— Module KnightsKnaves -

 ${\tt https://www.reddit.com/r/scala/comments/6} kpqqw/knights_and_knaves/$

CONSTANT Native

Constants Knight, Knave

ASSUME $KnightOrKnave \stackrel{\Delta}{=} Knight \cup Knave = Native \land Knight \cap Knave = \{\}$

 $\begin{array}{ccc} \mathit{Lying}(p) & \stackrel{\triangle}{=} & p \in \mathit{Knave} \\ \mathit{Truthful}(p) & \stackrel{\triangle}{=} & p \in \mathit{Knight} \end{array}$

 $p :> statement \stackrel{\triangle}{=} Truthful(p) \equiv statement p says$

Problem 1

Constants A, B, C

Assume ABC-Natives $\stackrel{\triangle}{=} \{A, B, C\} \subseteq Native$

 $\begin{array}{ll} \text{Assume } B_Says \ \stackrel{\triangle}{=} \ B :> (A :> (A \in Knave)) \\ \text{Assume } C_Says \ \stackrel{\triangle}{=} \ C :> Lying(B) \end{array}$

Theorem $C \in Knight$

PROOF BY KnightOrKnave, ABC_Natives, B_Says, C_Says DEF: >, Lying, Truthful