1.

- a) 1.
- b) 8, 9, 13, 6, 11, 15, 12.
- c) 1, 2, 4, 3, 5, 10, 14, 7.
- d) 5, 7.
- e) 5, 10, 13, 14, 15.
- f) 1, 3, 5, 10.
- g) 10, 13, 14, 15.
- h) 2, 4, 8, 9.
- i) 6, 7, 11, 12
- j) 1, 3, 5, 10, 14, 15.
- k) 4.
- 1) 4.
- m) 5.
- 2. A leaf is its own descendant. A leaf cannot have any proper descendants.
- **3.** Let A and B be distinct leaves. If A is an ancestor of B, then A has at least one descendant. Thus A is an interior node. But A is a leaf. We have reached a contradiction. We conclude that a leaf cannot be an ancestor of another leaf. The same follows if we swap the names.
- **4.** We prove the following statement by induction on n, the number of nodes in the tree.

STATEMENT S(n): A tree having n nodes under the nonrecursive definition is a tree under the recursive definition.

BASIS. The basis is n = 1. The tree has one node, the root. This is a one-node tree under the recursive definition. This proves the basis.

INDUCTION. Assume S(n) for $n \ge 1$. We shall prove S(n+1).