1.

- a) We select 3 letters from 26. Thus there are $\Pi(26,3)=26!/(26-3)!=26\times25\times24=15,600$ ways to form a sequence of 3 letters out of the 26 letters without replacement.
- b) We select 5 letters from 26. Thus there are $\Pi(26,5)=26!/(26-5)!=26\times25\times24\times23\times22=7,893,600$ ways to form a sequence of 5 letters out of the 26 letters without replacement.
- **2.** We select 4 students from 200. That is $\Pi(200,4) = 200!/(200-4)! = 200 \times 199 \times 198 \times 197 = 1,552,438,800$ ways of selecting these four officers.

3.

- a) $100!/97! = 100 \times 99 \times 98 = 970,200.$
- b) $200!/195! = 200 \times 199 \times 198 \times 197 \times 196 = 304,278,004,800.$

4.

- a) A code is a sequence of four pegs each having one of six colors and colors can be repeated. There are $6^4 = 1296$ different codes.
- b) The number of codes with pegs having non-distinct colors is the solution to (a). The number of codes with pegs having distinct colors is $\Pi(6,4) = 6 \times 5 \times 4 \times 3 = 360$. The number of codes having at least two or more pegs of the same color, which is the same as saying the codes with pegs not having distinct colors, is the difference. That being 1296 360 = 936.
- c) Remove red from the pool of colors. By (a) we have $5^4 = 625$ different codes.
- d) The number of codes with pegs having distinct colors without red is $\Pi(5,4) = 5 \times 4 \times 3 \times 2 = 120$. We subtract the number of codes with pegs having distinct colors without red from the number of codes with pegs having non-distinct colors without red. That is 625 120 = 505.