# **Specifying the Behavior of Expressions**

None of the exercises were tested.

## Exercise 3.1

## Exercise 3.2

A  $val \in ExpVal$  must be that which is in Int+Bool. Then a  $val \in ExpVal$  for which  $\lceil \lfloor val \rfloor \rceil \neq val$  is where  $val \in Bool$ , such as val = true.

## Exercise 3.3

We are able to describe the arithmetic operations in terms of subtraction. We cannot do so if we chose addition.

#### Exercise 3.4

Let 
$$\rho = [x=[33], y=[22]]$$
.

(value-of-program <(-(x,11)) then  $-(y,2)$  else  $-(y,4)>>)$ 

(value-of <(-(x,11)) then  $-(y,2)$  else  $-(y,4)>> \rho$ )

(value-of <(-(x,11))>> \rho) = (bool-val #f)

(value-of <<- $(y,4)>> \rho$ )

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## Exercise 3.5

```
(value-of <<let x = 7

in let y = 2

in let y = let x = -(x,1) in -(x,y)

\frac{\text{in } -(-(x,8),y) >> \rho_0)}{skibidi-too-hard}
```

For this exercise only, I expressed the operation in terms of others. Continuing this trend would have been a mistake.

#### Exercise 3.7

```
(equal?-exp
(exp1 expression?)
(exp2 expression?))
(greater?-exp
(exp1 expression?)
(exp2 expression?))
(less?-exp
(exp1 expression?)
(exp2 expression?))
(equal?-exp (exp1 exp2)
            (bool-val (= (expval->num (value-of exp1 env))
                         (expval->num (value-of exp2 env)))))
(greater?-exp (exp1 exp2)
              (bool-val (> (expval->num (value-of exp1 env))
                            (expval->num (value-of exp2 env)))))
(less?-exp (exp1 exp2)
           (bool-val (< (expval->num (value-of exp1 env))
                         (expval->num (value-of exp2 env)))))
```

#### Exercise 3.9

We express a list-val as two expressed values. To select from the

cons we use expval->list to return a Scheme cons, and apply either car or cdr to the cons.

```
(emptylist-val)
(list-val
(first expval?)
(rest expval?))
(define expval->list
  (lambda (val)
    (cases expval val
      (list-val (first rest) (cons first rest))
      (else (report-expval-extractor-error 'list val)))))
(cons-exp
(exp1 expression?)
(exp2 expression?))
(car-exp
(exp1 expression?))
(cdr-exp
(exp1 expression?))
(null?-exp
(exp1 expression?))
(emptylist-exp)
(cons-exp (exp1 exp2)
          (list-val (value-of expl env)
                    (value-of exp2 env)))
(car-exp (exp1)
         (car (expval->list (value-of exp1 env))))
(cdr-exp (exp1)
         (cdr (expval->list (value-of exp1 env))))
(null?-exp (exp1)
```

```
Expression ::= list(\{Expression\}^{*(,)})
```

We take advantage of using a list in the defining language to construct a list in the defined language. The Expressions are captured in a Scheme list. We map value-of to each Expression then transform the Scheme list into a nesting of list-vals, ending with (emptylist-val) when the Scheme list is null.

#### Exercise 3.11

We take the consequent expression of each variant in the cases and make a procedure out of it. Now value-of need only be modified by adding a

variant and procedure call, and the possibly large procedure can be made elsewhere.

```
(define value-of
  (lambda (exp env)
    (cases expression exp
      (const-exp (num) (const-op num))
      (var-exp (var) (var-op var env))
      (diff-exp (exp1 exp2) (diff-op exp1 exp2 env))
      (zero?-exp (exp1) (zero?-op exp1 env))
      (if-exp (exp1 exp2 exp3) (if-op exp1 exp2 exp3 env))
      (let-exp (var expl body) (let-op var expl body env))
      (minus-exp (exp1) (minus-op exp1 env))
      (add-exp (exp1 exp2) (add-op exp1 exp2 env))
      (mul-exp (exp1 exp2) (mul-op exp1 exp2 env))
      (div-exp (exp1 exp2) (div-op exp1 exp2 env))
      (equal?-exp (exp1 exp2) (equal?-op exp1 exp2 env))
      (greater?-exp (exp1 exp2) (greater?-op exp1 exp2 env))
      (less?-exp (exp1 exp2) (less?-op exp1 exp2 env))
      (cons-exp (exp1 exp2) (cons-op exp1 exp2 env))
      (car-exp (exp1) (car-op exp1))
      (cdr-exp (exp1) (cdr-op exp1))
      (null?-exp (exp1) (null?-op exp1 env))
      (emptylist-exp () (emptylist-op))
      (list-exp (exps) (list-op exps env)))))
(define const-op
  (lambda (num)
    (num-val num)))
(define var-op
  (lambda (var env)
    (apply-env env var)))
```

```
(define diff-op
  (lambda (exp1 exp2 env)
    (let ((val1 (value-of exp1 env))
          (val2 (value-of exp2 env)))
      (let ((num1 (expval->num val1))
            (num2 (expval->num val2)))
        (num-val (- num1 num2))))))
(define zero?-op
 (lambda (expl env)
    (let ((val1 (value-of exp1 env)))
      (let ((num1 (expval->num val1)))
        (if (zero? num1)
            (bool-val #t)
            (bool-val #f))))))
(define if-op
  (lambda (exp1 exp2 exp3 env)
    (let ((val1 (value-of exp1 env)))
      (if (expval->bool val1)
          (value-of exp2 env)
          (value-of exp3 env)))))
(define let-op
  (lambda (var expl body env)
    (let ((val1 (value-of exp1 env)))
      (value-of body
                (extend-env var val1 env))))
(define minus-op
 (lambda (expl env)
```

```
(value-of (diff-exp (const-exp 0) exp1)
              env)))
(define add-op
  (lambda (exp1 exp2 env)
    (num-val (+ (expval->num (value-of exp1 env))
                (expval->num (value-of exp2 env))))))
(define mul-op
  (lambda (exp1 exp2 env)
    (num-val (* (expval->num (value-of expl env))
                (expval->num (value-of exp2 env)))))
(define div-op
  (lambda (exp1 exp2 env)
    (let ((val2 (expval->num (value-of exp2 env))))
      (if (= 0 \text{ val2})
          (report-division-by-zero)
          (num-val (/ (expval->num (value-of expl env))
                      val2))))))
(define equal?-op
  (lambda (exp1 exp2 env)
    (bool-val (= (expval->num (value-of exp1 env))
                 (expval->num (value-of exp2 env)))))
(define greater?-op
  (lambda (exp1 exp2 env)
    (bool-val (> (expval->num (value-of expl env))
                 (expval->num (value-of exp2 env))))))
(define less?-op
```

```
(lambda (exp1 exp2 env)
    (bool-val (< (expval->num (value-of exp1 env))
                 (expval->num (value-of exp2 env))))))
(define cons-op
  (lambda (exp1 exp2 env)
    (list-val (value-of expl env)
              (value-of exp2 env))))
(define car-op
 (lambda (exp1)
    (car (expval->list exp1))))
(define cdr-op
  (lambda (exp1)
    (cdr (expval->list exp1))))
(define null?-op
  (lambda (expl env)
    (let ((val1 (value-of exp1 env)))
      (cases expval val1
        (emptylist-val () (bool-val #t))
        (else (bool-val #f))))))
(define emptylist-op
  (lambda ()
    (emptylist-val)))
(define list-op
 (lambda (exps env)
    (list->expval (map (lambda (expr) (value-of expr env))
                       exps))))
```

```
Exercise 3.12
```

```
(cond-exp
 (clauses (list-of (list-of expression?))))
(cond-exp (clauses) (cond-op clauses env))
(define cond-op
  (lambda (clauses env)
    (if (null? clauses)
        (error-all-false-predicates)
        (let* ((clause (car clauses))
               (predicate (car clause))
               (val (value-of predicate env)))
          (if (expval->bool val)
              (let ((consequent (cadr clause)))
                 (value-of consequent env))
               (cond-op (cdr clauses) env)))))
Exercise 3.13
(define-datatype expval expval?
```

```
(num-val
   (num number?)))
(zero?-exp (exp1)
           (let ((val1 (value-of exp1 env)))
             (let ((num1 (expval->num val1)))
               (if (zero? num1)
                   (num-val 1)
                   (num-val 0)))))
(if-exp (exp1 exp2 exp3)
        (let ((val1 (value-of exp1 env)))
```

```
(if (zero? (expval->num val1))
    (value-of exp3 env)
    (value-of exp2 env))))
```

We introduce a new nonterminal Bool - exp. We represent it as a data type having its variants be predicate operations. We declare that **value-of-bool-exp**:  $Bool - exp \times Env \rightarrow ExpVal$ , and that these ExpVals are Bools. Thus all the variants are predicates. Lastly, we add a production to the grammar of Expressions to include Bool - exps. This allows a predicate operation to be written by itself without needing to be in an if-exp.

```
(define-datatype bool-exp bool-exp?
 (zero?-exp
   (exp expression?))
  (equal?-exp
   (exp1 expression?)
   (exp2 expression?))
  (greater?-exp
   (exp1 expression?)
   (exp2 expression?))
  (less?-exp
   (exp1 expression?)
   (exp2 expression?)))
(define value-of-bool-exp
  (lambda (exp env)
    (cases bool-exp exp
      (zero?-exp (exp)
                 (let ((val (value-of exp env)))
                    (let ((num (expval->num val)))
                      (if (zero? num)
                          (bool-val #t)
                          (bool-val #f)))))
```

```
(equal?-exp (exp1 exp2)
                   (bool-val (= (expval->num (value-of exp1 env))
                                 (expval->num (value-of exp2 env))))
      (greater?-exp (exp1 exp2)
                     (bool-val (> (expval->num (value-of exp1 env))
                                   (expval->num (value-of exp2 env))
      (less?-exp (exp1 exp2)
                  (bool-val (< (expval->num (value-of exp1 env))
                                (expval->num (value-of exp2 env)))))
(bool-expr
 (bool-exp1 bool-exp?)))
(if-exp (bool-exp1 exp2 exp3)
        (let ((val1 (value-of-bool-exp bool-exp1 env)))
          (if (expval->bool val1)
              (value-of exp2 env)
              (value-of exp3 env))))
(bool-expr (bool-exp1)
           (value-of-bool-exp bool-exp1 env))
Exercise 3.15
(print-exp
 (exp expression?))
(print-exp (exp)
           (display (value-of exp env))
           (num-val 1))
Exercise 3.16
(let-exp
 (vars (list-of identifier?))
 (exps (list-of expression?))
```

```
(body expression?))
(let-exp (vars exps body)
         (value-of body
                    (extend-env∗ vars
                                  (map (lambda (exp)
                                          (value-of exp env))
                                       exps)
                                  env)))
Exercise 3.17
(let *-exp
 (vars (list-of identifier?))
 (exps (list-of expression?))
 (body expression?))
(let *-exp (vars exps body)
           (let*-op vars exps body env))
(define let*-op
  (lambda (vars exps body env)
    (if (null? vars)
        (value-of body env)
        (let*-op (cdr vars)
                  (cdr exps)
                  body
                  (extend-env (car vars)
                               (value-of (car exps) env)
                               env)))))
Exercise 3.18
(unpack-exp
 (vars (list-of identifier?))
```

```
(exp expression?)
(body expression?))
(unpack-exp (vars exp body)
            (unpack-op vars
                       (expand-expval->list (value-of exp env))
                       body
                       env))
(define unpack-op
  (lambda (vars lst body env)
    (if (null? vars)
        (if (null? lst)
            (value-of body env)
            (report-too-many-elements lst))
        (unpack-op (cdr vars)
                   (cdr lst)
                   body
                   (extend-env (car vars)
                                (car lst)
                                env)))))
(define expand-expval->list
  (lambda (val)
    (cases expval val
      (emptylist-val () '())
      (list-val (first rest)
                (cons first (expand-expval->list rest)))
      (else (report-not-a-list val)))))
```