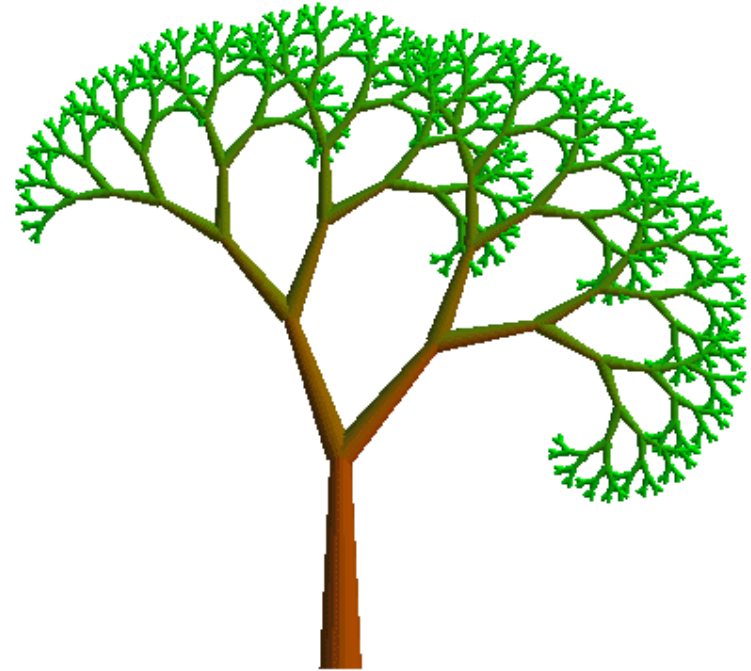


Dictionaries and Map Paths



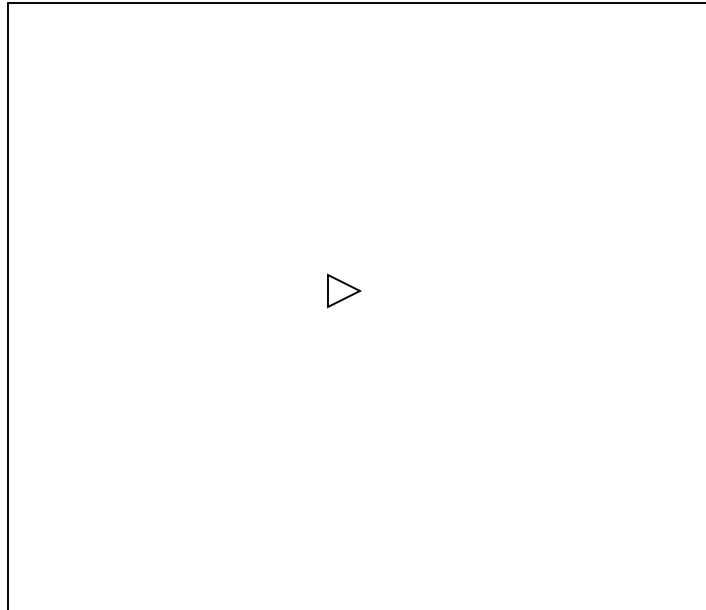
Recursive pictures

Tuples: immutable sequences

Dictionaries: a new data type

Using a dictionary to compute routes in a map

Turtle Graphics

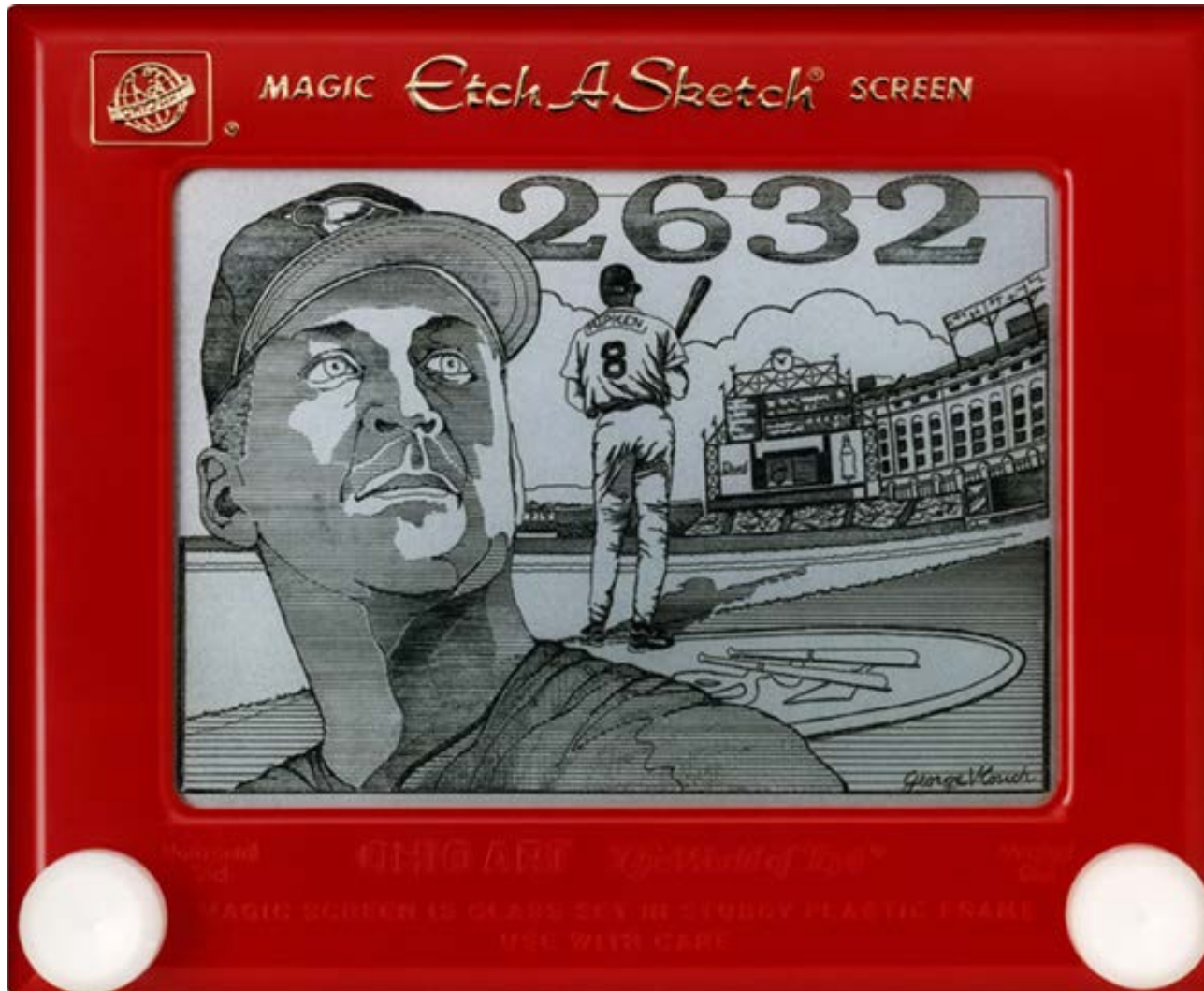


forward(100)

right(90)



Etch-a-Sketch craziness...



No way this is real...
except that it is !

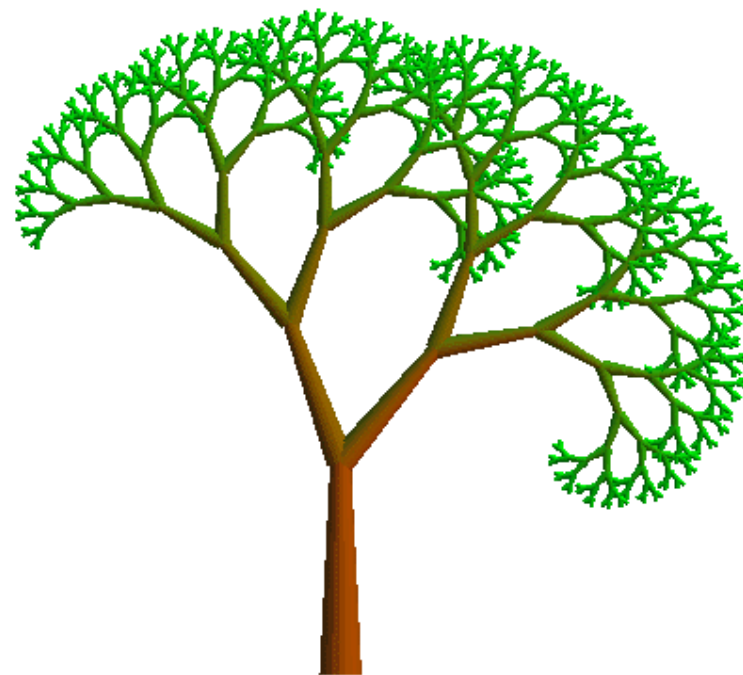
Turtle Graphics



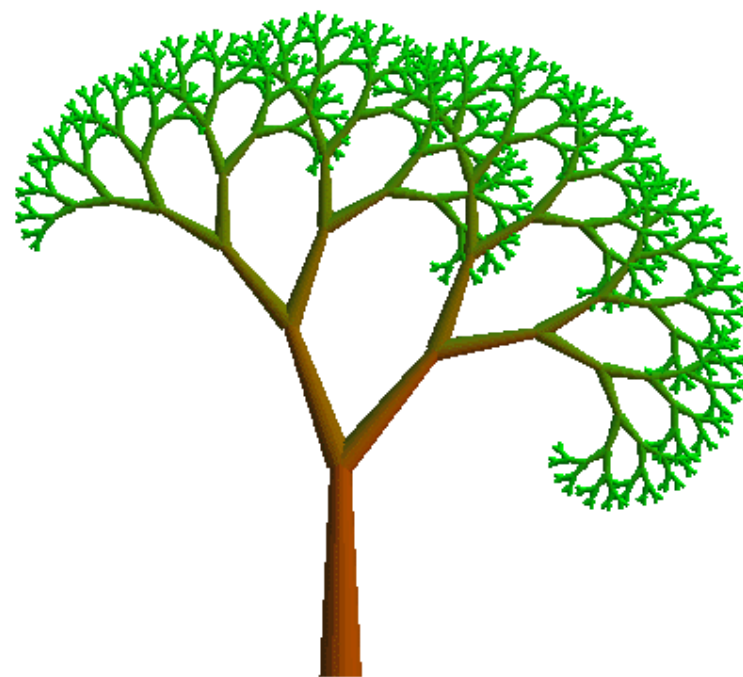
```
>>> import turtle
>>> turtle.forward(50)
>>> turtle.right(90)
>>> turte.backward(50)
```

degrees()	radians()	reset()
clear()	tracer(flag)	forward(distance)
backward(distance)	left(angle)	right(angle)
up()	down()	width(width)
color(*args)	fill(flag)	heading()
setheading(angle)	window_width()	window_height()
position()	setx(xpos)	sety(ypos)
goto(x,y)		

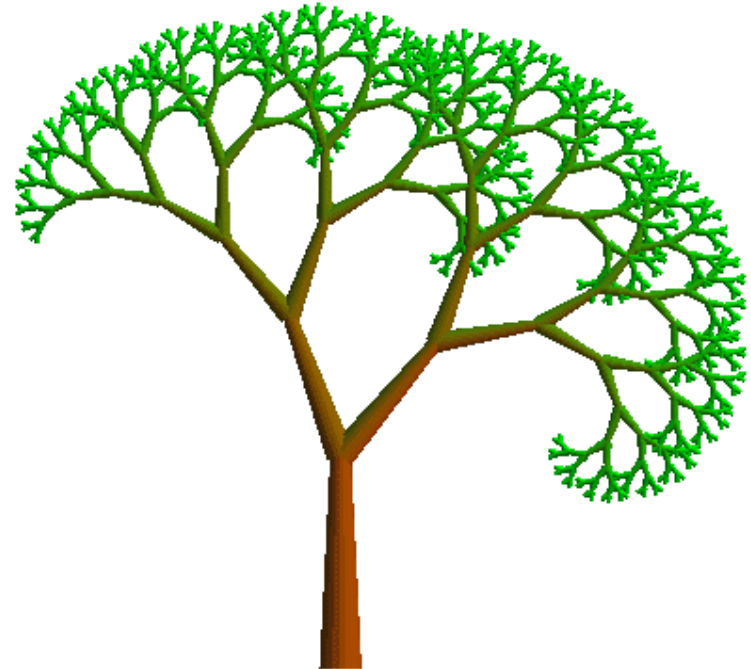
Fractals



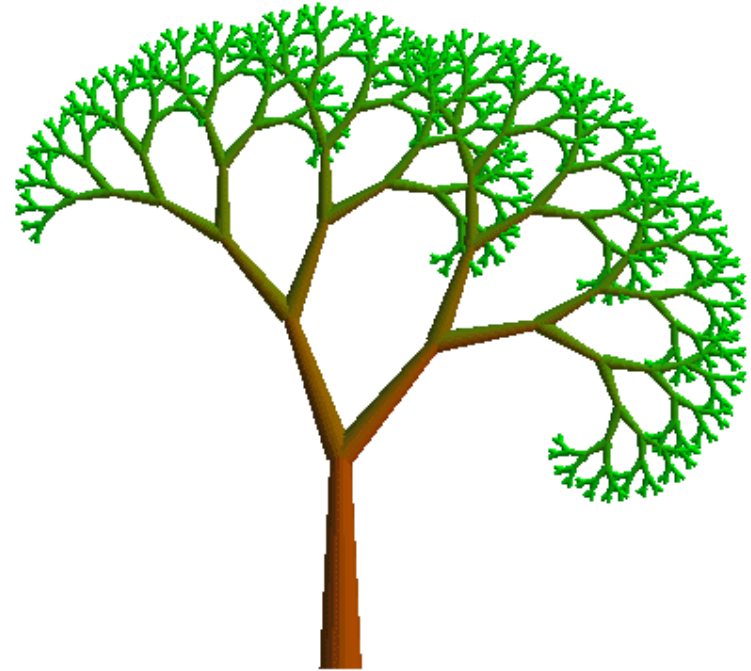
Fractals



Fractals



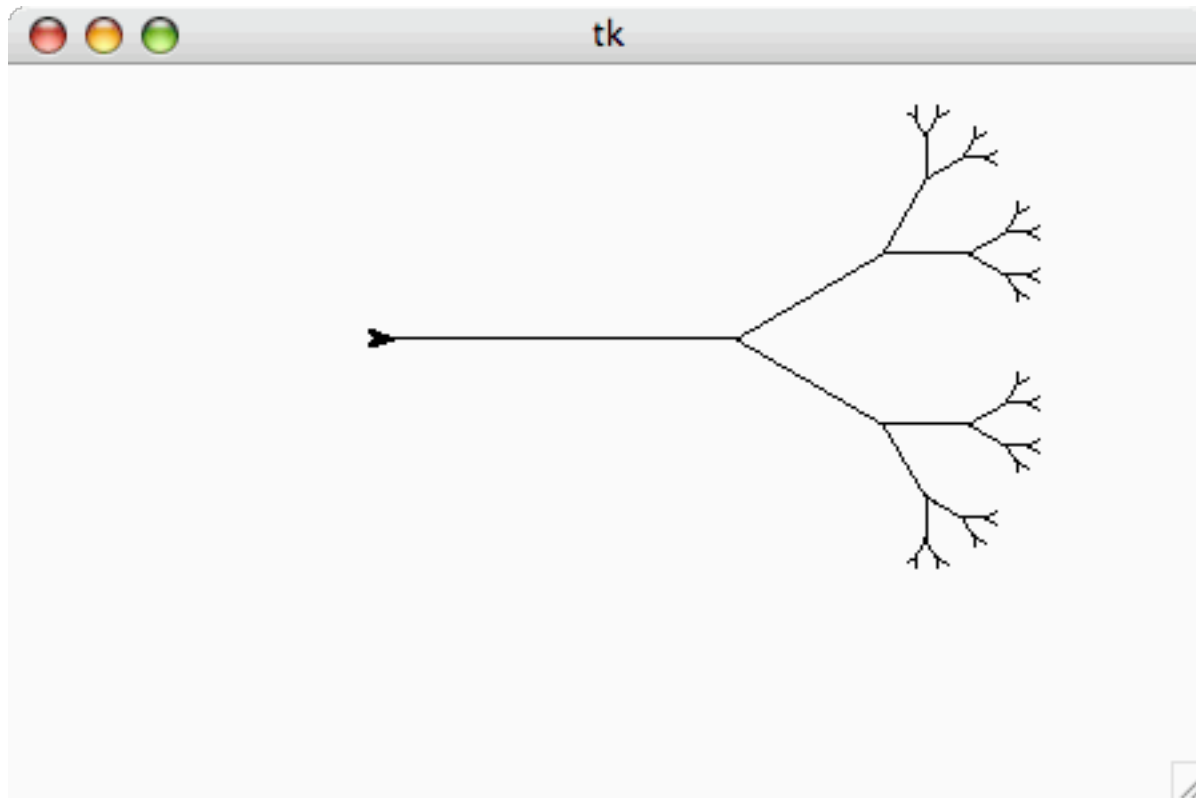
Fractals



“I wonder about Trees” – Robert Frost

“We wonder about Robert Frost” - Trees

```
>>> svTree(128, 6)
```



recursion level trunk length

>>> svTree(3, 100)



recursion level trunk length


>>> svTree(3, 100)



100 long!

recursion level trunk length

>>> svTree(3, 100)



svTree(2, 50)

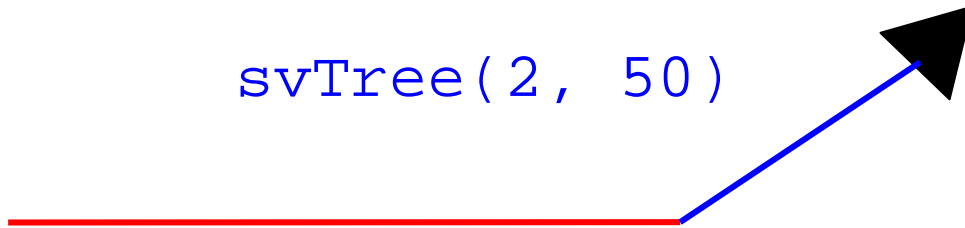


100 long!

recursion level trunk length

>>> svTree(3, 100)

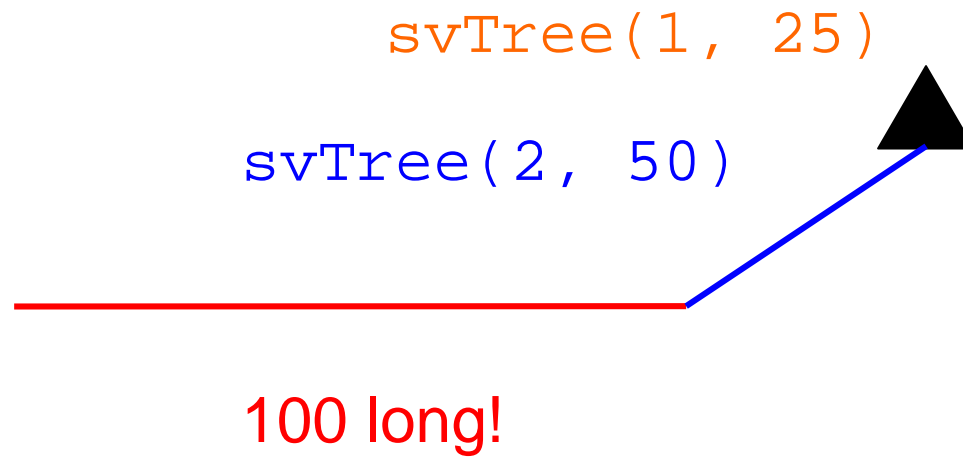
svTree(2, 50)



100 long!

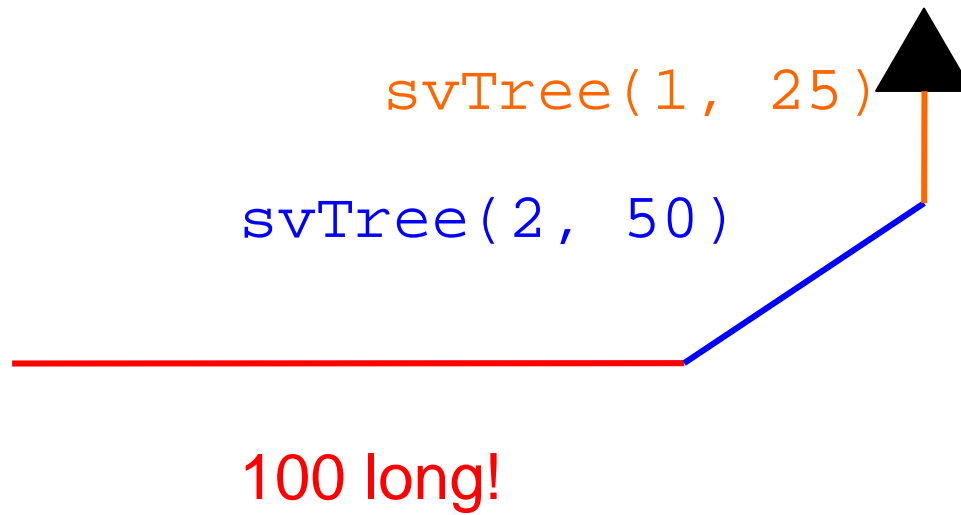
recursion level trunk length

>>> svTree(3, 100)



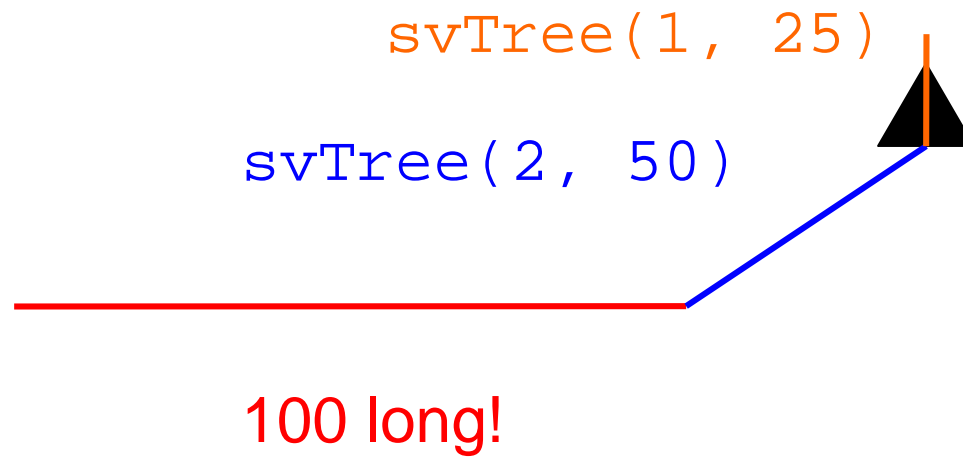
recursion level trunk length

```
>>> svTree(3, 100)
```



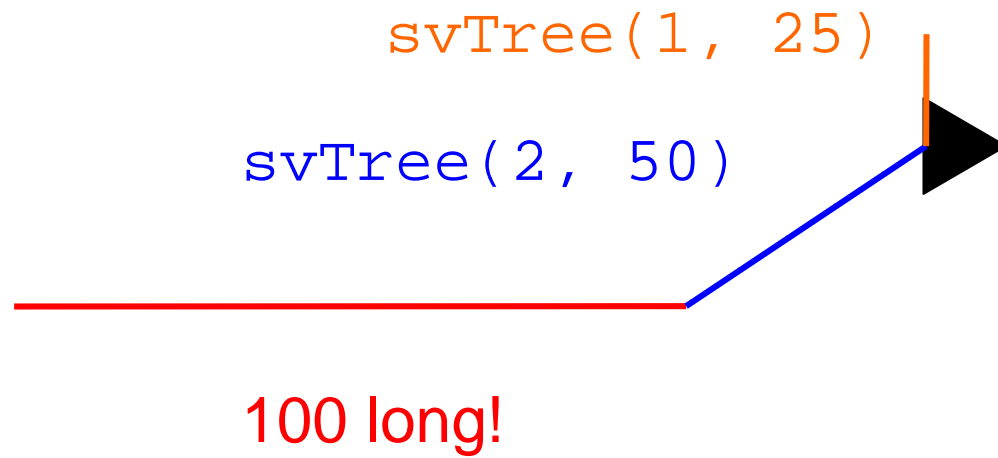
recursion level trunk length

>>> svTree(3, 100)



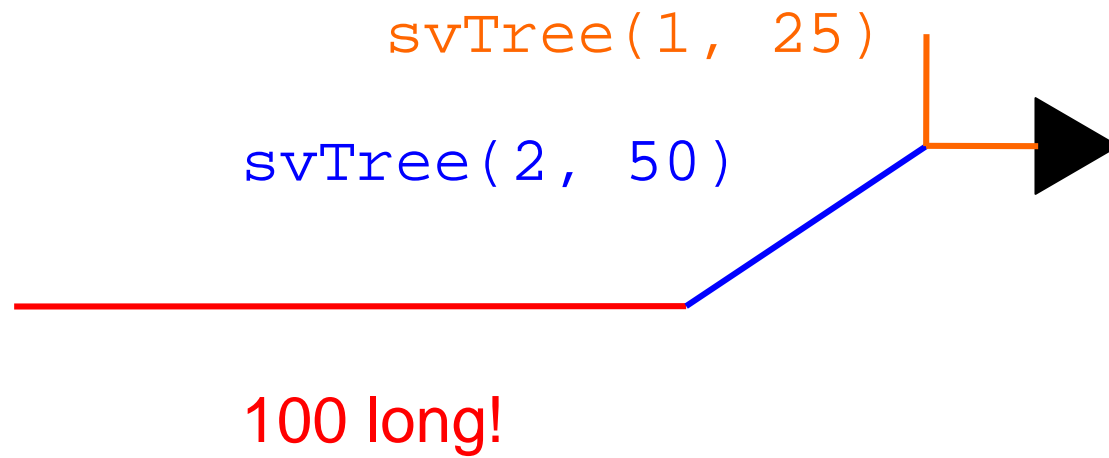
recursion level trunk length

>>> svTree(3, 100)



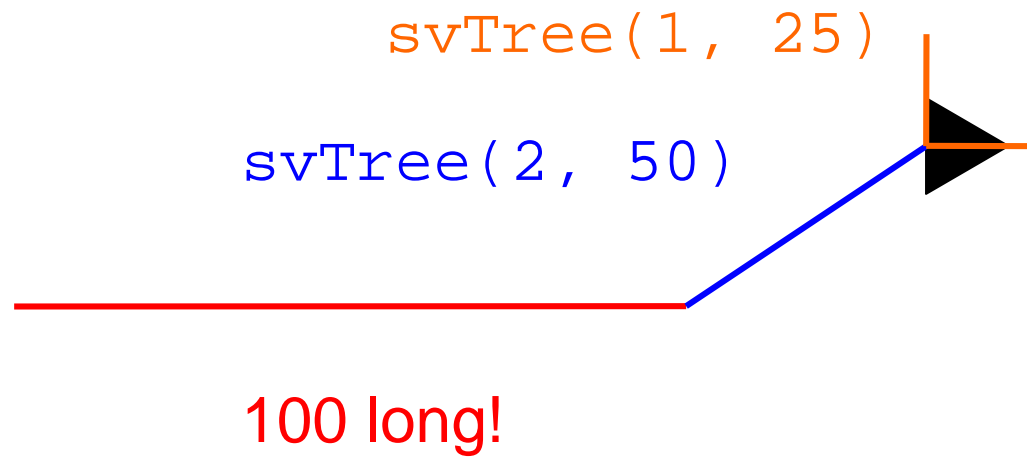
recursion level trunk length

>>> svTree(3, 100)



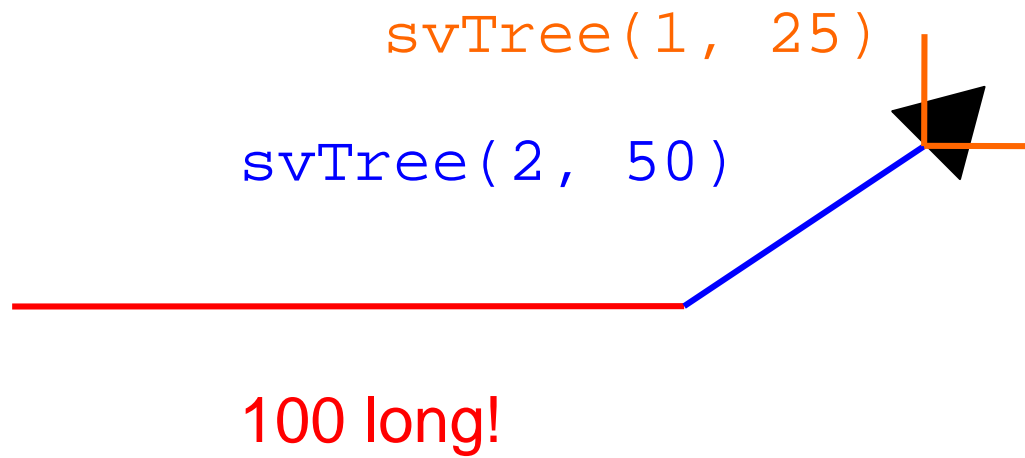
recursion level trunk length

>>> svTree(3, 100)



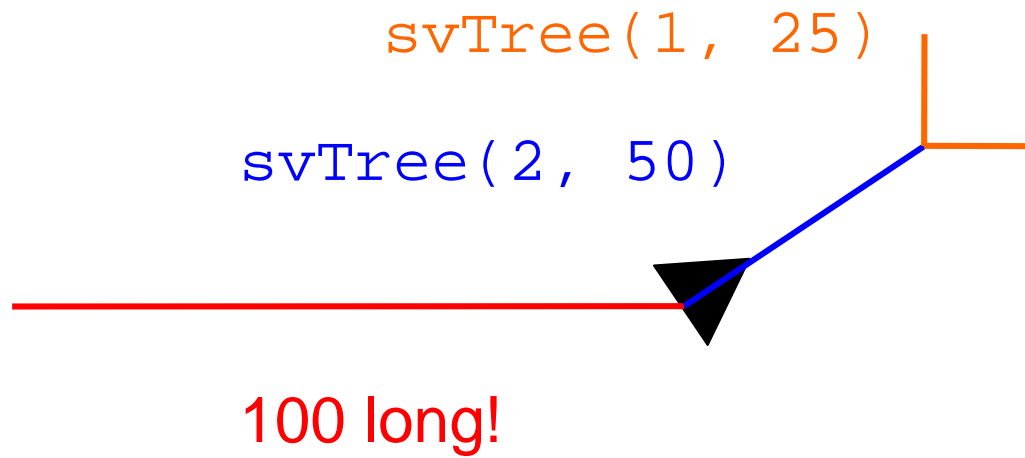
recursion level trunk length

>>> svTree(3, 100)



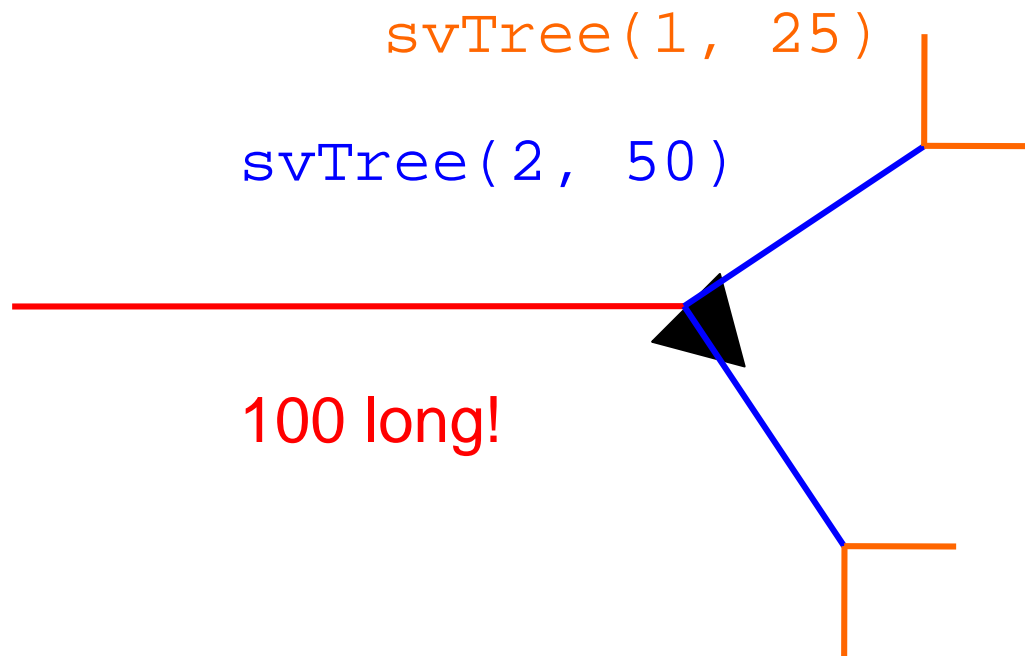
recursion level trunk length

>>> svTree(3, 100)



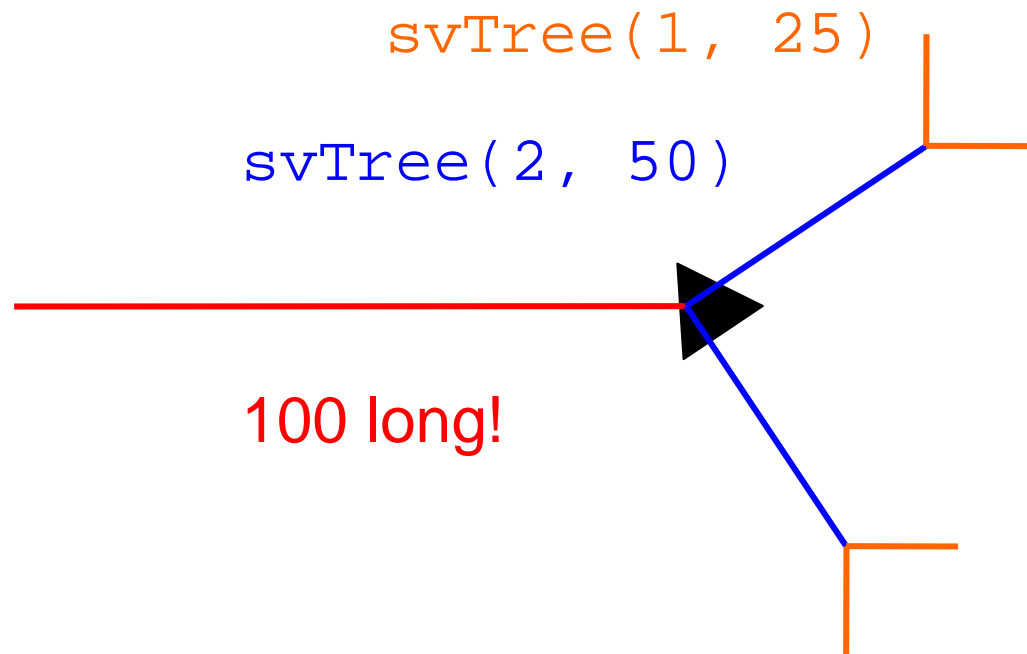
recursion level trunk length

```
>>> svTree(3, 100)
```



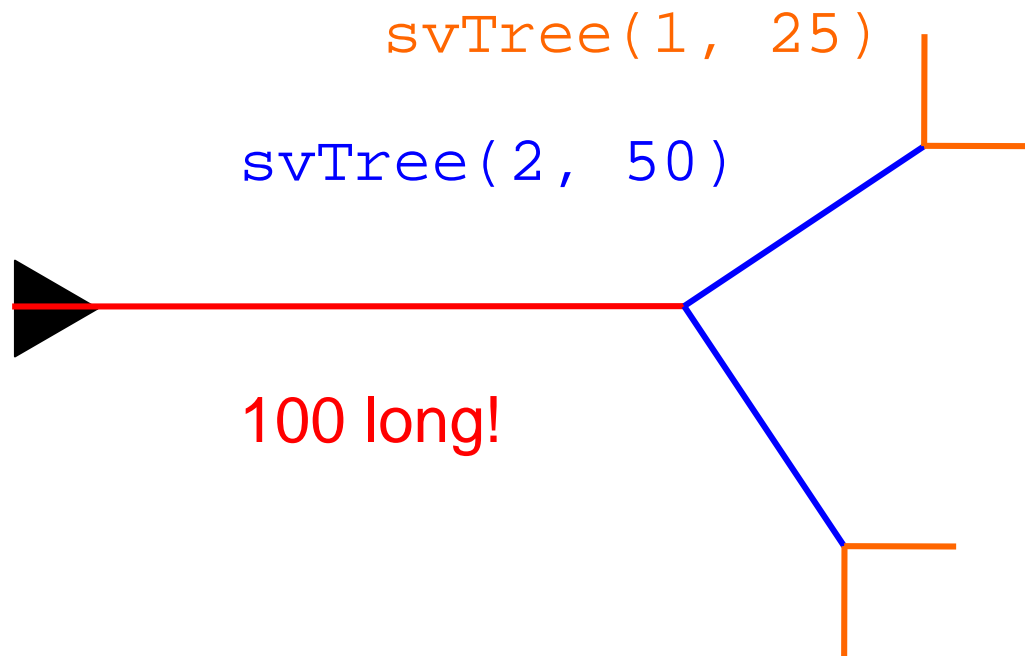
recursion level trunk length

```
>>> svTree(3, 100)
```



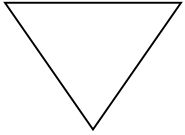
recursion level trunk length

```
>>> svTree(3, 100)
```

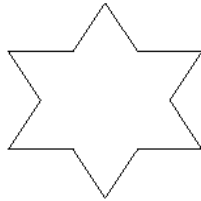


Snowflake Fractals

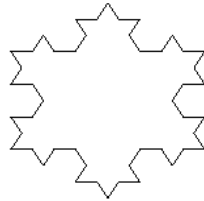
The Koch Snowflake Fractal:



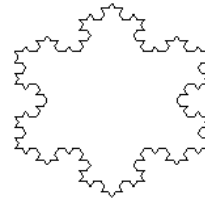
level 0



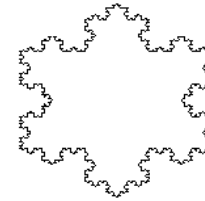
level 1



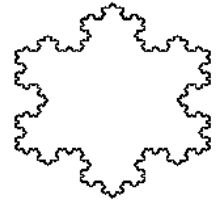
level 2



level 3



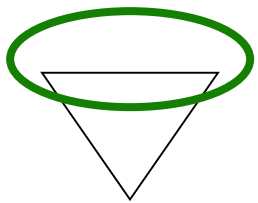
level 4



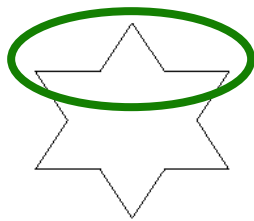
level 5

Snowflake Fractals

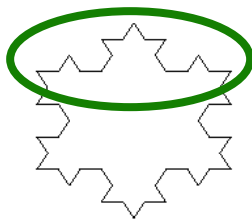
The Koch Snowflake Fractal:



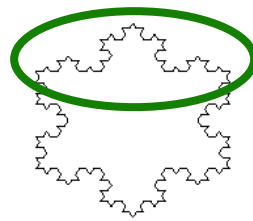
level 0



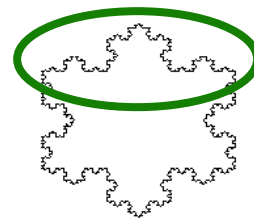
level 1



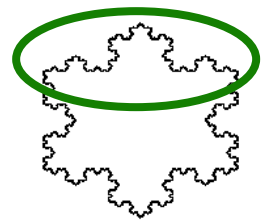
level 2



level 3



level 4

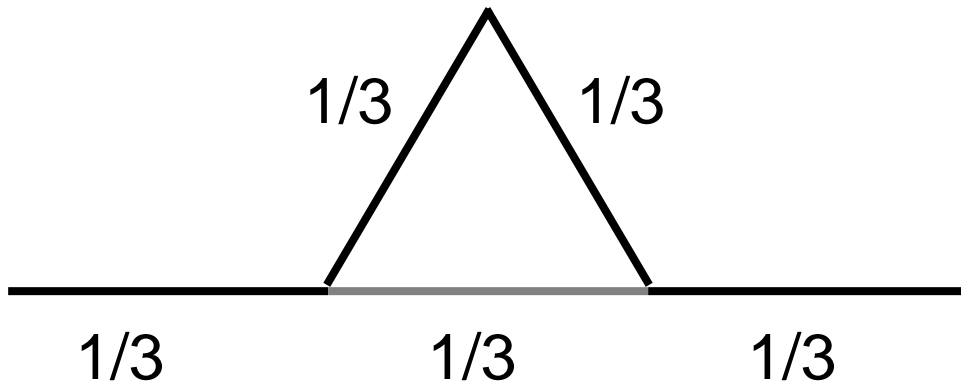


level 5

level 0



level 1



And now for something completely different...

(...or at least it will seem different until we see that it's not!)



Tuples (“immutable lists”)

```
>>> foo = (42, 'hello', (5, 'spam'), 'penguin')
>>> foo
(42, 'hello', (5, 'spam'), 'penguin')
>>> foo[0]
42
>>> foo[-1]
'penguin'
>>> foo[0:2]
(42, 'hello')
>>> foo[0:1]
(42,)
```

Tuples (“immutable lists”)

```
>>> foo = (42, 'hello', (5, 'spam'), 'penguin')
```

```
>>> foo
```

```
(42, 'hello', (5, 'spam'), 'penguin')
```

```
>>> foo[0]
```

```
42
```

```
>>> foo[-1]
```

```
'penguin'
```

```
>>> foo[0:2]
```

```
(42, 'hello')
```

```
>>> foo[0:1]
```

```
(42,)
```

```
>>> foo[0] = 100
```

```
BARF!!! (that's California-speak for 'error')
```


Dictionaries

```
>>> D = {}
>>> D["Ran"] = "spam"
>>> D["Zach"] = "donuts"
>>> D["Alien"] = 42
>>> D["Ran"]
'spam'
>>> D["Alien"]
42
>>> D["Napoleon Dynamite"]
BARF!
```

“Ran”, “Zach”, and “Alien” are called the “keys” in the dictionary. Any *immutable* object can be a key.

Dictionaries

```
>>> D = {}
>>> D["Ran"] = "spam"
>>> D["Zach"] = "donuts"
>>> D["Alien"] = 42
>>> D["Ran"]
'spam'
>>> D["Alien"]
42
>>> D["Napoleon Dynamite"]
BARF!
>>> D
{ 'Ran': 'spam', 'Zach': 'donuts', 'Alien': 42 }
```

Dictionaries - summary

A dictionary associates values with keys.

```
D = {}      # create an empty dictionary
D[k]= v     # make key k have value v
            # (replace old value if k already in D)
D[k]        # get value under key k
D.has_key(k) # whether k is a key in D
```

Example: {'cat':3, 'avatar':1, 'sprite':42}

v can be any value

k must be an immutable type (string, int,
tuple of immutables)

Finding Shortest Paths



382 Blaisdell Dr, Cla

Get Directions [My Maps](#)



A 382 Blaisdell Dr, Claremont, CA 91711

B 1600 Pennsylvania Avenue Northwest, Washingtc

[Add Destination](#) - [Show options](#)

Get Directions

Driving directions to 1600 Pennsylvania Ave NW, Washington D.C., DC 20500

Suggested routes

I-40 E 1 day 18 hours
2,628 mi

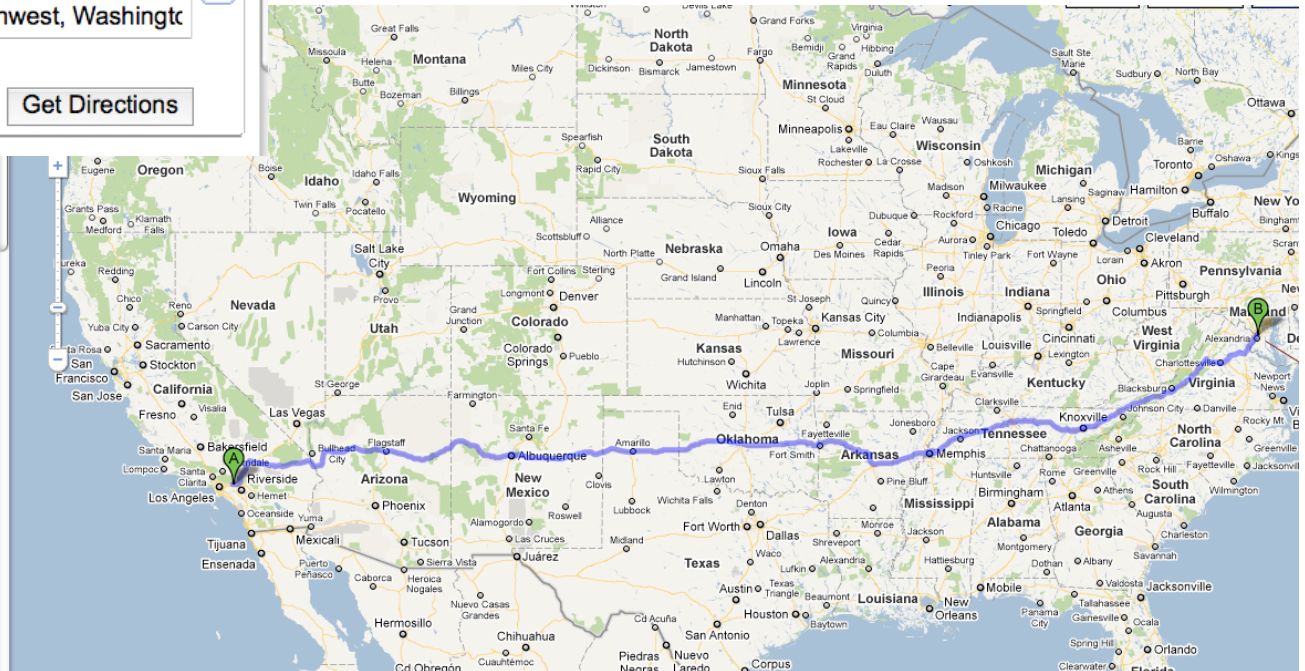
[I-40 E and I-64 E](#) 1 day 18 hours
2,657 mi

[I-70 E](#) 1 day 19 hours
2,652 mi

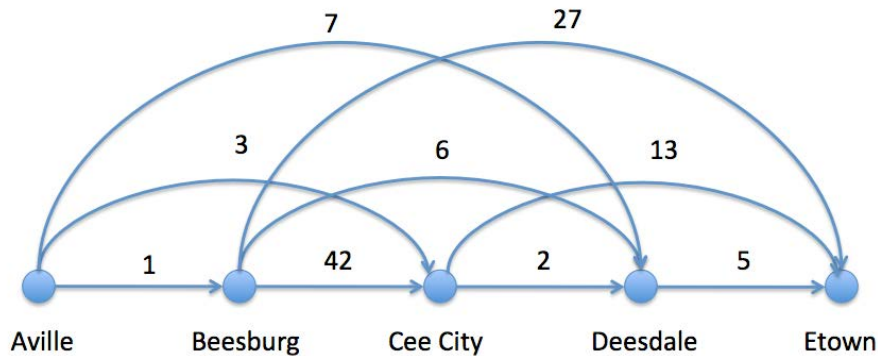
This route has restricted usage or private roads.

A 382 Blaisdell Dr
Claremont, CA 91711

1. Head east on Blaisdell Dr toward Bates Pl 0.1 mi
2. Take the 3rd left onto N Mills Ave 0.7 mi
3. Turn right at E Baseline Rd 0.7 mi



Google maps



```
Inf = float("inf")
```

```
FiveCities = ["A", "B", "C", "D", "E"]
```

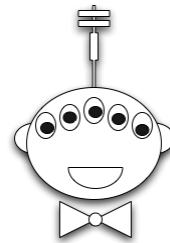
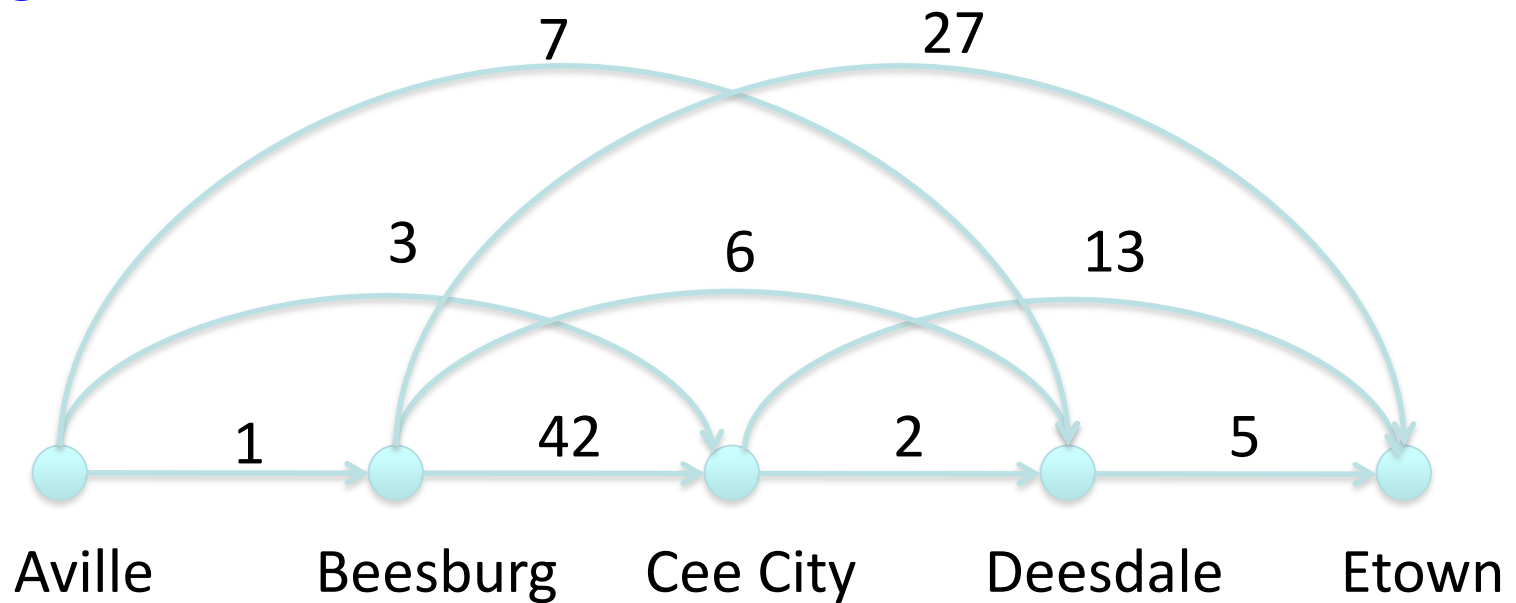
```
FiveDists = {("A", "A"):0, ("A", "B"):1, ("A", "C"):3, ("A", "D"):7, ("A", "E"):Inf,  
             ("B", "A"):Inf, ("B", "B"):0, ("B", "C"):42, ("B", "D"):6, ("B", "E"):27,  
             ("C", "A"):Inf, ("C", "B"):Inf, ("C", "C"):0, ("C", "D"):2, ("C", "E"):13,  
             ("D", "A"):Inf, ("D", "B"):Inf, ("D", "C"):Inf, ("D", "D"):0, ("D", "E"):5,  
             ("E", "A"):Inf, ("E", "B"):Inf, ("E", "C"):Inf, ("E", "D"):Inf, ("E", "E"):0  
}
```

```
>>> FiveDists[ ("B", "C") ]  
42
```

Sometimes we need to make more than 2 recursive calls!



Google maps

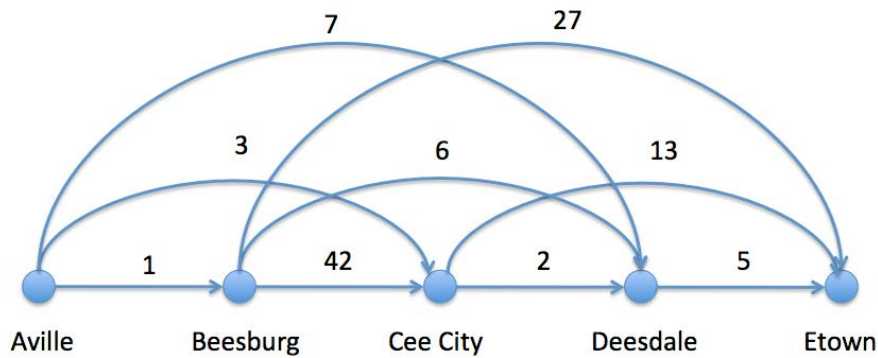


All roads point east!

Shortest path?

Is greed good?

How does the use-it-or-lose-it idea get used here?



```
Inf = float("inf")
```

```
FiveCities = ["A", "B", "C", "D", "E"]
```

```
FiveDists = {("A", "A"):0, ("A", "B"):1, ("A", "C"):3, ("A", "D"):7, ("A", "E"):Inf,
              ("B", "A"):Inf, ("B", "B"):0, ("B", "C"):42, ("B", "D"):6, ("B", "E"):27,
              ("C", "A"):Inf, ("C", "B"):Inf, ("C", "C"):0, ("C", "D"):2, ("C", "E"):13,
              ("D", "A"):Inf, ("D", "B"):Inf, ("D", "C"):Inf, ("D", "D"):0, ("D", "E"):5,
              ("E", "A"):Inf, ("E", "B"):Inf, ("E", "C"):Inf, ("E", "D"):Inf, ("E", "E"):0
            }
```

```
>>> shortestPath (FiveCities, FiveDists)
```

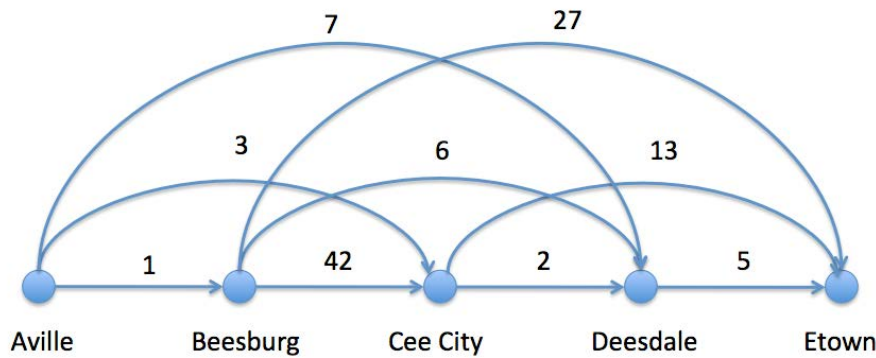
```
10
```

```
>>> shortestPath (["C", "D", "E"], FiveDists)
```

```
7
```

```
>>> shortestPath (["E"], FiveDists)
```

```
0
```



```
Inf = float("inf")
```

```
FiveCities = ["A", "B", "C", "D", "E"]
```

```
FiveDists = {("A", "A"):0, ("A", "B"):1, ("A", "C"):3, ("A", "D"):7, ("A", "E"):Inf,
              ("B", "A"):Inf, ("B", "B"):0, ("B", "C"):42, ("B", "D"):6, ("B", "E"):27,
              ("C", "A"):Inf, ("C", "B"):Inf, ("C", "C"):0, ("C", "D"):2, ("C", "E"):13,
              ("D", "A"):Inf, ("D", "B"):Inf, ("D", "C"):Inf, ("D", "D"):0, ("D", "E"):5,
              ("E", "A"):Inf, ("E", "B"):Inf, ("E", "C"):Inf, ("E", "D"):Inf, ("E", "E"):0
            }
```

```
def shortestPath (Cities, Distances):
```

```
    ''' returns the length of the shortest path
    from the leftmost to the rightmost city in
    the Cities list.'''
```

```
    if BLAH:    return BLAH BLAH
```

```
    else:    return BLAH BLAH BLAH
```



Just two lines
of code!!!

It's fitting that
map gets used
here!

Get Directions [My Maps](#)

A 382 Blaisdell Dr, Claremont, CA 91711
B 23 Ronald Avenue, Greenwich, New South Wales
[Add Destination](#) - [Show options](#)

Get Directions

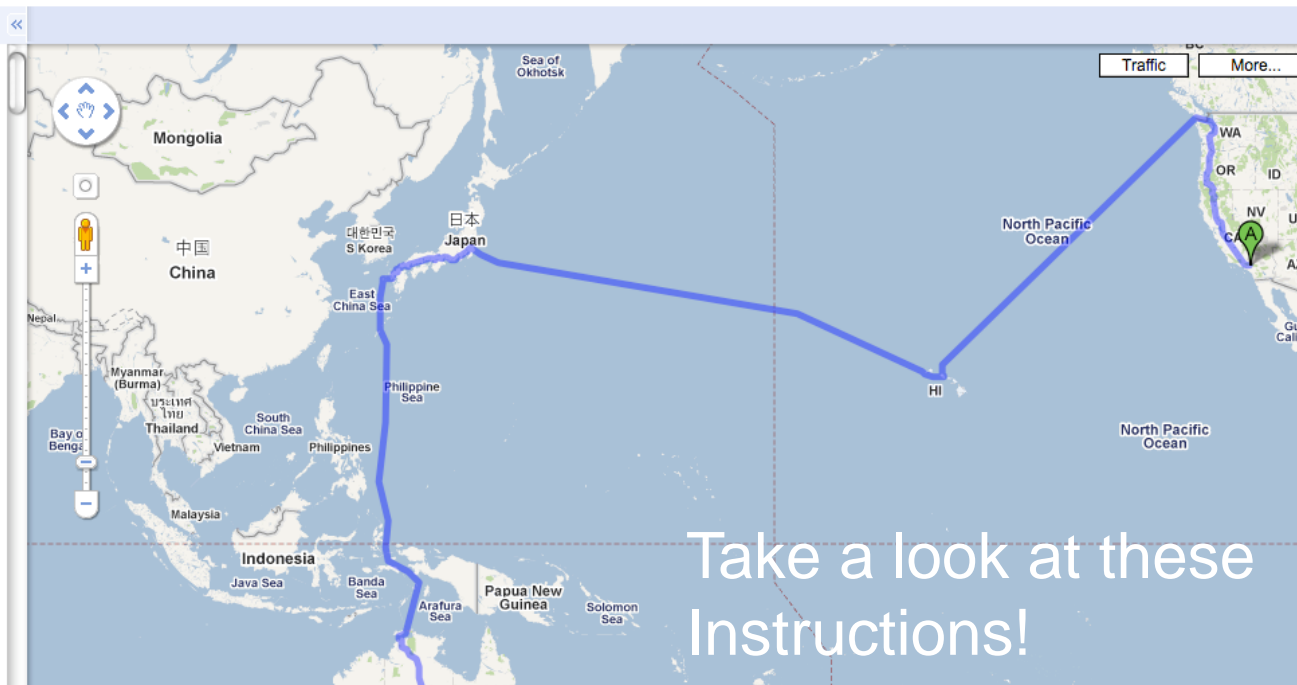
**Driving directions to 23 Ronald Ave,
Greenwich NSW 2065, Australia**

I-5 N **55 days 6 hours**
14,535 mi

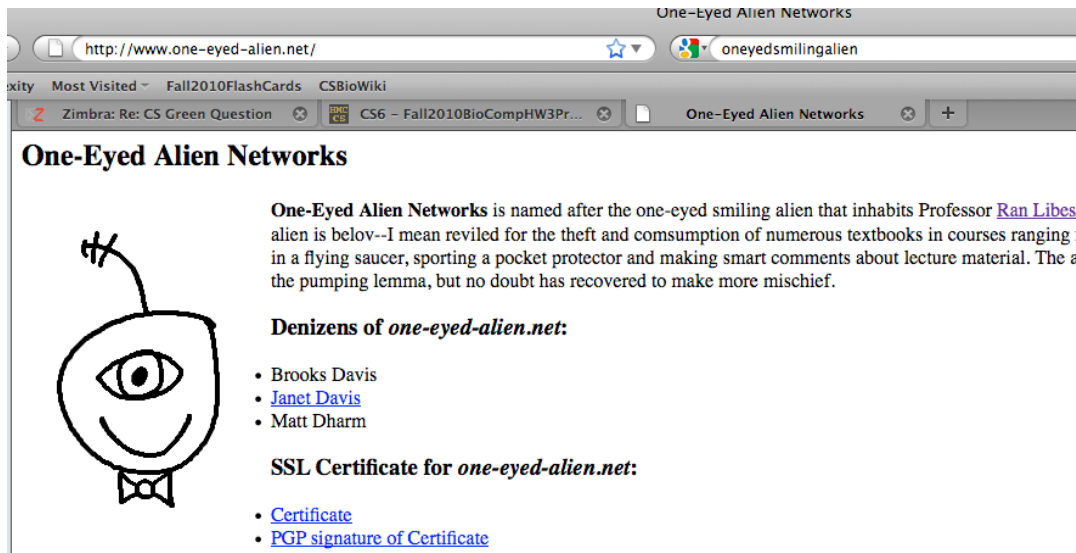
This route has tolls.
This route includes a ferry.
This route crosses through Japan.

A 382 Blaisdell Dr
Claremont, CA 91711

1. Head **east** on **Blaisdell Dr** toward **Bates Pl** 0.1 mi



The Recursion Theorem



Does it state
that recursion is
the secret to all
happiness?

Courtesy of Richard Bowen