HW1 2

January 20, 2022

## 1 Problem 2

**Problem 2.1** Given relationships:

$$M_A = 3M_B \tag{1}$$

and

$$x_A = \frac{z}{3} \text{ for } z = [0, 1]$$
 (2)

$$\omega_A = \frac{m_A}{m_A + m_B} \tag{3}$$

$$m = Mn \tag{4}$$

$$x_A = \frac{n_A}{n_A + n_B} \tag{5}$$

find  $\omega_A$  as a function of z: combining (3) and (4) gives

$$\omega_A = \frac{M_A n_A}{M_A n_A + M_B n_B}$$

and substituting (1) into  $M_A$  gives

$$\omega_A = \frac{3M_B n_A}{3M_B n_A + M_B n_B}$$

which can be simplified as

$$\omega_A = \frac{3n_A}{3n_A + n_B} \tag{6}$$

Next, by combining (2) and (5) and solving for  $n_B$  we get

$$x_A = \frac{z}{3} = \frac{n_A}{n_A + n_B}$$

$$n_B = \frac{3n_A}{z} - n_A \tag{7}$$

Now (7) can be substituted into (6) and simplified to get

$$\omega_{A} = \frac{3n_{A}}{3n_{A} + \frac{3n_{A}}{z} - n_{A}} = \frac{3}{3 + \frac{3}{z} - 1}$$

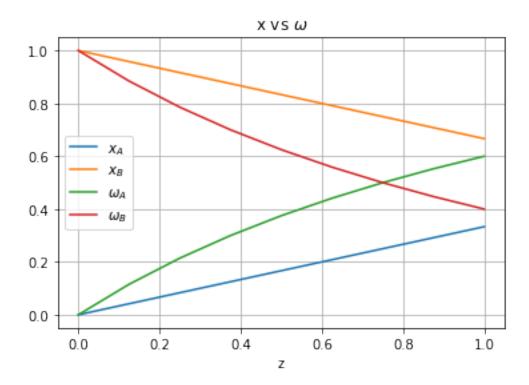
#### Problem 2.2 following is a plot of x and  $\omega$ 

```
[]: import matplotlib.pyplot as plt
 import numpy as np
 z = np.linspace(0,1,9)
 xa = z/3
 xb = 1-xa
 wa = 3/(3+3/z-1)
 wb = 1-wa
 plt.plot(z,xa,label='$x_A$')
 plt.plot(z,xb,label='$x_B$')
 plt.plot(z,wa,label='$\omega_A$')
 plt.plot(z,wb,label='$\omega_B$')
 plt.grid()
 plt.legend()
 plt.title('x vs $\omega$')
 plt.xlabel('z')
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```

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wa = 3/(3+3/z-1)

[]: ''



While the molar fraction is a linear profile, it's interesting that the profile for mass fraction is not linear. The mass fraction increases as the molar fraction increases.