BMEG 802 – Advanced Biomedical Experimental Design and Analysis

Repeated Measures (Within) Analysis of Variance (ANOVA)

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Recap

- Two-Way ANOVA
 - linear model approach
 - interpret main effects and interactions
 - follow up mean comparisons
- n-Way ANOVA
 - general concepts
 - limitations

Today

- 1-Way Repeated Measures ("within" subjects) Design
 - Repeated Meaures ANOVA
 - Greenhouse-Geisser Corrections
 - Multivariate Approach
 - Friedman Test
- 2-Way Repeated Measures
 - Repeated Meaures ANOVA
 - Greenhouse-Geisser Corrections
 - Multivariate Approach

Repeated Measures (Within) ANOVA

- each individual (or culture, etc) contributes a score for each level of a factor
- each individual contribures multiple scores (e.g., pre vs post tests)
 - paired differences between time points
- individuals serve as their own control
- variance between different conditions is no longer due to [effect + between-group sampling variance] multiple tests on the same individual, cell culture, etc.
- it's the same group of subjects! there is no "between- group" sampling variance
- variance only due to the effect

Examples of a Within Design

- 1. effects of placebo, drug A and drug B can be studied in the same subjects; each subject can serve as their own control
- 2. behaviour of a culture studied over time; a measurement can be taken from the same culture at multiple time points

Advantages of Repeated Measures Designs

- 1. more information is obtained from each subject than in a between-subjects design
- within-subjects design: each subject contributes a scores (a is the number of conditions tested)
- between-subjects design: each subject contributes only one score
- # of subjects needed to reach a given level of statistical power is often much lower with within-subjects designs
- 2. variability in individual differences between subjects is totally removed from the error term
- 3. each subject serves as his/her own control
- 4. error term is reduced
- 5. statistical power increases (few participants needed)

General Linear Model (GLM)

Let's develop a full and restricted model.

Full Model: $Y_{ij} = \mu + \alpha_j + \pi_i + \epsilon_{i,j}$

Restricted Model: $Y_{ij} = \mu + \pi_i + \epsilon_{i,j}$

Effect of Factor

Effect of Subjects

- restricted model only includes effect of subjects (effect of factor is zero)
- so the difference here compared to regular "between- subjects" models is simply the inclusion of terms accounting for the effects of subjects
- remember: the more variance you can account for, the smaller the error term, the higher the F value, and the more powerful the statistical test

Defining Error and DF For the General Case

just as always, we can compute an F statistic based on Error for the full model and Error for the restricted model:

$$F = rac{(E_{restricted} - E_{full})/(df_{restricted} - df_{full})}{(E_{full}/df_{full})}$$
 $df_{full} = (n-1)(a-1)$ $df_{restricted} = n(a-1)$

$$df_{restricted} - df_{full} = (a-1)$$

see Chapter 11 of Maxwell, Delaney, and Kelley for (the complicated) calculations of $E_{restricted}$ and E_{full}

Assumptions of Repeated Measures ANOVA

- random sampling from population
- independence of subjects
- normality
- homogeneity of treatment-difference variances
 - variance of difference scores between any two levels of a factor must be equal to variance of differences scores between all other pairs of levels of the factor
 - equivalent to showing that the population covariance matrix has a certain form, that
 is, it displays the property of sphericity
 - this is all very mathematical and we don't need to know the details
 - fortunately there is (1) a test to see if we have violated the assumption, and (2) a method to correct for violations

Homogeneity of Treatment-Difference Variances

- Within ANOVA very sensitive and often violates sphericity
- We will see how to perform a test of sphericity in R
- R will report a number of corrected versions of the F test assuming sphericity is violated
- "Greenhouse-Geisser" adjustment adjusts the degrees of freedom (reducing them) so that Fcrit is larger (more conservative test)
- many people use G-G
- others like Huynh-Feldt because it's slightly less conservative

Disadvantages of Repeated Measures Designs

- Position Effect
 - When an observed response differs due to order of treatment
 - Must randomize the sequence of treatments or counterbalance
- Carry-over effect:
 - When an observed response is actually due to residual effect of a previous treatment
 - Must allow sufficient time ("washout period") and a controlled amount of time between treatments
 - Can't always control with counterbalancing since some effects are permanent (e.g., learning, memory, etc.)
 - Some scientific questions are better suited to between-subjects designs

Experimental Design Considerations

Counterbalancing

- counterbalance the order in which treatments are administered
- e.g., Drug A then Drug B to half the participants. Drug B then Drug A to the other half
- Participants are randomly assigned to each group
- Known as a "crossover design"
- Counterbalance an experiment with more than two levels? (e.g. 4)
- there are actually 24 different orderings of 4 conditions
- we would need 24 subjects to represent each order only once (4! = 4x3x2x1)

Experimental Design Considerations

Two alternatives:

- randomize the order for each subject; order effects will be controlled for "in the long run"
- Latin Square Designs: an arrangement of conditions so that each condition appears exactly once in each possible order

Order								
Ss	_	2	3	4				
ı	Α	В	U	D				
2	В	U	D	Α				
3	C	D	Α	В				
4	D	Α	В	С				

Three Group Example in R

Let's determine if there is a main effect of physical therapy treatment over time. Lower values represent pain level out of 10.

Subject	Treatment 1	Treatment 2	Treatment 3	Treatment 4
S1	8	10	7	5
S2	9	9	8	6
S3	7	5	8	4
S4	9	6	5	7
S5	8	7	7	6
S6	5	4	4	3
S7	7	6	5	4
S8	8	8	6	6
S9	9	8	6	5
S10	7	7	4	5

$$H_0: \alpha_1 = \alpha_2 = \alpha_3 = \alpha_4$$

Restricted Model:
$$Y_{ij} = \mu + \pi_i + \epsilon_{i,j}$$

$$H_1: \alpha_1 \neq \alpha_2 \neq \alpha_3 \neq \alpha_4$$

Full Model:
$$Y_{ij} = \mu + \alpha_j + \pi_i + \epsilon_{i,j}$$

Four Treatment Group Example

Four Treatment Group Example

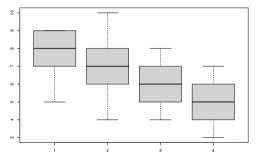
mydata

##		dν	treatment	subject	
##	1	8	1	1	
##	2	10	2	1	
##	3	7	3	1	
##	4	5	4	1	
##	5	9	1	2	
##	6	9	2	2	
##	7	8	3	2	
##	8	6	4	2	
##	9	7	1	3	
##	10	5	2	3	
##	11	8	3	3	
##	12	4	4	3	
##	13	9	1	4	
##	14	6	2	4	
##	15	5	3	4	
##	16	7	4	4	
##	17	8	1	5	
##	18	7	2	5	
##	19	7	3	5	
##	20	6	4	5	
##	21	5	1	6	
##	22	4	2	6	
##	23	4	3	6	
##	24	3	4	6	
44	O.F.	7	4	7	

Visualize Data

Many ways to visualize data. Lets try out a box and whisker plot this time.

boxplot(split(mydata\$dv,mydata\$treatment))



Repeated Measures ANOVA - Univariate Approach

```
m1 <- aov(dv ~ treatment + Error(subject/treatment), data=mydata)
summary(m1)
##
## Error: subject
            Df Sum Sq Mean Sq F value Pr(>F)
## Residuals 9 48.4 5.378
## Error: subject:treatment
            Df Sum Sq Mean Sq F value Pr(>F)
## treatment 3 38.9 12.967 12.24.3.06e-05 ***
## Residuals 27 28.6 1.059
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Here we see a significant influence of treatment (p < 0.001)

note: The Error() term tells R to slice out of the model an additional error term corresponding to the variance accounted for by subjects (MS = 5.378).

Univariate: a single dependent variables (we have been doing this throughout the course)

Repeated Measures ANOVA - Sphercity Violations

Repeated Measures are very sensitive to Sphericity Violations

- 1. Greenhouse-Geisser Corrections
- 2. Multivariate Approach
- less sensitive to sphericity violations
- assumes normality
- Can also consider one or more dependent measures (e.g., MANOVA).
- see Maxwell, Delaney, Kelley text for details.
- 3. Friedman Test
- nonparamtric
- 1-way designs only

Let's do the GG, and we'll come back to Multivariate & Friedman afterwords.

First, we must reorganize the data into a format in which each row represents a single subject, and columns represent levels of the treatment factor.

```
response <- with(mydata,cbind(dv[treatment==1], dv[treatment==2], dv[treatment==3], dv[treatment==4]))

response

## [,1] [,2] [,3] [,4]

## [1,] 8 10 7 5

## [2,] 9 9 8 6

## [3,] 7 5 8 4

## [4,] 9 6 5 7

## [6,] 8 7 7 6

## [6,] 5 4 4 3

## [7,] 7 6 5 4

## [8,] 8 8 6 6

## [9,] 9 8 6 5

## [9,] 9 8 6 5

## [9,] 7 7 7 4 5
```

Next, for the linear model.

```
mlm1 <- lm(response ~ 1)
m \rceil m 1
##
## Call:
## lm(formula = response ~ 1)
##
## Coefficients:
                [.1] [.2] [.3] [.4]
##
## (Intercept) 7.7 7.0 6.0 5.1
```

The $\sim\!1$ notation simply tells R that there are no between-subjects factors here

• in other words, only fit the model using intercepts.

Now we must set up a variable that defines the design of our study, which is a single factor with four levels:

```
rfactor <- factor(c("r1", "r2", "r3", "r4"))
design = data.frame(rfactor)</pre>
```

Now we must set up a variable that defines the design of our study, which is a single factor with four levels:

- mlm1, is our multivariate model defined above.
- idata=design defines the number of levels
- idesign=~rfactor defines repeated-measures variable.
- type="III", instructs Anova() to calculate the "Type-III" sums of squares (there are different types of sums of squares (see Maxwell, Delaney, Kelley)

See next slide for full output

Mauchly Tests for Sphericity

```
summary(mlm1.aov, multivariate=FALSE)
##
## Univariate Type III Repeated-Measures ANOVA Assuming Sphericity
##
##
             Sum Sq num Df Error SS den Df F value Pr(>F)
## (Intercept) 1664.1 1 48.4 9 309.440 2.808e-08 ***
## rfactor 38.9
                       3 28.6 27 12.241 3.060e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
```

```
## Univariate Type III Repeated-Measures ANOVA Assuming Sphericity
##
              Sum Sq num Df Error SS den Df F value
## (Intercept) 1664.1 1
                               48.4 9 309.440 2.808e-08 ***
                38.9
                               28.6
                                        27 12.241 3.060e-05 ***
## rfactor
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Mauchly Tests for Sphericity
##
          Test statistic p-value
                0.34613 0.14884
## rfactor
##
## Greenhouse-Geisser and Huvnh-Feldt Corrections
## for Departure from Sphericity
##
          GG eps Pr(>F[GG])
## rfactor 0.7426 0.0002388 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
             HF eps Pr(>F[HF])
## rfactor 0.9981017 3.106252e-05
```

Mauchly Test for Sphericity not violated (p = 0.149) [i.e., p > 0.05]

Look at GG correction if violated (p = 0.0002)

Organize Data by Treatment

Let's quickly split our data into each treatment

```
treat1 = response[1:10]
treat2 = response[11:20]
treat3 = response[21:30]
treat4 = response[31:40]
```

Testing normalility

```
Performed on the PAIRED differences
shapiro.test(treat2-treat1)$p.value #
## [1] 0.4208624
shapiro.test(treat3-treat1)$p.value #
## [1] 0.5195284
shapiro.test(treat4-treat1)$p.value #
## [1] 0.008488973
shapiro.test(treat3-treat2)$p.value #
## [1] 0.1526917
shapiro.test(treat4-treat2)$p.value #
## [1] 0.6088367
shapiro.test(treat4-treat3)$p.value #
## [1] 0.6420479
```

normality violated—consider using Friedman Test, Wilcoxon signed-rank, CLES

Follow up Mean Comparisons

```
p1v2 = t.test(treat1, treat2, paired = TRUE, alternative = "two.sided")$p.value #
p1v3 = t.test(treat1, treat3, paired = TRUE, alternative = "two.sided")$p.value #
p1v4 = t.test(treat1, treat4, paired = TRUE, alternative = "two.sided")$p.value #
p2v3 = t.test(treat2, treat3, paired = TRUE, alternative = "two.sided")$p.value #
p2v4 = t.test(treat2, treat4, paired = TRUE, alternative = "two.sided")$p.value #
p3v4 = t.test(treat3, treat4, paired = TRUE, alternative = "two.sided")$p.value #
pvals = c(p1v2, p1v3, p1v4, p2v3, p2v4,p3v4)
pvals_holm = p.adjust(pvals, method = "holm", n = length(pvals))
sprintf("%.5f", pvals_holm) #outputs in decimal (not scientific notation)
```

```
## [1] "0.31977" "0.02139" "0.00001" "0.31977" "0.02139" "0.31977"
```

There is a reduction in pain between treatments 1 and 3 (p = 0.021), treatments 1 and 4 (p < 0.001), and treatment 2 and 4 (p = 0.021)

Paired Sample Effect Sizes

```
install.packages("effsize")
library(effsize)
cohen.d(treat1, treat2, paired = TRUE)$estimate #
## [1] 0.4182333
cohen.d(treat1, treat3, paired = TRUE)$estimate #
## [1] 1.226729
cohen.d(treat1, treat4, paired = TRUE)$estimate #
## [1] 2.117492
cohen.d(treat2, treat3, paired = TRUE)$estimate #
## [1] 0.5951196
cohen.d(treat2, treat4, paired = TRUE)$estimate #
## [1] 1.181162
cohen.d(treat3, treat4, paired = TRUE)$estimate #
## [1] 0.6631177
```

ANOVA Effect Size in R

```
Bakeman, R. (2005). Recommended effect size statistics for repeated measures designs.
Behavior research methods, 37(3), 379-384.
install.packages("effectsize")
librarv(effectsize)
omega squared(mlm1.aov)
## Parameter | Omega2 (partial) |
                                           90% CI
                0.92 | [0.75, 0.96]
## rfactor
```

Summary of One-Way Repeated Measures ANOVA

We found a significant main effect of Treatment [F(3,27) = 12.24, p < 0.001 (GG-corrected), $\omega^2=0.92$]. There was a reduction in pain between treatments 1 and 3 (p = 0.021, d = 1.23), treatments 1 and 4 (p < 0.001, d = 2.12), and treatment 2 and 4 (p = 0.021, d = 1.18).

Power Analysis on ANOVA

Loading required package: lavaan

This is lawaan 0.6-7

```
install.packages("WebPower")
library(WebPower)
## Loading required package: MASS
## Loading required package: lme4
## Loading required package: Matrix
## Registered S3 methods overwritten by 'lme4':
##
     method
                                      from
     cooks.distance.influence.merMod car
##
##
     influence.merMod
                                      car
     dfbeta.influence.merMod
##
                                      car
##
     dfbetas.influence.merMod
                                      car
```

Power Analysis on ANOVA

We need 70 participants per group for a sufficiently powered.

```
install.packages("WebPower")
library(WebPower)
# n=sub, nq=#ofgroups, nm=#ofmeasurements, nscor=sphericity(1=perfect)
#type "0" between-effect; "1" within-effect; and "2" interaction effect
wp.rmanova(n = NULL, ng = 1, nm = 4, f = .4, nscor = 1,
           alpha = 0.05, power = 0.8, type = 1)
## Repeated-measures ANOVA analysis
##
##
              n f ng nm nscor alpha power
       69.45101 0.4 1 4 1 0.05 0.8
##
##
## NOTE: Power analysis for within-effect test
## URL: http://psychstat.org/rmanova
```

Repeated Measures ANOVA - Multivariate Approach

Multivariate approach does not require the assumption of sphericity

- Good news, we can use the same linear model and set Multivariate = TRUE
- See next slide for multivariate output

summary(mlm1.aov, multivariate=TRUE)

```
##
## Type III Repeated Measures MANOVA Tests:
##
##
## Term: (Intercept)
##
##
    Response transformation matrix:
```

Repeated Measures ANOVA - Multivariate Approach

```
Term: rfactor
Response transformation matrix:
    rfactor1 rfactor2 rfactor3
Γ1, ]
Γ2.7
ГЗ. Т
Γ4. 7
Sum of squares and products for the hypothesis:
        rfactor1 rfactor2 rfactor3
rfactor1
            67.6
                     49.4
                             23.4
                     36.1
                             17.1
rfactor2
            49.4
                              8.1
rfactor3
           23.4
                    17.1
Multivariate Tests: rfactor
                Df test stat approx F num Df den Df
                                                       Pr(>F)
Pillai
                     0.95080 45.09192
                                                 7 6.0316e-05 ***
                1 0.04920 45.09192
Wilks
                                             7 6.0316e-05 ***
Hotelling-Lawley 1 19.32511 45.09192
                                               7 6.0316e-05 ***
               1 19.32511 45.09192
                                                 7 6.0316e-05 ***
Signif codes: 0 (***, 0 001 (**, 0 01 (*) 0 05 ( ) 0 1 ( ) 1
```

There is a significant main effect of group (p < 0.001).

I suggest using Pillai's Trace because it is the most robust. Can use the same mean comparisons and effect size estimates we did with univariate approach.

Friedman Test

Nonparametric omnibus test for a 1-way repeated measures design. Let's perform this test on the previous example install.packages("rstatix")

library(rstatix)

```
##
## Attaching package: 'rstatix'
## The following object is masked from 'package:MASS':
##
## select
## The following objects are masked from 'package:effectsize':
##
## cohens d. eta squared
```

Friedman Test

```
library(rstatix)
friedman_test(dv ~ treatment | subject, data=mydata)

## # A tibble: 1 x 6

## .y. n statistic df p method

## * <chr> <int> <dbl> <dbl> <dbl> <chr>
## 1 dv 10 19.5 3 0.000219 Friedman test
```

There is a significant main effect of group (p < 0.001). Can follow up with tests for Wilcoxon signed-rank and common language effect size.

2-Way Repeated Measures

2-Way Repeated Measures

Factor A	Al			A2		
Factor B	ВІ	B2	В3	ВІ	B2	В3
Subject I	420	420	480	480	600	780
Subject 2	480	480	5 4 0	660	780	780
Subject 3	5 4 0	660	5 4 0	480	660	720
Subject 4	480	480	600	360	720	840
Subject 5	5 4 0	600	540	540	720	780

e.g., Is there an Influence of Sound Volume (Factor A) and Light Luminance (Factor B) cues on Reaction Time

2-Way - Univariate Approach

2-Way - Univariate Approach

##

```
see next slide for full output
m1 <- aov(dv1 ~ factorA*factorB + Error(subject1/(factorA*factorB)),
          data=mydata1)
summary(m1)
##
## Error: subject1
##
             Df Sum Sq Mean Sq F value Pr(>F)
## Residuals 4 33600
                           8400
```

Error: subject1:factorA

41

2-Way - Univariate Approach

```
Error: subject1
         Df Sum Sa Mean Sa F value Pr(>F)
Residuals 4 33600
                     8400
Error: subject1:factorA
         Df Sum Sa Mean Sa F value Pr(>F)
factorA 1 147000 147000 17.5 0.0139 *
Residuals 4 33600
                     8400
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Error: subject1:factorB
         Df Sum Sa Mean Sa F value Pr(>F)
factorB 2 138480 69240 14.16 0.00235 **
Residuals 8 39120
                     4890
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Error: subject1:factorA:factorB
               Df Sum Sa Mean Sa F value Pr(>F)
factorA:factorB 2 67920 33960 11.67 0.00425 **
               8 23280
                           2910
Residuals
Signif, codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
```

Significant Interaction between A and B (p = 0.004)

• Since there is a significant interaction, don't look at main effects (SAME RULES AS A 2-way between ANOVA!)

Reorganizing data

```
DV1 <- with(mydata1,cbind(dv1[(factorA==1 & factorB == 1)],
                                  dv1\lceil(factorA==1 \& factorB == 2)\rceil.
                                  dv1\lceil(factorA==1 \& factorB == 3)\rceil.
                                  dv1[(factorA==2 \& factorB == 1)],
                                  dv1\lceil(factorA==2 \& factorB == 2)\rceil.
                                  dv1[(factorA==2 & factorB == 3)]))
DV1
##
         [,1] [,2] [,3] [,4] [,5] [,6]
         420 420 480 480
## [1,]
                               600
                                    780
                    540
## [2,]
         480
               480
                         660
                               780
                                    780
## [3.]
               660
                    540
         540
                         480
                               660
                                    720
## [4.]
              480
                    600
                         360
         480
                               720
                                    840
## [5.]
         540
               600
                   540
                         540
                               720
                                    780
```

Defining the Design

```
FACTOR_A <- factor(c(rep(1,3),rep(2,3)))
FACTOR_B <- factor(rep(c(1,2,3),2))
design1 <- data.frame(FACTOR_A, FACTOR_B)
design1</pre>
```

##		${\tt FACTOR_A}$	FACTOR_B
##	1	1	1
##	2	1	2
##	3	1	3
##	4	2	1
##	5	2	2
##	6	2	3

Multivariate, linear model.

```
mlm2 \leftarrow lm(DV1 \sim 1)
mlm2
##
## Call:
## lm(formula = DV1 ~ 1)
##
## Coefficients:
                [,1] [,2] [,3] [,4] [,5] [,6]
##
## (Intercept) 492 528 540 504
                                        696
                                               780
```

See next slide for full output

```
summary(mlm2.aov, multivariate=FALSE, univariate=TRUE)
## Warning in summary. Anova.mlm(mlm2.aov, multivariate = FALSE, univariate
```

```
## HF eps > 1 treated as 1
```

##

(Intercept)

FACTOR A

FACTOR B

##

Univariate Type III Repeated-Measures ANOVA Assuming Sphericity

138480

Pr(>F)

2

```
Univariate Type III Repeated-Measures ANOVA Assuming Sphericity
                   Sum Sa num Df Error SS den Df E value
                                                             Pr(>F)
(Intercept)
                 10443000
                                     33600
                                               4 1243 214 3 861e-06 ***
FACTOR A
                    147000
                                     33600
                                                   17.500 0.013881 *
FACTOR B
                   138480
                                     39120
                                               8 14.159 0.002354 **
                                    23280
FACTOR_A: FACTOR_B 67920
                                               8 11 670 0 004246 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Mauchly Tests for Sphericity
                  Test statistic p-value
FACTOR B
                        0.76047 0.66317
FACTOR A: FACTOR B
                        0.96131 0.94254
Greenhouse-Geisser and Huvnh-Feldt Corrections
for Departure from Sphericity
                  GG eps Pr(>F[GG])
FACTOR R
                  0.80676
FACTOR A: FACTOR B Ø. 96275
                           0.004857 **
Signif. codes: 0 (***, 0.001 (**, 0.01 (*, 0.05 (., 0.1 (., 1
                   HF eps Pr(>F[HF])
FACTOR B
                 1.271242 0.002354093
FACTOR_A: FACTOR_B 1.838414 0.004245732
```

Sphericity not violated (Mauchly Test, p > 0.05). GG-corrected interaction significant (p = 0.004857)

2-Way - Multivariate Approach

See Partial Output on next page

```
summary(mlm2.aov, multivariate=TRUE, univariate=FALSE)
##
## Type III Repeated Measures MANOVA Tests:
##
##
## Term: (Intercept)
##
    Response transformation matrix:
##
##
        (Intercept)
## [1,]
## [2,]
```

2-Way - Multivariate Approach

```
Multivariate Tests: FACTOR A
               Df test stat approx F num Df den Df Pr(>F)
Pillai
               1 0.813953
                             17.5
                                            4 0.013881 *
Wilks
               1 0.186047
                            17.5 1
                                            4 0.013881 *
Hotelling-Lawley 1 4.375000 17.5 1
                                            4 0 013881 *
               1 4.375000
                             17.5
                                            4 0.013881 *
Rov
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Multivariate Tests: FACTOR B
               Df test stat approx F num Df den Df Pr(>F)
Pillai
               1 0.868521 9.908686
                                           3 0 047674 *
Wilks
              1 0.131479 9.908686 2 3 0.047674 *
Hotelling-Lawley 1 6.605791 9.908686
                                   2 3 0.047674 *
Rov
               1 6.605791 9.908686
                                           3 0.047674 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Multivariate Tests: FACTOR A: FACTOR B
              Df test stat approx E num Df den Df Pr(>E)
Pillai
              1 0.849438 8.462687 2 3 0.058421 .
               1 0.150562 8.462687 2 3 0.058421 .
Wilks
Hotelling-Lawley 1 5.641791 8.462687 2 3 0.058421 .
             1 5.641791 8.462687 2
                                           3 0.058421 .
Rov
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The multivariate approach suggests that there are only main effects of A (p = 0.013) and B (p = 0.048) on our dependent measure [Interaction (p = 0.058)]

Different Results, What do you do?

The 2-way RM ANOVA (with and without GG corrections) suggested there was a significant interaction between factor A and B (as well as main effects), but the multivariate approach suggests there were ONLY main effects.

- Can justify that GG corrections were made and look at interactions
 - Alternatively, go with the more conservative test and look at main effects (recommended)
 - replication crisis
- Ultimately you will have to justify your decisions in your paper and to reviewers.

Let's say we went with the conservative approach. Let's look at the mean comparisons for the main effects of A (sound) and B (light) on the DV (reaction time).

Main Effects of A (Sound)

Group all data sound 1 or sound 2 (ignore effect of light)

```
# sound1 vs sound2 --- group all data sound 1 or sound 2 (ignore effect of light)
sound1 = c(dv1[1:3],dv1[7:9],dv1[13:15], dv1[19:21], dv1[25:27])
sound2 = c(dv1[4:6],dv1[10:12],dv1[16:18], dv1[22:24], dv1[28:30])
t.test(sound1, sound2, paired = TRUE, alternative = "two.sided")$p.value
```

[1] 0.001168222

There is a significant difference in reaction time between sound 1 and 2

Main Effects of B (Light)

Group all data light 1, 2, or 3 (ignore effect of sound)

```
# light1 vs light2 --- group all data light 1 or light 2 (ignore effect of sound)

light1 = c(dv1[1],dv1[4],dv1[7], dv1[10], dv1[13], dv1[16], dv1[19], dv1[22], dv1[25],dv1[28])

light2 = c(dv1[2],dv1[6],dv1[8], dv1[11], dv1[14], dv1[17], dv1[20], dv1[23], dv1[26],dv1[29])

light3 = c(dv1[3],dv1[6],dv1[9], dv1[12], dv1[13], dv1[13], dv1[21], dv1[21], dv1[24],dv1[27],dv1[20])

pval_l1v12 = t.test(light1, light2, paired = TRUE, alternative = "two.sided")$p.value

pval_l1v13 = t.test(light1, light3, paired = TRUE, alternative = "two.sided")$p.value

pval_l2v13 = t.test(light2, light3, paired = TRUE, alternative = "two.sided")$p.value

pvals = c(pval_l1v12, pval_l1v13, pval_l2v13)

p.adjust(pvals, method = "holm", n = length(pvals))
```

[1] 0.03034858 0.06358186 0.66374348

There is a significant difference in reaction time between light $1\ \mathrm{and}\ 2$

Note: You would also have to find effect sizes, test assumption, etc., as in the univariate example, but we'll stop here for today lecture.

Next Week

• Factorial (Between and Within) ANOVA