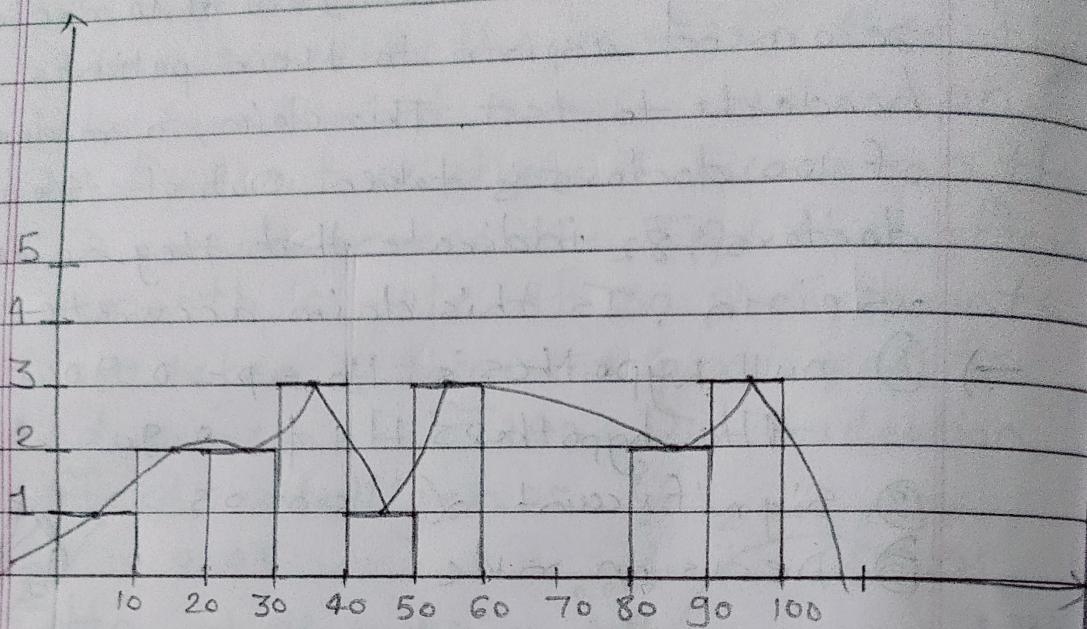


Q1.



Q2.

→ We want to create a 80% CI. That means we have an alpha of 0.10 (20%) which is split into two equal tails. This 10% refers to the value we took up in the T-table in order to find the t-score we need to plug into the equation.

A sample of 25 test-takers has a mean of 520 with a standard deviation of 100.

Because we are using the t-distribution first we must calculate degrees of freedom.

$$df = n - 1 = 25 - 1 = 24$$

$$t = 2.4922$$

$$\bar{x} \pm t_{\frac{\alpha}{2}} \left(\frac{s}{\sqrt{n}} \right)$$

$$520 - 2.4922 \left(\frac{100}{\sqrt{25}} \right) = 470.156$$

$$520 + 2.4922 \left(\frac{100}{\sqrt{25}} \right) = 569.844$$

After plugging everything into the equation, we find a lower bound of 470.156 & an upper bound of 569.844.

We are 80% confident that the mean SAT score between 470.156 & 569.844

Q3.

$$\rightarrow H_0: P = 0.60 \\ H_a: P \neq 0.60$$

$$n = 250 \quad x = 170 \\ \hat{P} = \frac{x}{n} = \frac{170}{250} = 0.68$$

$$P_0 = 0.60 \quad q_0 = 0.40$$

$$n\hat{P} = 250(0.68) = 170 > 10 \\ n(1-\hat{P}) = 250(1-0.68) = 80 > 10$$

$$P_0 = 0.60 \quad x = 170, \quad n = 250$$

$$Z \text{ score} = \frac{x - \mu}{\sigma} = \frac{170 - 150}{25} = 0.80$$

$$P(x < 170) = 0.75099$$

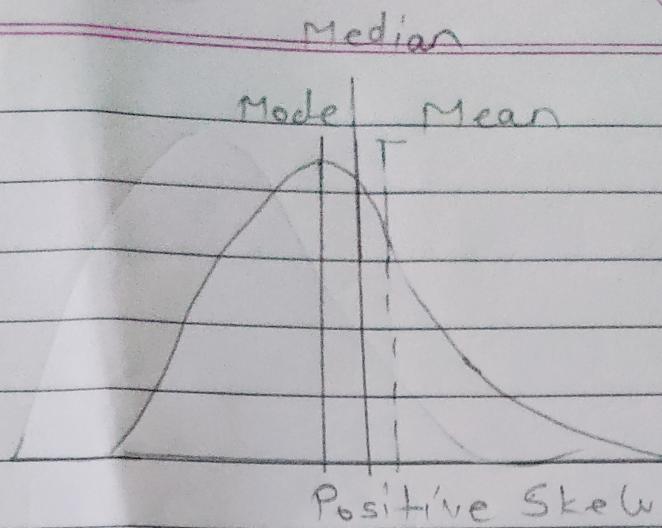
$$P(x > 170) = 1 - P(x < 170) = 0.24901$$

$$P(150 < x < 170) = P(x < 170) - 0.5 \\ = 0.25099$$

$$Q4. \quad 99^{\text{th}} \text{ percentile} = \frac{99}{100} \times (20+1) = 20.79$$

$$\therefore 99 \text{ percentile} = 20.79$$

Q5.

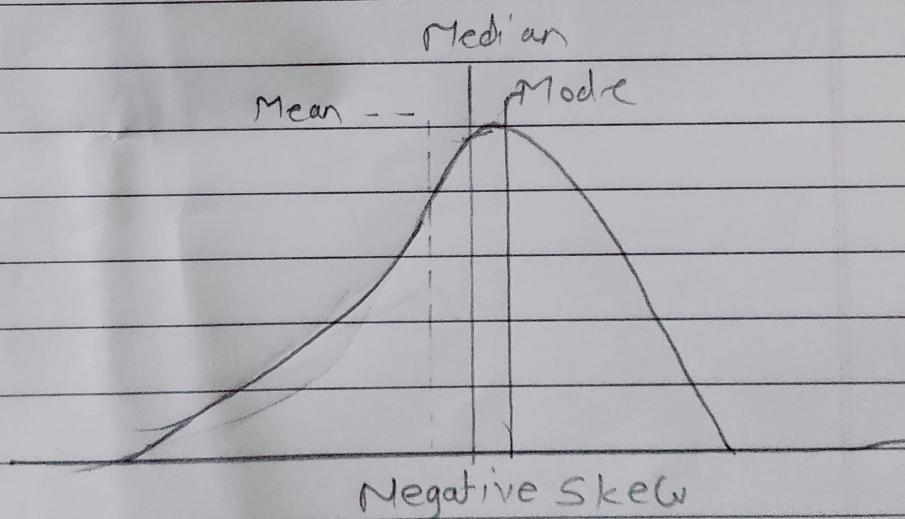


i) Right skewed distribution -

In right skewed distribution,

$\text{Mean} > \text{Median} > \text{Mode}$.

e.g. Wealth distribution.



ii) Left skewed distribution -

In left skewed distribution,

$\text{Mode} > \text{Median} > \text{Mean}$

e.g. Life span of human being.