

Inoculum Dose, Diversity, Dispersal, and Damage: Simulating Optimal Economic Control of an Aerially-Dispersed Plant Pathogen at the Regional Scale

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Abstract

Plant pathogens that disperse by airborne propagules may cause damage that extends beyond the borders of individual fields. Developing sound management strategies therefore requires consideration of heterogeneity in pathogen transmission, the effectiveness of control measures, host susceptibility and pathogen virulence, and the resulting economic outcomes that scale up at the regional level with coordinated management. We use hop powdery mildew as a motivating pathosystem to develop a coupled epidemiological-economic model to enable simulation of the impact of epidemic conditions and coordinated management interventions on profitability. This pathosystem is a well-suited case study because disease development may be limited by primary inoculum and fungicide applications, yet the pathogen can spread via long-distance dispersal between fields and rapidly damage both crop yield and quality. We parameterized the model using data collected from a census sample of commercial hop yards in Oregon during 2014 to 2017, including the monthly incidence of plants with powdery mildew, fungicides applied by growers, and estimated revenue depending on how the incidence of diseased hop cones affects yield and the likelihood of crop devaluation. We show that conditions in the early stages of epidemics related to primary inoculum dose, pathogen diversity, and the intensity of management intervention interact and determine the optimal regional control strategy. As the likelihood of primary infection increases, due to either the dose of primary inoculum or virulence of the pathogen population, mean profitability decreases. These effects are most pronounced when primary infection occurs in yards most central in the network. The choice of how many fungicide applications to make in response to initial infection has little effect on profitability when primary inoculum is relatively infrequent. However, as primary inoculum increases, targeted fungicide applications made in the early stages of epidemics are essential for maximizing

profitability region-wide. These principles hold across a range of market demand scenarios that change crop quality standards, even though relative profit losses increases under low demand conditions. Our research provides a framework for formally understanding factors that influence the cost of disease in complex agricultural systems where pathogens disperse across management units.

Keywords: plant disease, pathogens, epidemiology, economic impacts, disease management, landscape-scale

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Introduction

There is increasing scrutiny of pesticides in agriculture and a need to develop management strategies and policies that reduce inputs while maintaining productivity and profitability [1] [2]. Disease management efforts are most often directed at the scale of individual fields or farms, but plant pathogens do not respect management units or jurisdictional boundaries [3]. Management may be suboptimal or ineffective when not properly matched to the scale of pathogen dispersal [4]. The relative importance of inoculum produced endogenously within a given field or exogenously in other locations may dictate the mitigation strategies and the need for collective action in the form of area-wide management [5].

Foundational theory in plant disease epidemiology suggests that mitigation efforts that reduce primary inoculum only delay epidemics, with the effect being inversely proportional to epidemic velocity [11]. Yet, a number of empirical studies and modeling suggest that early intervention is critical for containing the spread of disease outbreaks [12] [13]. Epidemics caused by pathogens capable of long-distance dispersal appear sensitive to the conditions in the initial outbreak area [14] [15]. Final epidemic severity may depend on the size of the initial focus, pattern of initial inoculum, proportion of susceptible hosts in the population, and connectivity to other susceptible hosts [16] [17]. The importance of these factors may depend sensitively on parameters controlling pathogen transmission and

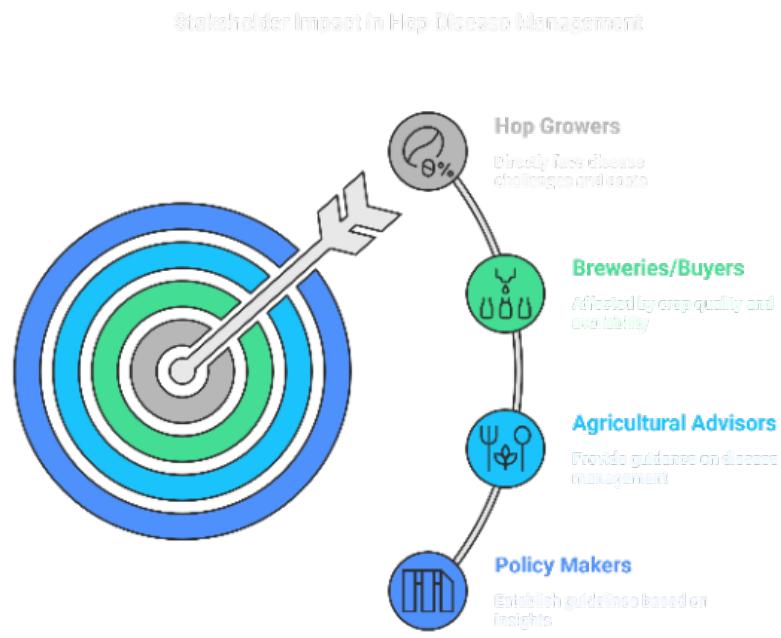


Figure 1: ../figures/logseq_flowchart for hops project.png

stochasticity in the earliest stages of an epidemic [18]. Concrete recommendations for control strategies also depend on the relative effectiveness and costs of controls [19].

The need for modeling to explicitly express processes and current understanding of a system is clear [20] [23], yet linking epidemiological models to crop damage and economic outcomes when pathogens potentially disperse over long distances is a challenging problem [24]. The motivating pathosystem for the research we present, hop powdery mildew, engenders many of these challenging aspects. The disease is caused by the fungus *Podosphaera macularis* and remains one of the most difficult and costly problems affecting hop producers in the western U.S. and other production regions. Success in breeding cultivars resistant to the disease have been met by emergence of strains of the fungus that can overcome host resistance when the said resistance is broadly deployed in the landscape. Therefore, management still relies heavily on cultural practices that reduce inoculum density and fungicides to slow the rate of disease progression.

This pathosystem has several biological and economic attributes that make it an exemplar for developing the modeling framework we propose herein, and also broadly of interest for other aerially-dispersed plant pathogens in complex social-ecological systems.

First, the causal pathogen is an obligate biotroph with a host range limited to the plant family Cannabaceae, with hop being the dominant and most important host cultivated at the time of these studies. Consequently, it is possible to infer disease transmission between yards because other sources of inoculum are trivial. Further, this system is amendable to modeling dispersal between yards as *P. macularis* exhibits annual cycles of emergence, colonization, and extinction. The fungus persists from season to season in the Pacific Northwestern U.S. only in association with living host tissue, provisioned by infected crown buds due to the absence of the sexual stage of the pathogen in this region. Bud infection and overwintering of the pathogen leads to highly focal infections owing to the emergence of heavily infected shoots in spring, the so-called flag shoots, which occur at a low frequency in commercial hop yards. From these focal infections, *P. macularis* disperses via wind and readily spreads within the network of hop yards to create regional epidemics. At the end of the cropping season, the pathogen becomes locally extinct in most yards due to its low overwintering survival. Thus, a new realization of the disease development and transmission process can be observed annually.

Pathogenic variation is common in pathogens across plant and animal hosts and has important implications for the dynamics of disease transmission and severity. This is especially relevant in agricultural systems where R-gene-mediated resistance is deployed and creates a mosaic of resistant and susceptible hosts. Host resistance to powdery mildew is commercially available in hop and multiple pathogenic variants (strains) exist in *P. macularis* in certain populations. As hop plants are long-lived perennials, relatively stable patterns of resistant and susceptible cultivars are present in the landscape.

The pathosystem is further of interest because powdery mildew may cause economic losses by reducing both yield and potentially crop quality. This is a common scenario in agricultural systems where crop damage is not attributed solely to direct losses in yield, but additionally or primarily from reductions in crop quality. This is particularly important for crops marketed directly to consumers with cosmetic value. In these situations, the financial loss incurred by the grower may be linked in complex ways to market demand. Indeed, this is the situation with hops and powdery mildew because the disease may reduce brewing value and cause conspicuous visual defects from degraded cone color. For this reason, growers apply fungicides repeatedly during the season with the goal of minimizing inoculum pressure for the critical cone phase of the disease. Fungicide applications for powdery mildew may occur over a period of multiple months to minimize foliar infections in spring and then later in summer to minimize cone infection. Thus, growers must make multiple decisions on when to begin treatment and how intensively to treat.

Adding even more uncertainty, hops are sold almost entirely through marketing contracts that stipulate quality standards, usually with vague or subjective quality standards. Contracting is conducted for numerous agricultural commodities, and in 2017 21 percent of total U.S. crop production was under a contract agreement. Price risk reduction is stated as a major incentive for contracting. The potential for crop devaluation or, in the worst case rejection, may substantially affect disease management choices since the producer assumes firstly the risk of crop damage and secondly the penalty for failing on a contractual obligation. We expect that optimal disease control strategies may therefore be sensitive to contract structure when crop value or saleability is inseparably linked to crop quality metrics. Furthermore, the optimal control strategy may depend on practices in other fields and other farms given the potential for long-distance dispersal of the pathogen.

Motivated by this pathosystem, we draw upon an exceptional rich data set collected from a census sample of hop yards in Oregon over a four-year period for our analyses. We formulate an epidemiological model for the development and spread of powdery mildew at the regional level, including the effect of fungicides applied in a field of interest and all other potential source fields. We couple the epidemiological model to an economic model of expected revenue and costs associated with disease management, devaluation or rejection due to quality defects, and market conditions. We then simulate varying conditions of the initial phases of epidemics related to primary inoculum dose (frequency), pathogen diversity, centrality in the transmission network of fields, and management intervention to identify control strategies that maximize profit under varying market demand scenarios.

Material and Methods

Study System

Our study system is the hop production region in western Oregon. Oregon is one of the leading hop producing regions in the U.S. and commercial production is concentrated in a few counties in the Willamette Valley in the western portion of the state. Hop powdery mildew was first confirmed in the field in Oregon in 1998 and has occurred annually each year since then. Historically, powdery mildew has tended to occur most regularly and most severely in production regions in the eastern extent of the Willamette Valley, presumably due to the frequency of overwintered inoculum and subsequent dispersal from the resultant disease foci [6]. We intentionally focused on hop farms in the eastern production regions for data acquisition. The diversity of cultivars and production practices in this region are summarized elsewhere [7].

Biological Data Acquisition

We obtained monthly data on the incidence of plants with powdery mildew or primary infection (i.e., occurrence of a flag shoot) from a census survey of hop yards. Disease assessments were conducted monthly from April to July during each of 2014 to 2017. For brevity, a summary of the disease assessments methods is provided here; a complete description of the methods are given in the referenced work [8]. There were 8 to 10 farms sampled per year, all within Marion County, Oregon, with a maximum distance between yards of 26 km. After cleaning, data were available for 99 yards assessed in 2014, 113 in 2015, 116 in 2016, and 122 in 2017. All cultivars were evaluated, independent of their susceptibility to powdery mildew. The incidence of plants with powdery mildew was assessed using a modification of cluster sampling methods described previously [9].

As noted previously, there are multiple pathogenic strains of *P. macularis* that differ in their ability to cause disease on hop plants with specific resistance genes (R-genes). Two strains of the pathogen were relevant at the time of the field surveys and are differentiated based on their ability to cause disease on plants with a resistance termed R6. The presence of R6 resistance is analogous to immunization that provides complete, but strain-specific, protection from disease. The presence of R6 in hop plants provides resistance to powdery mildew only when the pathogen lacks a corresponding virulence (V). For shorthand, we refer to strains that cannot infect plants with R6 resistance as non-V6-virulent. Other strains of the pathogen may infect susceptible plants that lack R6, but importantly, can also infect plants that possess R6. These strains are dubbed V6-virulent. V6-virulent strains are promiscuous in the yards they may affect, as they infect hop cultivars that both possess or do not possess R6, analogous to a vaccine-evasive strain of a pathogen.

When we detected powdery mildew in a given hop yard it was necessary to match the strain of the pathogen present to potential yards where the pathogen

could disperse to cause disease. Therefore, the initial strain of the pathogen present was determined to be V6-virulent or non-V6-virulent using bioassays as described previously.

Pesticide Use and Costs

We obtained pesticide application records from each grower for all yards sampled during 2014 to 2017 and interrogated their records to determine the timing and dosage of applications of herbicides, fungicides with activity against powdery mildew, and adjuvant additives. We did not consider insecticides or miticides because these were not directly relevant for the present analysis of powdery mildew. We then estimated the January 2022 real costs of the relevant pesticides and adjuvants applied by requesting price quotes for each product from each of three vendors in western Oregon that service hop producers as described in the referenced work. We estimated real prices using January 2022 as the base by adjusting the nominal price by the producer price index for farm products for each year available from the U.S. Bureau of Labor Statistics, and then averaged over all available years to derive a single real price per unit.

General Modeling Approach

We introduce a linked epidemiological-economic statistical model of epidemic development and apply this model to hop powdery mildew to simulate economic outcomes due to disease management costs and crop damage from direct losses in yield and quality defects. The epidemic model contains both stochastic and deterministic components to estimate development of the foliar phase of powdery mildew originating from initial occurrences of *P. macularis* via bud perennation, autoinfection at the scale of individual hop yards from inoculum endogenous to a given yard, and exogenous inoculum dispersed from other yards in the region. The population moment estimate of the incidence of plants with powdery mildew is derived from a function of the probability of plant being diseased, as moderated by fungicide use. Profits are the summation of revenue and fixed and variable costs as influenced by fungicide inputs, and yield and crop devaluation due to quality defects as a function of disease incidence. External drivers are inputs of wind data, fungicide use, and initializing values of the probability of initial (primary) infection due to bud perennation, expected crop yield in the absence of disease, and price per unit of yield. The model is spatially explicit at the scale of individual hop yards and uses the actual location and size of hop yards in the data set for a representative year; there is no attempt to account mechanistically for focus development or disease spread within hop yards.

We use the linked models to simulate profit levels resulting from the varying epidemic conditions. Concretely, these conditions were related to initial infection frequency, pathogenic diversity of the initial strain of the pathogen, the location of the initial infections, and the number of fungicide applications made in the first month of the epidemic. We aggregate responses from individual yards to scale to the regional population of yards. We then ran each simulation scenario

under three market demand scenarios to understand the sensitivity of the results to market conditions.

Submodels

Epidemic Network Model An individual hop yard is considered a node in a network of yards in the spatial extent of interest. Disease status of a yard in a given month is a nonlinear function of its disease incidence in the preceding month, susceptibility to two races of *P. macularis*, and disease spread from other nodes as influenced by their disease incidence and area (source strength), distance apart, and wind run in the preceding month. We expanded this model by introducing two parameters that moderate disease in a given hop yard and disease spread from other hop yards based on the number of fungicide applications made in the prior month. We also generalized the model by expressing the dispersal kernel as a function of distance and source strength to accommodate various functional forms. The impact of exogenous inoculum depends jointly on the pathogen virulence in the source yards and susceptibility of the cultivar planted in the target yard.

The number diseased plants is given by Y_i , among a sample of n_i plants, with $i = 1, \dots, N$ indexing yard identity. The probability of Y_i , is taken as binomially distributed with the predictor function expressed on the log-odds scale as:

$$\log \left(\frac{p_i}{1 - p_i} \right) = \beta + \delta \left(\frac{\tilde{y}_i}{n_{\tilde{y}_i}} \exp(-\eta_1 s_i) \right) + \gamma \sum_{j=1}^{M_i} \left(\frac{a_j z_j}{n_{z_j}} w_{ij} \exp(-\eta_2 s_j) f(d_{ij}; \alpha) \right)$$

Covariates and parameter interpretations are given in Tables 1 and 2. Parameters are allowed to vary for time transition periods from May to June and June to July. The equation defines the model for disease development on foliage at the plant scale. We explored an exponential and also a power-law function for the dispersal kernel, but present results only for the power-law function given theoretical considerations of expected dispersal characteristics of *P. macularis*.

Table 1: Covariate notations for each yard of interest $i = 1, \dots, N$ in a particular month, and all other yards $j = 1, \dots, M_i$ relative to yard i .

Variable	Description
\tilde{y}_i	Number of diseased plants at yard i in the prior month
$n_{\tilde{y}_i}$	Number of plants sampled at yard i in the prior month
a_i	Area (hectares) of yard i
z_j	Number of diseased plants at yard j in the prior month

Variable	Description
n_{z_j}	Number of plants sampled at yard j in the prior month
a_j	Area (hectares) of yard j
d_{ij}	Distance (kilometers) from centroids of yard i to yard j
w_{ij}	Wind vector on $i - j$ direction in the prior month
s_i	Number of fungicide sprays in yard i in prior month
s_j	Number of fungicide sprays in yard j in prior month

Table 2: Interpretation of model parameters.

Parameter	Interpretation
β	Baseline log-odds of disease, after accounting for autoinfection and dispersal.
δ	Change in log-odds of disease associated with autoinfection at the yard scale, after accounting for disease spread.
γ	Distance-adjusted change in log-odds of disease associated with disease spread from other yards, after accounting for autoinfection.
α	Dispersal parameter providing distance adjustment to change in log-odds of disease associated with individual source yards.
η_1	Change in log-odds of disease associated with autoinfection at the yard scale, after accounting for fungicide sprays.
η_2	Dispersal parameter providing fungicide spray adjustment to change in log-odds of disease associated with individual source yards.

Economic Model The profit function Π at time t over the growing season ($t = 0, \dots, T$) measures the total profit per hectare across all hop yards $i = 1 \dots N$:

$$\Pi(s_{it}) = \sum_{i=1}^N (\pi_{it})$$

where π_{it} is the profit per hectare at time t for yard i . This profit equation is conditioned on the number of fungicide sprays s_{it} across the season and subject

to constraints imposed by the epidemic network model and by the price-quality relationships detailed below. Here, we assume risk neutrality of growers.

The profit π_{it} for each yard i at time t is defined as the difference between revenue and cost for each yard at time t :

$$\pi_{it} = R_t(q_i, v; p_i) - C_i(s_{it})$$

Revenue is only realized in the final period T , so that revenue is defined by $R_i(q_i, v; p_i) = R_T$, otherwise $R_i(q_i, v; p_i) = 0$. Revenue is a function of both yield q_i and price v , conditioned on the disease probability level p_i . Costs C_i , defined in more detail below, are a function of fixed costs and the number of fungicide sprays, s_{it} .

Both yield quantity and price are adjusted by the incidence of cones with disease and associated quality defects as inferred from cone color. We used relationships reported in the literature to link the foliar phase of the disease to incidence of cones with powdery mildew yield, and defects to cone color. First, the incidence of leaves with powdery mildew was estimated from the incidence of plants, p_i , with powdery mildew through the hierarchical relationship between disease at these scales:

$$\text{Leaf Incidence} = 1 - (1 - p_i)^{D/n}$$

where n is the number of leaves sampled per plant and D is the index of dispersion. We assume $n = 50$ and D as reported previously. The incidence of cones with powdery mildew was assumed to be a linear function of the incidence of leaves with powdery mildew as:

$$\text{Cone Incidence} = a_1 \times \text{Leaf Incidence} + b_1$$

Yield loss was then estimated assuming a linear relationship with cone incidence, which is in turn derived from leaf incidence:

$$\text{Yield Loss} = a_2 \times \text{Cone Incidence}$$

We considered cone color a surrogate for quality defects associated with powdery mildew that could lead to crop devaluation or rejection based on production contract standards. Cone color is modeled using an exponential decay function:

$$\text{Cone Color} = 10 + a_3 \cdot (1 - \exp(-b_3 \times \text{Cone Incidence}))$$

These empirical relationships are presented in Figure 1.

Market conditions and production contracts also impact revenue. Production contracts were reviewed and plausible damage functions were derived from expert opinion for crop devaluation from moderate damage, salvage value if the crop was severely affected and was alternatively extracted for alpha-acids, or unsaleable due to extreme damage. We modeled these scenarios as a sigmoid function with varying thresholds dependent on low, medium, and high market demand, as:

$$\text{Adjusted Price} = \text{Initial Price} \times \sigma(\theta_0 + \theta_1 \cdot \text{Cone Color})$$

where σ is the sigmoid function and θ_0, θ_1 are parameters estimated for different market demand scenarios. Revenue in a given yard is then calculated as the product of Adjusted Price and expected yield. Yield in the absence of disease was taken as the average yield reported in 2020 by the National Agricultural Statistics Service for the four cultivars we considered, as we describe below. Initial price was taken from representative production contracts for each of the three estimated levels of demand.

The cost function for each hop yard C_i incorporates the costs associated with fungicide sprays along with fixed costs and other variable costs over the production season:

$$C_i(s_{i,t}) = C_F + C_V + \sum_{t=0}^T (C_{s,t} + C_{a,t})$$

where C_F is the fixed cost, C_V represents other variable costs, $C_{s,t}$ is the fungicide cost, and $C_{a,t}$ is the application cost at period t . Fixed and other variables costs were obtained from Galinato (2020).

Parameter Estimation The parameters in the epidemic network model were estimated using maximum likelihood. The likelihood function was constructed by assuming the number of diseased plants Y_i in each yard i follows a binomial distribution with probability p_i given by the inverse logit of η_i in the equation above. The log-likelihood of the parameters $\boldsymbol{\theta} = (\beta, \delta, \gamma, \alpha, \eta_1, \eta_2)$ given the observed data $\mathcal{D} = (y_i, n_i, \tilde{y}_i, n_{\tilde{y}_i}, a_i, s_i, z_j, n_{z_j}, a_j, d_{ij}, w_{ij}, s_j)$ where $i = 1 \dots N$ and $j = 1 \dots M_i$ is:

$$\ell(\boldsymbol{\theta}; \mathcal{D}) = \sum_{i=1}^N [y_i \log p_i + (n_i - y_i) \log(1 - p_i)]$$

where $p_i = \text{logit}^{-1}(\eta_i)$ and η_i is a function of $\boldsymbol{\theta}$ and the observed covariates.

The maximum likelihood estimator $\hat{\boldsymbol{\theta}}$ was obtained by maximizing $\ell(\boldsymbol{\theta}; \mathcal{D})$ subject to bounds on the parameters to ensure they were biologically plausible. This was done using the Sequential Least Squares Programming (SLSQP) algorithm,

a gradient-based nonlinear constrained optimization method. Analytical expressions for the gradient and Hessian of the negative log-likelihood were derived and provided to the algorithm to improve convergence. Multiple random initializations of the parameters were used to ensure a global optimum was reached. The model was fit using data for all years, but separately for the May to June and June to July transition periods to allow parameters to vary between these periods. Convergence was assessed by monitoring the magnitude of the largest gradient and the positive definiteness of the Hessian matrix at the obtained solution.

All analyses were conducted in Python, making use of the NumPy, SciPy, and Statsmodels libraries for numerical computing and statistical modeling.

Simulation Experiments

For the simulation experiments described below, we constructed a synthetic landscape using the actual locations and sizes of hop yards in each of the years 2014 to 2017 from our data set. Each hop yard was planted to one of four representative cultivars (Chinook, Simcoe®, Nugget, or Mosaic®), chosen because they were commercially relevant at the time of this research, either possessed (R6) or did not possess the R6 resistance, and can be sold for direct use in brewing or alternatively can be processed to extract alpha-acids as a secondary market. We assumed equal susceptibility to powdery mildew given a compatible strain of pathogen. Cultivar assignments were made at random for each yard, subject to a 1:1 ratio of cultivars that possess R6 or non-R6 in the entire landscape. The same yard-level assignments were used across simulation runs for a given year.

We initiated epidemics at the start of May under varying scenarios by specifying an *initial probability of disease*, which governed the expected frequency of initial infections (flag shoots) in the population of hop yards. In reality, any given yard may or may not harbor flag shoots, making the true distribution of early-season disease unknown. We therefore modeled the occurrence of initial infections stochastically as follows. For each yard in the landscape, we first identified the proportion of plants there that were susceptible, which depends on whether a yard was planted to a cultivar susceptible to V6-virulent and/or non-V6-virulent strains. We also identified which quantile of the degree-centrality distribution the yard occupied, where degree-centrality weights each yard by the product of yard area, average wind run, and a decreasing function of inter-yard distance as a measure of disease transmission potential. Denote this quantile by q_i for yard i , and let $0 \leq q_i \leq 1$ (discretized into 20% quantile bins).

Next, we specified a desired mean initial probability of disease across the *entire* landscape, denoted by p_0 . Because yards differ in their centrality and susceptibility, we introduced an adjustment factor so that the final landscape-wide fraction of plants with flag shoots would closely match p_0 . Specifically, within each centrality quantile q , let:

$$(\text{proportion susceptible in quantile } q) = \mathcal{S}_q, \quad (\text{proportion of yards in quantile } q) = \mathcal{P}_q.$$

We then scaled p_0 by $\frac{1}{\mathcal{S}_q} \frac{1}{\mathcal{P}_q}$, effectively concentration flag shoots into those yards that were actually susceptible in the particular quantile q . Denote this adjusted probability by $p_0^*(q)$. For each yard i in quantile q , we then drew:

$$y_{0,i} = \text{Binomial}(n_i, p_0^*(q)),$$

where n_i is the number of plants in yard i . Thus, $y_{0,i}$ is the number of initial infections (flag shoots) in yard i at the start of May. $y_{0,i}$ was set to zero if the initial strain that was randomly placed was biologically impossible with the cultivar in that yard.

With these initial conditions set, we simulated disease progression through May, June, July, and into the early cone-development period using the network-based epidemiological model described in Section 2. In each monthly step, the incidence of infected plants in yard i was predicted using the fitted coefficients from the equation above. Fungicide applications served as an input to the model via coefficients that reduce the rate of new infections in both the focal yard and the potential source yards; the number of sprays in a yard was itself predicted by a Poisson regression fitted from the data on how many fungicide applications growers made in a yard in response to the incidence of diseased plants in the previous month. In May, we specified that if a yard did not contain disease then it still received a baseline of 0.43 fungicide applications, which was the average number of sprays for yards with no disease in the raw data. We additionally allowed a user-defined number of early sprays in May for yards that *did* harbored at least one flag shoot (i.e. $y_{0,i} > 0$). These early sprays could range from zero, no additional sprays beyond the baseline, up to 10 sprays to represent an extremely aggressive early-season spray strategy.

After simulating disease progress through the end of July, we computed the incidence of diseased cones using the relationship in Figure 1C. The economic model then used these incidence levels to estimate yield losses, potential quality reductions (via the cone-color model), and resulting net returns after accounting for fixed costs, variable costs, and the cost of sprays. We repeated these simulations for a range of p_0 values, different fractions of V6-virulent strains present in the initial inoculum, and different yard-level centralities at which the initial flag shoots occurred. For primary inoculum dose, we varied p_0 from 0.00001 to 0.01, a large but plausible range of primary infections levels. The proportion of initial infections caused V6 or non-V6-virulent strains were varied from 0% to 100% in 25% steps. For degree centrality, we placed the primary inoculum in into each 20% quantile. Unless otherwise noted, each scenario was run 100 times to capture variability in binomial draws. We report either the mean or percentiles of the *relative* change in profit per hectare compared to a no-disease/no-spray baseline.

Summary of Simulation Parameters

Table 3 provides a concise overview of the key parameters we varied in the nested for-loops of our simulation experiments. Each parameter name is kept brief so it fits on a single line in the table. For every combination of these parameter values, we ran the simulation for each of the four years (2014–2017) and for each of three market-demand scenarios (low, moderate, high).

Table 3: Key parameters varied in the simulation, their tested ranges, and the rationale or source.

Parameter	Values Tested	Rationale / Data Source
Year	2014, 2015, 2016, 2017	Real yard size, distance and wind patterns were available for each year, reflecting distinct conditions.
Simulations	100	Each scenario is replicated to capture variability from binomial draws of initial disease.
Quantiles	5	Yards are classified into five bins by degree-centrality, used when varying location-based initial infections.
Pathogen-diversity	0.0, 0.25, 0.50, 0.75, 1.0	Varies fraction of initial inoculum from V6-virulent vs. non-V6-virulent strains.
Sprays in May	0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10	Extra sprays (beyond baseline) if a yard has flag shoots. Upper end (10) tests diminishing returns.
Initial infection probability	0.00001, 0.00005, 0.0001, 0.0005, 0.001, 0.005, 0.01	Represents the probability of a plant harboring overwintered infection. Spans extremely rare (e.g. 0.00001) to modestly frequent (e.g. 0.01).
Market scenario	low, moderate, high	Captures three contrasting demand/price structures, impacting crop-value and quality penalties.

Beyond these parameters, the simulation code uses yard-level attributes (area, distance matrices, wind data) and the fitted model coefficients described in Sections 2 and 3. In each scenario, the model outputs include time-series of disease incidence and final net profit estimates under the specified market-demand conditions, allowing for comparisons of how early-season sprays and pathogen diversity affect economic outcomes.

Results

The simulation results demonstrate a strong dependence of profitability on initial epidemic conditions, specifically highlighting the influence of initial inoculum

dose, pathogen diversity, and the dispersal centrality of the initially infected yards on disease management strategies.

Impact of Initial Inoculum Dose

The initial probability of disease (p_0) emerged as a dominant factor influencing the profitability and efficacy of fungicide applications.

- **Low Inoculum ($p_0 \leq 0.0001$):** Across all market demand scenarios, when the initial probability of disease was very low ($p_0 = 0.00001$ or 0.00005), the relative change in profit remained close to zero regardless of the number of fungicide sprays in May. For example, in 2014 under low demand, the profit change was consistently between 0% and -1% for all spray numbers and dispersal centrality percentiles.
- **Moderate to High Inoculum ($p_0 \geq 0.001$):** As p_0 increased, profitability became more sensitive to the number of sprays. For $p_0 = 0.005$ or 0.01 , failing to spray (0 sprays) resulted in profit losses of up to -10% (especially in high centrality yards and under high demand).
 - In contrast, applying 4–6 sprays in May minimized losses, with profit changes typically between -1% and -3%. For example, in the high demand scenario, at $p_0 = 0.01$, 0 sprays led to losses of -10% to -12% in the most central yards, while 5–6 sprays reduced losses to about -2% to -3%.

Effect of Pathogen Diversity

Pathogen strain diversity also played an influential role, particularly in scenarios where the pathogen population included varying proportions of the V6-virulent strain capable of infecting a broader range of cultivars. As the proportion of the V6-virulent strain increased, the optimal number of fungicide sprays required to maximize profitability rose accordingly. When pathogen populations consisted predominantly or entirely of the V6-virulent strain, fungicide applications became increasingly essential to maintaining profitability. Thus, pathogen diversity directly affected both the necessity and frequency of fungicide interventions, emphasizing the need for careful monitoring and targeted responses to pathogen strain composition.

Quantitatively, in the high demand scenario for $p_0 = 0.01$ and 100% V6, profit losses without spraying reached -10% to -12%, while 5–6 sprays reduced losses to -2% to -3%.

Influence of Dispersal Centrality

The location of initial infections, measured by the dispersal centrality of infected yards, significantly impacted profitability, particularly under high inoculum pressure scenarios. Initial infections in highly central yards were more detrimental, exacerbating the spread and subsequent economic losses across the region. For

example, in the high demand scenario at $p_0 = 0.01$, 0 sprays led to losses of -10% to -12% in the most central yards, compared to -6% to -8% in the least central yards. In contrast, when initial infections occurred in less central yards, the relative economic losses were reduced, particularly under higher market demand scenarios. This finding underscores the strategic importance of identifying and rapidly addressing outbreaks in central locations within a network of interconnected agricultural units.

Market Demand Conditions

Different market demand conditions notably influenced the optimal disease management strategy. Under high market demand conditions, the impact of early fungicide interventions on profitability was moderate, reflecting more flexible quality standards. Conversely, under moderate and low market demand conditions, where quality requirements were more stringent, the profitability was much more sensitive to fungicide application strategies. Increased fungicide use was essential under these lower demand scenarios to prevent severe quality-related profit reductions. For instance, under low demand, the economic penalty for under-spraying was greatest, with losses up to -10% at high p_0 and 0 sprays, and only reduced to -2% to -3% with 5–6 sprays.

Summary Table of Key Quantitative Results (2014):

Scenario	0 Sprays ($p_0 = 0.01$)	5–6 Sprays ($p_0 = 0.01$)	0 Sprays ($p_0 = 0.00001$)
Low Demand, High Centrality	-10%	-2%	0%
Moderate Demand, High Centrality	-8%	-2%	0%
High Demand, High Centrality	-12%	-3%	0%

Comparison of Parameter Estimates Between May–June and June–July

Table 4: Parameter estimates for epidemic model

Parameter	May–June	June–July
Epidemic Model		
β_1 (Baseline log-odds)	-2.06	-2.79
β_2 (Baseline log-odds)	-4.15	-3.88
δ_1 (Autoinfection effect)	2074.35	2.94
δ_2 (Autoinfection effect)	120.46	8.04
γ_1 (Dispersal effect)	34358.91	1390.71
γ_2 (Dispersal effect)	14536.03	286.8
α_1 (Dispersal kernel)	0.71	1.0
α_2 (Dispersal kernel)	2.67	2.04
η_{11} (Fungicide effect)	3.51	0.02
η_{12} (Fungicide effect)	1.62	0.31
η_{21} (Fungicide effect)	2.9	0.95
η_{22} (Fungicide effect)	0.27	0.37

To better understand the temporal dynamics of the epidemic model, we compared the parameter estimates for the two key transition periods: May–June and June–July (see Table 4).

Several notable differences emerge between these periods:

- The baseline log-odds of disease (β_1, β_2) are lower (more negative) in May–June (-2.06, -4.15) than in June–July (-2.79, -3.88), indicating a lower baseline risk of disease early in the season.
- The effect of autoinfection (δ_1, δ_2) is much larger in May–June (2074.35, 120.46) compared to June–July (2.94, 8.04), suggesting that local sources of inoculum are most influential at the start of the epidemic.
- The effect of dispersal from other yards (γ_1, γ_2) is also much greater in May–June (34358.91, 14536.03) than in June–July (1390.71, 286.8), highlighting the importance of regional spread early in the epidemic.
- The dispersal kernel parameters (α_1, α_2) are higher in June–July (1.0, 2.04) than in May–June (0.71, 2.67), indicating a possible shift in the spatial scale of dispersal as the season progresses.
- The fungicide effect parameters ($\eta_{11}, \eta_{12}, \eta_{21}, \eta_{22}$) are generally larger in May–June, especially η_{11} (3.51 vs 0.02), suggesting that fungicide applications are more effective at reducing disease early in the season.

Overall, these differences indicate that both local and regional sources of inoculum are most important in the early epidemic phase, and that fungicide applications have their greatest impact when applied early. As the season progresses, the epidemic becomes less sensitive to these factors, possibly due to depletion of susceptible hosts or environmental changes.

Discussion

Our analysis addresses a multifaceted challenge in agricultural disease management where epidemic control decisions must account for complex interactions between pathogen biology, management practices, market conditions, and regional-scale disease transmission. Three key findings emerge from our simulations: first, epidemic control is exquisitely sensitive to conditions in the earliest stages of outbreaks, with relatively small changes in initial inoculum dose and early-season fungicide applications translating to substantial economic differences; second, there exists a critical threshold in pathogen pressure below which intensive management becomes unnecessary, suggesting opportunities for area-wide interventions targeting primary inoculum reduction; and third, quality-sensitive market conditions paradoxically drive more intensive fungicide use under depressed demand scenarios, challenging traditional economic injury level concepts when crop value is tied to quality standards rather than yield alone.

Threshold Effects and Early Intervention Sensitivity

The most striking finding from our simulations is the threshold-like response in optimal control strategies as initial inoculum probability increases. When initial probability of disease remained below 0.0001, economic losses were minimal regardless of fungicide application intensity, pathogen strain diversity, or initial infection location. Above this threshold, however, the system exhibited dramatic sensitivity to early-season management decisions, with the optimal number of fungicide applications in the first month becoming the dominant factor determining economic outcomes.

This pattern aligns with theoretical predictions for epidemic systems where containment efficiency depends critically on early-stage contact rates and intervention timing [19] [21]. For spatially-explicit epidemics with long-distance dispersal capabilities, small changes in primary inoculum can cascade through the transmission network, leading to non-linear responses in final epidemic size [24]. Our results provide empirical support for this theoretical framework while demonstrating its practical implications for management. The sensitivity we observed—where a 10-fold reduction in initial inoculum could largely eliminate economic damage—suggests that area-wide interventions targeting primary inoculum reduction may be more cost-effective than field-level fungicide intensification.

This threshold behavior has been documented across diverse host-pathogen systems, from livestock diseases [22] to forest pathogens [23], suggesting our findings may generalize beyond the hop powdery mildew system. The critical insight is that epidemic management strategies should be calibrated to the regime in which the system operates: below-threshold conditions favor prevention and minimal intervention, while above-threshold conditions require rapid, coordinated response.

Complexity and Unique Contributions of the Modeling Approach

Our pathosystem represents an unusually complex scenario for economic epidemiology, combining several challenging features: a highly dispersible pathogen capable of long-distance transmission, damage to both yield and quality metrics, market-sensitive quality standards, and strain-specific host resistance creating heterogeneous susceptibility landscapes. This complexity necessitated a novel modeling approach that simultaneously captures network-scale disease transmission, multi-dimensional crop damage functions, and market-dependent economic outcomes.

The richness of our four-year census dataset enables parameterization of this complex system in unprecedented detail. Few studies have combined such extensive disease observations with comprehensive records of grower management decisions and market conditions across multiple years and spatial scales. This allows us to model not only disease spread within individual fields but also the community effects of disease management—how fungicide applications in one field influence disease pressure and economic outcomes in neighboring fields.

This methodological approach provides a roadmap for analyzing other agricultural systems where pathogens exhibit aerial dispersal and cause multi-dimensional damage. The framework is particularly relevant for high-value crops where quality defects carry disproportionate economic penalties and where production occurs in spatially-concentrated regions that facilitate pathogen transmission between farms. Examples include wine grapes affected by powdery mildew, fruit crops susceptible to fire blight, or ornamental crops where visual quality is paramount.

Market Sensitivity and Economic Injury Level Paradigms

Our finding that depressed market conditions lead to more intensive fungicide use challenges conventional economic injury level (EIL) concepts in pest management [25]. Traditional EIL theory predicts that lower crop values should reduce the economic threshold for control action, thereby decreasing pesticide use. In our system, the opposite occurs because quality standards become more stringent under low-demand scenarios, creating asymmetric penalties for quality defects versus over-treatment.

This pattern reflects a broader challenge in crops where value depends on meeting specific quality criteria rather than maximizing yield. When crop rejection or severe devaluation becomes possible, risk-averse growers may adopt intensive management strategies that exceed the classical EIL optimization. Under high pathogen pressure in our simulations, the economic penalty for under-treatment became as severe as over-treating by two to three times the necessary level.

The sensitivity of optimal strategies to market conditions has important implications for pest management recommendations and policy. Extension programs typically provide fungicide guidance based on disease pressure alone, but our

results suggest that market context should also inform management decisions. Furthermore, the vague language in many U.S. hop production contracts regarding quality standards may exacerbate this issue by increasing uncertainty and encouraging conservative (intensive) management approaches.

Comparative Context and Theoretical Implications

The patterns we observe are consistent with broader principles of epidemic theory and management across biological systems. The threshold effects we document parallel phase transitions observed in theoretical epidemiology, where epidemic behavior changes qualitatively as basic reproduction numbers cross critical values [26]. Similarly, the sensitivity to early intervention aligns with the “golden hour” concept in human disease outbreak response, where rapid action in the initial stages determines overall outbreak severity [27].

Our findings regarding spatial effects—where initial infections in highly connected yards caused greater regional damage—mirror results from network epidemiology in other systems, from computer virus spread [28] to wildlife disease management [29]. The principle that controlling highly connected nodes can disproportionately reduce system-wide transmission appears to be robust across diverse epidemic contexts.

The economic aspects of our analysis contribute to the growing literature on bioeconomic modeling in plant pathology [30]. Our demonstration that multi-dimensional damage functions can create counter-intuitive relationships between crop value and management intensity adds to understanding of how market forces shape disease management decisions in modern agriculture.

Study Limitations and Future Directions

Several limitations should be considered when interpreting our results. The damage functions linking disease incidence to cone color and subsequent price adjustments rely on relationships derived from literature rather than direct observation, introducing uncertainty in the precise magnitude of economic effects. The vague language in production contracts that we identify as problematic also complicates model parameterization. Future work should involve controlled studies to better quantify these damage relationships and their variability across market conditions.

Our analysis assumes risk-neutral growers, but the quality-sensitivity we document suggests that risk preferences may significantly influence management decisions. Incorporating risk aversion into the economic framework could refine predictions and better explain the conservative management strategies we observe in practice.

The model also does not explicitly account for fungicide resistance development or long-term sustainability concerns. As resistance to current fungicide modes of action emerges in hop powdery mildew populations, the optimal strategies

we identify may require modification. Similarly, environmental concerns and regulatory pressures may constrain the intensive fungicide regimes that appear economically optimal under certain scenarios.

Implications for Management and Policy

Our results suggest several actionable insights for disease management and agricultural policy. The threshold effects we document indicate that area-wide programs targeting primary inoculum reduction—through cultural practices, resistant cultivar deployment, or coordinated sanitation—may be more effective than field-level intensification of fungicide programs. The 10-fold reduction in initial inoculum that could largely eliminate economic damage appears achievable through coordinated implementation of existing cultural practices.

The sensitivity to early-season management emphasizes the importance of rapid response capabilities and early-season monitoring programs. Extension services should prioritize early-season disease detection and ensure that fungicide recommendations account for both disease pressure and market conditions.

Finally, our finding regarding contract language and quality standards suggests that policy interventions to clarify quality metrics could potentially reduce both economic uncertainty for growers and unnecessary pesticide applications. More explicit, demand-independent quality standards might allow for more precise optimization of management strategies.

The coupled epidemiological-economic modeling framework we develop provides a foundation for analyzing similar systems and evaluating policy interventions. As concerns about pesticide use intensify and climate change alters pest pressure patterns, such integrated approaches will become increasingly important for developing sustainable disease management strategies that balance economic, environmental, and social objectives.

Appendix

We expand on the generalized regression model developed in previous work. For a given yard i , we estimate the log-odds of disease η_i given by:

$$\eta_{i,\tau} = \sum_{k=1}^K I_k^{(t)}(i) \left[\beta_{k,\tau} + \delta_{k,\tau} \left(\frac{\tilde{y}_i}{n_{\tilde{y}_i}} \exp(-\eta_{1k}s_i) \right) + \gamma_{k,\tau} \sum_{j=1}^{M_i} \left(\frac{a_j z_j}{n_{z_j}} \exp(-\eta_{2k}s_j) w_{ij} \exp(-\alpha_{k,\tau}d_{ij}) I_k^{(s)}(j) \right) \right]$$

Parameter Estimates

Table 5: Parameter estimates for damage functions

Parameter	Estimate
Cone Incidence Model	
a_1	[value]
b_1	[value]
Yield Loss Model	
a_2	[value]
Cone Color Model	
a_3	[value]
b_3	[value]
Adjusted Price Model (Sigmoid Function)	
<i>High Demand</i>	
θ_0	[value]
θ_1	[value]
<i>Moderate Demand</i>	
θ_0	[value]
θ_1	[value]
<i>Low Demand</i>	
θ_0	[value]
θ_1	[value]

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