

Import the data:

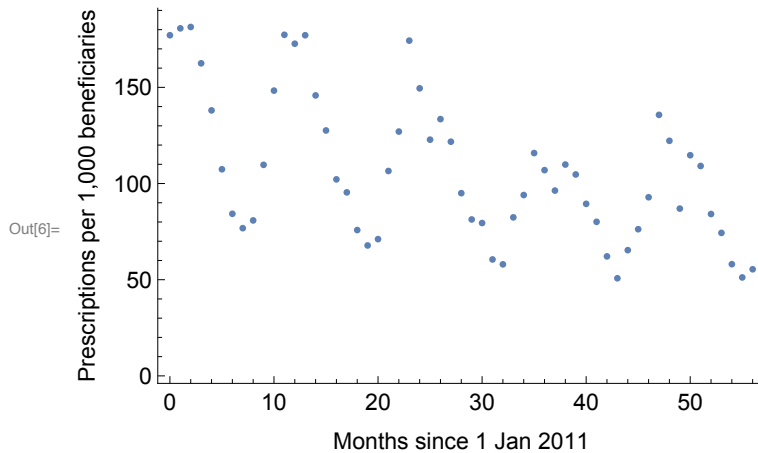
```
In[4]:= rxpkp = Import["~/Desktop/underfive.csv"][[2 ;;]];
```

```
In[5]:= rxpkp[[Range[1, 10]]]
```

```
Out[5]= {{0, 177.1}, {1, 180.679}, {2, 181.387}, {3, 162.501}, {4, 138.025},
        {5, 107.407}, {6, 84.2726}, {7, 76.7897}, {8, 80.8254}, {9, 109.721}}
```

Plot the data:

```
In[6]:= ListPlot[rxpkp, Frame → {True, True, False, False},
    FrameLabel → {"Months since 1 Jan 2011",
        "Prescriptions per 1,000 beneficiaries"}, BaseStyle → FontSize → 12]
```



Fit the sinusoid:

β_0 : intercept of the upper trend line (peak monthly prescribing rate per 1,000 beneficiaries)

β_1 : slope of the upper trend line (peak monthly prescribing rate per 1,000 beneficiaries)

γ_0 : intercept of the lower trend line (trough monthly prescribing rate per 1,000 beneficiaries)

γ_1 : slope of the lower trend line (trough monthly prescribing rate per 1,000 beneficiaries)

δ : phase shift of the sinusoid

```
In[7]:= upper[x_] :=  $\beta_0 + \beta_1 x$  ; (*The upper trend line*)
```

```
lower[x_] :=  $\gamma_0 + \gamma_1 x$  ; (*The lower trend line*)
```

```
In[9]:= fit = NonlinearModelFit[rxpkp, {
     $\frac{1}{2} (\text{upper}[x] + \text{lower}[x]) + \frac{1}{2} (\text{upper}[x] - \text{lower}[x]) \left( \cos\left[\frac{2\pi}{12} (x - \delta)\right] \right)$ 
    }, { $\beta_0, \beta_1, \gamma_0, \gamma_1, \delta$ }, x];
```

```
In[10]:= fit
```

```
Out[10]= FittedModel[ $\frac{1}{2}(274.494 - 2.21045 x) + \frac{1}{2}(108.275 - 1.16668 x) \cos\left[\frac{1}{6}\pi(-0.658059 + x)\right]$ ]
```

In[11]:= **Normal[fit]**

$$\text{Out[11]} = \frac{1}{2} (274.494 - 2.21045 x) + \frac{1}{2} (108.275 - 1.16668 x) \cos \left[\frac{1}{6} \pi (-0.658059 + x) \right]$$

In[12]:= **fit["BestFitParameters"]**

Out[12]= $\{\beta_0 \rightarrow 191.384, \beta_1 \rightarrow -1.68856, \gamma_0 \rightarrow 83.1096, \gamma_1 \rightarrow -0.521889, \delta \rightarrow 0.658059\}$

In[13]:= **fit["ParameterConfidenceIntervalTable"]**

	Estimate	Standard Error	Confidence Interval
β_0	191.384	5.61896	{180.109, 202.659}
β_1	-1.68856	0.181924	{-2.05362, -1.32351}
γ_0	83.1096	6.06145	{70.9464, 95.2727}
γ_1	-0.521889	0.176705	{-0.876474, -0.167303}
δ	0.658059	0.123528	{0.410181, 0.905937}

Plot the output:

In[14]:= **fitplot = Plot[fit[x], {x, rxpkp[[1, 1]], rxpkp[[-1, 1]]},
PlotRange → All, PlotStyle → Black, PlotLegends → {"Sinusoid fit"}];**

In[15]:= **upperplot = Plot[upper[x] /. fit["BestFitParameters"],
{x, rxpkp[[1, 1]], rxpkp[[-1, 1]]}, PlotStyle → Blue, PlotLegends → {"Envelope"}];
lowerplot = Plot[lower[x] /. fit["BestFitParameters"],
{x, rxpkp[[1, 1]], rxpkp[[-1, 1]]}, PlotStyle → Blue];**

In[17]:= **dataplot = ListLinePlot[rxpkp, PlotMarkers → Automatic,
PlotStyle → {Gray}, PlotRange → All, PlotLegends → {"Data"}];**

In[18]:= **figunder5sinusoid = Show[dataplot, fitplot, upperplot, lowerplot,
PlotRange → {0, Automatic}, Frame → {True, True, False, False},
FrameLabel → {None, "Prescriptions per 1,000\nbeneficiaries"},
BaseStyle → FontSize → 14, ImageSize → 400,
FrameTicks → {{{0, "2011"}, {12, "2012"}, {24, "2013"},
{36, "2014"}, {48, "2015"}}, Automatic},
GridLines → {Table[i, {i, 0, 54, 6}], {50, 100, 150, 200}}]**

