

1.

a) We prove the following statement by induction on  $T$ , the root of a tree.

STATEMENT  $S(T)$ : Calling **preorder** on a tree  $T$  prints the labels of  $T$  in preorder.

BASIS. The basis is where  $T$  is a single node. Then line (1) prints the label of  $T$ , line (2) gets the leftmost child which is **NULL**, and thus line (3) fails, stopping execution of **preorder**.

INDUCTION. Suppose  $T$  is not a leaf. Then  $T$  has at least one child. Assume by the inductive hypothesis that **preorder** prints the labels of the children of  $T$ . Clearly the label of the root of  $T$  is printed by line (1). This proves the inductive step. We conclude that  $S(T)$  is true for all labeled trees  $T$ . ♦