

**1.** We assign values to items, that being colors to houses.

a) There are  $n = 3$  items and  $k = 4$  values. Thus there are  $k^n = 4^3 = 64$  assignments or ways to paint the houses.

b) There are  $5^5 = 3125$  ways to paint the houses.

c) There are  $10^2 = 100$  ways to paint the houses.

**2.** There are 26 lower-case letter values, 26 upper-case letter values, and 10 number values that can be assigned to the positions in the password, the items. If the password is 8 characters long, then there are  $(26+26+10)^8 = 62^8$  possible passwords. If the password is 9 long, then there are  $62^9$ , and if the password is 10 long then there are  $62^{10}$  possible passwords. For passwords consisting of eight to ten of the allowed characters there are  $62^8 + 62^9 + 62^{10}$  possible passwords.

**3.** Each statement can mutate  $n$  alongside at most seven other statements. Each statement has a condition that is either true or false and these are the values.

Taking one item, we have  $2^1$  assignments. Alongside the other seven items there are  $2^7$  assignments. Hence there are  $2^1 \times 2^7 = 2^8 = 256$  different values  $\mathbf{f}$  can return.

**4.** There are nine items, the squares, with three possible values, blank, containing an X, or containing an O. Thus there are  $3^9$  different boards.

**5.** There are  $n$  items, the number of positions in the string, and ten values, the digits. Hence there are  $10^n$  different strings.

**6.** There are  $26^n$  different strings that can be formed.

**7.**  $2^{13} = 2^3 \times 2^{10}$  is 8K.