

1. Lines (1) through (3) and (7) each take 1 time unit. The loop on lines (4) through (6) executes $n - i + 1$ times. But i is given and is 2, thus the loop executes $n - 1$ times. Each instruction, including the condition, takes 1 time unit. But the condition also is executed by one more than how many times the body is executed. Hence the loop takes $3(n - 1) + 1$ time units. Together with the 4 time units spent in the instructions other than the loop, the total time taken by the program is $3n + 2$. Since n is the size of the data the program operates on, then the running time $T(n) = 3n + 2$.

2. Consider Exercise 2.5.1. Line (4) is executed n times taking 1 time unit each. The incrementation on line (3) takes 1 time unit as well and executes n times. The condition on line (3) is executed $n + 1$ times and takes 1 time unit each. Lines (1) and (2) each take 1 time unit. The initialization on line (3) takes 1 time unit. The size of the data is n . Thus we have the running time $T(n) = 3n + 4$.

Consider Fig. 2.14. Lines (1) and (2) each take 1 time unit. Lines (4) and (5) each take 1 time unit and execute n times. Line (3) takes 1 time unit and executes $n + 1$ times. The size of the data is n , the number of elements to be used as input. The running time of the program $T(n) = 3(n + 1)$.

3. We use a program to determine this. For $1 \leq n \leq 29$, program A takes less time than program B . The value of the procedure call given below is 30 which represents the first number n such that program A takes more time than program B .

```
(define (cmp A B)
  (define (cmp-iter n)
    (if (> (A n) (B n))
        n
        (cmp-iter (+ n 1))))
  (cmp-iter 1))

(cmp (lambda (n) (/ (expt 2 n) 1000))
     (lambda (n) (* 1000 (square n))))
```

The procedure may never terminate, given certain inputs.

4. We use a program to determine this. For program A , the maximum problem sizes are (a) 29, (b) 39, (c) 49. For program B , the maximum problem sizes are (a) 31, (b) 1000, (c) 31622.

```
(define (max-size seconds)
  (lambda (exp)
    (define (ms n seconds)
      (cond ((null? seconds) '())
            ((> (exp n) (car seconds))
             (cons (- n 1) (ms n (cdr seconds))))
            (else (ms (+ n 1) seconds))))
    (ms 1 seconds)))

(define big-max-size
  (max-size (list (expt 10 6) (expt 10 9) (expt 10 12))))
```

```
(big-max-size (lambda (n) (/ (expt 2 n) 1000)))  
(big-max-size (lambda (n) (* 1000 (square n))))
```

The definition `(define small-max-size (max-size (list 1 10 100 1000)))` is how we can determine those maximum problem sizes found in Fig. 3.3.