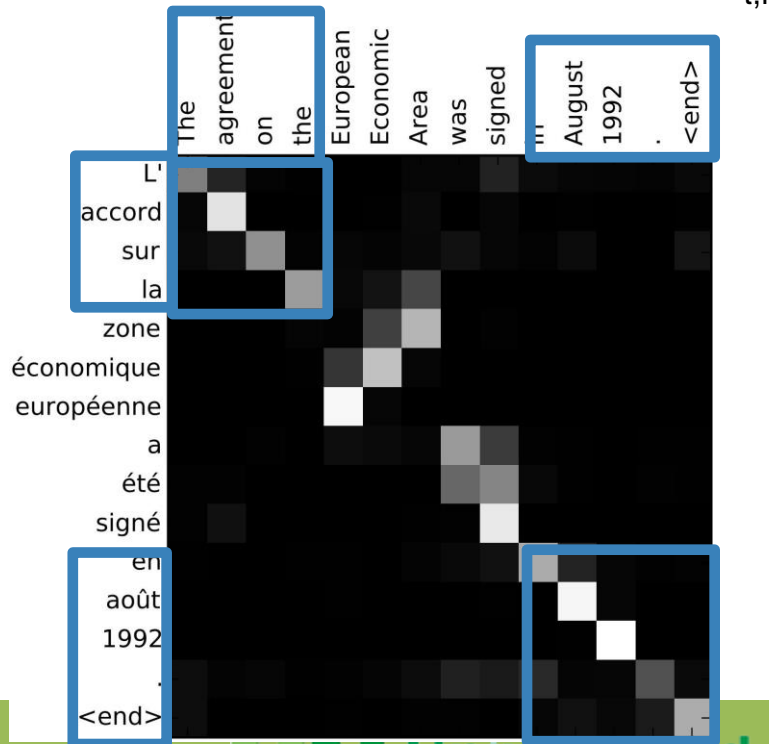
Input: “**The agreement on the** European Economic Area was signed **in August 1992.**”

Output: “**L'accord sur la** zone économique européenne a été signé **en août 1992.**”

Diagonal attention means words correspond in order

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Sequence to Sequence with RNNs and Attention

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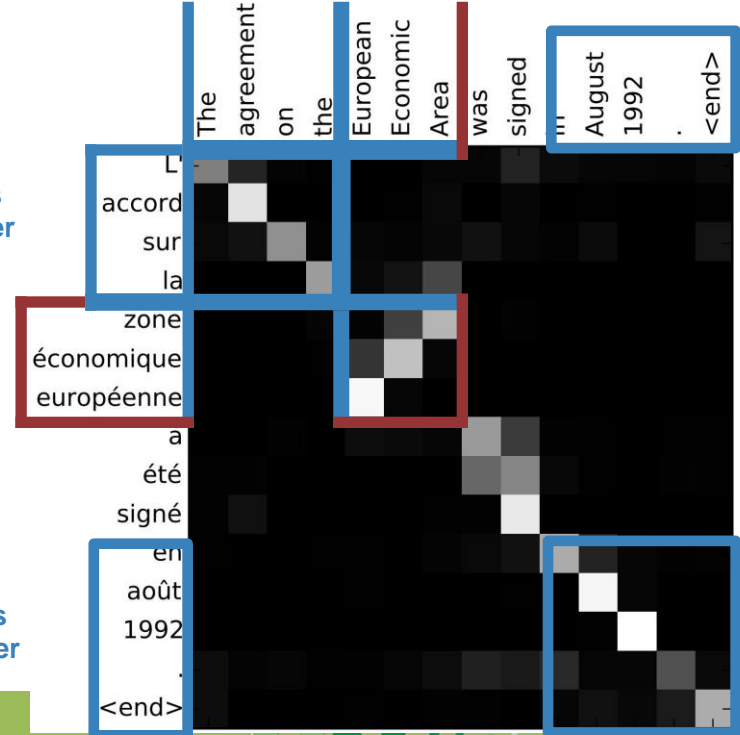
Output: “L'accord sur la zone économique européenne a été signé en août 1992.”

Diagonal attention means words correspond in order

Attention figures out different word orders

Diagonal attention means words correspond in order

Visualize attention weights $a_{t,i}$



Sequence to Sequence with RNNs and Attention

The decoder doesn't use the fact that h_i form an ordered sequence – it just treats them as an unordered set $\{h_i\}$

Can use similar architecture given any set of input hidden vectors $\{h_i\}$!

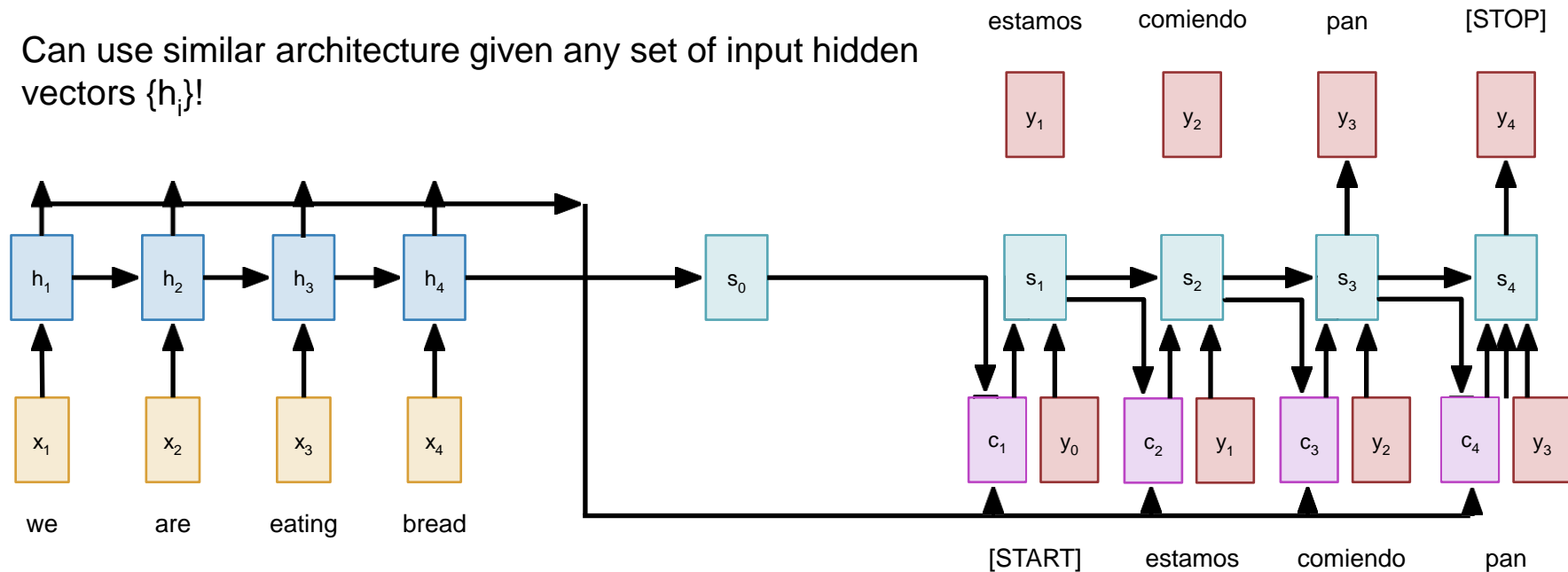
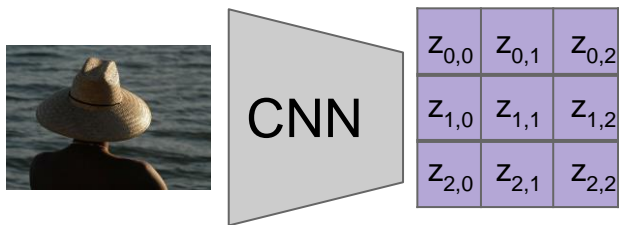


Image Captioning using spatial features

Input: Image I

Output: Sequence $\mathbf{y} = y_1, y_2, \dots, y_T$



Extract spatial features from a pretrained CNN

Features:
 $H \times W \times D$

Image Captioning using spatial features

Input: Image I

Output: Sequence $\mathbf{y} = y_1, y_2, \dots, y_T$

Encoder: $h_0 = f_w(\mathbf{z})$

where \mathbf{z} is spatial CNN features

$f_w(\cdot)$ is an MLP

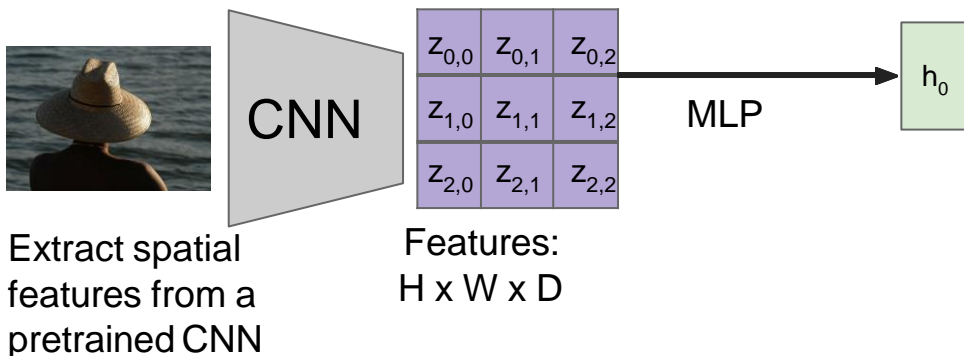


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Decoder: $y_t = g_v(y_{t-1}, h_{t-1}, c)$

where context vector c is often $c = h_0$

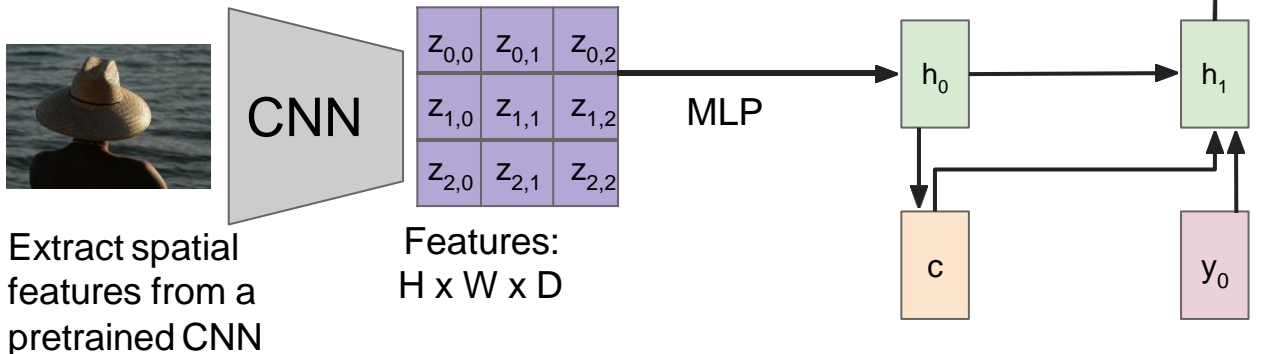


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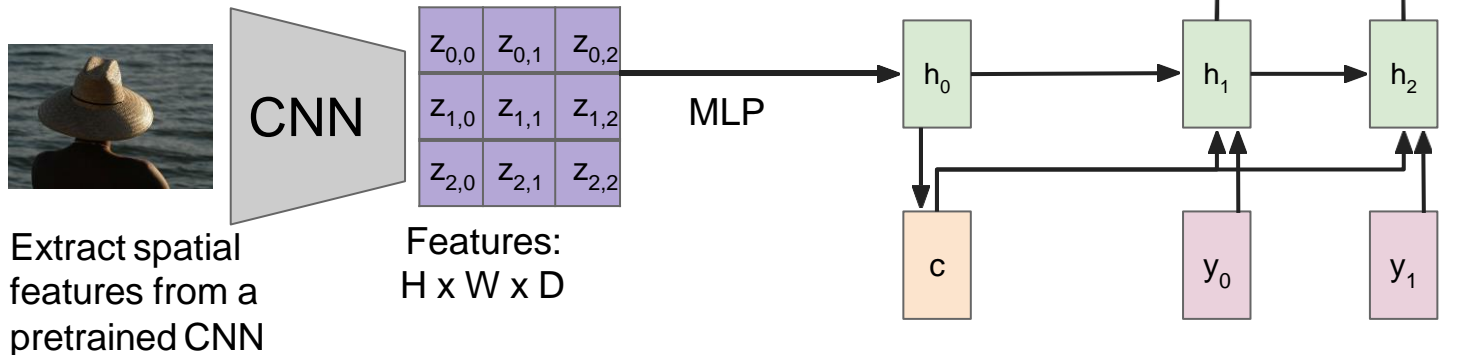


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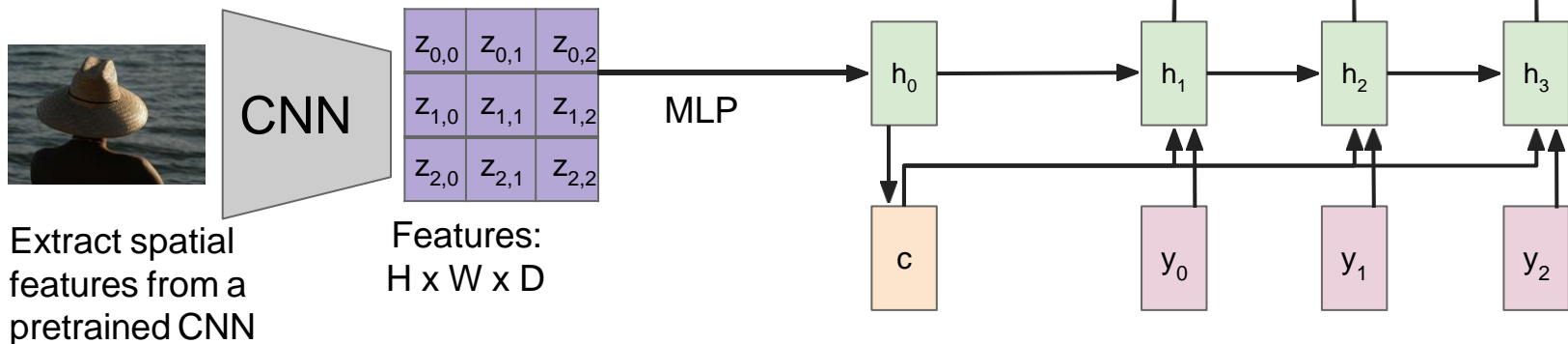


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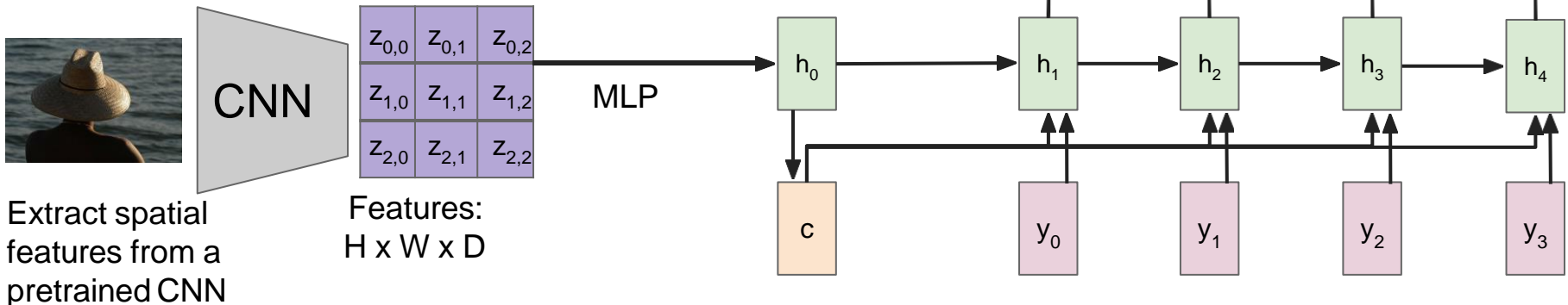


Image Captioning using spatial features

Problem: Input is "bottlenecked" through c

- Model needs to encode everything it wants to say within c

This is a problem if we want to generate really long descriptions? 100s of words long

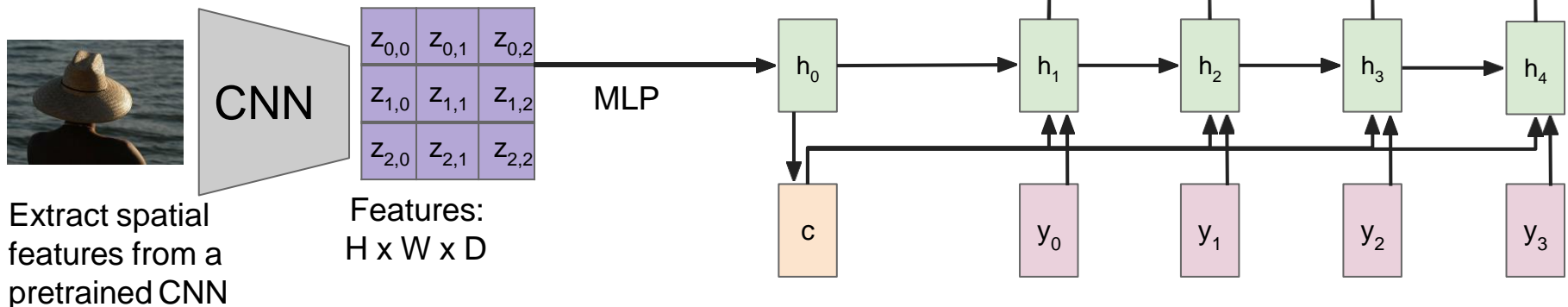
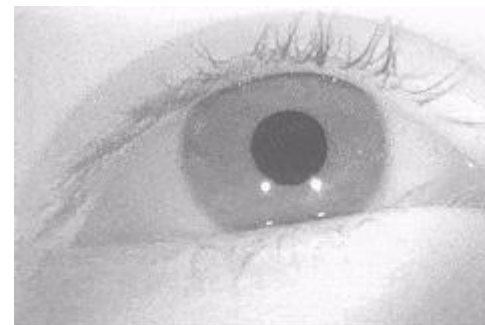


Image Captioning with RNNs and Attention

Attention idea: New context vector at every time step.

Each context vector will attend to different image regions

[gif source](#)



Attention Saccades in humans

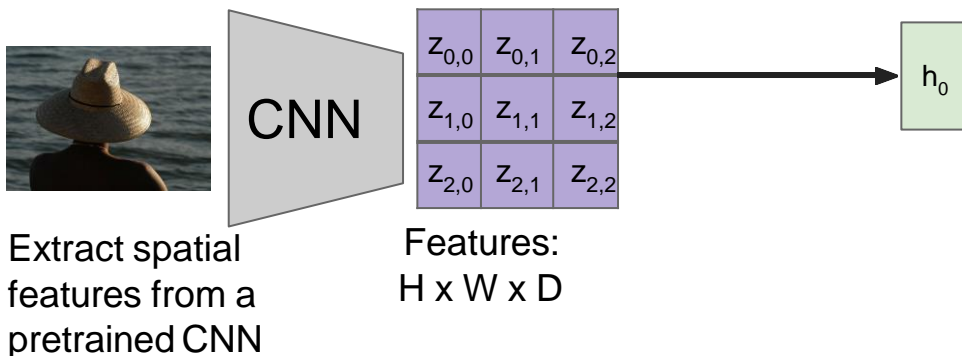


Image Captioning with RNNs and Attention

Compute alignments
scores (scalars):

$$e_{t,i,j} = f_{att}(h_{t-1}, z_{i,j})$$

$f_{att}(\cdot)$ is an MLP

Alignment scores:

H x W

$e_{1,0,0}$	$e_{1,0,1}$	$e_{1,0,2}$
$e_{1,1,0}$	$e_{1,1,1}$	$e_{1,1,2}$
$e_{1,2,0}$	$e_{1,2,1}$	$e_{1,2,2}$



CNN

Extract spatial
features from a
pretrained CNN

$z_{0,0}$	$z_{0,1}$	$z_{0,2}$
$z_{1,0}$	$z_{1,1}$	$z_{1,2}$
$z_{2,0}$	$z_{2,1}$	$z_{2,2}$

Features:

H x W x D

h_0

Image Captioning with RNNs and Attention

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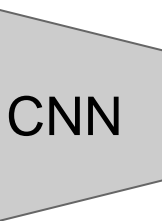
Attention:
H x W

$a_{1,0,0}$	$a_{1,0,1}$	$a_{1,0,2}$
$a_{1,1,0}$	$a_{1,1,1}$	$a_{1,1,2}$
$a_{1,2,0}$	$a_{1,2,1}$	$a_{1,2,2}$

Normalize to get attention weights:

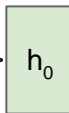
$$a_{t,:,:) = \text{softmax}(e_{t,:,:})$$

$0 < a_{t,i,j} < 1$,
attention values sum to 1



$z_{0,0}$	$z_{0,1}$	$z_{0,2}$
$z_{1,0}$	$z_{1,1}$	$z_{1,2}$
$z_{2,0}$	$z_{2,1}$	$z_{2,2}$

Features:
H x W x D



Extract spatial features from a pretrained CNN

Image Captioning with RNNs and Attention

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Alignment scores:
H x W

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Attention:
H x W

$a_{1,0,0}$	$a_{1,0,1}$	$a_{1,0,2}$
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Normalize to get attention weights:

$$a_{t,:,:) = \text{softmax}(e_{t,:,:)}$$

$0 < a_{t,i,j} < 1$,
attention values sum to 1

Compute context vector:

$$c_t = \sum_{i,j} a_{t,i,j} z_{t,i,j}$$



CNN

Extract spatial features from a pretrained CNN

$z_{0,0}$	$z_{0,1}$	$z_{0,2}$
$z_{1,0}$	$z_{1,1}$	$z_{1,2}$
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Features:
H x W x D

h_0



c_1

Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

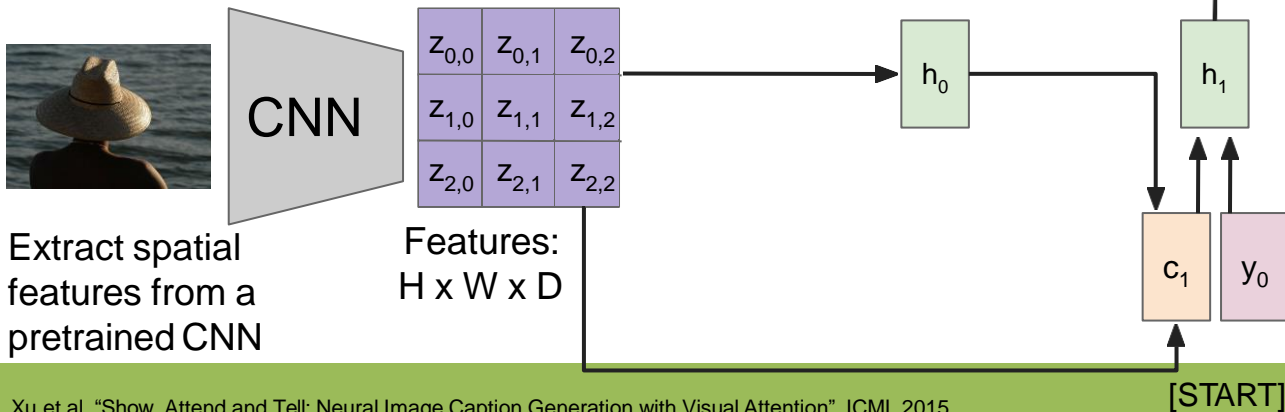
Attention and Transformers

Image Captioning with RNNs and Attention

Each timestep of decoder uses a different context vector that looks at different parts of the input image

$$e_{t,i,j} = f_{att}(h_{t-1}, z_{i,j})$$
$$a_{t,:,:} = \text{softmax}(e_{t,:,:})$$
$$c_t = \sum_{i,j} a_{t,i,j} z_{i,j}$$

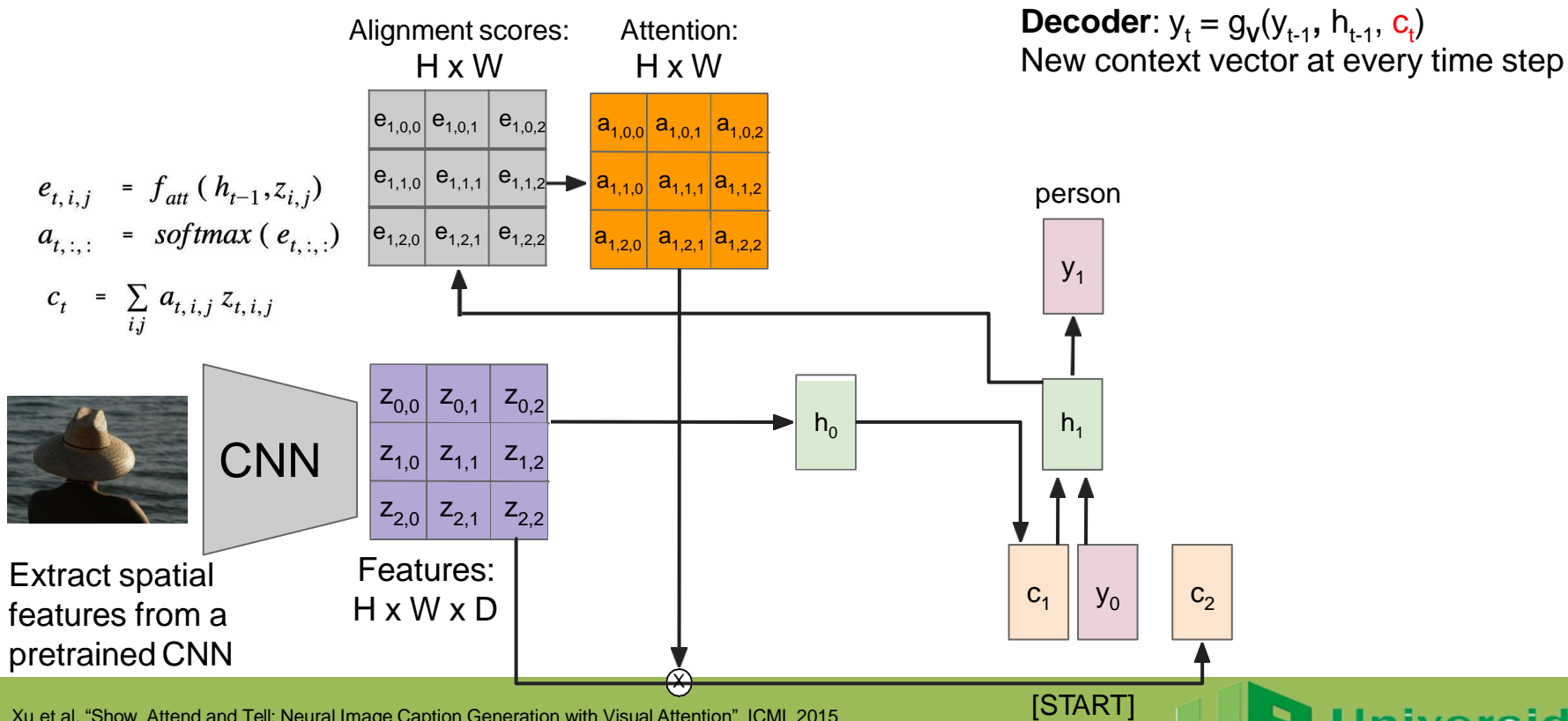
Decoder: $y_t = g_v(y_{t-1}, h_{t-1}, c_t)$
New context vector at every time step



Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

Attention and Transformers

Image Captioning with RNNs and Attention



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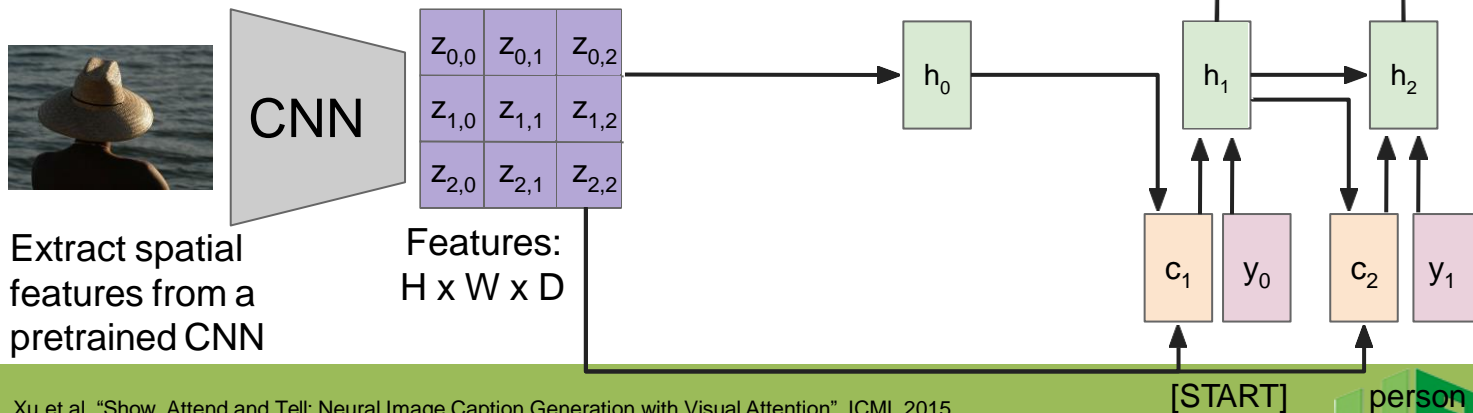
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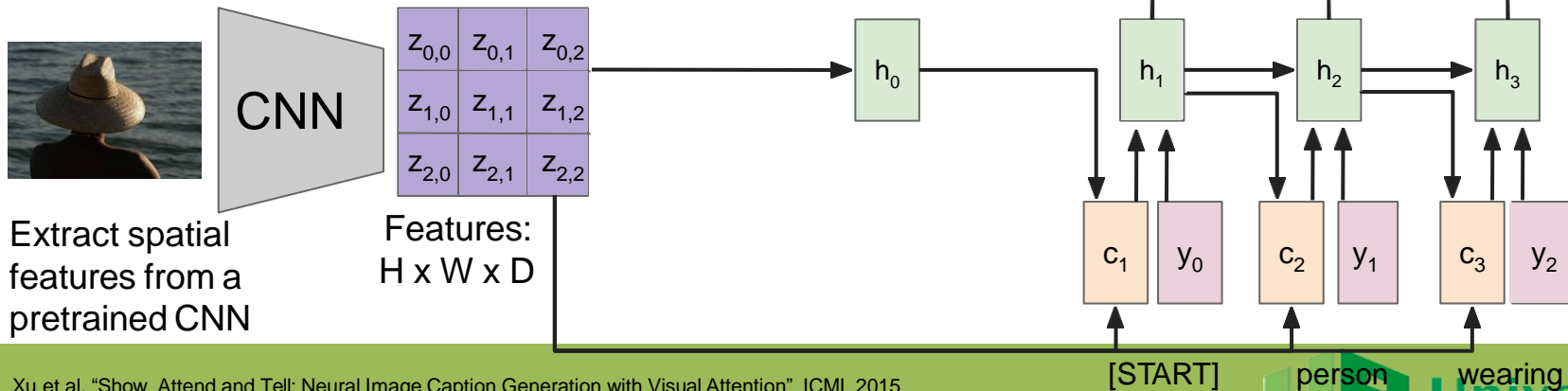
Attention and Transformers

Image Captioning with RNNs and Attention

Each timestep of decoder uses a different context vector that looks at different parts of the input image

$$e_{t,i,j} = f_{att}(h_{t-1}, z_{i,j})$$
$$a_{t,:,\cdot} = \text{softmax}(e_{t,:,\cdot})$$
$$c_t = \sum_{i,j} a_{t,i,j} z_{i,j}$$

Decoder: $y_t = g_v(y_{t-1}, h_{t-1}, c_t)$
New context vector at every time step



Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

Attention and Transformers

Image Captioning with RNNs and Attention

Each timestep of decoder uses a different context vector that looks at different parts of the input image

$$e_{t,i,j} = f_{att}(h_{t-1}, z_{i,j})$$
$$a_{t,:} = \text{softmax}(e_{t,:})$$
$$c_t = \sum_{i,j} a_{t,i,j} z_{i,j}$$



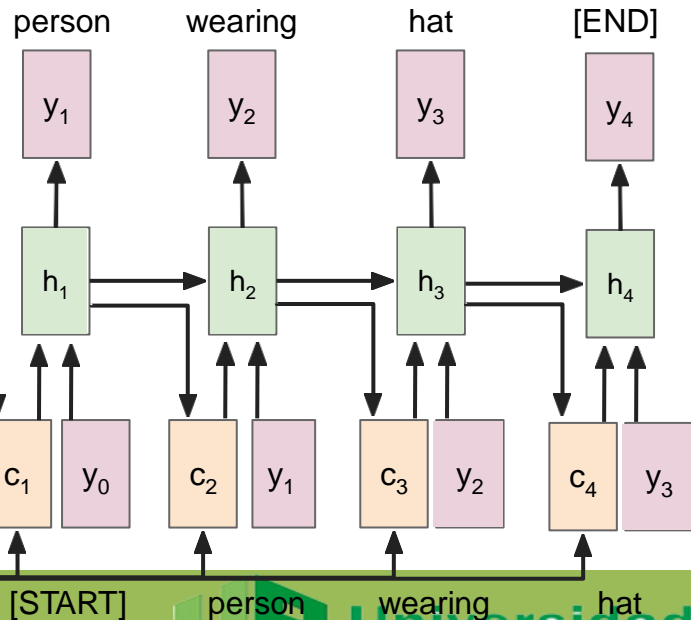
CNN

Extract spatial features from a pretrained CNN

$z_{0,0}$	$z_{0,1}$	$z_{0,2}$
$z_{1,0}$	$z_{1,1}$	$z_{1,2}$
$z_{2,0}$	$z_{2,1}$	$z_{2,2}$

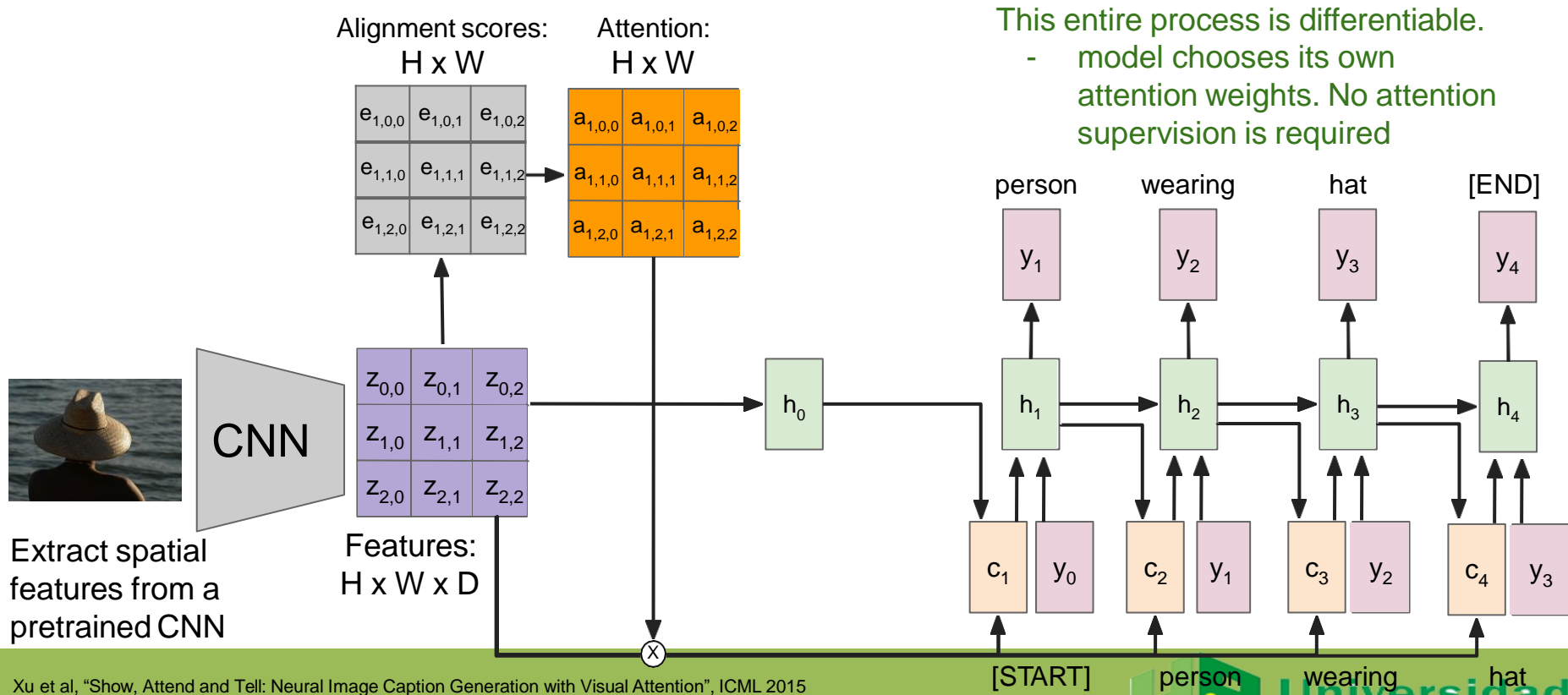
Features:
H x W x D

h_0



Decoder: $y_t = g_v(y_{t-1}, h_{t-1}, c_t)$
New context vector at every time step

Image Captioning with RNNs and Attention

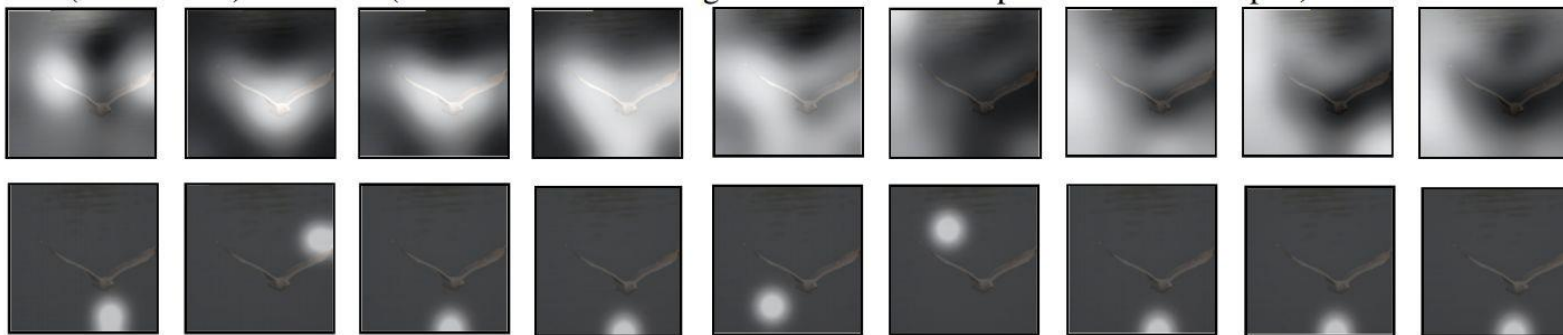


Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

Attention and Transformers

Image Captioning with Attention

Soft attention



A

bird

flying

over

a

body

of

water

■

Hard attention
(requires
reinforcement
learning)

Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

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Attention and Transformers

Image Captioning with Attention



A woman is throwing a frisbee in a park.



A dog is standing on a hardwood floor.



A stop sign is on a road with a mountain in the background.



A little girl sitting on a bed with a teddy bear.



A group of people sitting on a boat in the water.

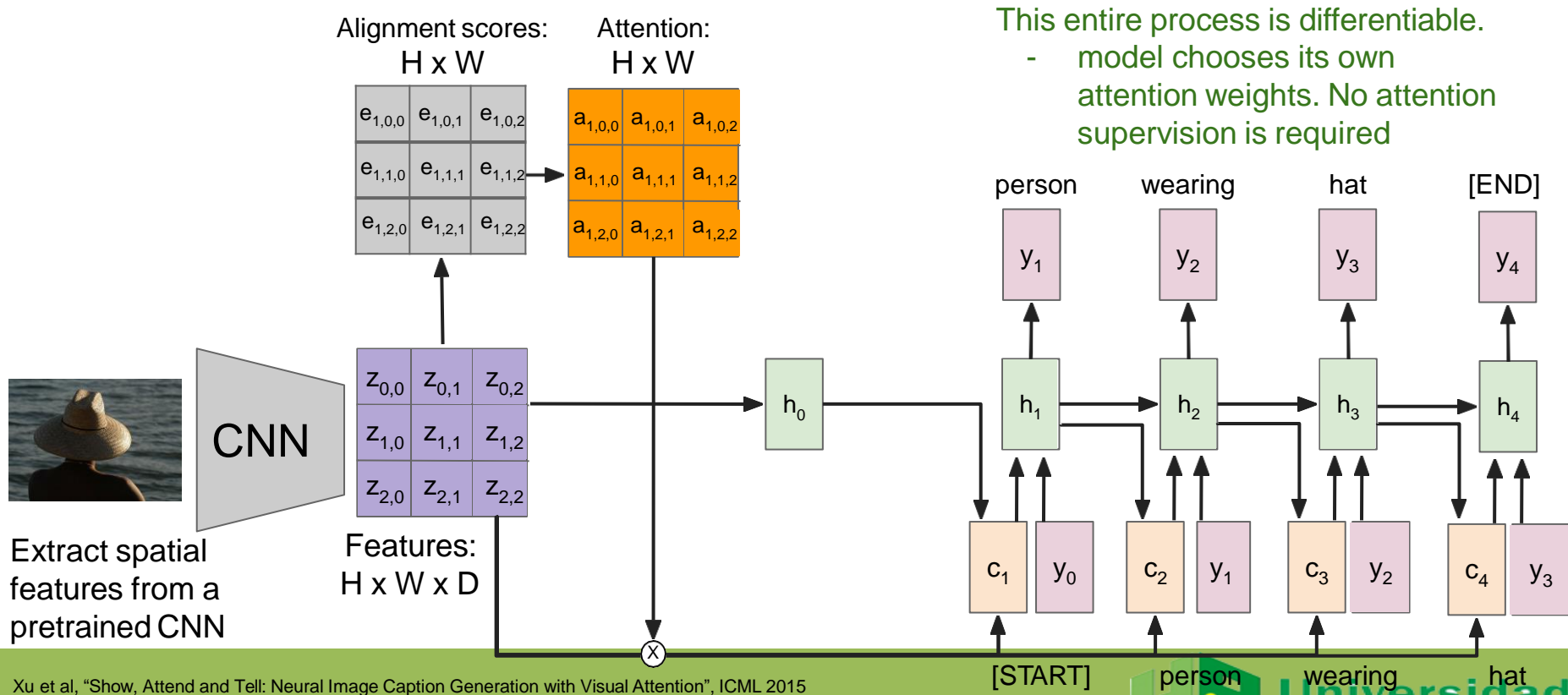


A giraffe standing in a forest with trees in the background.

Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

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Image Captioning with RNNs and Attention



Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

Attention and Transformers

Attention we just saw in image captioning

Features

$z_{0,0}$	$z_{0,1}$	$z_{0,2}$
$z_{1,0}$	$z_{1,1}$	$z_{1,2}$
$z_{2,0}$	$z_{2,1}$	$z_{2,2}$

h

Inputs:

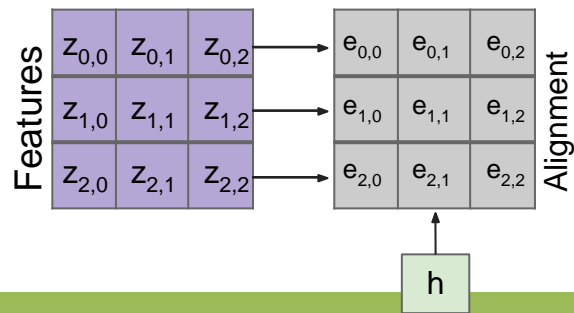
Features: \mathbf{z} (shape: $H \times W \times D$)

Query: \mathbf{h} (shape: D)

Attention we just saw in image captioning

Operations:

Alignment: $e_{i,j} = f_{\text{att}}(h, z_{i,j})$

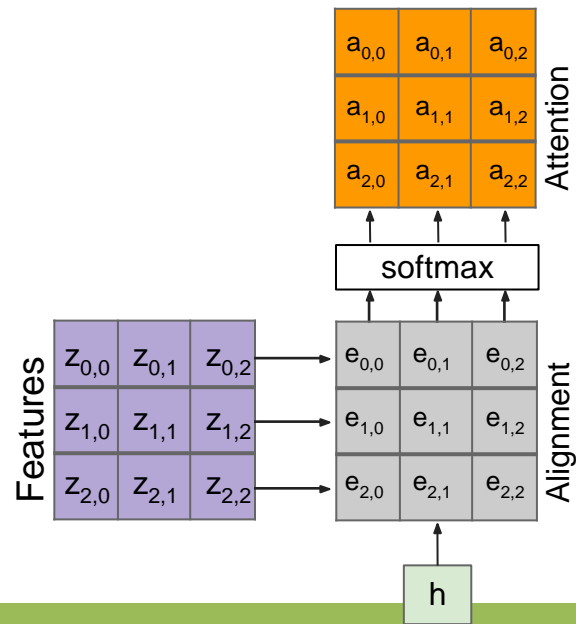


Inputs:

Features: \mathbf{z} (shape: $H \times W \times D$)

Query: \mathbf{h} (shape: D)

Attention we just saw in image captioning



Operations:

Alignment: $e_{i,j} = f_{\text{att}}(h, z_{i,j})$

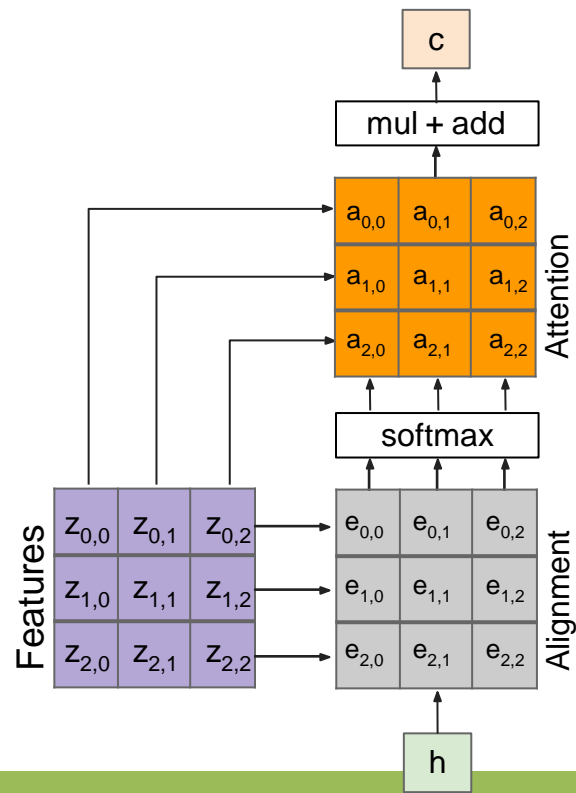
Attention: $\mathbf{a} = \text{softmax}(\mathbf{e})$

Inputs:

Features: \mathbf{z} (shape: $H \times W \times D$)

Query: \mathbf{h} (shape: D)

Attention we just saw in image captioning



Outputs:

context vector: **c** (shape: D)

Operations:

Alignment: $e_{i,j} = f_{\text{att}}(h, z_{i,j})$

Attention: $\mathbf{a} = \text{softmax}(\mathbf{e})$

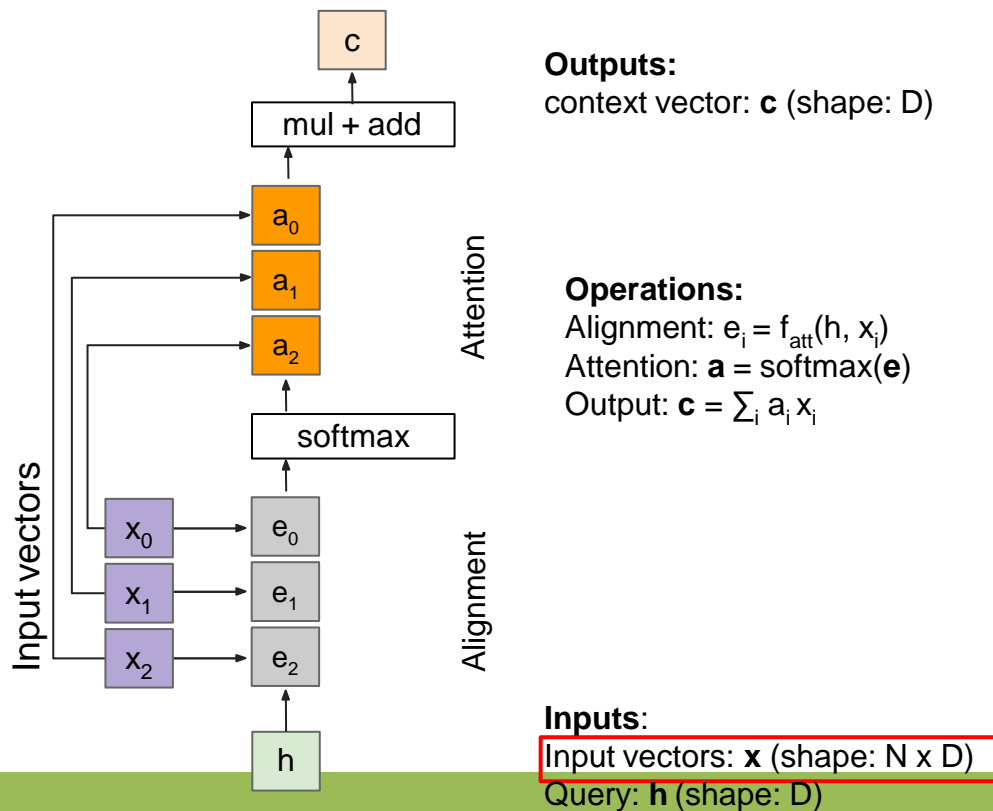
Output: $\mathbf{c} = \sum_{i,j} a_{i,j} z_{i,j}$

Inputs:

Features: **z** (shape: H x W x D)

Query: **h** (shape: D)

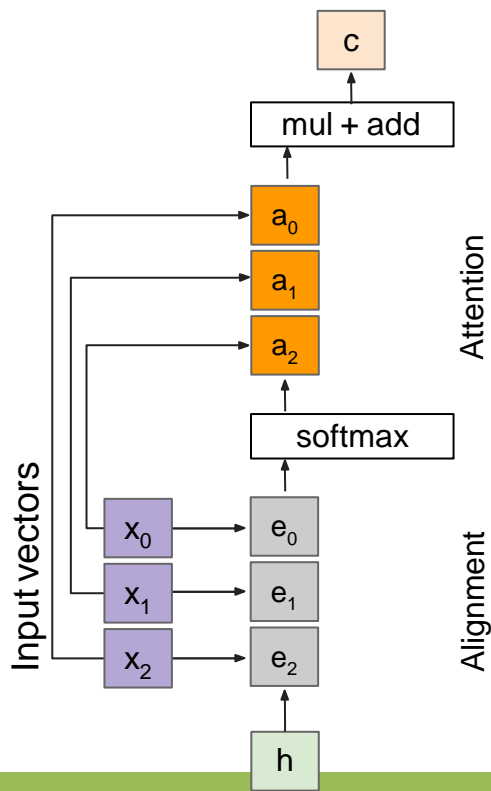
General attention layer



Attention operation is **permutation invariant**.

- Doesn't care about ordering of the features
- Stretch $H \times W = N$ into N vectors

General attention layer



Outputs:

context vector: \mathbf{c} (shape: D)

Operations:

Alignment: $e_i = h \cdot x_i$

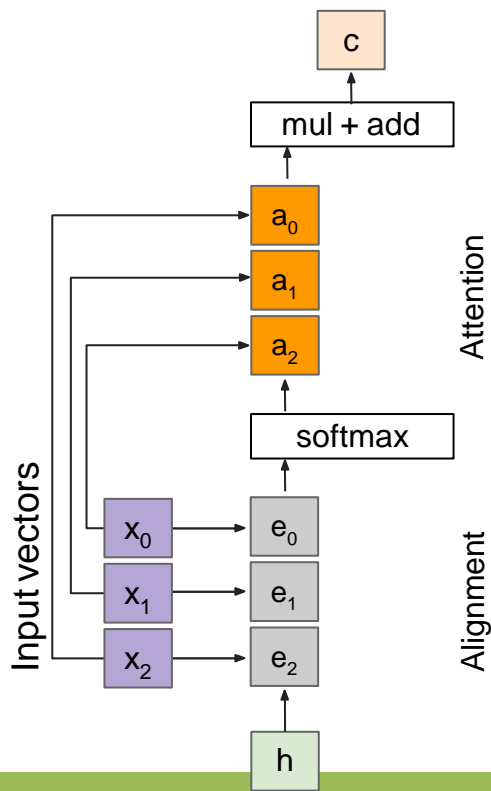
Attention: $\mathbf{a} = \text{softmax}(\mathbf{e})$

Output: $\mathbf{c} = \sum_i a_i x_i$

Change $f_{\text{att}}(\cdot)$ to a simple dot product

- only works well with key & value transformation trick (will mention in a few slides)

General attention layer



Outputs:

context vector: \mathbf{c} (shape: D)

Operations:

Alignment: $e_i = \mathbf{h} \cdot \mathbf{x}_i / \sqrt{D}$

Attention: $\mathbf{a} = \text{softmax}(\mathbf{e})$

Output: $\mathbf{c} = \sum_i a_i \mathbf{x}_i$

Inputs:

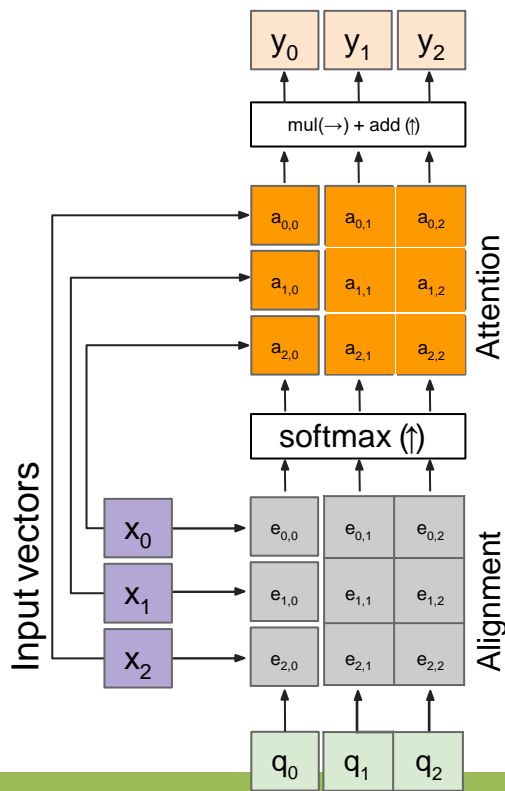
Input vectors: \mathbf{x} (shape: N x D)

Query: \mathbf{h} (shape: D)

Change $f_{\text{att}}(\cdot)$ to a **scaled** simple dot product

- Larger dimensions means more terms in the dot product sum.
- So, the variance of the logits is higher. Large magnitude vectors will produce much higher logits.
- So, the post-softmax distribution has lower-entropy, assuming logits are IID.
- Ultimately, these large magnitude vectors will cause softmax to peak and assign very little weight to all others
- Divide by \sqrt{D} to reduce effect of large magnitude vectors

General attention layer



Outputs:

context vectors: \mathbf{y} (shape: D)

Operations:

Alignment: $e_{i,j} = q_j \cdot x_i / \sqrt{D}$

Attention: $\mathbf{a} = \text{softmax}(\mathbf{e})$

Output: $y_j = \sum_i a_{i,j} x_i$

Multiple query vectors

- each query creates a new output context vector

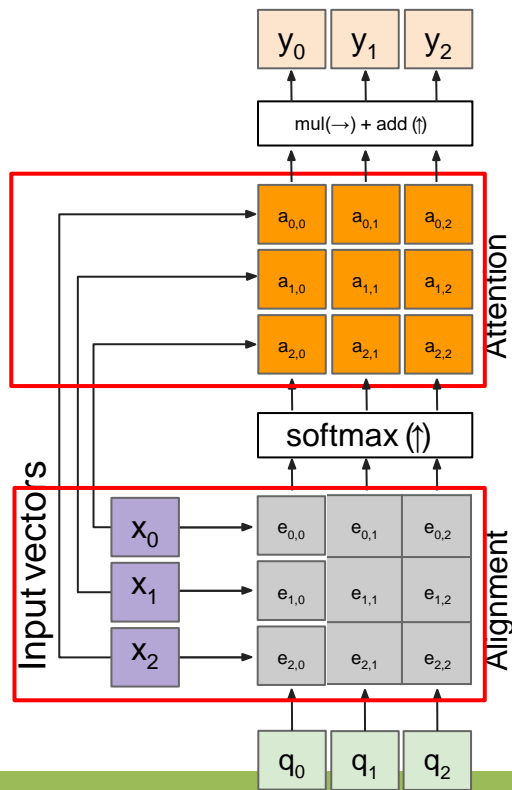
Inputs:

Input vectors: \mathbf{x} (shape: N x D)

Queries: \mathbf{q} (shape: M x D)

Multiple query vectors

General attention layer



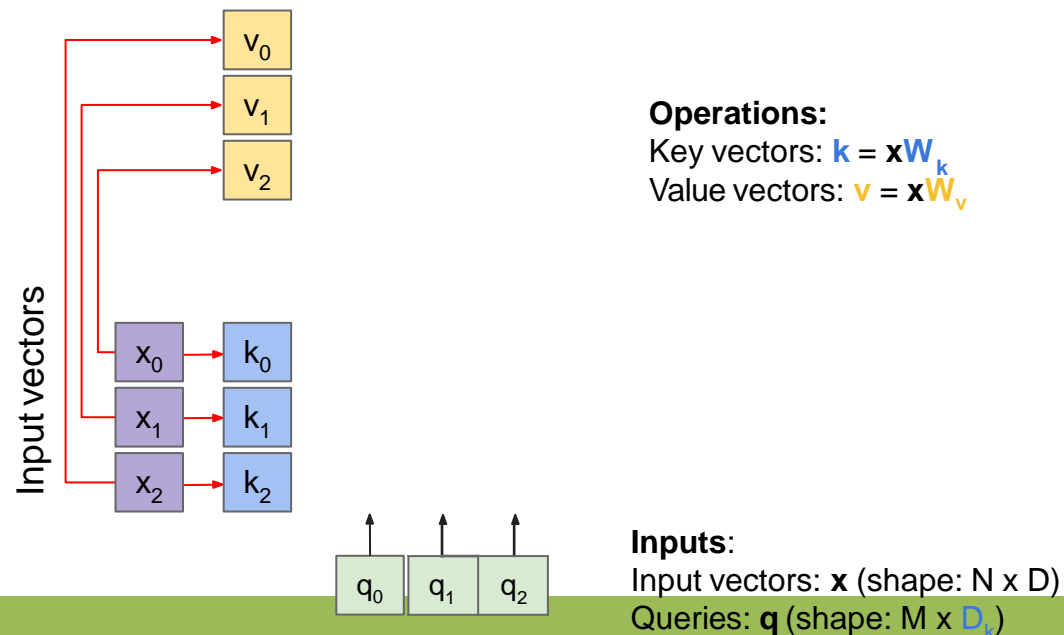
Outputs:
context vectors: \mathbf{y} (shape: D)

Operations:
Alignment: $e_{i,j} = q_j \cdot x_i / \sqrt{D}$
Attention: $\mathbf{a} = \text{softmax}(\mathbf{e})$
Output: $y_j = \sum_i a_{i,j} x_i$

Notice that the input vectors are used for both the alignment as well as the attention calculations.

- We can add more expressivity to the layer by adding a different FC layer before each of the two steps.

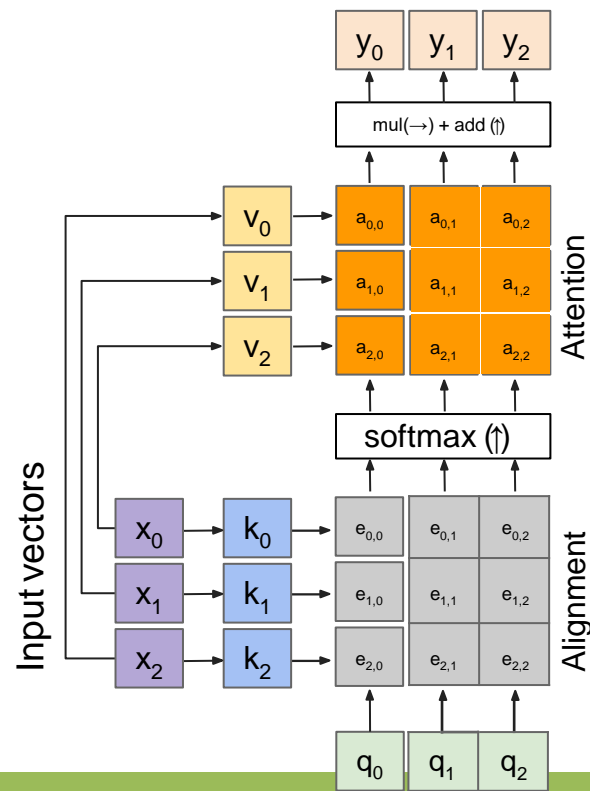
General attention layer



Notice that the input vectors are used for both the alignment as well as the attention calculations.

- We can add more expressivity to the layer by adding a different FC layer before each of the two steps.

General attention layer



Outputs:

context vectors: y (shape: D_y)

Operations:

Key vectors: $k = xW_k$

Value vectors: $v = xW_v$

Alignment: $e_{i,j} = q_i \cdot k_j / \sqrt{D}$

Attention: $a = \text{softmax}(e)$

Output: $y_j = \sum_i a_{i,j} v_i$

The input and output dimensions can now change depending on the key and value FC layers

Notice that the input vectors are used for both the alignment as well as the attention calculations.

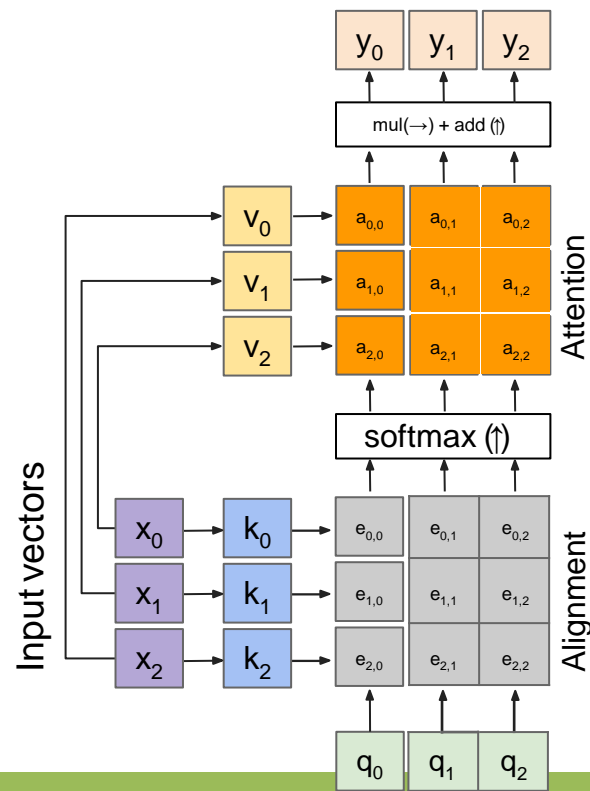
- We can add more expressivity to the layer by adding a different FC layer before each of the two steps.

Inputs:

Input vectors: x (shape: $N \times D$)

Queries: q (shape: $M \times D_k$)

General attention layer



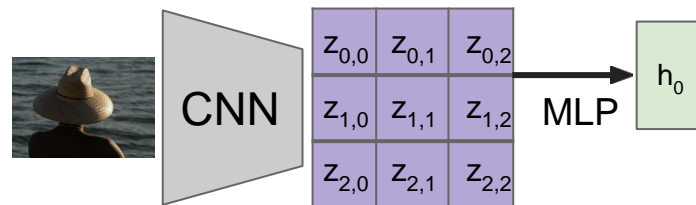
Outputs:
context vectors: \mathbf{y} (shape: D_v)

Operations:
Key vectors: $\mathbf{k} = \mathbf{x}W_k$
Value vectors: $\mathbf{v} = \mathbf{x}W_v$
Alignment: $e_{i,j} = q_j \cdot k_i / \sqrt{D}$
Attention: $\mathbf{a} = \text{softmax}(\mathbf{e})$
Output: $y_j = \sum_i a_{i,j} v_i$

Inputs:
Input vectors: \mathbf{x} (shape: $N \times D$)
Queries: \mathbf{q} (shape: $M \times D_k$)

Recall that the query vector was a function of the input vectors

Encoder: $h_0 = f_w(\mathbf{z})$
where \mathbf{z} is spatial CNN features
 $f_w(\cdot)$ is an MLP



Self attention layer

Operations:

Key vectors: $\mathbf{k} = \mathbf{x}\mathbf{W}_k$

Value vectors: $\mathbf{v} = \mathbf{x}\mathbf{W}_v$

Query vectors: $\mathbf{q} = \mathbf{x}\mathbf{W}_q$

Alignment: $e_{ij} = \mathbf{q}_i \cdot \mathbf{k}_j / \sqrt{D}$

Attention: $\mathbf{a} = \text{softmax}(\mathbf{e})$

Output: $y_j = \sum_i a_{ij} v_i$

We can calculate the query vectors from the input vectors, therefore, defining a "self-attention" layer.

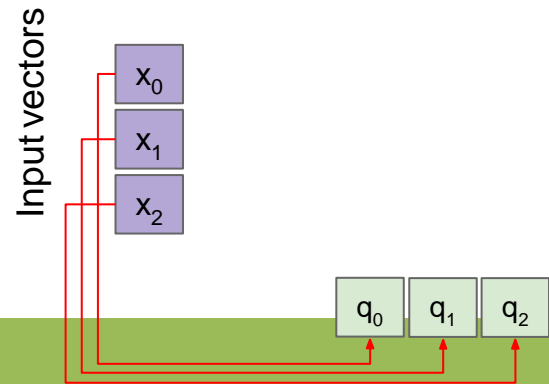
Instead, query vectors are calculated using a FC layer.

No input query vectors anymore

Inputs:

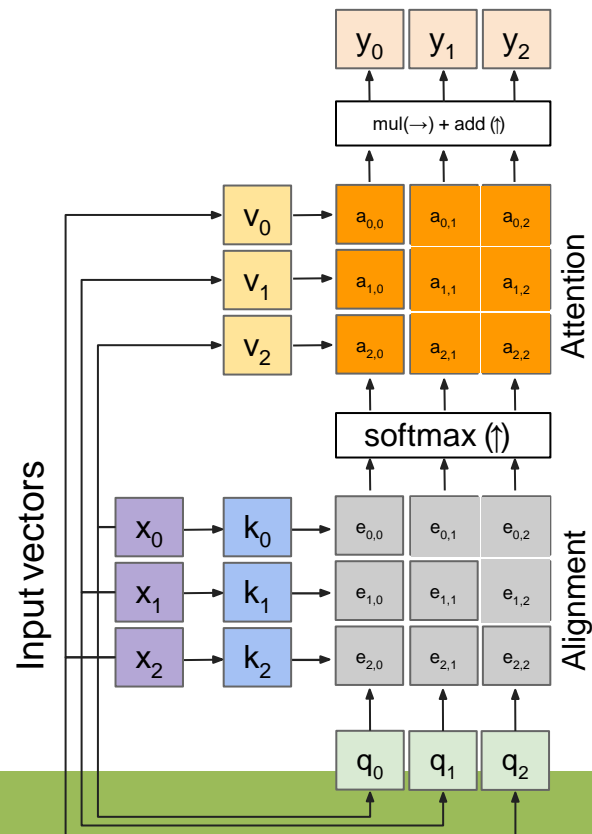
Input vectors: \mathbf{x} (shape: $N \times D$)

Queries: \mathbf{q} (shape: $M \times D_q$)



Attention and Transformers

Self attention layer



Outputs:

context vectors: y (shape: D_v)

Operations:

Key vectors: $k = xW_k$

Value vectors: $v = xW_v$

Query vectors: $q = xW_q$

Alignment: $e_{i,j} = q_i \cdot k_j / \sqrt{D}$

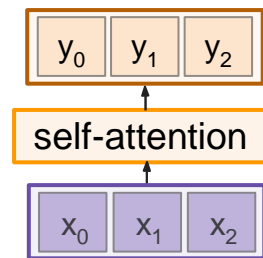
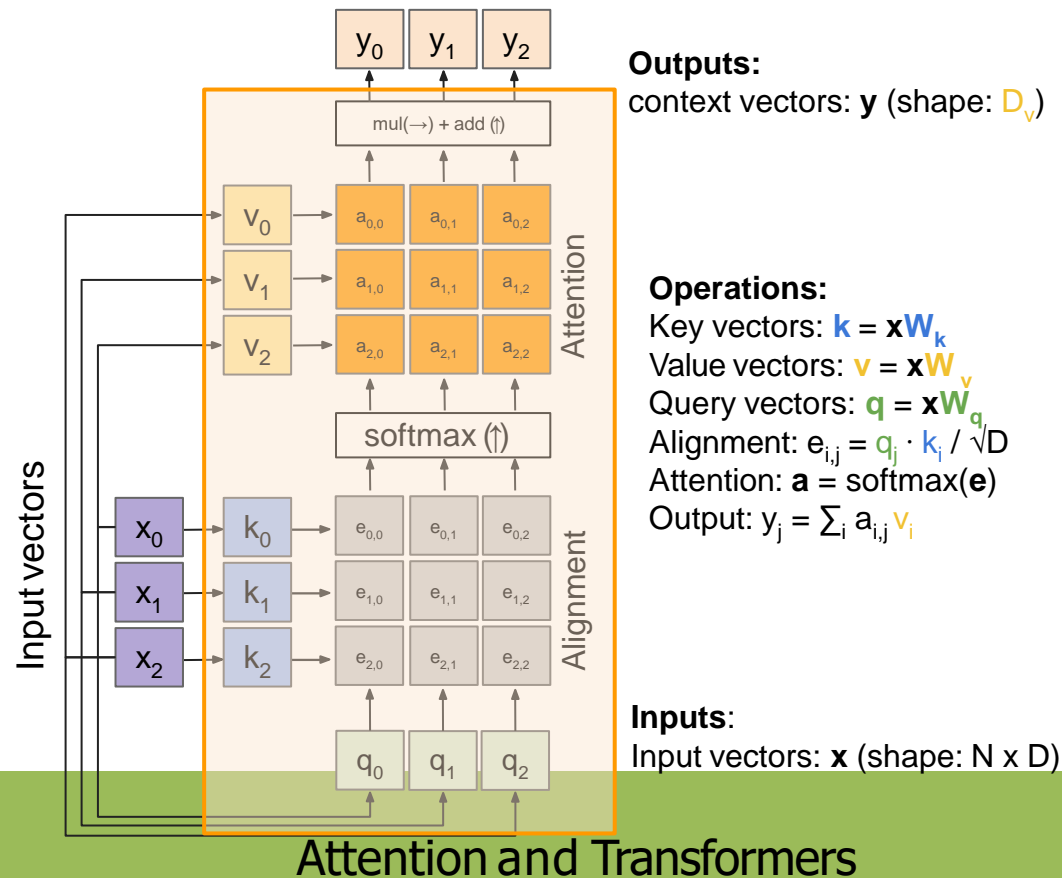
Attention: $a = \text{softmax}(e)$

Output: $y_j = \sum_i a_{i,j} v_i$

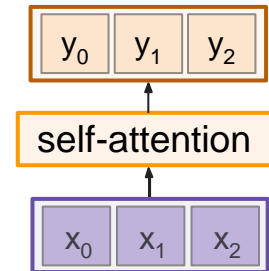
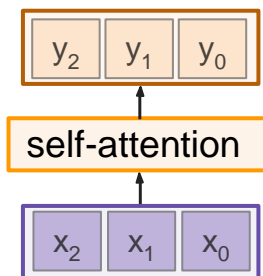
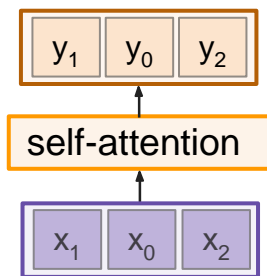
Inputs:

Input vectors: x (shape: $N \times D$)

Self attention layer - attends over sets of inputs



Self attention layer - attends over sets of inputs

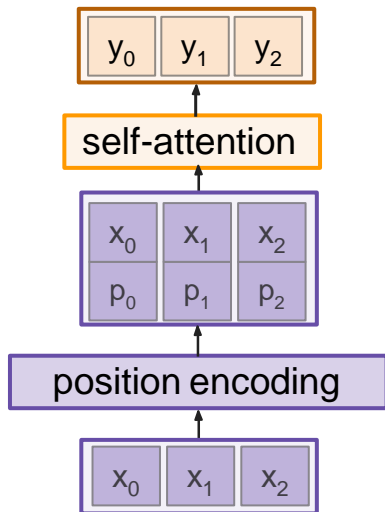


Permutation equivariant

Self-attention layer doesn't care about the orders of the inputs!

Problem: How can we encode ordered sequences like language or spatially ordered image features?

Positional encoding



Concatenate/add special positional encoding p_j to each input vector x_j

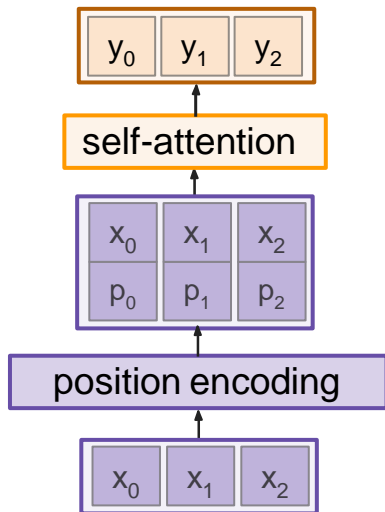
We use a function $pos: \mathbb{N} \rightarrow \mathbb{R}^d$ to process the position j of the vector into a d -dimensional vector

Desiderata of $pos(.)$:

1. It should output a **unique** encoding for each time-step (word's position in a sentence)
2. **Distance** between any two time-steps should be consistent across sentences with different lengths.
3. Our model should generalize to **longer** sentences without any efforts. Its values should be bounded.
4. It must be **deterministic**.

So, $p_j = pos(j)$

Positional encoding



Concatenate special positional encoding p_j to each input vector x_j

We use a function $pos: \mathbb{N} \rightarrow \mathbb{R}^d$ to process the position j of the vector into a d -dimensional vector

Options for $pos(\cdot)$

1. Learn a lookup table:
 - Learn parameters to use for $pos(t)$ for $t \in [0, T)$
 - Lookup table contains $T \times d$ parameters.

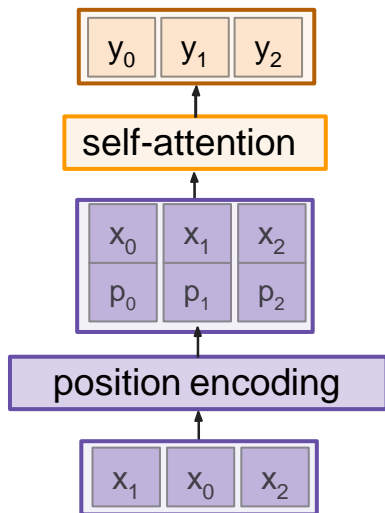
Desiderata of $pos(\cdot)$:

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Attention and Transformers

Positional encoding



Concatenate special positional encoding p_j to each input vector x_j

We use a function $pos: \mathbb{N} \rightarrow \mathbb{R}^d$ to process the position j of the vector into a d -dimensional vector

So, $p_j = pos(j)$

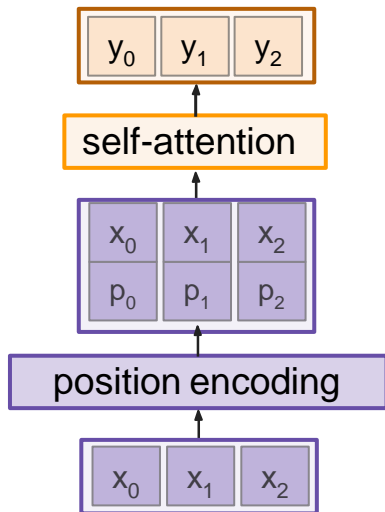
Options for $pos(\cdot)$

1. Learn a lookup table:
 - Learn parameters to use for $pos(t)$ for $t \in [0, T)$
 - Lookup table contains $T \times d$ parameters.
2. Design a fixed function with the desiderata

$$p(t) = \begin{bmatrix} \sin(\omega_1 \cdot t) \\ \cos(\omega_1 \cdot t) \\ \\ \sin(\omega_2 \cdot t) \\ \cos(\omega_2 \cdot t) \\ \\ \vdots \\ \sin(\omega_{d/2} \cdot t) \\ \cos(\omega_{d/2} \cdot t) \end{bmatrix}_d$$

where $\omega_k = \frac{1}{10000^{2k/d}}$

Positional encoding



Concatenate special positional encoding p_j to each input vector x_j

We use a function $pos: N \rightarrow R^d$ to process the position j of the vector into a d -dimensional vector

So, $p_j = pos(j)$

Options for $pos(.)$

1. Learn a lookup table:
 - Learn parameters to use for $pos(t)$ for $t \in [0, T)$
 - Lookup table contains $T \times d$ parameters.
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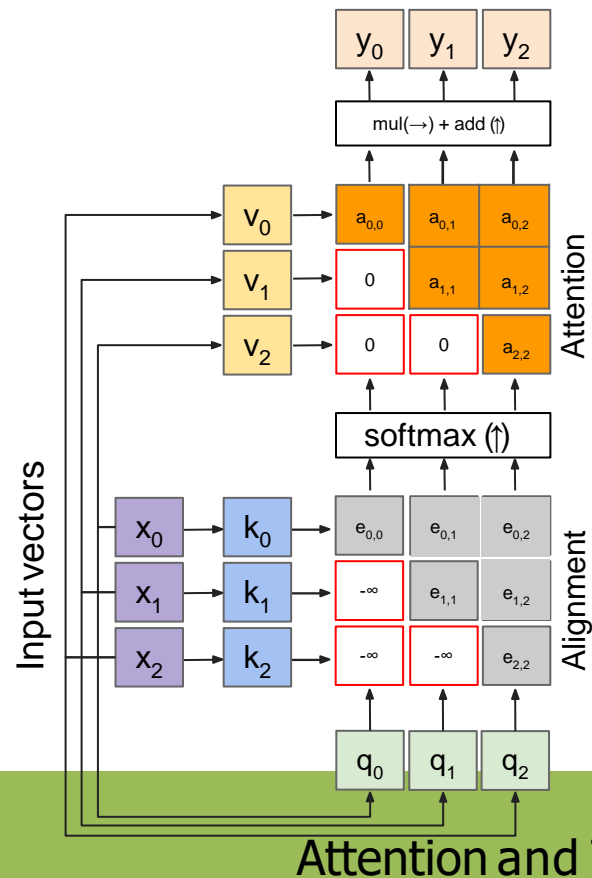
$$p(t) = \begin{bmatrix} \sin(\omega_1 \cdot t) \\ \cos(\omega_1 \cdot t) \\ \\ \sin(\omega_2 \cdot t) \\ \cos(\omega_2 \cdot t) \\ \\ \vdots \\ \\ \sin(\omega_{d/2} \cdot t) \\ \cos(\omega_{d/2} \cdot t) \end{bmatrix}_d$$

Intuition:

0 :	0	0	0	0		8 :	1	0	0	0
1 :	0	0	0	1		9 :	1	0	0	1
2 :	0	0	1	0		10 :	1	0	1	0
3 :	0	0	1	1		11 :	1	0	1	1
4 :	0	1	0	0		12 :	1	1	0	0
5 :	0	1	0	1		13 :	1	1	0	1
6 :	0	1	1	0		14 :	1	1	1	0
7 :	0	1	1	1		15 :	1	1	1	1

where $\omega_k = \frac{1}{10000^{2k/d}}$

Masked self-attention layer



Outputs:

context vectors: y (shape: D_v)

Operations:

Key vectors: $k = xW_k$
Value vectors: $v = xW_v$
Query vectors: $q = xW_q$
Alignment: $e_{i,j} = q_i \cdot k_j / \sqrt{D}$
Attention: $a = \text{softmax}(e)$
Output: $y_j = \sum_i a_{i,j} v_i$

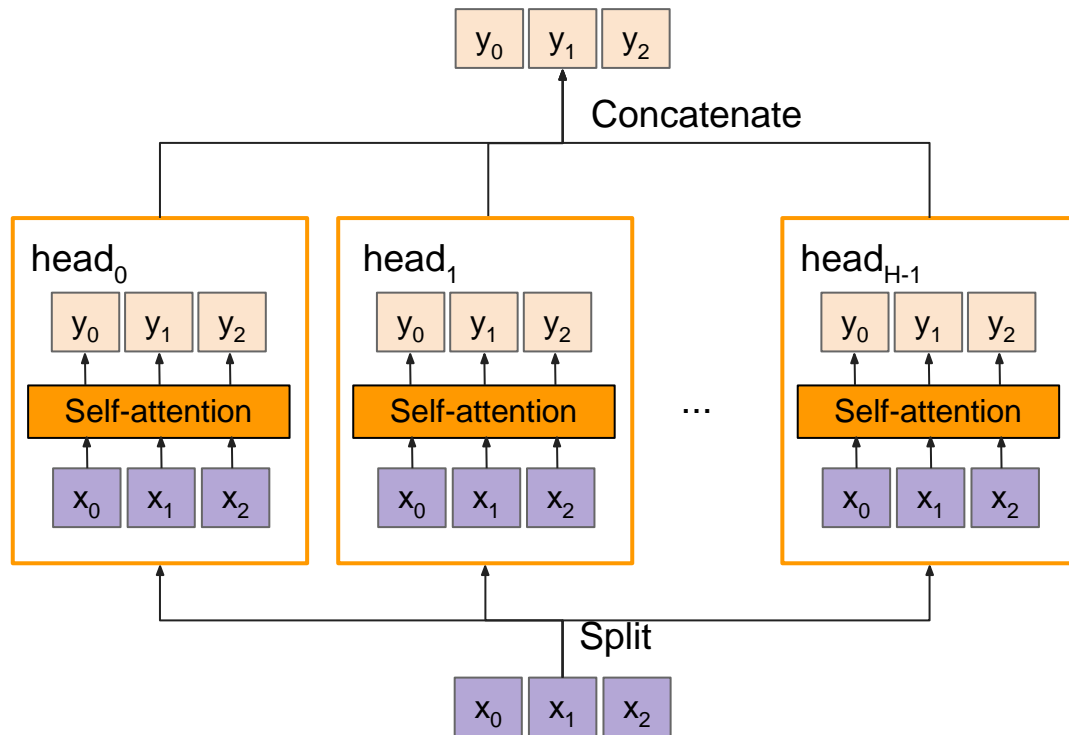
Inputs:

Input vectors: x (shape: $N \times D$)

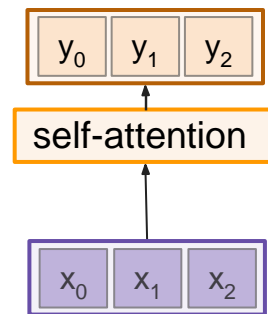
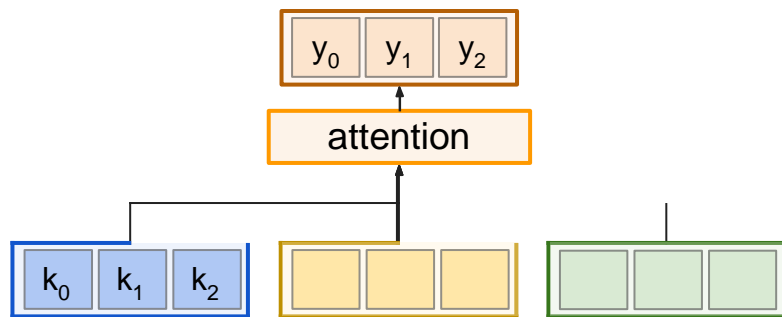
- Prevent vectors from looking at future vectors.
- Manually set alignment scores to -infinity

Multi-head self-attention layer

- Multiple self-attention heads in parallel



General attention versus self-attention



Example: CNN with Self-Attention

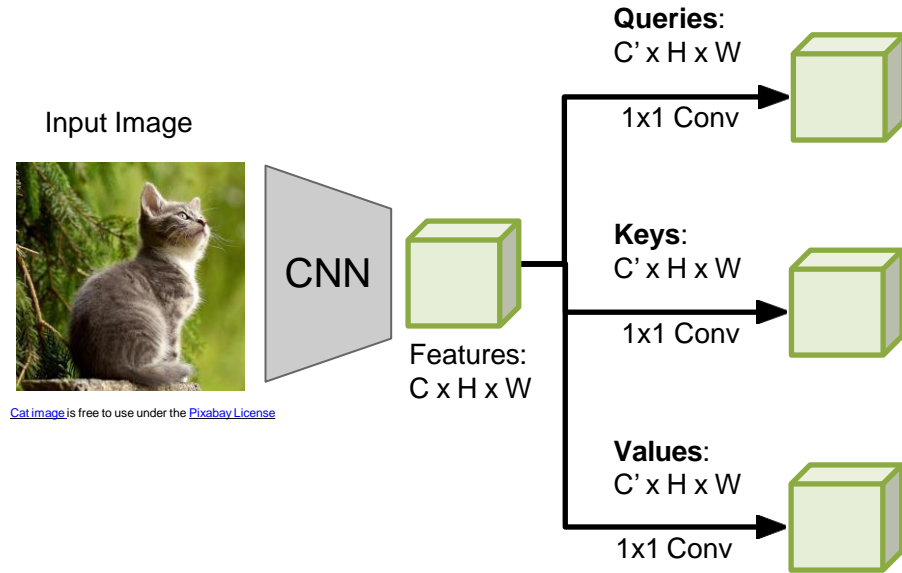
Input Image



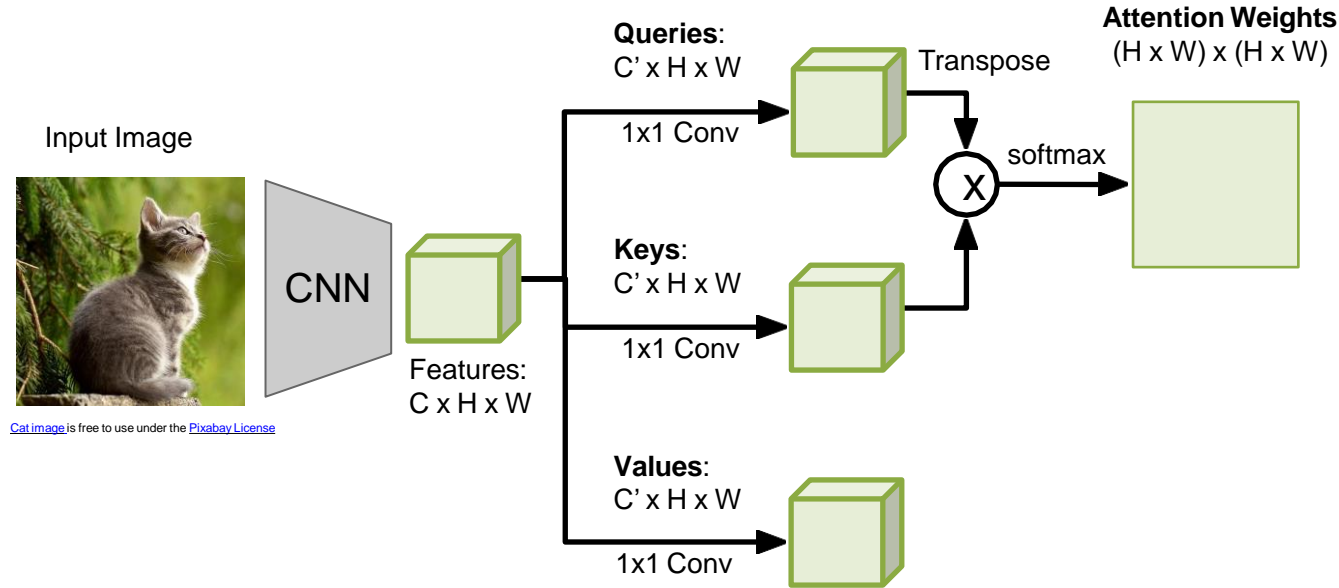
Features:
 $C \times H \times W$

[Cat image](#) is free to use under the [Pixabay License](#)

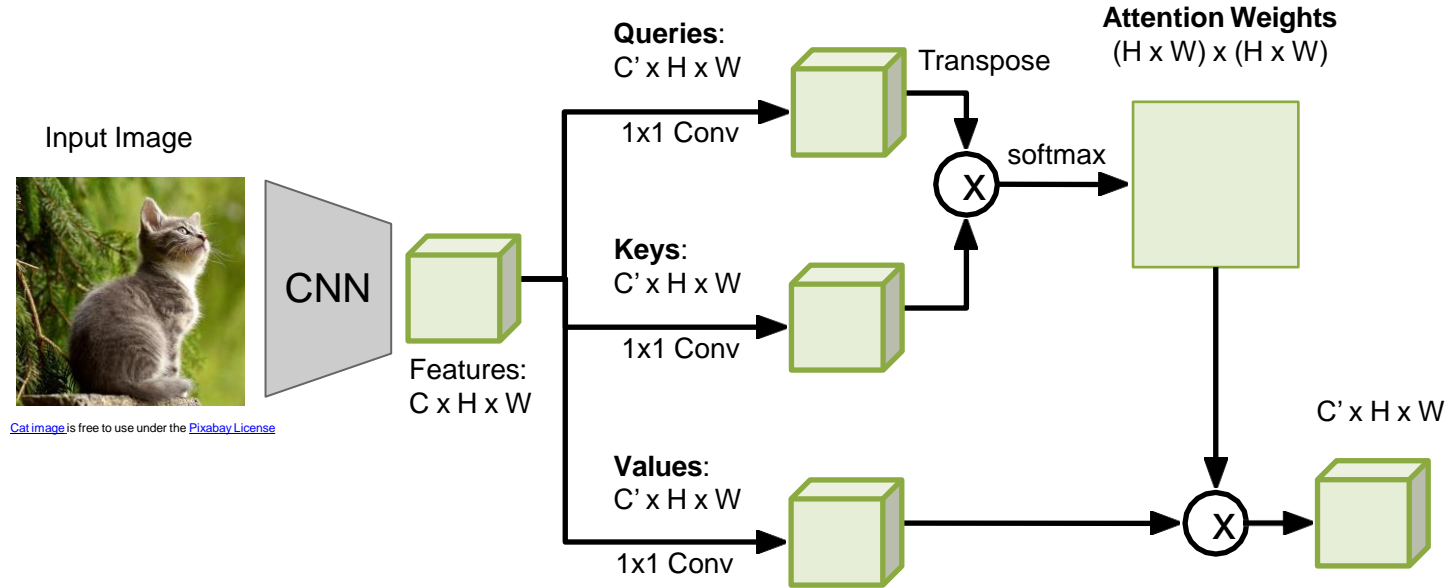
Example: CNN with Self-Attention



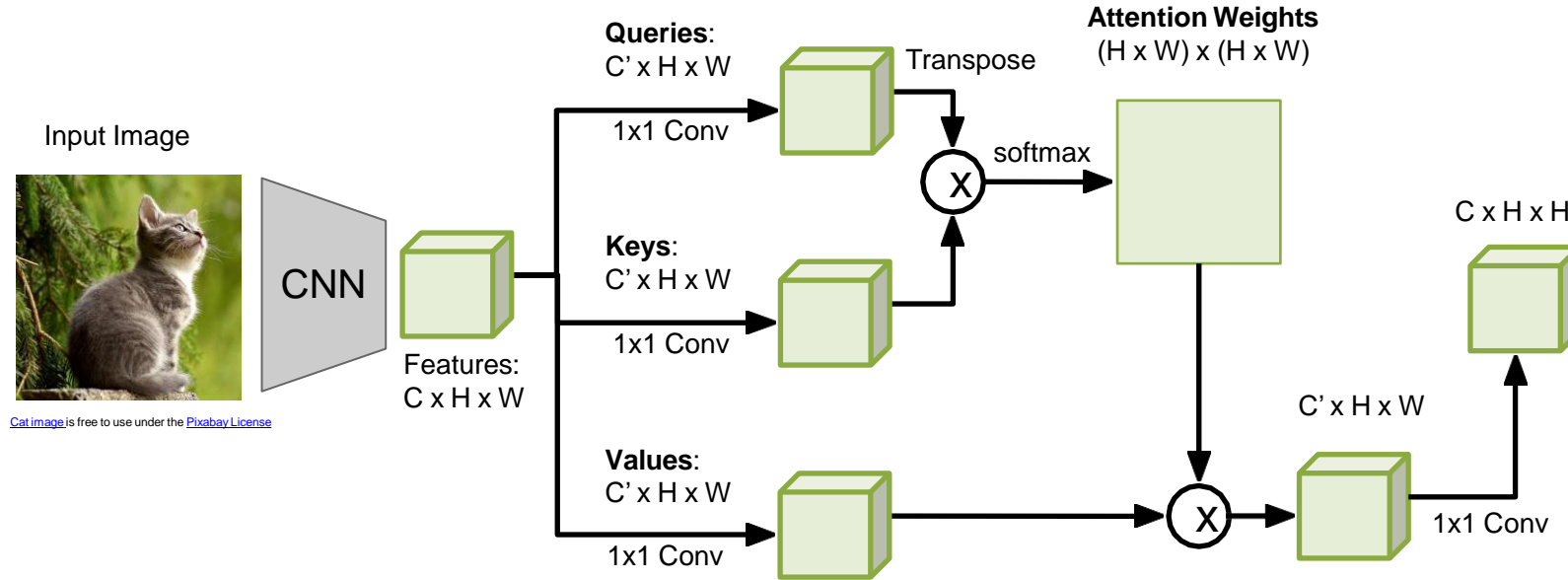
Example: CNN with Self-Attention



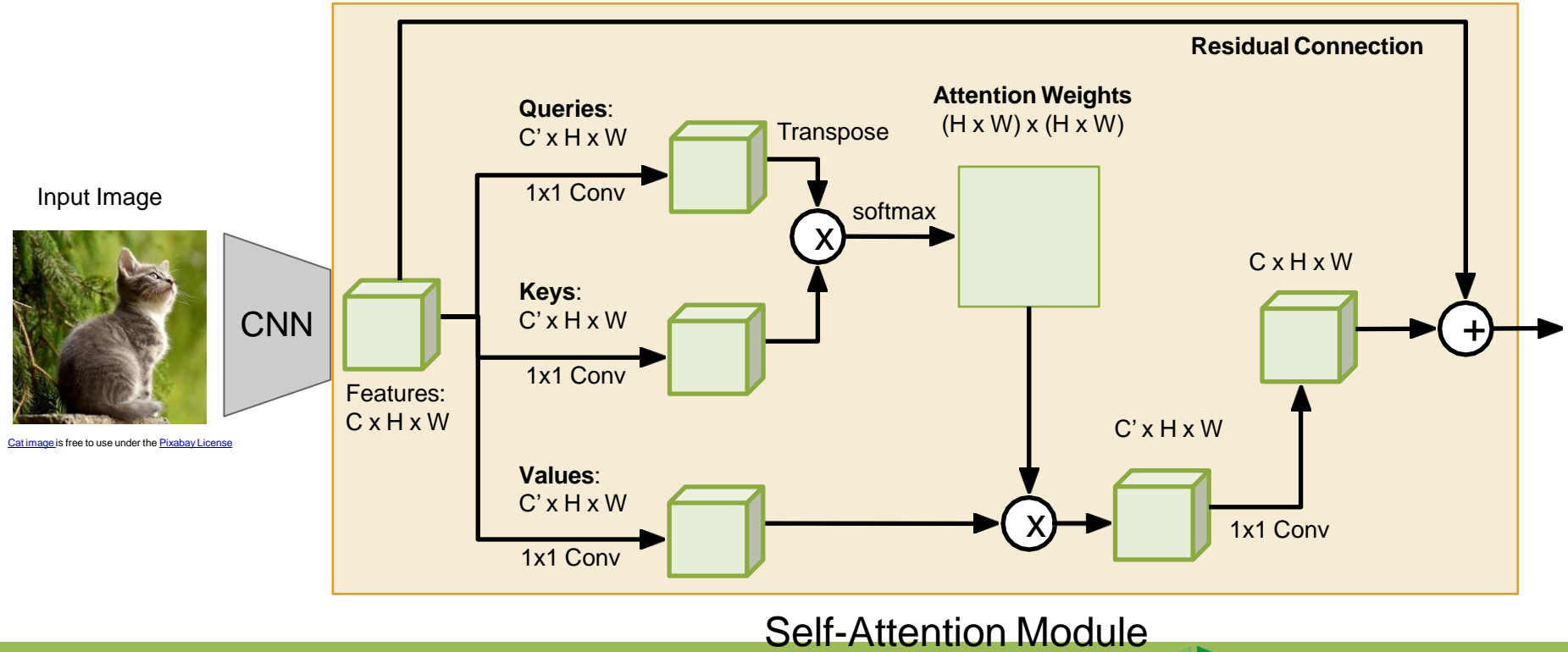
Example: CNN with Self-Attention



Example: CNN with Self-Attention



Example: CNN with Self-Attention



Comparing RNNs to Transformer

RNNs

- (+) LSTMs work reasonably well for long sequences.
- (-) Expects an ordered sequences of inputs
- (-) Sequential computation: subsequent hidden states can only be computed after the previous ones are done.

Transformer:

- (+) Good at long sequences. Each attention calculation looks at all inputs.
- (+) Can operate over unordered sets or ordered sequences with positional encodings.
- (+) Parallel computation: All alignment and attention scores for all inputs can be done in parallel.
- (-) Requires a lot of memory: $N \times M$ alignment and attention scalars need to be calculated and stored for a single self-attention head. (but GPUs are getting bigger and better)

Attention Is All You Need

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“ImageNet Moment for Natural Language Processing”

Pretraining:

Download a lot of text from the internet

Train a giant Transformer model for language modeling

Finetuning:

Fine-tune the Transformer on your own NLP task

On the Opportunities and Risks of Foundation Models

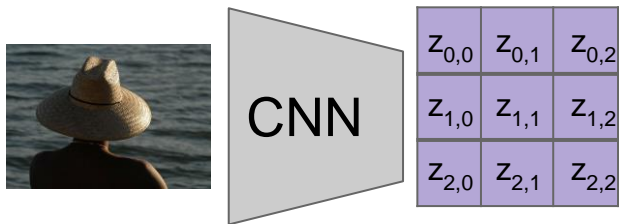
Rishi Bommasani* Drew A. Hudson Ehsan Adeli Russ Altman Simran Arora
Sydney von Arx Michael S. Bernstein Jeannette Bohg Antoine Bosselut Emma Brunskill
Erik Brynjolfsson Shyamal Buch Dallas Card Rodrigo Castellon Niladri Chatterji
Annie Chen Kathleen Creel Jared Quincy Davis Dorottya Demszky Chris Donahue
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Shelby Grossman Neel Guha Tatsunori Hashimoto Peter Henderson John Hewitt
Daniel E. Ho Jenny Hong Kyle Hsu Jing Huang Thomas Icard Saahil Jain
Dan Jurafsky Pratyusha Kalluri Siddharth Karamcheti Geoff Keeling Fereshte Khani
Omar Khattab Pang Wei Koh Mark Krass Ranjay Krishna Rohith Kuditipudi
Ananya Kumar Faisal Ladhak Mina Lee Tony Lee Jure Leskovec Isabelle Levent
Xiang Lisa Li Xuechen Li Tengyu Ma Ali Malik Christopher D. Manning
Suvir Mirchandani Eric Mitchell Zanele Munyikwa Suraj Nair Avanika Narayan
Deepak Narayanan Ben Newman Allen Nie Juan Carlos Nieves Hamed Nilforoshan
Julian Nyarko Giray Ogut Laurel Orr Isabel Papadimitriou Joon Sung Park Chris Piech
Eva Portelance Christopher Potts Aditi Raghunathan Rob Reich Hongyu Ren
Frieda Rong Yusuf Roohani Camilo Ruiz Jack Ryan Christopher Ré Dorsa Sadigh
Shiori Sagawa Keshav Santhanam Andy Shih Krishnan Srinivasan Alex Tamkin
Rohan Taori Armin W. Thomas Florian Tramèr Rose E. Wang William Wang Bohan Wu
Jiajun Wu Yuhuai Wu Sang Michael Xie Michihiro Yasunaga Jiaxuan You Matei Zaharia
Michael Zhang Tianyi Zhang Xikun Zhang Yuhui Zhang Lucia Zheng Kaitlyn Zhou
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Image Captioning using Transformers

Input: Image I

Output: Sequence $\mathbf{y} = y_1, y_2, \dots, y_T$



Extract spatial features from a pretrained CNN

Features:
 $H \times W \times D$

Image Captioning using Transformers

Input: Image I

Output: Sequence $\mathbf{y} = y_1, y_2, \dots, y_T$

Encoder: $\mathbf{c} = T_w(\mathbf{z})$

where \mathbf{z} is spatial CNN features

$T_w(\cdot)$ is the transformer encoder

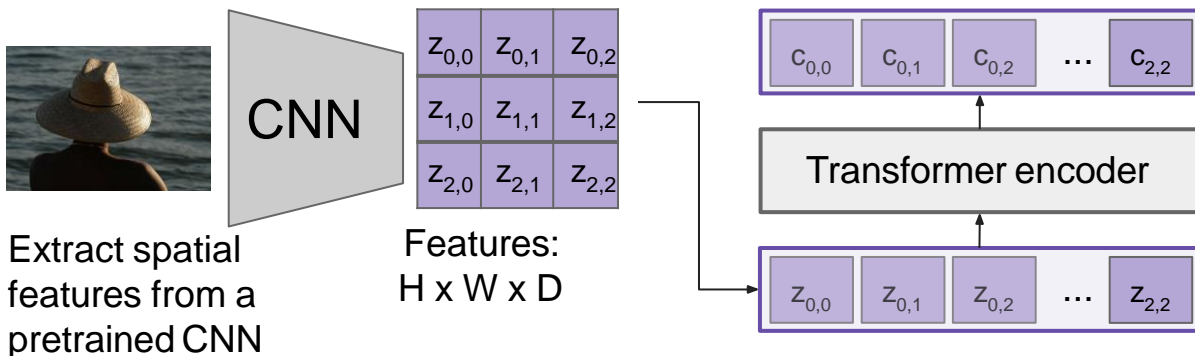


Image Captioning using Transformers

Input: Image I

Output: Sequence $\mathbf{y} = y_1, y_2, \dots, y_T$

Decoder: $y_t = T_D(y_{0:t-1}, \mathbf{c})$

where $T_D(\cdot)$ is the transformer decoder

Encoder: $\mathbf{c} = T_w(\mathbf{z})$

where \mathbf{z} is spatial CNN features

$T_w(\cdot)$ is the transformer encoder

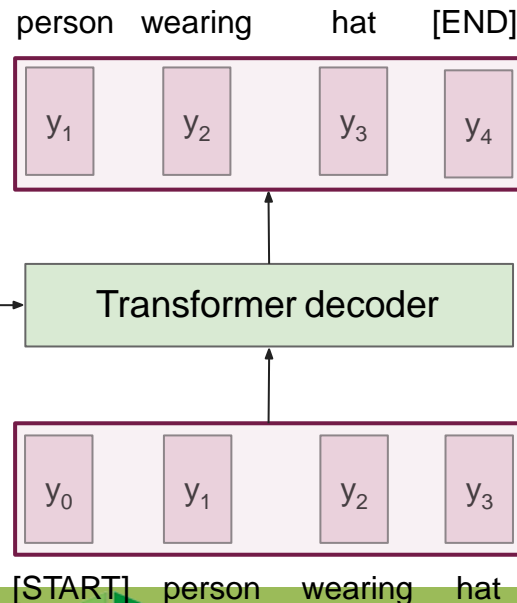
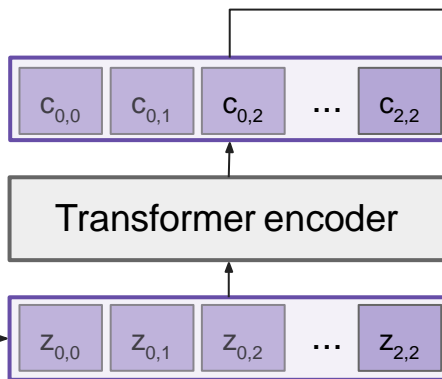


CNN

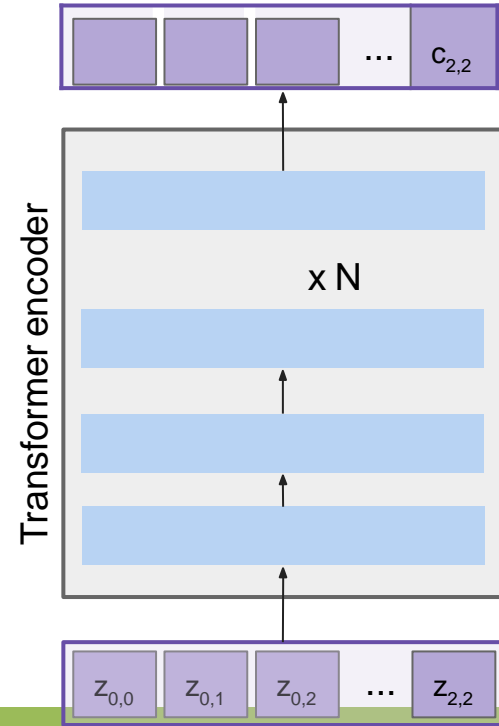
Extract spatial features from a pretrained CNN

$z_{0,0}$	$z_{0,1}$	$z_{0,2}$
$z_{1,0}$	$z_{1,1}$	$z_{1,2}$
$z_{2,0}$	$z_{2,1}$	$z_{2,2}$

Features:
 $H \times W \times D$



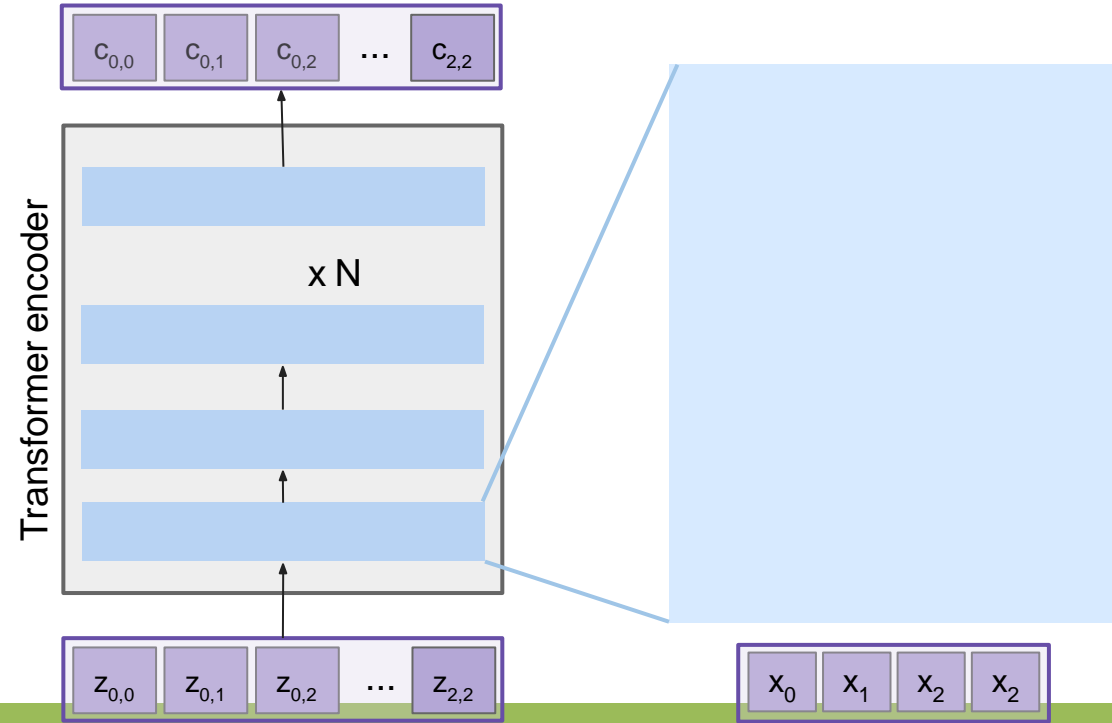
The Transformer encoder block



Made up of N encoder blocks.

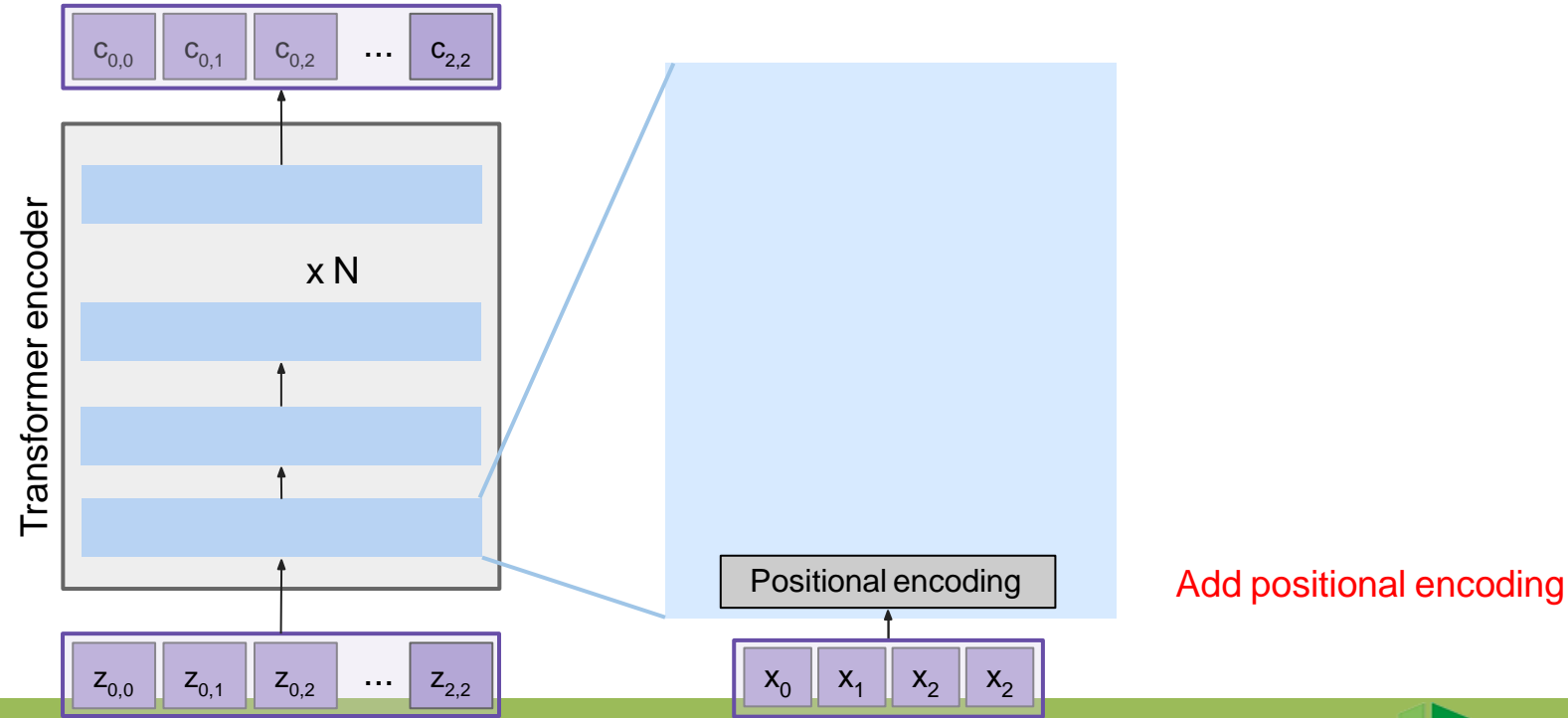
In vaswani et al. $N = 6$, $D_q = 512$

The Transformer encoder block

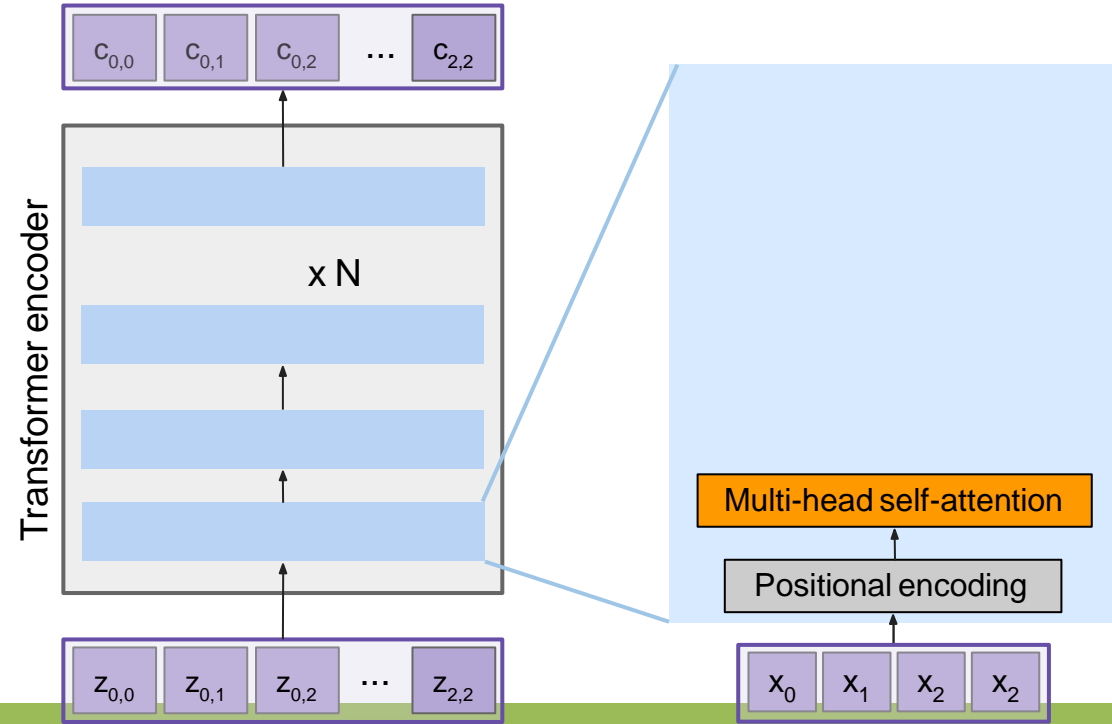


Let's dive into one encoder block

The Transformer encoder block



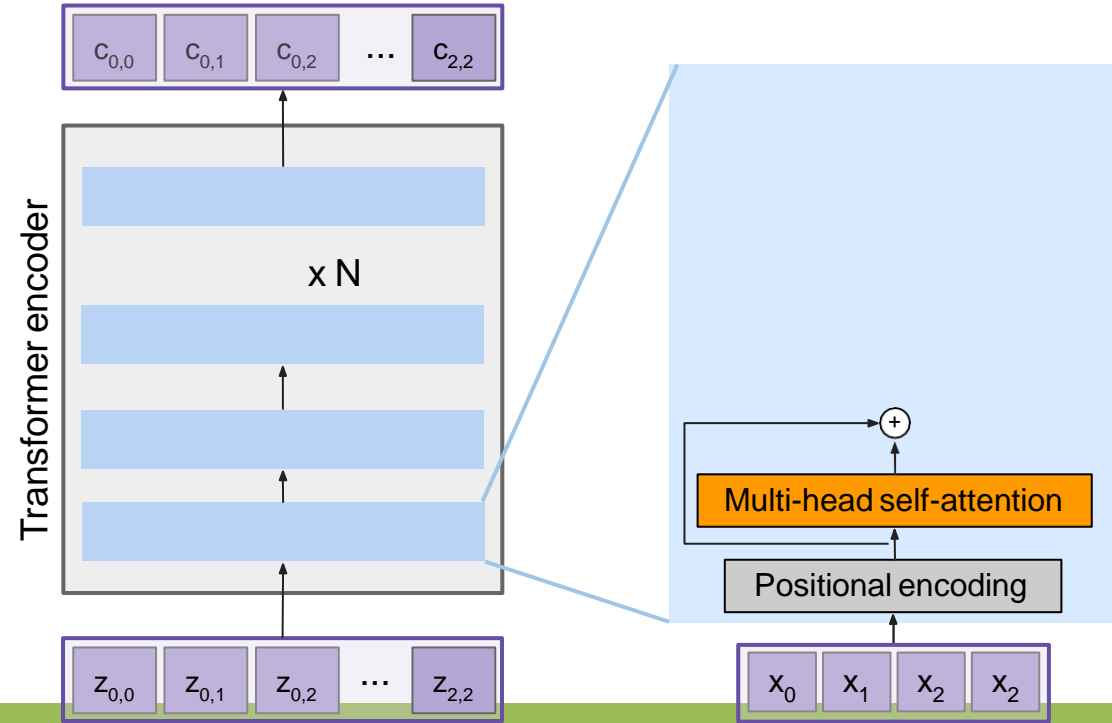
The Transformer encoder block



Attention attends over all the vectors

Add positional encoding

The Transformer encoder block

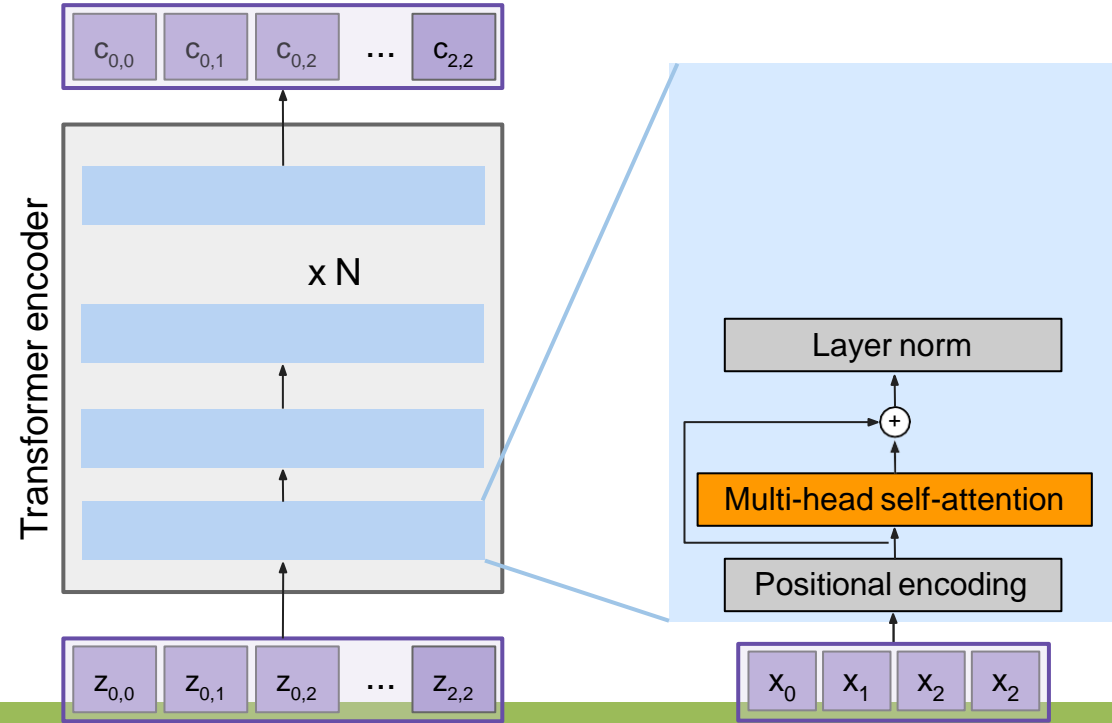


Residual connection

Attention attends over all the vectors

Add positional encoding

The Transformer encoder block



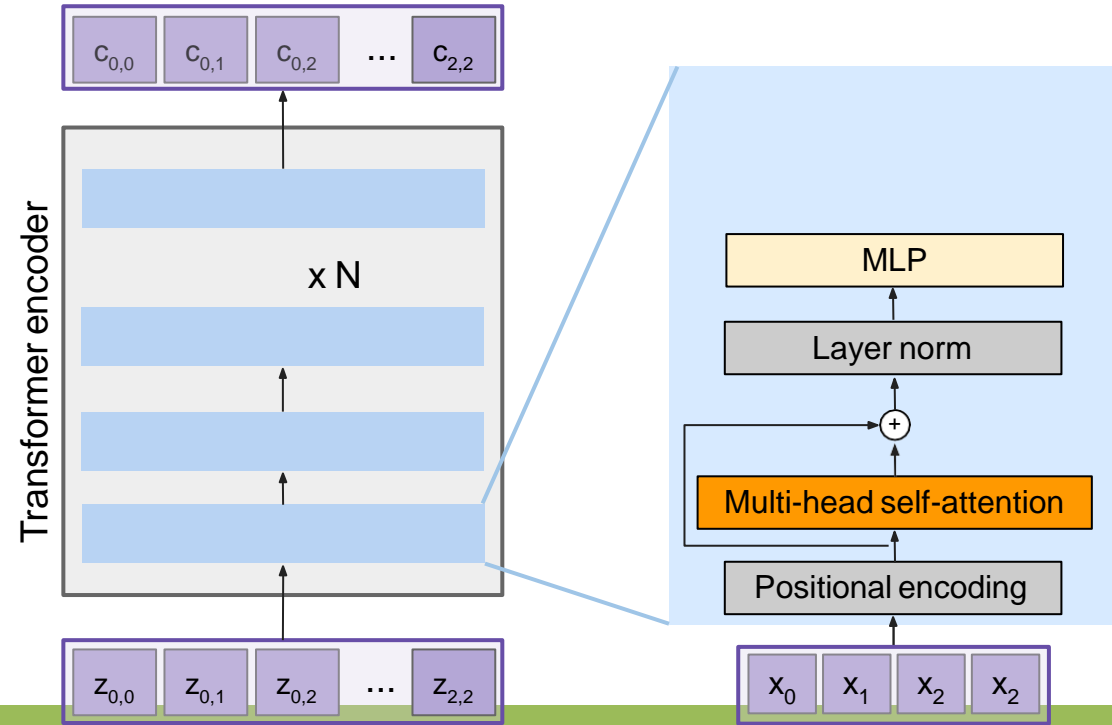
LayerNorm over each vector individually

Residual connection

Attention attends over all the vectors

Add positional encoding

The Transformer encoder block



MLP over each vector individually

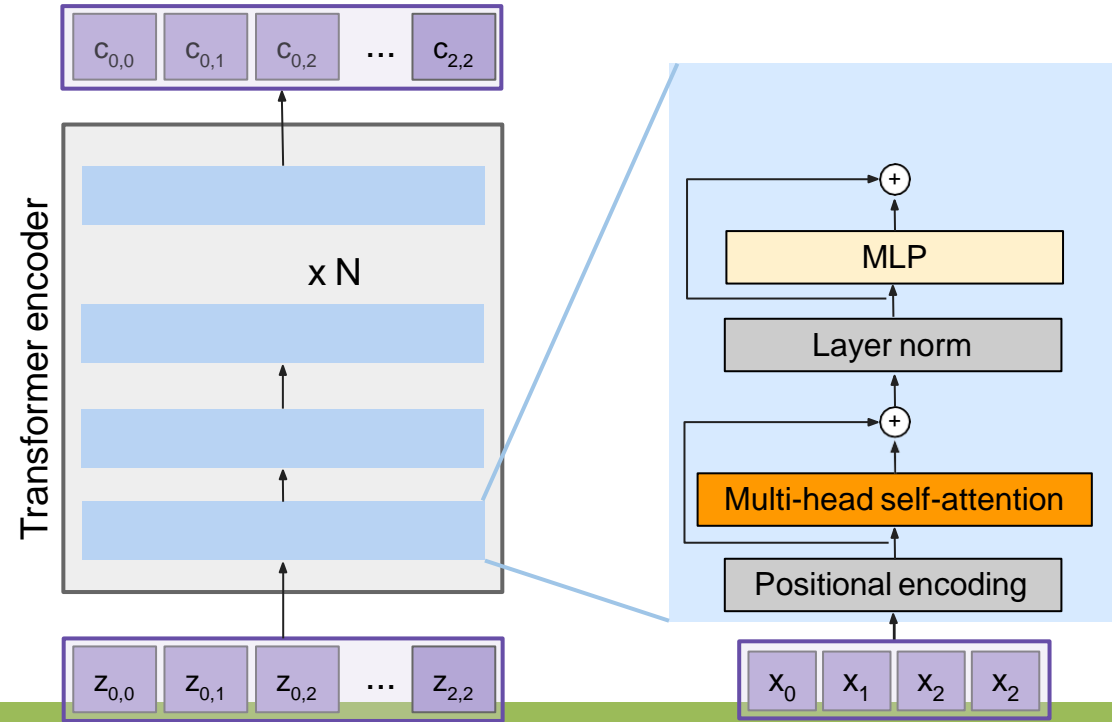
LayerNorm over each vector individually

Residual connection

Attention attends over all the vectors

Add positional encoding

The Transformer encoder block



Residual connection

MLP over each vector individually

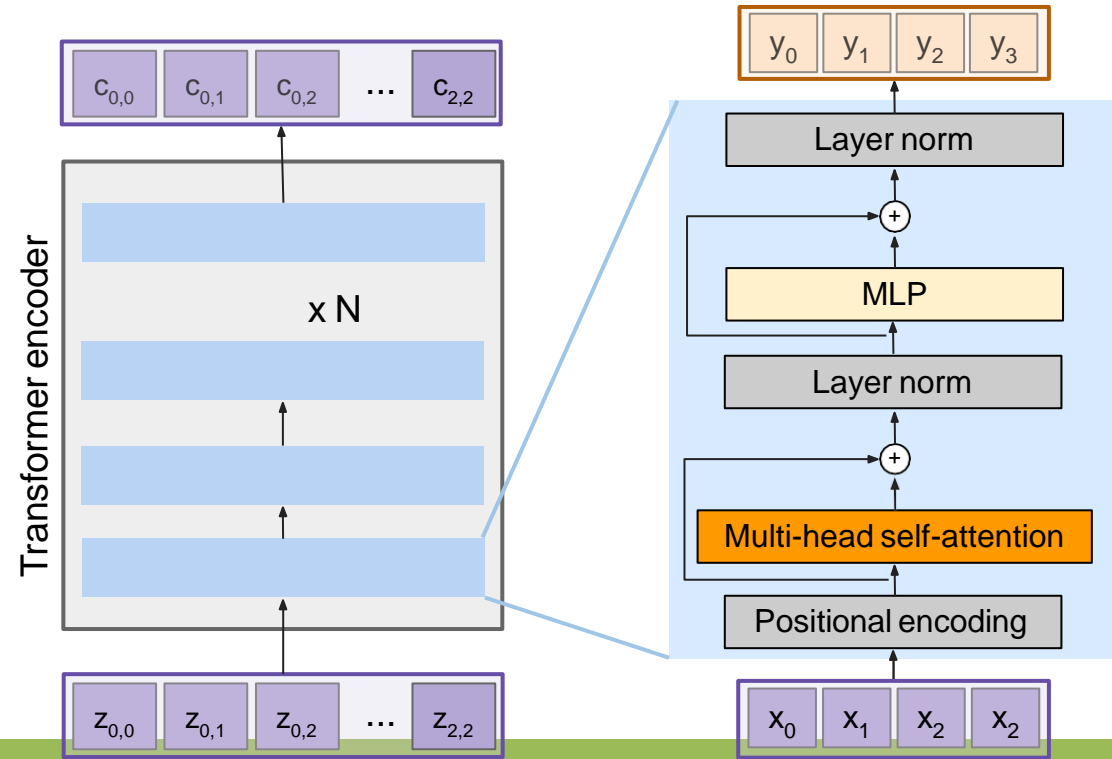
LayerNorm over each vector individually

Residual connection

Attention attends over all the vectors

Add positional encoding

The Transformer encoder block



Transformer Encoder Block:

Inputs: Set of vectors x

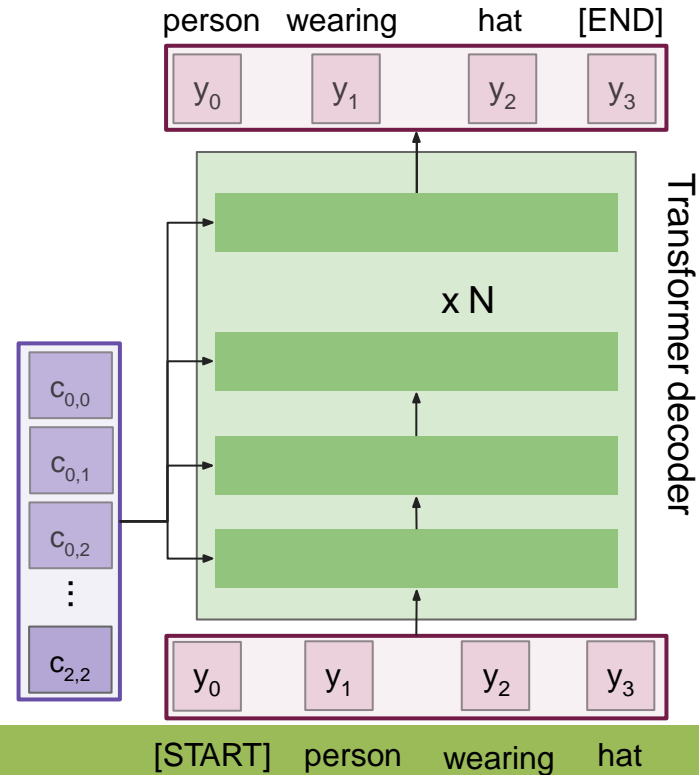
Outputs: Set of vectors y

Self-attention is the only interaction between vectors.

Layer norm and MLP operate independently per vector.

Highly scalable, highly parallelizable, but high memory usage.

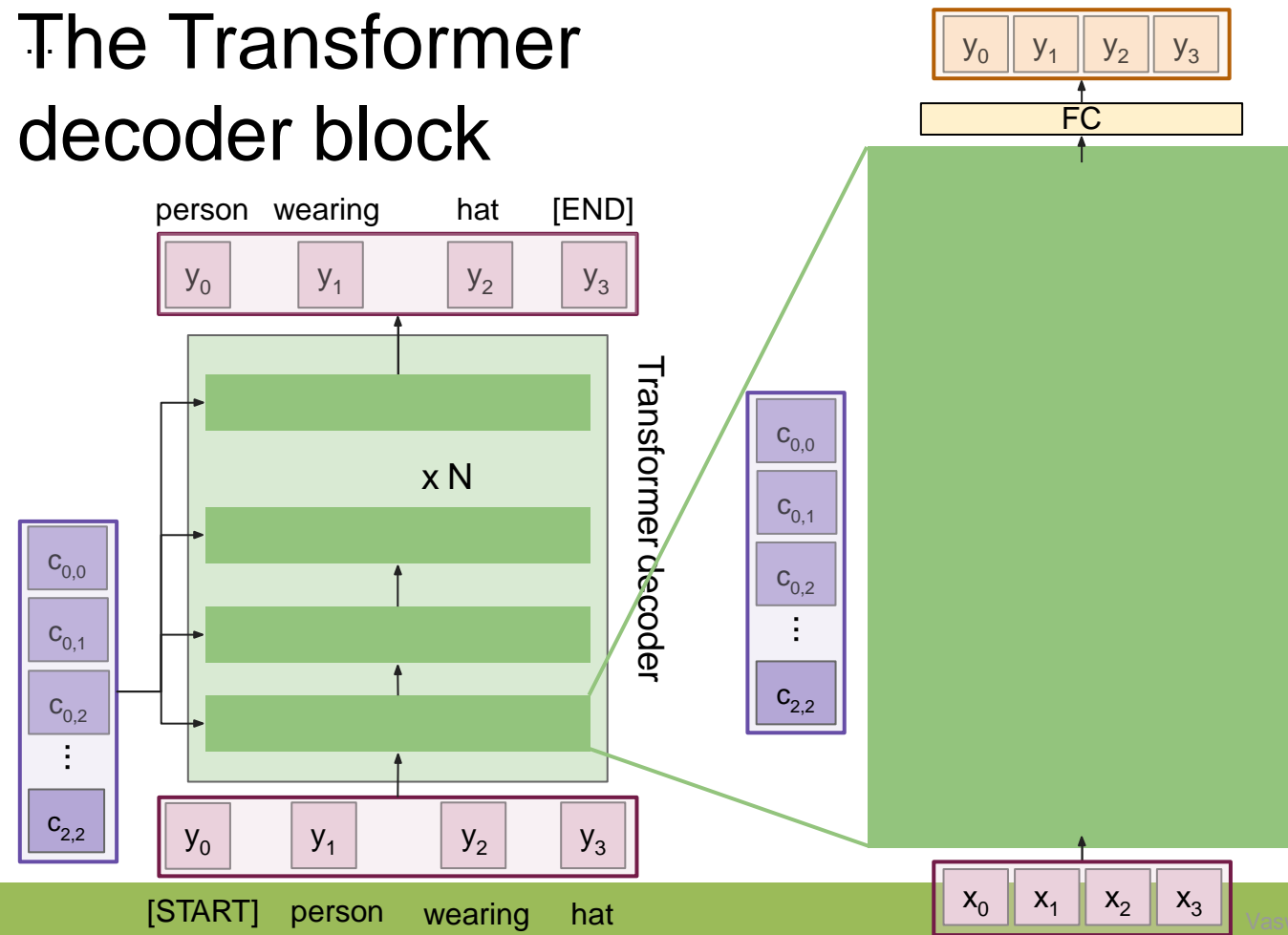
The Transformer decoder block



Made up of N decoder blocks.

In vaswani et al. $N = 6, D_q = 512$

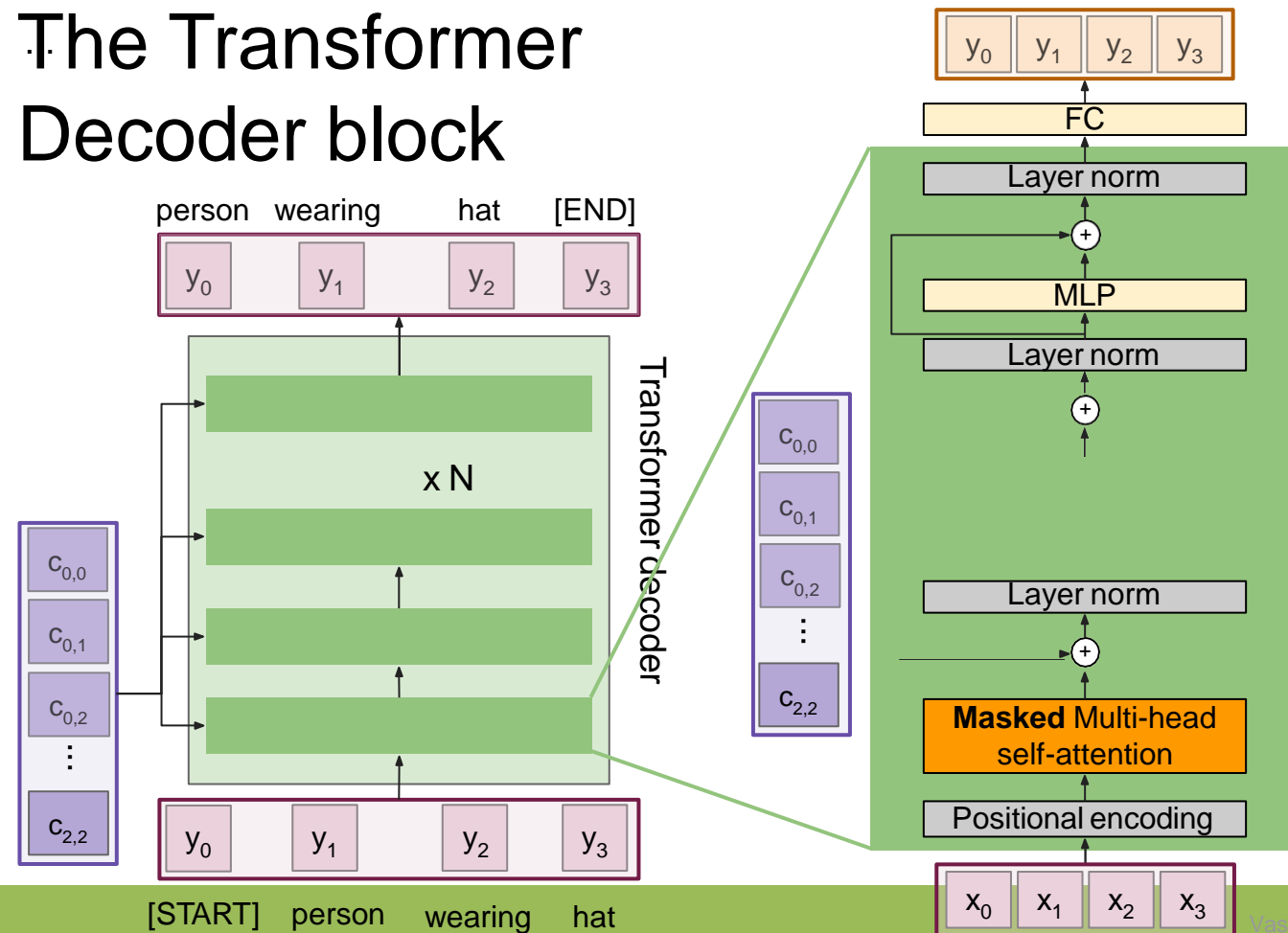
The Transformer decoder block



Let's dive into the transformer decoder block

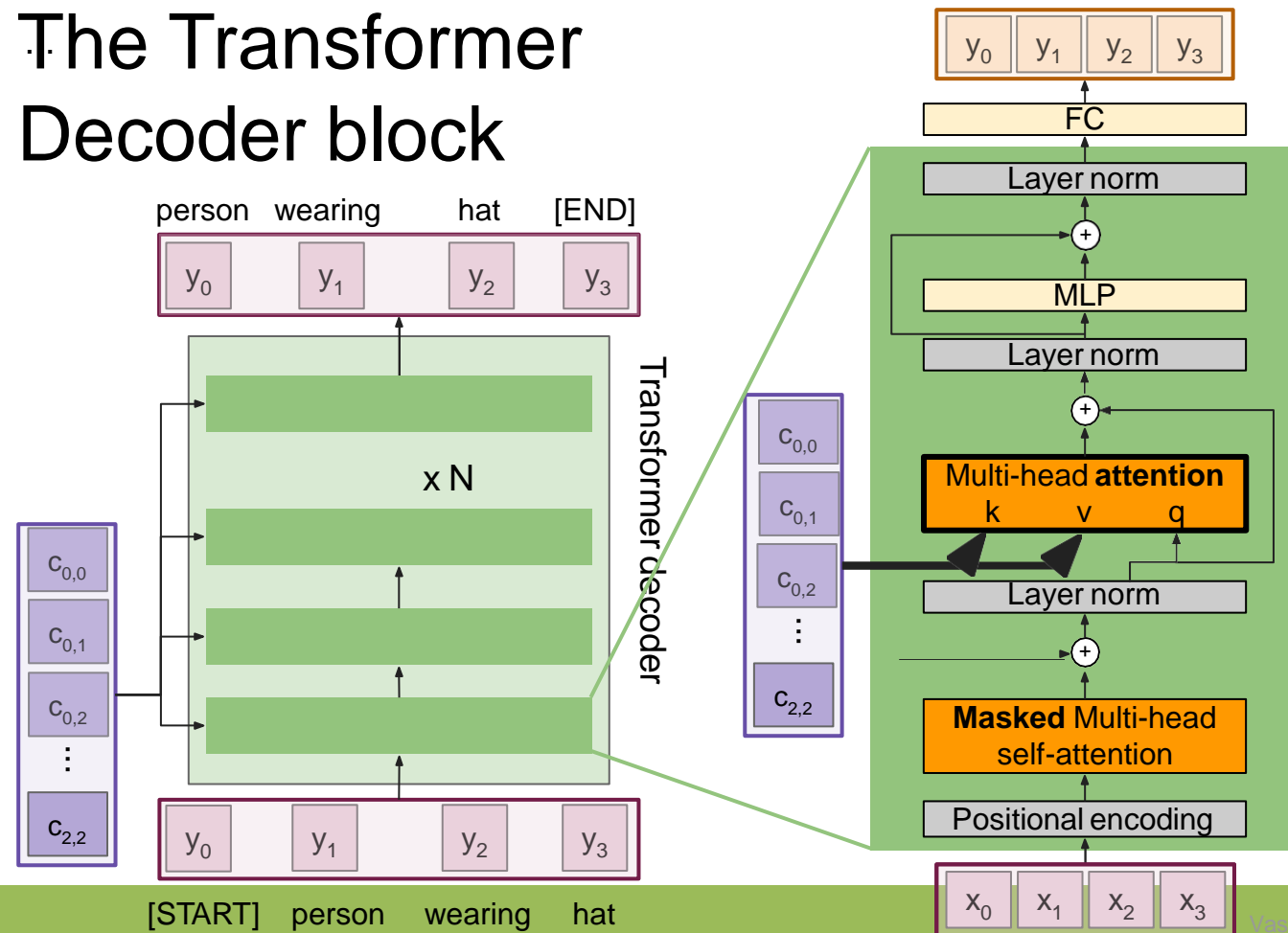
The Transformer

Decoder block



Most of the network is the same the transformer encoder.

The Transformer Decoder block

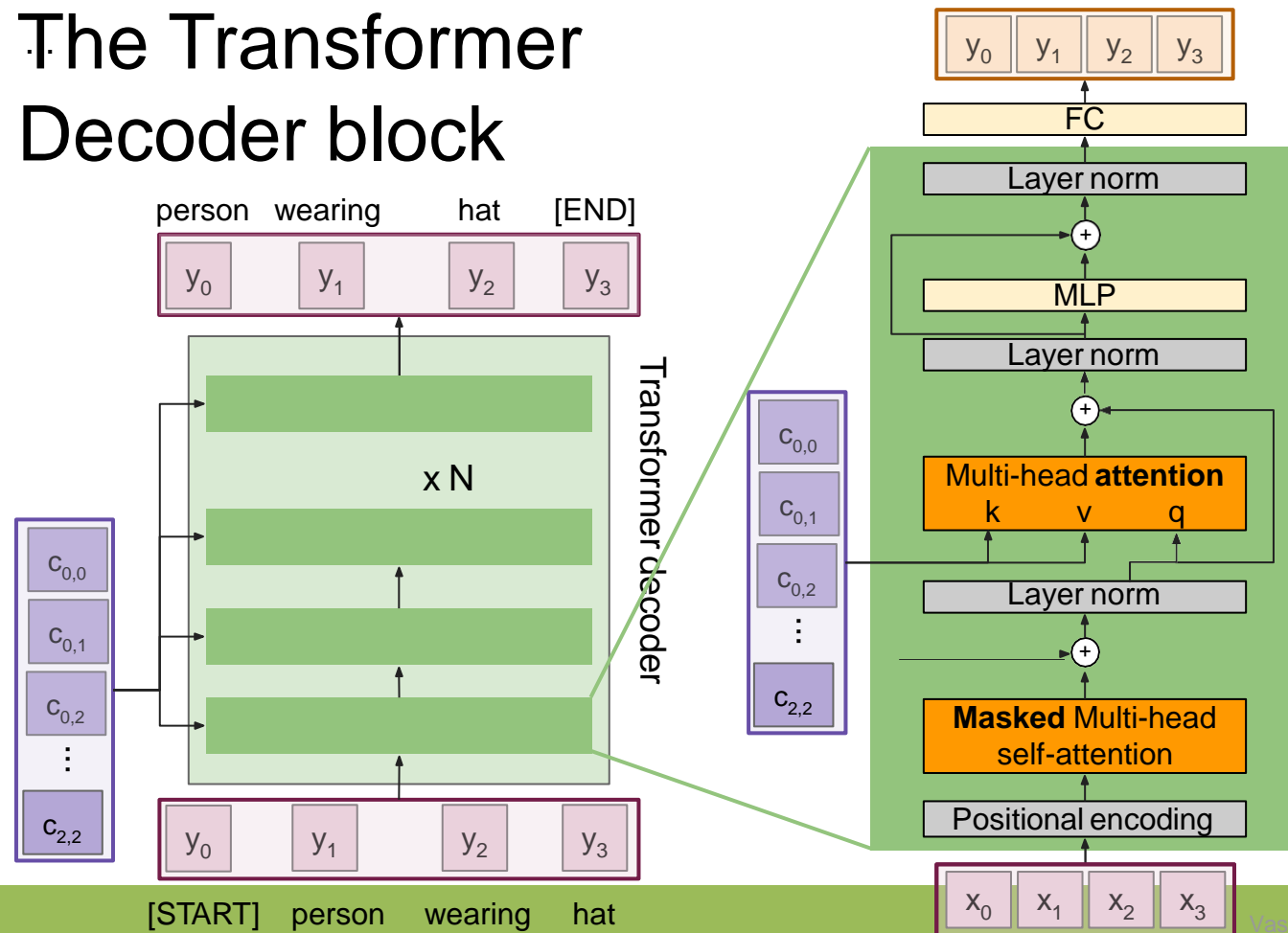


Multi-head attention block attends over the transformer encoder outputs.

For image captioning, this is how we inject image features into the decoder.

The Transformer

Decoder block



Transformer Decoder Block:

Inputs: Set of vectors \mathbf{x} and Set of context vectors \mathbf{c} .
Outputs: Set of vectors \mathbf{y} .

Masked Self-attention only interacts with past inputs.

Multi-head attention block is NOT self-attention. It attends over encoder outputs.

Highly scalable, highly parallelizable, but high memory usage.

Image Captioning using transformers

- No recurrence at all

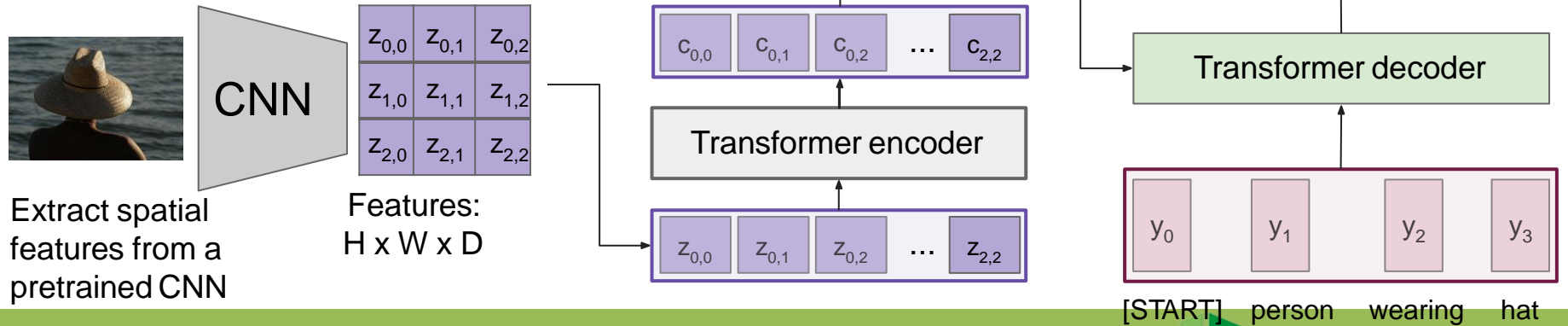


Image Captioning using transformers

- Perhaps we don't need convolutions at all?

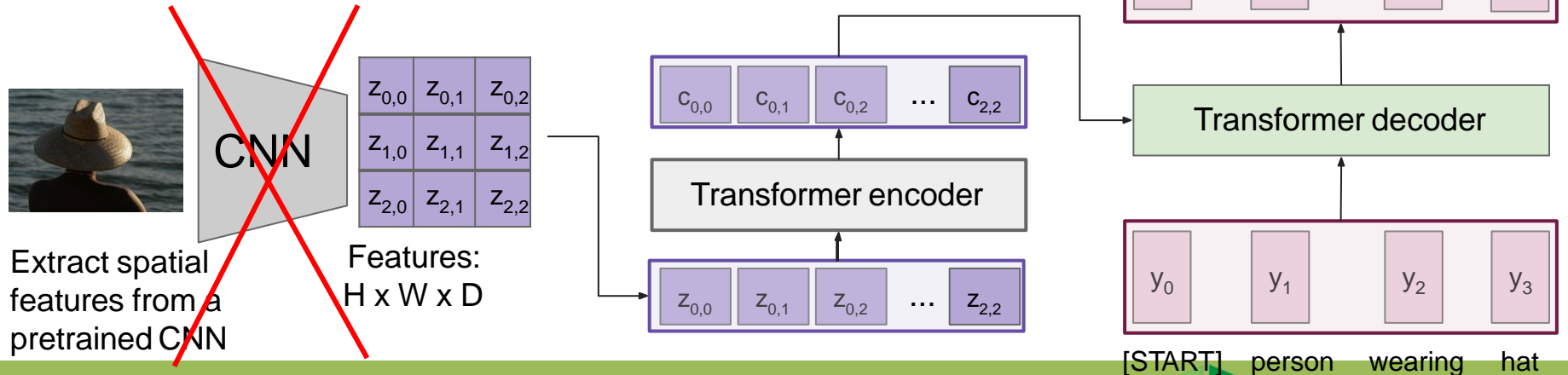
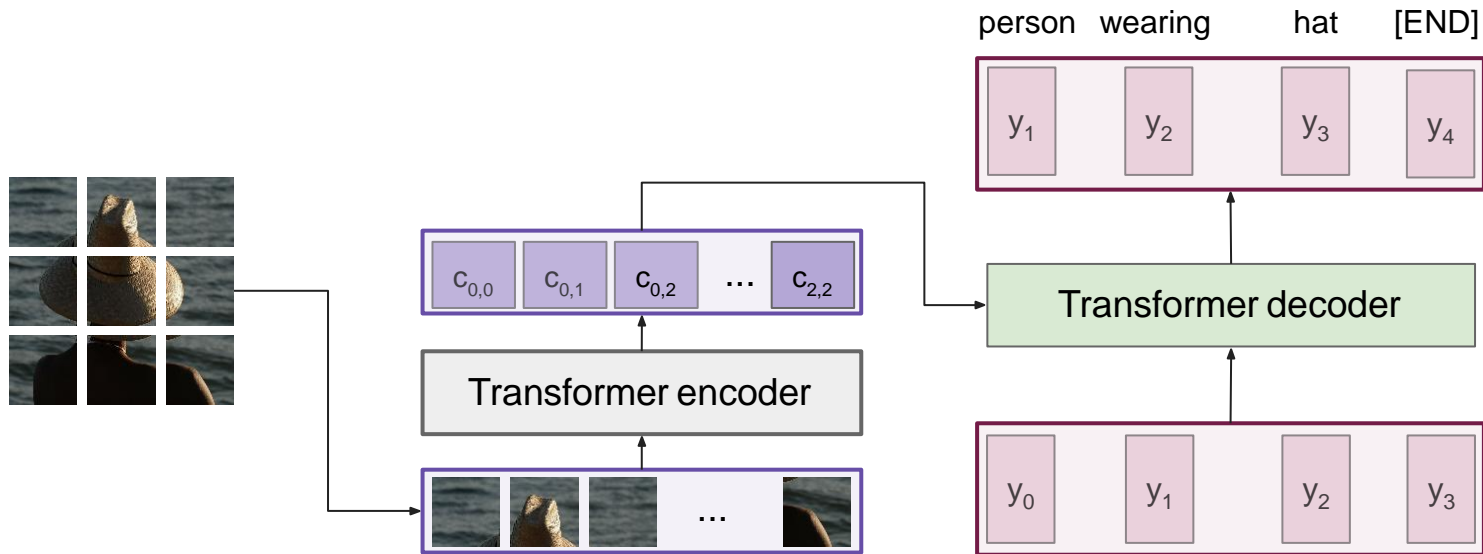


Image Captioning using **ONLY** transformers

- Transformers from pixels to language



Dosovitskiy et al, "An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale", ArXiv 2020
[Colab link](#) to an implementation of vision transformers

Attention and Transformers

Vision Transformers vs. ResNets

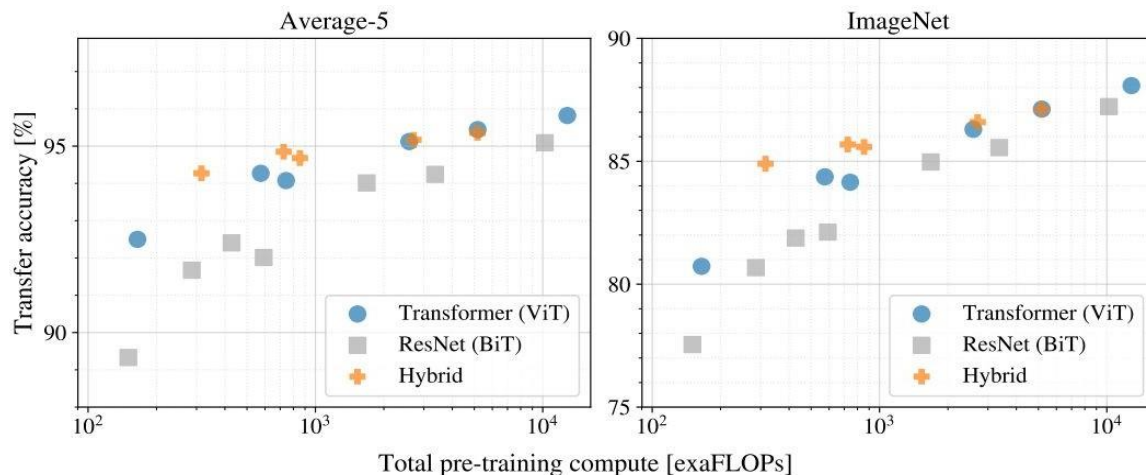
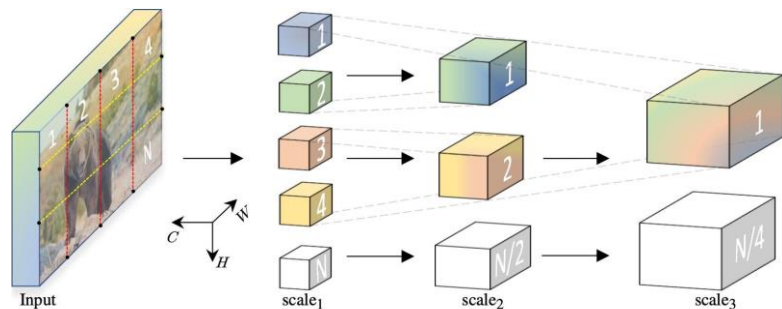
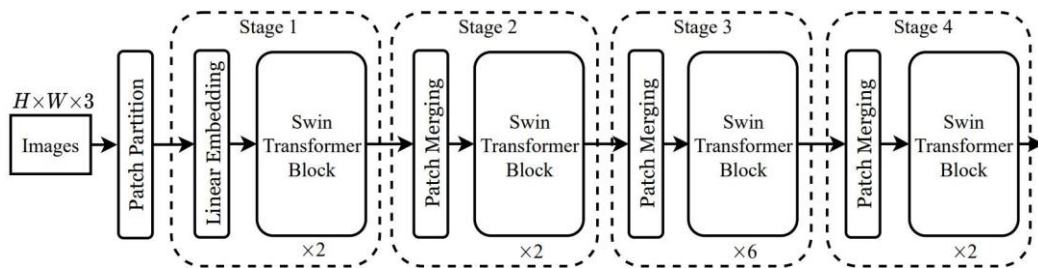


Figure 5: Performance versus cost for different architectures: Vision Transformers, ResNets, and hybrids. Vision Transformers generally outperform ResNets with the same computational budget. Hybrids improve upon pure Transformers for smaller model sizes, but the gap vanishes for larger models.

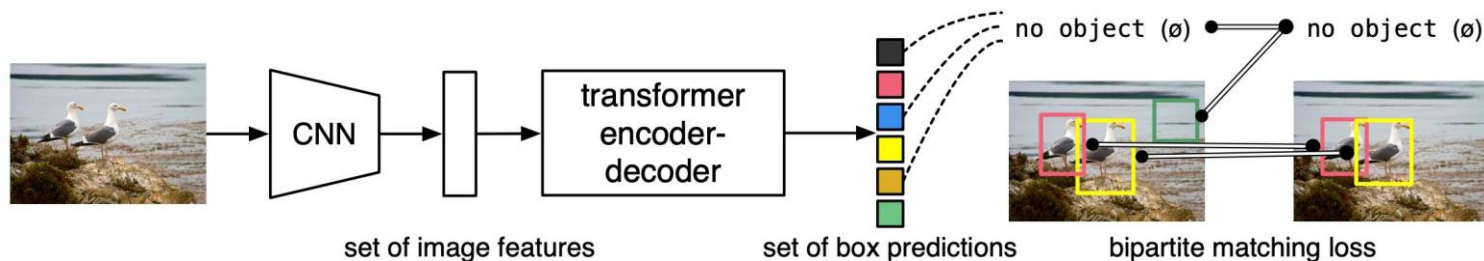
Vision Transformers



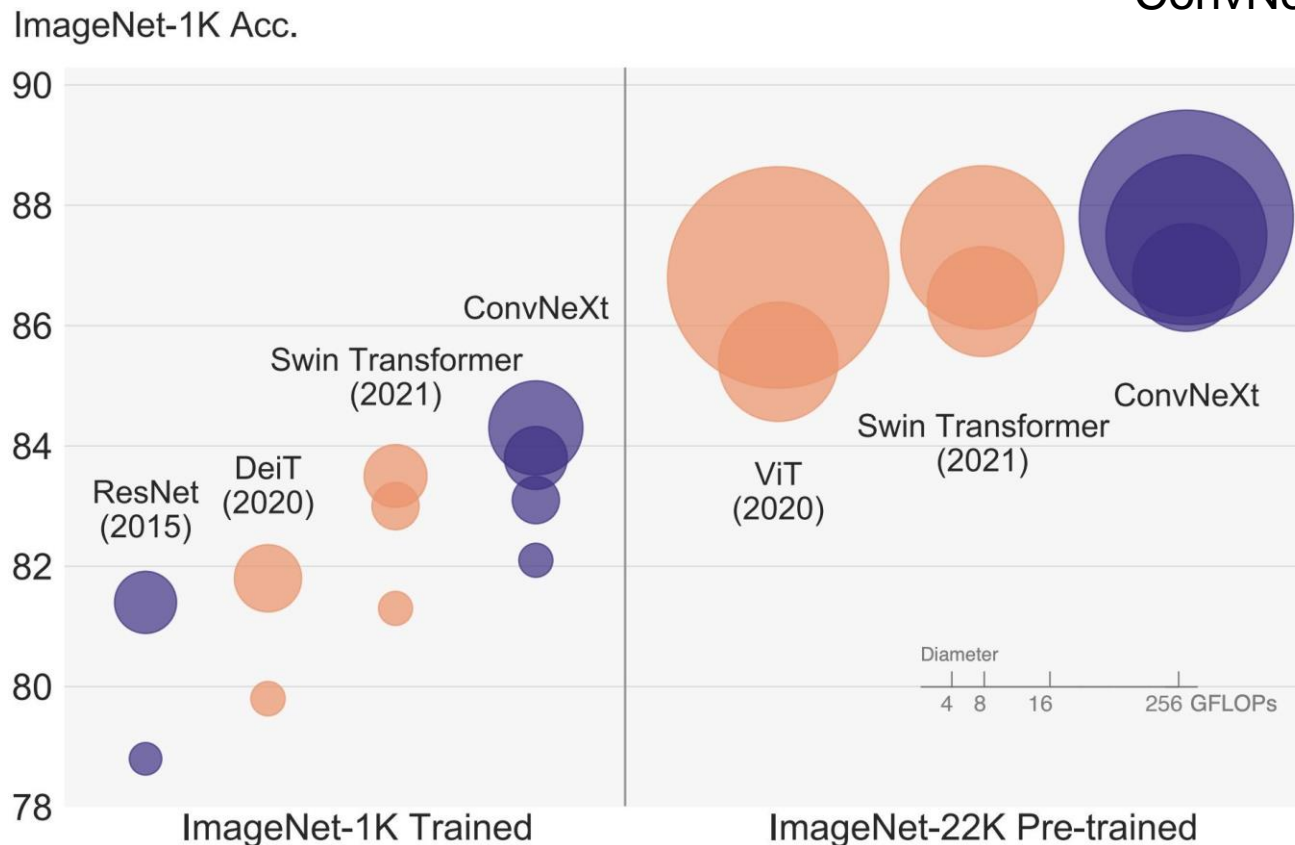
Fan et al, "Multiscale Vision Transformers", ICCV 2021



Liu et al, "Swin Transformer: Hierarchical Vision Transformer using Shifted Windows", CVPR 2021



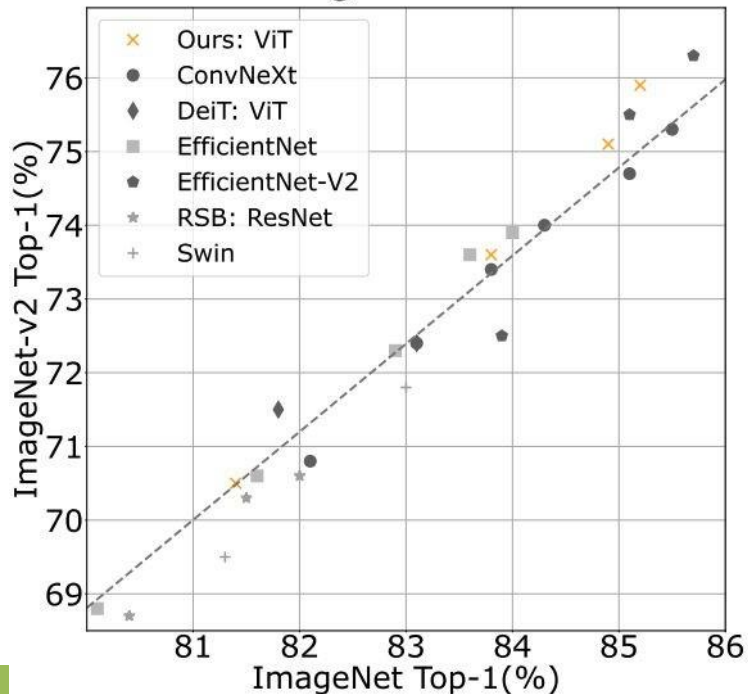
Carion et al, "End-to-End Object Detection with Transformers", ECCV 2020



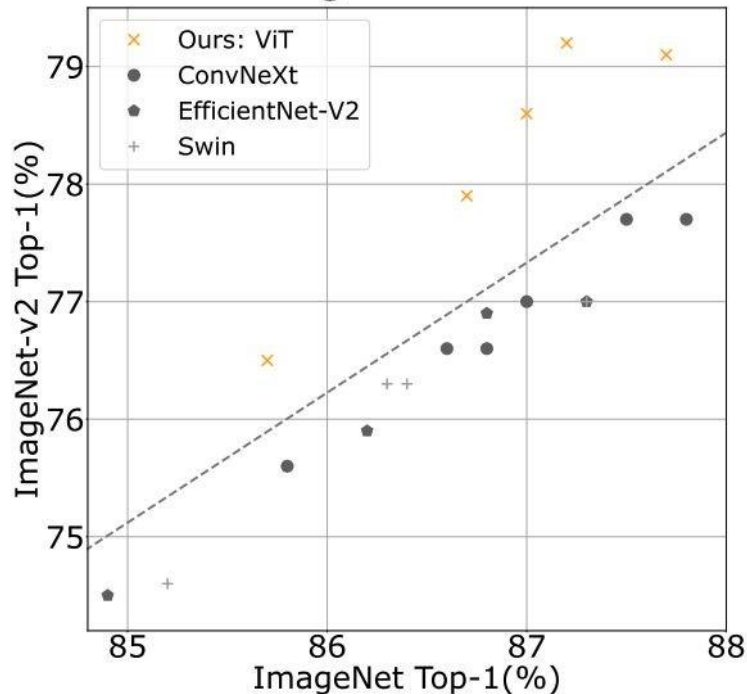
DeiT III: Revenge of the ViT

Hugo Touvron^{*,†} Matthieu Cord[†] Hervé Jégou^{*}

ImageNet-1k



ImageNet-21k



Summary

- Adding **attention** to RNNs allows them to "attend" to different parts of the input at every time step
- The **general attention layer** is a new type of layer that can be used to design new neural network architectures
- **Transformers** are a type of layer that uses **self-attention** and layer norm.
 - It is highly **scalable** and highly **parallelizable**
 - **Faster** training, **larger** models, **better** performance across vision and language tasks
 - They are quickly replacing RNNs, LSTMs, and may(?) even replace convolutions.

Next time: Video Understanding