

4.

29  $t x'' + (t-2) x' + x = 0$

$\mathcal{L}\{x\} = \bar{x}$

~~$\mathcal{L}\{x''\} = s^2 \bar{x} - k$~~

$k = x'(0)$

~~$\mathcal{L}\{x'\} = s \bar{x}$~~

$\mathcal{L}\{t x''\} = -\frac{d}{ds}(s^2 \bar{x} - k) = -s^2 \bar{x}' - 2s \bar{x}$

~~$\mathcal{L}\{t x'\} = s \bar{x} + x$~~

~~$\mathcal{L}\{t x\} = -\bar{x}'$~~

~~$s^2 \bar{x}' - 2s \bar{x} + (t-2)(s \bar{x} + \bar{x}) = 0$~~

$\mathcal{L}\{t x'\} = s \bar{x}' + \bar{x}$

$\mathcal{L}\{t x\} = -2 \bar{x}' s + \bar{x}$

$-s^2 \bar{x}' - 2s \bar{x} + s \bar{x}' + \bar{x} - 2 \bar{x}' s + \bar{x} = 0$

$-s^2 \bar{x}' + s \bar{x}' - 2s \bar{x} + \bar{x} - 2 \bar{x}' s + \bar{x} = 0$

$-s^2 \bar{x}' + s \bar{x}' - 4s \bar{x} + 2 \bar{x}$

$s^2 \bar{x}' + s \bar{x}' = 4s \bar{x} - 2 \bar{x}$

$\frac{\bar{x}'}{\bar{x}} = \frac{4s-2}{s^2+s}$