1. We determine the backward induction form of the definition by substituting n for n-1 and if we let F represent the square function. We have

```
F(n) = F(n-1) + 2(n-1) + 1
= F(n-1) + 2n - 2 + 1
= F(n-1) + 2n - 1.
a)
int square(int n)
{
    if (n <= 1) /* defense */
        return 1;
    else
        return square(n-1) + 2*n - 1;
}
```

STATEMENT S(n): The recursive definition of n^2 given in exercise 2.7.1 correctly computes n^2 .

BASIS. The basis is true immediately from the definitions.

INDUCTION. Assume the recursive definition correctly computes squares of $j \leq n$. We shall prove S(n+1). Let F be the function that computes squares as given by the recursive definition. By the inductive hypothesis, we know $F(n) = n^2$. Therefore

$$F(n+1) = F(n) + 2(n+1) - 1$$
$$= n^{2} + 2n + 2 - 1$$
$$= (n+1)^{2}.$$

Hence F(n+1) correctly computes $(n+1)^2$, which proves S(n+1). We conclude that the recursive definition correctly computes n^2 for all $n \ge 1$.

2. For now we use a whitespace-separated list enclosed in braces to denote the elements of an array.

```
recSS({10 13 4 7 11}, 0, 5)
recSS({4 13 10 7 11}, 1, 5)
recSS({4 7 10 13 11}, 2, 5)
recSS({4 7 10 13 11}, 3, 5)
recSS({4 7 10 11 13}, 4, 5)

3.
BOOLEAN find(LIST L, int n)
{
    if (L == NULL) return FALSE;
    else if (L->element == n) return TRUE;
    else return find(L->next, n);
```

```
}
BOOLEAN find1698(LIST L)
    return find(L, 1698);
}
4.
int add(LIST L)
{
    if (L == NULL) return 0;
    else return L->element + add(L->next);
}
5.
void selectionsort(LIST L)
   LIST small;
    int temp;
    if (L == NULL) return;
    else {
        small = smallest(L, L->next);
        temp = L->element;
        L->element = small->element;
        small->element = temp;
        selectionsort(L->next);
    }
}
LIST smallest(LIST small, LIST current)
    if (current == NULL) return small;
    else if (current->element < small->element)
         return smallest(current, current->next);
    else return smallest(small, current->next);
}
6.
void recSS(T A[], int i, int n)
    int j, small;
    T temp;
    if (i < n-1) {
        small = i;
```

```
for (j = i+1; j < n; j++)
            if (lt(key(A[j]), key(A[small])))
                small = j;
        temp = A[small];
        A[small] = A[i];
        A[i] = temp;
        recSS(A, i+1, n);
    }
}
7.
void binary(int i)
    if (i == 0) printf("0");
    else b(i);
}
void b(int i)
    if (i <= 0) return;</pre>
        printf("%d", i%2);
        b(i/2);
    }
}
8.
int gcd(int i, int j)
    if (i\%j == 0) return j;
    else return gcd(j, i%j);
}
```

9.