

1. We determine the backward induction form of the definition by substituting n for $n - 1$ and if we let F represent the square function. We have

$$\begin{aligned} F(n) &= F(n - 1) + 2(n - 1) + 1 \\ &= F(n - 1) + 2n - 2 + 1 \\ &= F(n - 1) + 2n - 1. \end{aligned}$$

a)

```
int square(int n)
{
    if (n <= 1) /* defense */
        return 1;
    else
        return square(n-1) + 2*n - 1;
}
```

b)

STATEMENT $S(n)$: The recursive definition of n^2 given in exercise 2.7.1 correctly computes n^2 .

BASIS. The basis is true immediately from the definitions.

INDUCTION. Assume the recursive definition correctly computes squares of $j \leq n$. We shall prove $S(n+1)$. Let F be the function that computes squares as given by the recursive definition. By the inductive hypothesis, we know $F(n) = n^2$. Therefore

$$\begin{aligned} F(n + 1) &= F(n) + 2(n + 1) - 1 \\ &= n^2 + 2n + 2 - 1 \\ &= (n + 1)^2. \end{aligned}$$

Hence $F(n + 1)$ correctly computes $(n + 1)^2$, which proves $S(n + 1)$. We conclude that the recursive definition correctly computes n^2 for all $n \geq 1$. ♦

2. For now we use a whitespace-separated list enclosed in braces to denote the elements of an array.

```
recSS({10 13 4 7 11}, 0, 5)
recSS({4 13 10 7 11}, 1, 5)
recSS({4 7 10 13 11}, 2, 5)
recSS({4 7 10 13 11}, 3, 5)
recSS({4 7 10 11 13}, 4, 5)
```

3.