

Mecânica Quântica

Sobreposição de estados

1-

$$P_{\uparrow} = |0,9|^2 = 0,81$$

$$P_{\downarrow} = |0,866|^2 = 0,75$$

2-

$$\begin{aligned} a^2 &= 1 - |0,1|^2 - |0,3i|^2 - |0,5|^2 - |0,4|^2 = \\ &= 1 - 0,01 - 0,09 - 0,25 - 0,16 = 0,49 \end{aligned}$$

3-

a) $\left|\frac{1}{2}\right|^2 \times 4 = 1$ Normalizado

b) $\left|\frac{1}{\sqrt{2}}\right|^2 \times 2 = 1$ Normalizado

c) $\left|\frac{1}{2}\right|^2 + \left|\frac{\sqrt{3}}{2}\right|^2 \times 2 = \frac{7}{4}$ Não normalizado

d) $|\cos \alpha|^2 + |\sin \alpha|^2 = 1$ Normalizado

4-

$$|A\uparrow\rangle, |A\downarrow\rangle, |A\leftarrow\rangle, |A\rightarrow\rangle, |B\uparrow\rangle, |B\downarrow\rangle, |B\leftarrow\rangle, |B\rightarrow\rangle$$

5-

a) $|0,55|^2 = 0,3025 \rightarrow |111\rangle$ Calcular todos e ver qual é maior

b) $P_{010} = |0,2|^2 = 0,04 \rightarrow$ Quando é x medidos em x sistemas idênticos
 $200 \times 0,04 = 8$

c) 20 ou 0 \rightarrow Quando é x medidos no mesmo sistema, ou calha x vezes ou 0

d) $|0,1|^2 + 0,25 + |0,2|^2 + |0,5|^2 = 0,55$

e) Sim $|110\rangle$

6-

$$a_H b_H = \frac{1}{\sqrt{2}}$$

$$a_H b_V = 0$$

$$a_H = \frac{1}{\sqrt{2}}$$

$$b_H = 1$$

$$b_V = 0$$

É entrelaçado

$$a_V b_H = 0$$

$$a_V b_V = \frac{1}{\sqrt{2}}$$

$$a_V = 0$$

$$a_V b_V \neq \frac{1}{\sqrt{2}}$$

8-

Estados de spin possíveis: $|+z\rangle$ e $|-z\rangle$ logo $P = 0,5$

7-

a) $a_H b_H = \frac{1}{2}$ $a_V b_H = \frac{1}{2}$ $a_H = b_H = \frac{1}{\sqrt{2}} = b_V = a_V$ logo não é entrelaçado

$a_H b_V = \frac{1}{2}$ $a_V b_V = \frac{1}{2}$

b) $a_H b_H = \frac{1}{2}$ $a_V b_H = \frac{1}{2}$ $a_H = b_H = \frac{1}{\sqrt{2}} = b_V = a_V$

$a_H b_V = \frac{1}{2}$ $a_V b_V = -\frac{1}{2}$ mas $\frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} \neq -\frac{1}{2}$ É entrelaçado

c) $a_H b_H = \frac{1}{2}$ $a_H b_V = 0$ $a_H = \frac{1}{\sqrt{2}} = b_H$ $b_V = 0$ É entrelaçado

$a_V b_H = \sqrt{\frac{3}{8}}$ $a_V b_V = \sqrt{\frac{3}{8}}$ $a_V = \frac{\sqrt{3}}{\sqrt{4}}$ $a_V b_V \neq \sqrt{\frac{3}{8}}$

d) $a_H b_H = \cos \alpha$ $a_V b_H = 0$

$a_H b_V = 0$ $a_V b_V = \sin \alpha$

É entrelaçado porque não existe a_V, a_H, b_H, b_V que satisfaça todas as condições

e) $a_H b_H = 0$ $a_V b_H = -\frac{1}{\sqrt{2}}$

$a_H b_V = \frac{1}{\sqrt{2}}$ $a_V b_V = 0$

Para que $a_H b_H = 0$, a_H ou b_H tem de ser 0
logo $a_H b_V = 0$ ou $a_V b_H = 0$
É entrelaçado

9-

a) $|S_z\rangle = \sqrt{\frac{2}{3}} |+_z\rangle - \sqrt{\frac{1}{3}} |-_z\rangle$

$|+_z\rangle = \frac{1}{\sqrt{2}} (|+_x\rangle + |-_x\rangle)$

$|-_z\rangle = -\frac{1}{\sqrt{2}} (|+_x\rangle - |-_x\rangle)$

$|S_z\rangle = \sqrt{\frac{2}{3}} \times \frac{1}{\sqrt{2}} (|+_x\rangle + |-_x\rangle) - \sqrt{\frac{1}{3}} \times \frac{1}{\sqrt{2}} (|+_x\rangle - |-_x\rangle)$ $P_{+_x} = 0,029$

$= \sqrt{\frac{2}{6}} (|+_x\rangle + |-_x\rangle) - \frac{1}{\sqrt{6}} (|+_x\rangle - |-_x\rangle)$

$= \sqrt{\frac{2}{6}} |+_x\rangle + \sqrt{\frac{2}{6}} |-_x\rangle - \frac{1}{\sqrt{6}} |+_x\rangle + \frac{1}{\sqrt{6}} |-_x\rangle$
 $= \left(\sqrt{\frac{2}{6}} - \frac{1}{\sqrt{6}}\right) |+_x\rangle + \left(\sqrt{\frac{2}{6}} + \frac{1}{\sqrt{6}}\right) |-_x\rangle$

$$b) |S_z\rangle = \sqrt{\frac{2}{3}} |+\rangle - \sqrt{\frac{1}{3}} |-\rangle$$

$$\begin{aligned} |S_z\rangle &= \sqrt{\frac{2}{3}} \times \frac{1}{\sqrt{2}} (|+\rangle + |-\rangle) - \sqrt{\frac{1}{3}} \times \frac{1}{i\sqrt{2}} (|+\rangle - |-\rangle) \\ &= \sqrt{\frac{2}{6}} |+\rangle + \sqrt{\frac{2}{6}} |-\rangle - \frac{1}{i\sqrt{6}} |+\rangle + \frac{1}{i\sqrt{6}} |-\rangle = \\ &= \left(\sqrt{\frac{2}{6}} - \frac{1}{i\sqrt{6}} \right) |+\rangle + \left(\sqrt{\frac{2}{6}} + \frac{1}{i\sqrt{6}} \right) |-\rangle \end{aligned}$$

$$P_{+y} = \left| \sqrt{\frac{2}{6}} - \frac{1}{i\sqrt{6}} \right|^2 = \frac{2}{6} + \frac{1}{6} = \frac{3}{6} = \frac{1}{2}$$

Relações de De Broglie

13-

$$a) p^2 = 2mE_c$$

$$p = \frac{h}{\lambda} \Rightarrow \lambda = \frac{h}{p} = \frac{h}{\sqrt{2m \times \frac{1}{2} m v^2}} = \frac{h}{\sqrt{m^2 v^2}} = \frac{6,63 \times 10^{-34}}{\sqrt{(9,11 \times 10^{-31})^2 \times 277,78^2}} = 2,62 \times 10^{-6} \text{ m}$$

$$1000 \text{ km/h} = \frac{1000}{3,6} = 277,78 \text{ m/s}$$

$$b) E_c = 10 \text{ keV} = 10 \times 1000 \times 1,6 \times 10^{-19} = 1,6 \times 10^{-15} \text{ J} \quad p^2 = 2mE_c + \frac{E_c^2}{c^2}$$

$$\lambda = \frac{6,63 \times 10^{-34}}{\sqrt{2 \times 9,11 \times 10^{-31} \times 1,6 \times 10^{-15} + \frac{(1,6 \times 10^{-15})^2}{(3 \times 10^8)^2}}} = 1,22 \times 10^{-11} \text{ m}$$

$$c) E_c = 30 \text{ keV} = 30 \times 10^3 \times 1,6 \times 10^{-19} = 4,8 \times 10^{-15} \text{ J}$$

$$\lambda = \frac{6,63 \times 10^{-34}}{\sqrt{2 \times 9,11 \times 10^{-31} \times 4,8 \times 10^{-15} + \frac{(4,8 \times 10^{-15})^2}{(3 \times 10^8)^2}}} = 6,99 \times 10^{-12}$$

$$d) E_c = 15 \text{ GeV} = 15 \times 10^9 \times 1,6 \times 10^{-19} =$$

14-

$$\lambda = 5890 \text{ \AA} = 5890 \times 10^{-10} \text{ m}$$

$$\lambda = \frac{h}{p} \quad \text{e} \quad p = \frac{6,63 \times 10^{-34}}{5890 \times 10^{-10}} = 1,13 \times 10^{-27}$$

$$p^2 = 2m E_c \quad \Leftrightarrow \quad E_c = \frac{p^2}{2m} = \frac{(1,13 \times 10^{-27})^2}{2 \times 9,11 \times 10^{-31}} = 7,01 \times 10^{-25} \text{ J} = 4,38 \times 10^{-6} \text{ eV}$$

15-

$$\lambda = 2,0 \text{ \AA} = 2 \times 10^{-10} \text{ m} \quad \text{Elétron NÃO tem velocidade relativística}$$

$$a) \quad p = \frac{h}{\lambda} = \frac{6,63 \times 10^{-34}}{2 \times 10^{-10}} = 3,315 \times 10^{-24} \text{ kg m/s}$$

b) $E_c \text{ total ?}$

$$\text{Elétron} \quad E_c = \frac{p^2}{2m} = \frac{(3,315 \times 10^{-24})^2}{2(9,11 \times 10^{-31})} = 6,03 \times 10^{-18} \text{ J}$$

fóton

$$p^2 = 2m E_c + \frac{E_c^2}{c^2} \quad \text{e} \quad E_c = \sqrt{p^2 c^2} \quad \text{e} \quad E_c = pc, \quad p c > 0$$

$$\text{e} \quad E_c = 3,315 \times 10^{-24} \times 3 \times 10^8 = 9,945 \times 10^{-16} \text{ J}$$

$$E_{c \text{ total}} = 9,945 \times 10^{-16} + 6,03 \times 10^{-18} = 1 \times 10^{-15} \text{ J}$$

c) $E_{c f} > E_{c e}$

16-

$$n(\text{Partícula NÃO relativística}) = 3 n_e$$

$$\frac{\lambda_p}{\lambda_e} = 1,813 \times 10^{-4}$$

$$\frac{\lambda_p}{\lambda_e} = \frac{\frac{h}{p_p}}{\frac{h}{p_e}} = \frac{p_e}{p_p} = \frac{m_e n_e}{m_p n_p} = \frac{9,11 \times 10^{-31} \times 1}{m_p \times 3} = 1,813 \times 10^{-4}$$

$$\text{e} \quad m_p = \frac{9,11 \times 10^{-31}}{3 \times 1,813 \times 10^{-4}} = 1,67 \times 10^{-27} \text{ kg}$$

Neutrão

17-

$$E_c = \frac{3}{2} k_B T \quad T = 300 \text{ K} \quad k_B = 1,38 \times 10^{-23} \text{ J/K}$$

Estão em equilíbrio térmico

$$a) E_c = \frac{3}{2} \times 1,38 \times 10^{-23} \times 300 = 6,21 \times 10^{-21} \text{ J} = \frac{6,21 \times 10^{-21}}{1,6 \times 10^{-19}} \text{ eV} = 0,0388 \text{ eV}$$

$$b) \lambda = \frac{h}{p} = \frac{6,63 \times 10^{-34}}{\sqrt{2,07414 \times 10^{-47}}} = 1,46 \times 10^{-10} \text{ m}$$

$$p^2 = 2m E_c = 2 \times 1,67 \times 10^{-27} \times 6,21 \times 10^{-21} = 2,07414 \times 10^{-47}$$

18-

$$E_{cp} = m$$

$$\lambda = 1,7898 \times 10^{-6} \text{ Å} = 1,7898 \times 10^{-16} \text{ m}$$

Se $2E_c$, λ ?

$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2mE_c}} = \frac{h}{\sqrt{2E_c^2}} = \frac{h}{E_c \sqrt{2}}, E_c > 0$$

$$\lambda_2 = \frac{h}{2E_c \sqrt{2}} = \frac{1}{2} \times \lambda = \frac{1}{2} \times 1,7898 \times 10^{-16} = 8,949 \times 10^{-17} \text{ m}$$

19- Relativística acelerador de partículas elétricas

$$E_c = 50 \text{ GeV} = 50 \times 10^9 \times 1,6 \times 10^{-19} = 8 \times 10^{-9} \text{ J}$$

$$p^2 = 2mE_c + \frac{E_c^2}{c^2} \quad \Leftrightarrow$$

$$\text{ou } p = \sqrt{\frac{2mE_c + \frac{E_c^2}{c^2}}{c^2}}, p > 0 = \sqrt{\frac{2 \times 9,11 \times 10^{-31} \times 8 \times 10^{-9} + \frac{(8 \times 10^{-9})^2}{(3 \times 10^8)^2}}{(3 \times 10^8)^2}} = 2,67 \times 10^{-17}$$

$$\lambda = \frac{h}{p} = \frac{6,63 \times 10^{-34}}{2,67 \times 10^{-17}} = 2,48 \times 10^{-17} \text{ m}$$

Função de onda

20- $\psi(x) = \frac{1}{\pi} \frac{\sin(x)}{x}$

p a)

$$|\psi(0)|^2 = \left| \frac{1}{\pi} \times \frac{\sin 0}{0} \right|^2 = \frac{1}{\pi^2}$$

b) $|\psi(5)|^2 = \left| \frac{1}{\pi} \times \frac{\sin 5}{5} \right|^2 = 3,72 \times 10^{-3}$

21-

$$\psi(x) = A \sin\left(\frac{n\pi}{a} x\right)$$

a) $\int |\psi(x)|^2 dx = 1$

$$\int_0^a |\psi(x)|^2 dx = \int_0^a A^2 \sin^2\left(\frac{n\pi}{a} x\right) dx$$

$$= A^2 \int_0^a \sin^2\left(\frac{n\pi}{a} x\right) dx = A^2 \left[\frac{x}{2} - \frac{1}{\frac{4n\pi}{a}} \sin\left(\frac{2n\pi}{a} x\right) \right]_0^a$$

$$= A^2 \left(\frac{a}{2} - \frac{a}{4n\pi} \sin\left(\frac{2n\pi}{a} a\right) \right) = A^2 \left(\frac{a}{2} - \frac{a}{4n\pi} \overbrace{\sin(2n\pi)}^0 \right) =$$

$$A^2 \left(\frac{a}{2} \right) = 1 \quad \text{em} \quad A^2 = \frac{2}{a} \quad \text{em} \quad A = \sqrt{\frac{2}{a}}, \quad A > 0$$

b) $\psi(x) = \sqrt{\frac{2}{a}} \sin\left(\frac{n\pi}{a} x\right)$

$$P_m\left(\frac{a}{2}\right) = \left| \psi\left(\frac{a}{2}\right) \right|^2 = \frac{2}{a} \sin^2\left(\frac{n\pi}{a} \times \frac{a}{2}\right) = \frac{2}{a} \sin^2\left(\frac{n\pi}{2}\right)$$

c) $p^2 = 2m E_c \quad \text{em} \quad E_c = \frac{p^2}{2m}$

$$E_c = \frac{(\hbar k)^2}{2m} = \frac{\hbar^2 \left(\frac{n\pi}{a}\right)^2}{2m} = \frac{\hbar^2 m^2 \pi^2}{2m a^2}$$

22-

$$P = e^{-2\alpha L}$$

$L \rightarrow$ comprimento da barreira

$$\alpha = \sqrt{\frac{2m(U-E)}{\hbar^2}}$$

$$P? \quad E_e = 0,5 \text{ eV} = 8 \times 10^{-20} \text{ J}$$

$$U = 3 \text{ eV} = 4,8 \times 10^{-19} \text{ J} \quad L = 1 \text{ nm} = 1 \times 10^{-9} \text{ m}$$

$$\alpha = \sqrt{\frac{2 \times 9,11 \times 10^{-31} (4,8 \times 10^{-19} - 8 \times 10^{-20})}{(6,63 \times 10^{-34})^2}} = 80904098,31$$

$$P = e^{-2\alpha \times 10^{-9}} = 9,39203 \times 10^{-8}$$

11-

$$\hat{H} |0\rangle = \frac{1}{\sqrt{2}} (|10\rangle + |11\rangle)$$

$$\hat{H} |1\rangle = \frac{1}{\sqrt{2}} (|10\rangle - |11\rangle)$$

$$|\psi\rangle = \frac{1}{\sqrt{2}} (|101\rangle + |1010\rangle)$$

Só aplica no 2 qubit
e mantém os outros

$$\begin{aligned} \hat{H} \left(\frac{1}{\sqrt{2}} (|101\rangle + |1010\rangle) \right) &= \frac{1}{\sqrt{2}} \left(\frac{1}{\sqrt{2}} (|1101\rangle + |1111\rangle) + \frac{1}{\sqrt{2}} (|1000\rangle - |1010\rangle) \right) \\ &= \frac{1}{2} (|1101\rangle + |1111\rangle + |1000\rangle - |1010\rangle) \end{aligned}$$

10-

$$\psi = a|0\rangle + b|1\rangle \quad \text{com } |a|^2 + |b|^2 = 1$$

$$\psi_1 = \hat{H}(\psi) = a \left(\frac{1}{\sqrt{2}} (|10\rangle + |11\rangle) \right) + b \left(\frac{1}{\sqrt{2}} (|10\rangle - |11\rangle) \right)$$

$$\hat{H}(\psi_1) = a \left(\frac{1}{\sqrt{2}} \left(\frac{1}{\sqrt{2}} (|10\rangle + |11\rangle) + \frac{1}{\sqrt{2}} (|10\rangle - |11\rangle) \right) \right) + b \left(\frac{1}{\sqrt{2}} \left(\frac{1}{\sqrt{2}} (|10\rangle + |11\rangle) - \frac{1}{\sqrt{2}} (|10\rangle - |11\rangle) \right) \right)$$

feito os cálculos = $a|0\rangle + b|1\rangle = \psi$ logo é unário

$$\hat{X} |0\rangle = |1\rangle$$

$$\hat{X} |1\rangle = |0\rangle$$

$$\psi_1 = \hat{H}(\psi) = a|1\rangle + b|0\rangle$$

$$\hat{H}(\psi_1) = a|0\rangle + b|1\rangle = \psi \text{ logo } \hat{H} \text{ é unitário}$$

23- deu diferente mas
verifiquei e tá certo

$$\Delta x \Delta p \geq \frac{\hbar}{2}$$

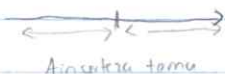
$$5 \times 10^{-9} \cdot \Delta p \geq \frac{\hbar}{2}$$

$$5 \text{ mm} = 5 \times 10^{-9} \text{ m}$$

$$\text{em } \Delta p \geq 1,055 \times 10^{-26}$$

$$x = (2,5 \pm 2,5) \text{ mm}$$

$$\text{em } \Delta v \geq 1,055 \times 10^{-26}$$



A largura da fenda

Sempre o valor maior entra

para que ele seja mínimo

tem que estar o metade

$$\text{em } \Delta v \geq 11582,84602 \text{ m/s}$$

$$\delta = \frac{\Delta v}{v} = \frac{0,1}{100} \text{ em } v = 1000 \Delta v$$

$$\text{em } v = 1,16 \times 10^7$$

24-

$$\frac{\Delta \lambda}{\lambda} = 10^{-7}$$

$$\Delta \lambda \Delta x = \frac{\lambda^2}{4\pi} \text{ em } \Delta x = \frac{\lambda^2}{\Delta \lambda 4\pi} = \frac{\lambda}{\Delta \lambda} \times \frac{\lambda}{4\pi}$$

$$\text{a) } 10^{-7} \times \frac{5 \times 10^{-4}}{4\pi} = 3,98 \times 10^{-12} \text{ \AA}$$

$$\text{b) } 10^{-7} \times \frac{5}{4\pi} = 3,98 \times 10^{-8} \text{ \AA}$$

$$\text{c) } 10^{-7} \times \frac{5000}{4\pi} = 3,98 \times 10^{-5} \text{ \AA}$$

25-

$$\lambda = 800 \pm 5 \text{ nm}$$

$$\Delta \lambda = 10 \times 10^{-9} \text{ m}$$

$$\lambda = 800 \times 10^{-9} \text{ m}$$

$$\Delta \lambda \Delta t = \frac{\lambda^2}{4\pi c}$$

$$\Delta t = \frac{\lambda^2}{4\pi c \Delta \lambda} = \frac{(800 \times 10^{-9})^2}{4\pi \times 3 \times 10^8 \times 10 \times 10^{-9}} = 1,6977 \times 10^{-14}$$

$$1 \text{ s} = 1 \times 10^{15} \text{ fs} \longrightarrow 1,697 \times 10^{-14} \times 10^{15} = 16,98 \text{ fs}$$

26-

$$\boxed{\Delta E \Delta t \geq \frac{\hbar}{2}} \quad \Delta E \geq \frac{\frac{\hbar}{2}}{\frac{\Delta t}{1}} \quad \Delta E \geq \frac{6,67 \times 10^{-34}}{2\pi \cdot 2 \times 10^{-12}} \quad \Delta E \geq 5,30 \times 10^{-23} \text{ J}$$

27-

$$\Delta t_1 = 1,2 \times 10^{-8} \text{ s}$$

$$\Delta t_2 = 2,3 \times 10^{-8} \text{ s}$$

$$\Delta E_1 \Delta t_1 \geq \frac{\hbar}{2} \quad \Delta E_1 \geq \frac{6,67 \times 10^{-34}}{2\pi \cdot 1,2 \times 10^{-8}} \quad \Delta E_1 \geq 4,42 \times 10^{-27} \text{ J}$$

$$\Delta E_2 \Delta t_2 \geq \frac{\hbar}{2} \quad \Delta E_2 \geq \frac{6,67 \times 10^{-34}}{2\pi \cdot 2,3 \times 10^{-8}} \quad \Delta E_2 \geq 2,31 \times 10^{-27} \text{ J}$$

$$\Delta E = \Delta E_2 + \Delta E_1 = 6,73 \times 10^{-27} \text{ J} = \frac{6,73 \times 10^{-27}}{1,6 \times 10^{-19}} \text{ eV} = 4,21 \times 10^{-8} \text{ eV}$$

Transições

29-

$$n=2 \rightarrow E_2 = (-13,6 \text{ eV}) \frac{1}{2^2} = -3,4 \text{ eV}$$

$$n=1 \rightarrow -13,6 \text{ eV}$$

$$n=3 \rightarrow E_3 = (-13,6 \text{ eV}) \frac{1}{3^2} = -1,51 \text{ eV}$$

$$n=4 \rightarrow E_4 = (-13,6 \text{ eV}) \frac{1}{4^2} = -0,85 \text{ eV}$$

$$\text{De } n=1 \text{ para } n=2 \rightarrow |E_2 - E_1| = -3,4 + 13,6 = 10,2 \text{ eV}$$

$$\text{De } n=1 \text{ para } n=3 \rightarrow |E_3 - E_1| = -1,51 + 13,6 = 12,09 \text{ eV}$$

$$\text{De } n=1 \text{ para } n=4 \rightarrow |E_4 - E_1| = -0,85 + 13,6 = 12,75 \text{ eV}$$

30-

$$a \rightarrow \text{largura do poço} = 1 \text{ nm} = 1 \times 10^{-9} \text{ m}$$

n é um inteiro

$$\boxed{E = \hbar f}$$

$$E_n = \frac{n^2 \pi^2 \hbar^2}{2ma^2}$$

$$m=4 \rightarrow E_4 = \frac{4^2 \pi^2 \hbar^2}{2 \times 9,11 \times 10^{-31} \times (9 \times 10^{-9})^2} = 9,65 \times 10^{-19} \text{ J}$$

$$m=3 \rightarrow E_3 = 5,428 \times 10^{-19} \text{ J}$$

$$m=2 \rightarrow E_2 = 2,41 \times 10^{-19} \text{ J}$$

$$\Delta E \text{ entre } m=4 \text{ e } m=3 = |E_3 - E_4| = -4,222 \times 10^{-19} \text{ J}$$

$$f = \frac{E}{h} = 6,37 \times 10^{14} \text{ Hz}$$

$$\Delta E \text{ entre } m=4 \text{ e } m=2 = |E_2 - E_4| = 7,24 \times 10^{-19}$$

$$f = \frac{E}{h} = 1,09 \times 10^{15} \text{ Hz}$$

31 -

$$\omega_c = \sqrt{\frac{K}{m}} \quad E_m = \left(m + \frac{1}{2}\right) \hbar \omega_c$$

$$\omega_c = \sqrt{\frac{K}{2m}} \quad \omega_c' = \sqrt{\frac{K}{2m}} = \frac{1}{\sqrt{2}} \times \frac{\sqrt{K}}{\sqrt{m}} = \frac{1}{\sqrt{2}} \omega_c = \frac{\omega_c}{\sqrt{2}}$$

Corpo negro

32 -

$$T = 10^6 \text{ K}$$

$b \rightarrow$ constante

$$\lambda_{\text{max}} T = b \rightarrow 2,898 \times 10^{-3}$$

$$\boxed{\lambda_{\text{max}} T = b}$$

$$\lambda_{\text{max}} = \frac{b}{T} = \frac{2,898 \times 10^{-3}}{10^6} = 2,898 \times 10^{-9} \text{ m} = 2,898 \text{ nm}$$

33 -

$$\lambda = 100 \text{ \AA}$$

$$\lambda_{\text{max}} = \frac{b}{T} \text{ ou } T = \frac{b}{\lambda_{\text{max}}} = \frac{2,898 \times 10^{-3}}{100 \times 10^{-10}} = 289800 \text{ K}$$

35-

$$T = 2500 \text{ K}$$

$$\lambda_{\text{max}} = ?$$

$$\lambda_{\text{máx.}} = \frac{b}{T} = \frac{2,898 \times 10^{-3}}{2500} = 1,16 \times 10^{-6} \text{ m} \rightarrow \text{Não está na parte visível, está na parte do infravermelho}$$