Specifying the Behavior of Expressions

Exercise 3.1

[(value-of
$$<< x>> \rho$$
)] = 10
[(value-of $<< 3>> \rho$)] = 3
[(value-of $<< v>> \rho$)] = 5
[(value-of $<< i>> \rho$)] = 1

Let $\rho = [x=[33], y=[22]]$.

Exercise 3.2

A $val \in ExpVal$ must be that which is in Int+Bool. Then a $val \in ExpVal$ for which $\lceil |val| \rceil \neq val$ is where $val \in Bool$, such as val = true.

Exercise 3.3

We are able to describe the arithmetic operations in terms of subtraction. We cannot do so if we chose addition.

Exercise 3.4

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Exercise 3.5

```
(value-of <<let x=7 in let y=2 in let y= let x=-(x,1) in -(x,y) in -(-(x,8),y)>> \rho_0) skib
```

Exercise 3.6

Exercise 3.7

Exercise 3.8

```
(equal?-exp
(exp1 expression?)
(exp2 expression?))
(greater?-exp
(exp1 expression?)
(exp2 expression?))
(less?-exp
 (exp1 expression?)
(exp2 expression?))
(equal?-exp (exp1 exp2)
            (bool-val (= (expval->num (value-of exp1 env))
                          (expval->num (value-of exp2 env)))))
(greater?-exp (exp1 exp2)
              (bool-val (> (expval->num (value-of expl env))
                            (expval->num (value-of exp2 env)))))
(less?-exp (exp1 exp2)
           (bool-val (< (expval->num (value-of exp1 env))
                         (expval->num (value-of exp2 env)))))
```

Exercise 3.9

We express a list-val as two expressed values. To select from the cons we use expval->list to return a Scheme cons, and apply either car or cdr to the cons.

```
(emptylist-val)
(list-val
(first expval?)
(rest expval?))
(define expval->list
  (lambda (val)
    (cases expval val
      (list-val (first rest) (cons first rest))
      (else (report-expval-extractor-error 'list val)))))
(cons-exp
(exp1 expression?)
(exp2 expression?))
(car-exp
(exp1 expression?))
(cdr-exp
(exp1 expression?))
(null?-exp
(exp1 expression?))
(emptylist-exp)
(cons-exp (exp1 exp2)
          (list-val (value-of exp1 env)
                    (value-of exp2 env)))
(car-exp (exp1)
         (car (expval->list exp1)))
(cdr-exp (exp1)
         (cdr (expval->list exp1)))
(null?-exp (exp1)
           (let ((val1 (value-of exp1 env)))
             (cases expval val1
```

Exercise 3.10

```
Expression ::= list(\{Expression\}^{*(,)})
```

We take advantage of using a list in the defining language to construct a list in the defined language. The Expressions are captured in a Scheme list. We map value-of to each Expression then transform the Scheme list into a nesting of list-vals, ending with (emptylist-val) when the Scheme list is null.

Exercise 3.11

We take the consequent expression of each variant in the cases and make a procedure out of it. Now value-of need only be modified by adding a variant and procedure call, and the possibly large procedure can be made elsewhere.

```
(define value-of
  (lambda (exp env)
    (cases expression exp
      (const-exp (num) (const-op num))
      (var-exp (var) (var-op var env))
      (diff-exp (exp1 exp2) (diff-op exp1 exp2 env))
      (zero?-exp (exp1) (zero?-op exp1 env))
      (if-exp (exp1 exp2 exp3) (if-op exp1 exp2 exp3 env))
      (let-exp (var exp1 body) (let-op var exp1 body env))
      (minus-exp (exp1) (minus-op exp1 env))
      (add-exp (exp1 exp2) (add-op exp1 exp2 env))
      (mul-exp (exp1 exp2) (mul-op exp1 exp2 env))
      (div-exp (exp1 exp2) (div-op exp1 exp2 env))
      (equal?-exp (exp1 exp2) (equal?-op exp1 exp2 env))
      (greater?-exp (exp1 exp2) (greater?-op exp1 exp2 env))
      (less?-exp (exp1 exp2) (less?-op exp1 exp2 env))
      (cons-exp (exp1 exp2) (cons-op exp1 exp2 env))
      (car-exp (exp1) (car-op exp1))
      (cdr-exp (exp1) (cdr-op exp1))
      (null?-exp (exp1) (null?-op exp1 env))
      (emptylist-exp () (emptylist-op))
      (list-exp (exps) (list-op exps env)))))
(define const-op
  (lambda (num)
    (num-val num)))
(define var-op
  (lambda (var env)
    (apply-env env var)))
(define diff-op
```

```
(lambda (exp1 exp2 env)
    (let ((val1 (value-of exp1 env))
          (val2 (value-of exp2 env)))
      (let ((num1 (expval->num val1))
            (num2 (expval->num val2)))
        (num-val (- num1 num2))))))
(define zero?-op
 (lambda (exp1 env)
    (let ((val1 (value-of exp1 env)))
      (let ((num1 (expval->num val1)))
        (if (zero? num1)
            (bool-val #t)
            (bool-val #f))))))
(define if-op
  (lambda (exp1 exp2 exp3 env)
    (let ((val1 (value-of exp1 env)))
      (if (expval->bool val1)
          (value-of exp2 env)
          (value-of exp3 env))))
(define let-op
 (lambda (var expl body env)
    (let ((val1 (value-of exp1 env)))
      (value-of body
                (extend-env var val1 env))))
(define minus-op
 (lambda (expl env)
    (value-of (diff-exp (const-exp 0) exp1)
              env)))
```

```
(define add-op
  (lambda (exp1 exp2 env)
    (num-val (+ (expval->num (value-of expl env))
                (expval->num (value-of exp2 env))))))
(define mul-op
  (lambda (exp1 exp2 env)
    (num-val (* (expval->num (value-of expl env))
                (expval->num (value-of exp2 env)))))
(define div-op
  (lambda (exp1 exp2 env)
    (let ((val2 (expval->num (value-of exp2 env))))
      (if (= 0 \text{ val2})
          (report-division-by-zero)
          (num-val (/ (expval->num (value-of expl env))
                      val2))))))
(define equal?-op
  (lambda (expl exp2 env)
    (bool-val (= (expval->num (value-of expl env))
                 (expval->num (value-of exp2 env))))))
(define greater?-op
  (lambda (exp1 exp2 env)
    (bool-val (> (expval->num (value-of expl env))
                 (expval->num (value-of exp2 env))))))
(define less?-op
  (lambda (exp1 exp2 env)
    (bool-val (< (expval->num (value-of exp1 env))
```

```
(expval->num (value-of exp2 env))))))
(define cons-op
 (lambda (exp1 exp2 env)
    (list-val (value-of exp1 env)
              (value-of exp2 env))))
(define car-op
 (lambda (exp1)
    (car (expval->list exp1))))
(define cdr-op
 (lambda (exp1)
    (cdr (expval->list exp1))))
(define null?-op
 (lambda (expl env)
    (let ((val1 (value-of exp1 env)))
      (cases expval val1
        (emptylist-val () (bool-val #t))
        (else (bool-val #f))))))
(define emptylist-op
 (lambda ()
    (emptylist-val)))
(define list-op
  (lambda (exps env)
    (list->expval (map (lambda (expr) (value-of expr env))
                       exps))))
```