

# ELEM/ ADATSZERKEZETEK & ADATTÍpusok

Stack

- A: T[]

- m: N

- constant max:  $N_f := 16$

+ Stack(max:  $N_f := m_0$ )

{ A := new T[max]; m := 0 }

+ push(X: T)

+ pop(): T

+ top(): T

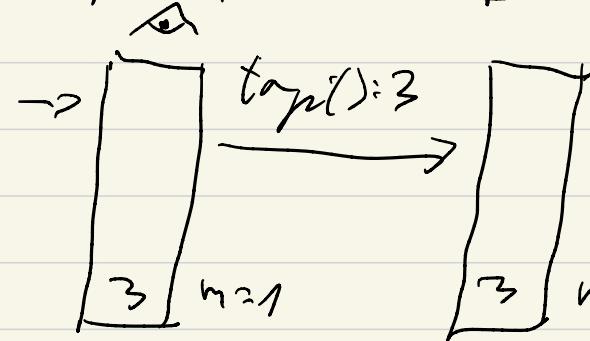
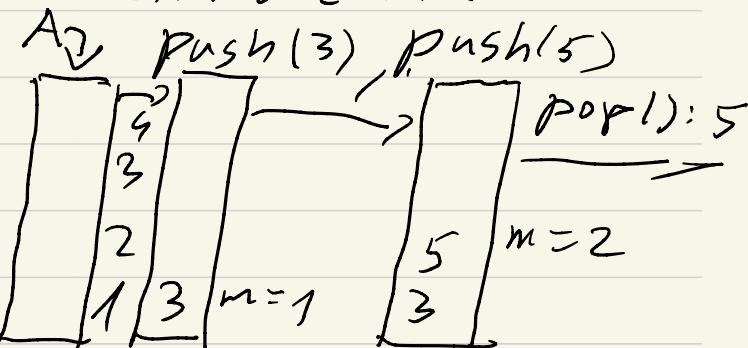
+ isEmpty(): B { return m = 0 }

+ setEmpty() { m := 0 }

+ ~Stack() { delete A }

UML körz (Verum)

LIFO tároló

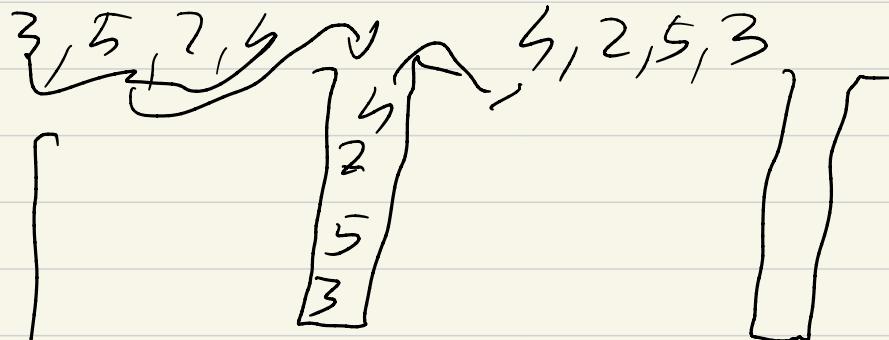


{ S: Stack; . . . } | AT<sub>push</sub><sup>(m) ∈ Θ(1)</sup>, |  $\Theta(1)$  // init. push() { not ∈  $\Theta(1)$  } | MT<sub>push</sub><sup>(m) ∈ Θ(m)</sup>

`read(&x:y):B`

function

`S:Stack`  
`read(x)`  
`S.push(x)`  
`G.using(y)`  
`write(S.pop())`



## Queue

- constante  $m_0 := N_t := 16$

-  $Z : \mathbb{T}^{\lceil \rceil}$

-  $k, n : \mathbb{N}$

+ Queue( $m := N_t := m_0$ )

{ $Z := \text{new } \mathbb{T}^{\lceil \rceil}[m]; k := n := 0$ }

+ add( $x : \mathbb{T}$ )

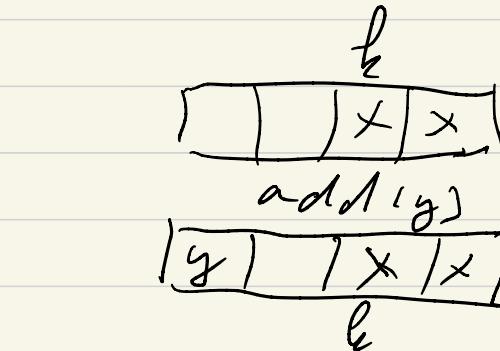
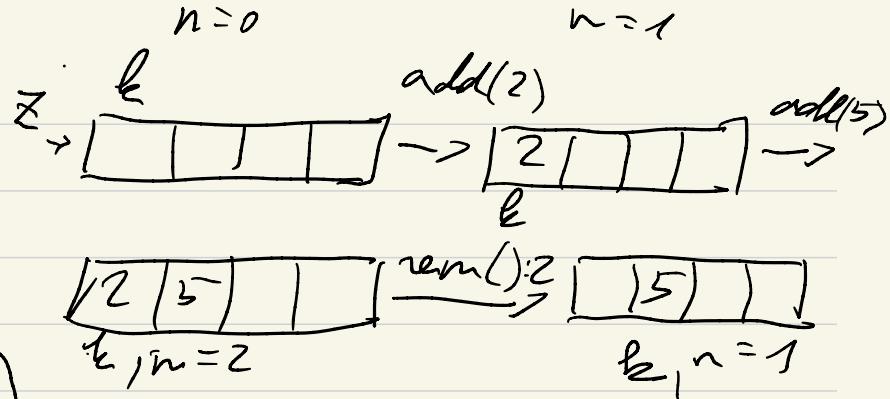
+ rem() :  $\mathbb{T}$

+ first() :  $\mathbb{T}$

+ length() :  $\mathbb{N}$  {return  $n$ }

+ setEmpty() { $k := n := 0$ }

+ ~Queue() {delete  $Z$ }



$\Theta(1)$

$\left\{ \begin{array}{l} \text{MT}(n) \in \Theta(n) \\ \text{AT}(n) \in \Theta(1) \\ \text{mT}(n) \in \Theta(1) \end{array} \right.$

AMORTIZIERT  
ZALT min.  
wegen  
Nameita,

Möglichkeit:  $\Theta(1)$ , bzw.,  $\text{add}(x)$

$\left\{ \begin{array}{l} \text{AT}(n) \in \Theta(1) \\ \text{mT}(n) \in \Theta(1) \end{array} \right.$

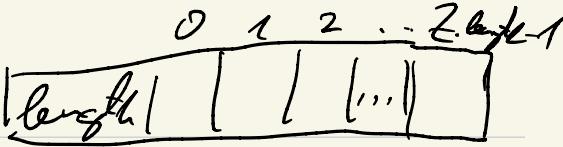
Queue :: add(x: T)

$n = Z.length$

DoubleQueueArray(Z, k) | X

$Z[(k+n) \bmod Z.length] := x$

$n++$



$Z$

$*Z = Z[0]$

$*Z + 1 = Z[1]$   
:

Queue :: rem(): T

1

$n \geq 0$

$i := k; n--$

$k := (k+1) \bmod Z.length$

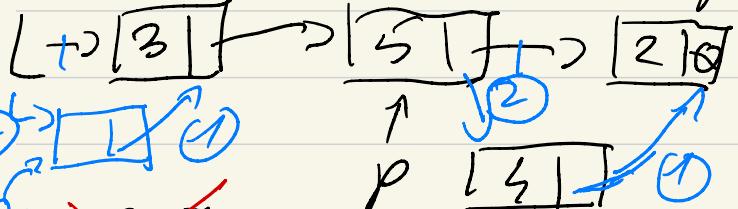
return  $Z[i]$

throw

EMPTY\_QUEUE\_ERROR

# LÄNCÖLJS LISTÁK

$\langle 3, 5, 2 \rangle$  reprezentációja



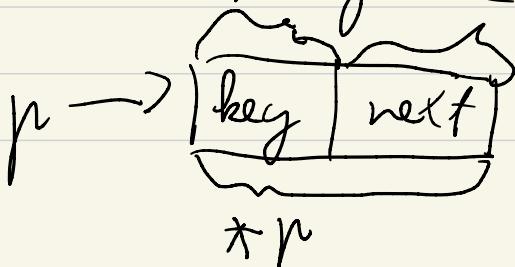
$L[i]$

Beszívás

a lista elején

$p \rightarrow \text{key}$

$(\ast p), \text{key}$



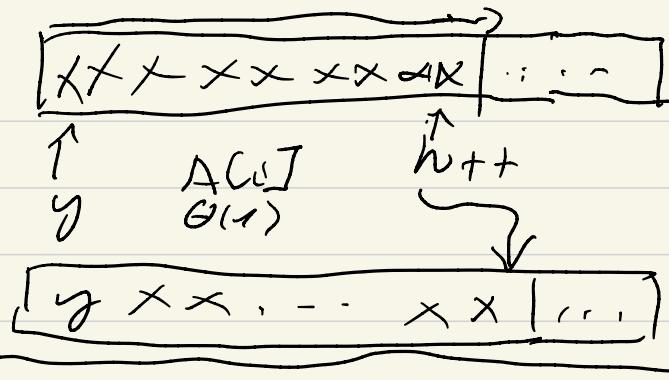
$p \rightarrow \text{next}$

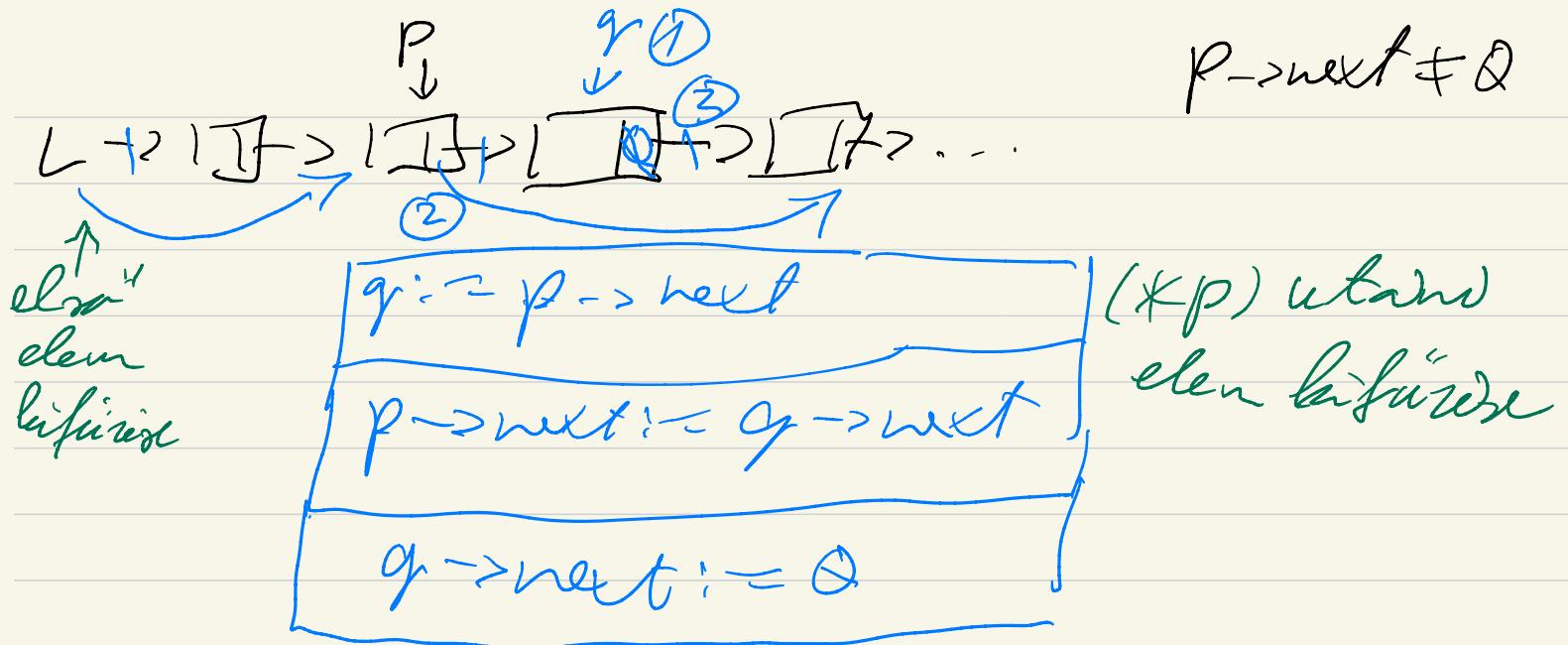
$(\ast p), \text{next}$

Beszívás( $\ast p$ )  
után

$\uparrow$

$q \rightarrow \text{next} := p \rightarrow \text{next}$   
 $p \rightarrow \text{next} := q$





$S1L - \text{el}$  (lines:  $L = \emptyset$ )

# Lancolt listák

eggyéinnyű

egyszerű  
(S1L)

$$L = \emptyset$$

$$L \rightarrow [5] \emptyset \rightarrow [2] \emptyset \rightarrow [3] \emptyset$$

$$H \rightarrow \boxed{1} \emptyset$$

$$H \rightarrow \boxed{1} \emptyset \rightarrow [5] \emptyset \rightarrow [2] \emptyset \rightarrow [3] \emptyset$$

$$[5] \emptyset \rightarrow [2] \emptyset \rightarrow [3] \emptyset \rightarrow \boxed{1}$$

kétirányú

fejelemes  
(H1L)

végelemes  
(1LT)

$$\begin{array}{c} 1 \\ \uparrow \\ f \end{array} \quad \begin{array}{c} t \\ \uparrow \\ t \end{array}$$

$$\begin{array}{c} 5 \\ \uparrow \\ f \end{array} \quad \begin{array}{c} 2 \\ \uparrow \\ t \end{array} \quad \begin{array}{c} 3 \\ \uparrow \\ t \end{array} \quad \begin{array}{c} 1 \\ \uparrow \\ H \end{array}$$

$$\begin{array}{c} 5 \\ \uparrow \\ f \end{array} \quad \begin{array}{c} 2 \\ \uparrow \\ t \end{array} \quad \begin{array}{c} 3 \\ \uparrow \\ t \end{array} \quad \begin{array}{c} 1 \\ \uparrow \\ H \end{array}$$

ciklikus  
(C1L)

$$\begin{array}{c} L \rightarrow \boxed{1} \\ \downarrow \\ \boxed{1} \rightarrow \boxed{2} \rightarrow \boxed{3} \rightarrow \boxed{1} \end{array}$$

p := new E1

Q = q +> ~~1~~

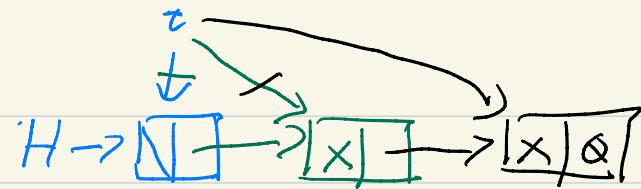
SOK reprezentációjaihoz

$$p \rightarrow \boxed{1} \emptyset$$

delete q ; ... ; r -> next := s

???

read\_HL(): E14

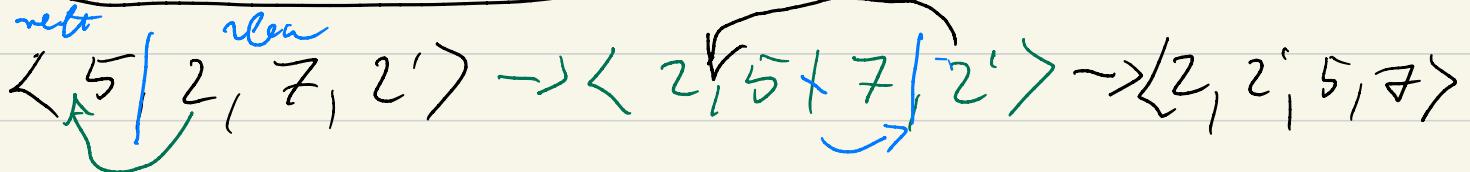


$t := H := \text{new } E1$

$\text{read}(x)$

$t := t \rightarrow \text{next} := \text{new } E1$

$t \rightarrow \text{key}. = x$

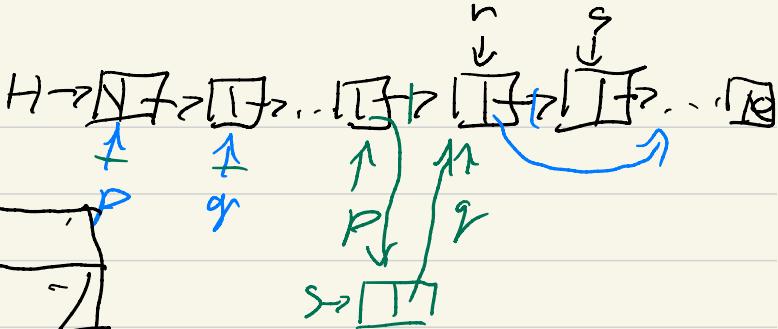


Insertion-Sort (IS)

IS~HIL (H := E1\*)

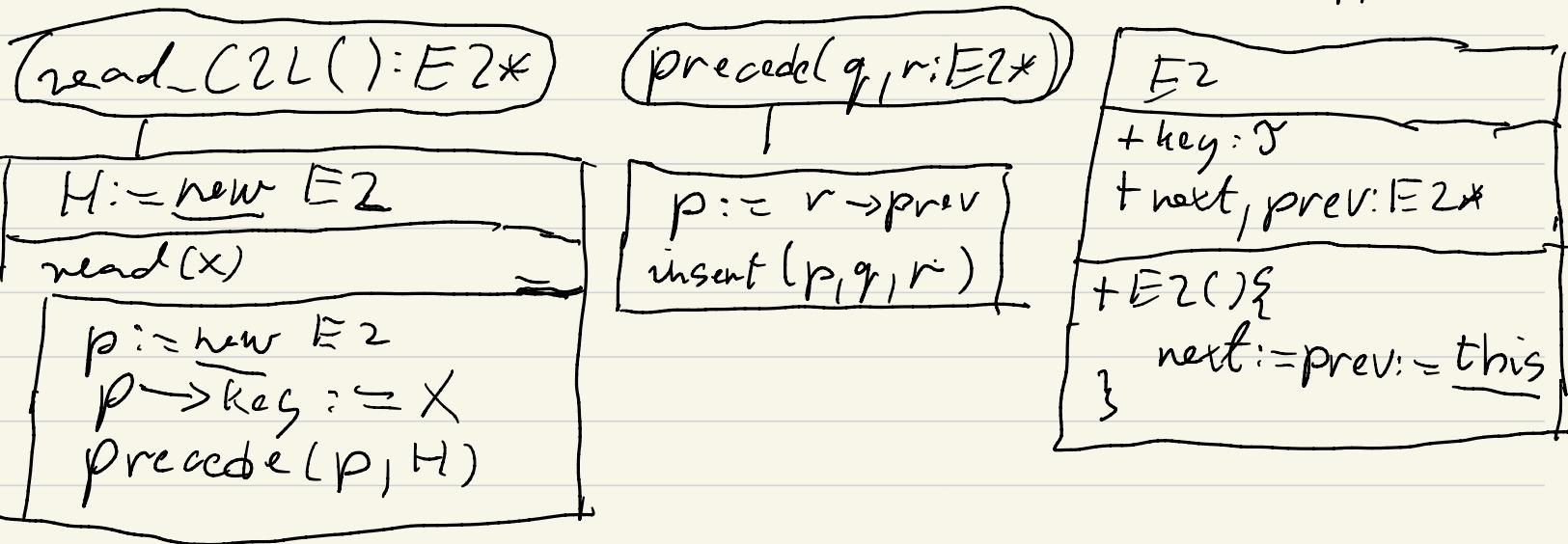
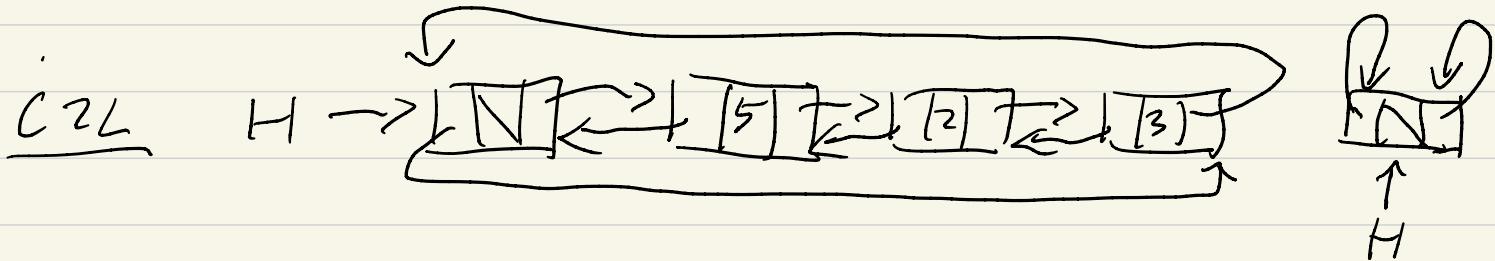
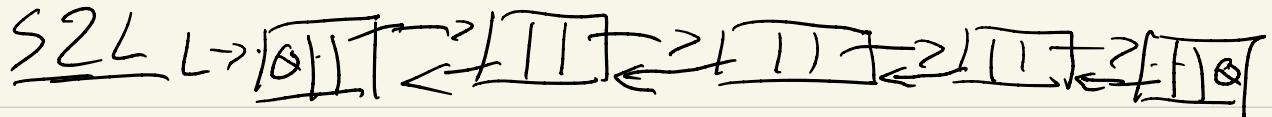
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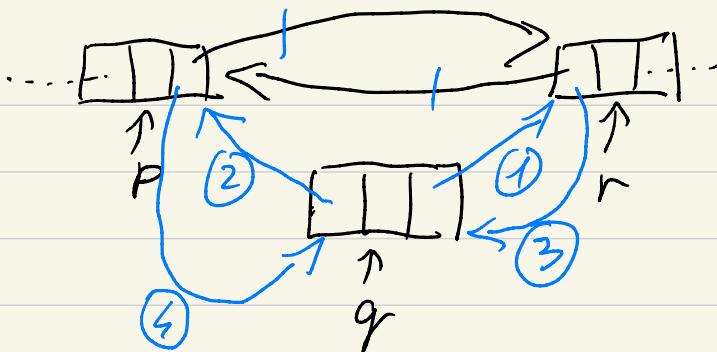
r := H->next
r ≠ Q
s := r->next
s ≠ Q
r->key ≤ s->key
r->next := s->next
:= q->key ≥ s->key
s
p := r; q := q->next
s->next := q
p->next := s
s := r->next
    
```



$$mT(n) \in \Theta(n)$$

$$\left. \begin{array}{l} mT(n) \\ AT(n) \end{array} \right\} \in \Theta(n^2)$$





$\text{insert}(p, q, r : E2\&)$

```

 $q \rightarrow \text{next} := r$ 
 $q \rightarrow \text{prev} := p$ 
 $r \rightarrow \text{prev} := q$ 
 $p \rightarrow \text{next} := r$ 

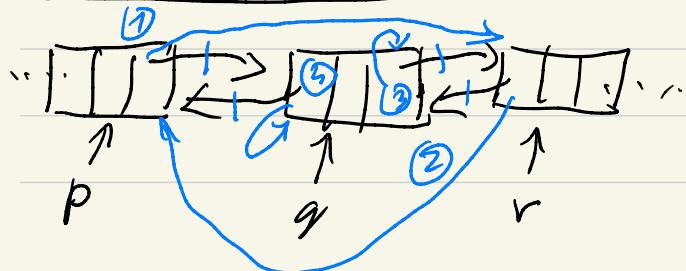
```

$\text{follow}(p, q : E2\&)$

```

 $r := p \rightarrow \text{next}$ 
 $\text{insert}(p, q, r)$ 

```



$\text{unlink}(q : E2\&)$

```

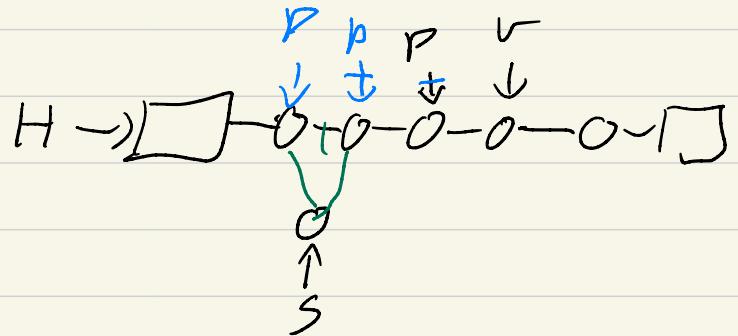
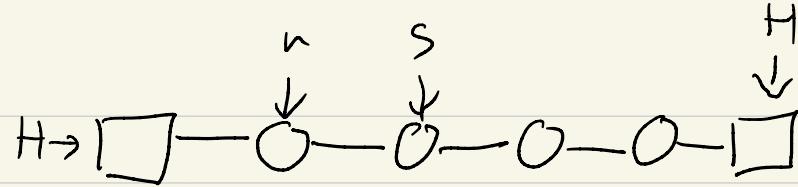
 $p := q \rightarrow \text{prev}; r := q \rightarrow \text{next}$ 
 $p \rightarrow \text{next} := r$ 
 $r \rightarrow \text{prev} := p$ 
 $q \rightarrow \text{prev} := q \rightarrow \text{next} := q$ 

```

IS\_C2L(H:EZ\*)

```

r := H->next; s := r->next
S ≠ H
    r->key ≤ s->key
    r | unlink(s)
    := p := r->prev
    s | p ≠ H ∧ p->key > s->key
        p := p->prev
    } follow(p, s)
    s := r->next
  
```



$$mT(n) \in \Theta(n)$$

$$\left. \begin{array}{l} mT(n) \\ AT(n) \end{array} \right\} \in \Theta(n^2)$$

QUICKSORT(QS)

QuickSort( $A : \mathcal{F}[n]$ )

QS( $A, 0, n-1$ )

QS( $A : \mathcal{F}[]; p, r : \mathbb{N}$ )

$\{5, 2, 9, 7, 1, 8, 1, 1, 3, 6\}$

$\{2, 1, 3, 5, 7, 8, 6\}$

QS

QS

//  $A[p..r]$  renderize

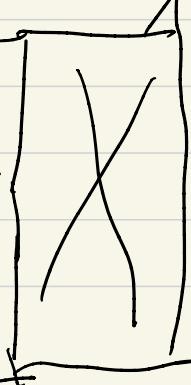
$p \leq r$

$q := \text{partition}(A, p, r)$

//  $A[p..q-1] \leq A[q] \leq A[q+1..r]$

QS( $A, p, q-1$ )

QS( $A, q+1, r$ )



$$l := r - p + 1$$

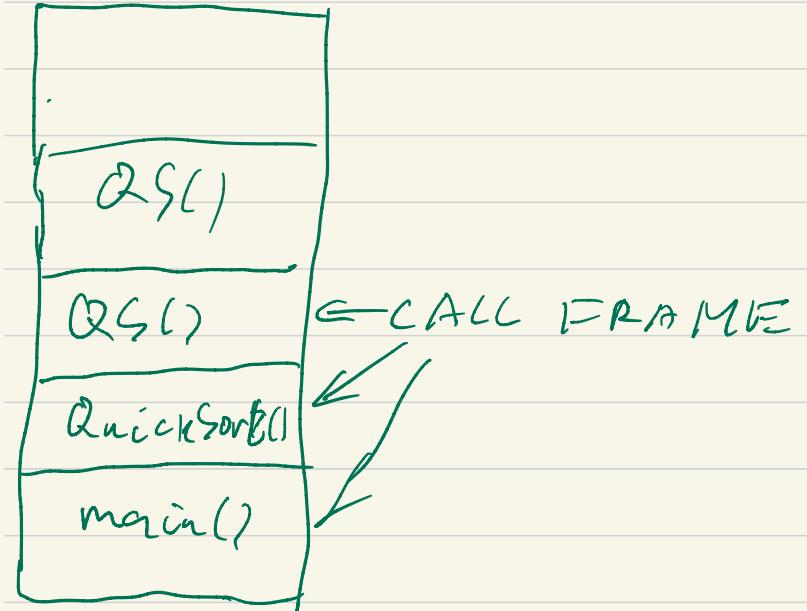
$$\underset{\text{Part}}{MT(l)}, \underset{\text{Part}}{mT(l)} \approx l$$

$$mT_{QS}(n) \leq n \cdot \log n$$

$$\begin{aligned} MT_{QS}(n) &\geq n + (n-1) + (n-2) + \dots + 1 \\ &\stackrel{=}{=} \frac{n(n+1)}{2} = \frac{1}{2}n^2 + \frac{1}{2}n \end{aligned}$$

PARTITIONALS

# CALL STACK



Biz. hat  $mT(n)$   
 $QS$   $AT(n)$

$MT_{QS}(n) \in \Theta(n^2)$

$mS_{QS}(n) \in \Theta(\log n)$

$MS_{QS}(n) \in \Theta(n)$

$mS_{MS}(n) = MS(n) \in \Theta(n)$

$mS_{IS}(n) = MS_{IS}(n) \in \Theta(1)$  HELIBEN-RENDERED

partition( $A: 5[1:p, r:N]$ ): N)

$i := \text{random}(p, r)$   
 $\text{swap}(A[i], A[r])$

$i := p$

$i < r \wedge A[i] \leq A[r]$

$i++$

$i < r$

$j := i+1$

$j < r$

$A[j] < A[r]$

$\text{swap}(A[i+1], A[j])$  | X

$j++$

$\text{swap}(A[i], A[r])$

return i

$\langle 2, 4, 8, 3, 5, 1, 6, 9, 2 \rangle$

$\langle 2, 4, 8, 3, 2, 5, 1, 6, 9, 5 \rangle$

$p \leq i < j \leq r$

$\leq t$	$\geq t$	$? t$
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$\langle 2, 4, 3, 8, 2, 5, 1, 6, 9, 5 \rangle$

$\langle 2, 4, 3, 2, 8, 1, 5, 1, 6, 9, 5 \rangle$

$\langle 2, 4, 3, 2, 1, 5, 1, 8, 1, 6, 9, 5 \rangle$

$\langle 2, 4, 3, 2, 1, 5, 1, 8, 6, 9, 5 \rangle$

$$P \leq i < j=r$$

A horizontal bar diagram with three segments. The first segment is labeled  $\geq t$  and has a bracket below it. The second segment is labeled  $t$  and has a bracket below it. The third segment is labeled  $\leq t$  and has a bracket below it. The entire bar is labeled  $P$  at its left end and  $j=r$  at its right end.

$$P \leq i < r$$

A horizontal bar diagram with three segments. The first segment is labeled  $\geq t$  and has a bracket below it. The second segment is labeled  $t$  and has a bracket below it. The third segment is labeled  $\leq t$  and has a bracket below it. The entire bar is labeled  $P$  at its left end and  $r$  at its right end.

## ASZIMPTOTIKA

D<sub>1</sub>  $\exists N(n) : P(n) \stackrel{\text{def}}{\Leftrightarrow} \exists N \in \mathbb{N}_+ : \forall n \geq N : P(n)$

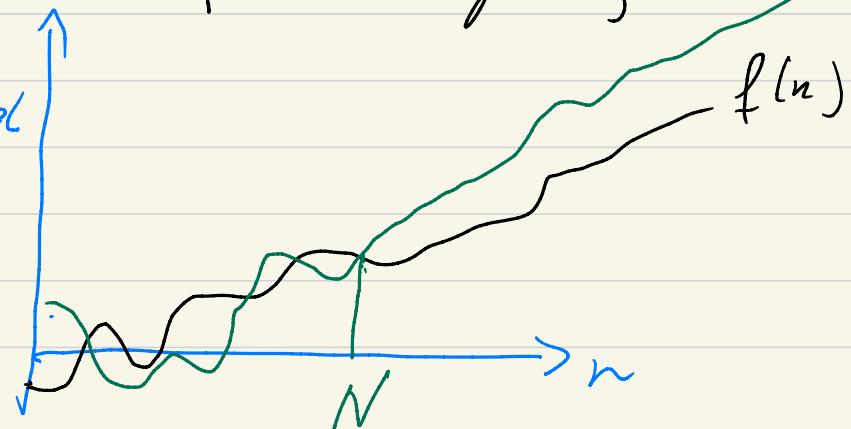
D<sub>2</sub>  $f : \mathbb{N} \rightarrow \mathbb{R}$  AP  $\stackrel{\text{def}}{\Leftrightarrow} \exists N(n) : f(n) > 0$

$f, g, h : \text{AP fü-ek}$  ;  $\varphi, \psi : \mathbb{N} \rightarrow \mathbb{R}$

D<sub>3</sub>  $O(g) = \{f \mid \exists d > 0 : \exists N(n) : f(n) \leq d \cdot g(n)\}$

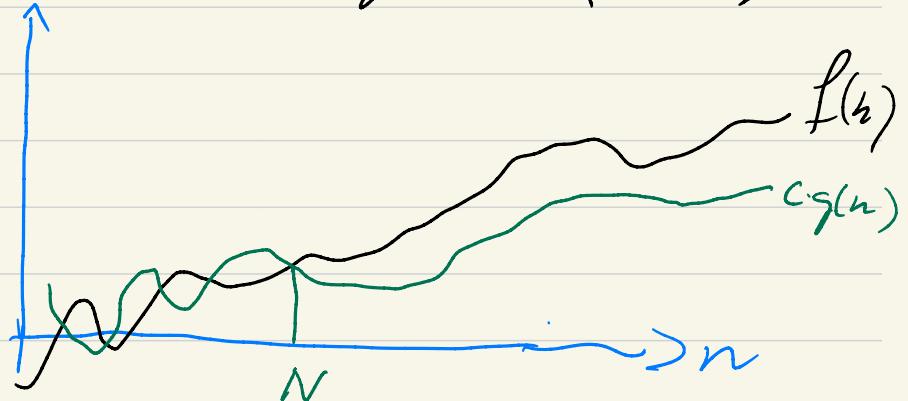
$f \in O(g)$ : (f legfeljebb g-val)

arányos; f aszimptotikus  
felső korlátja g)



$$D_1 \Omega(g) = \{f \mid \exists c > d : \forall n \in \mathbb{N} : c \cdot g(n) \leq f(n)\}$$

$f \in \Omega(g)$ :  $f$  legalább  $g$ -val arányos;  $f$  aszimptotikus alsó korlátja  $g$ )



$$\text{I} f \in \Omega(g) \Leftrightarrow g \in O(f)$$

$$D_1 \Theta(g) \stackrel{\text{def}}{=} O(g) \cap \Omega(g)$$

$$\text{I} f \in \Theta(g) \Leftrightarrow g \in \Theta(f) \quad (\text{f és } g \text{ aszimptotikusan ekvivalens})$$