

# Homework 6

## Problem 1.1

Determine the dew point temperature and composition of the first droplet for a mixture of 70% methanol.   
 Vapor-Liquid Equilibrium Data for Methanol(A) and Water(B)

| $T$<br>°C | $y_A$ | $x_A$ |
|-----------|-------|-------|
| 64.5      | 1.000 | 1.000 |
| 66.0      | 0.958 | 0.900 |
| 69.3      | 0.870 | 0.700 |
| 73.1      | 0.779 | 0.500 |
| 78.0      | 0.665 | 0.300 |
| 84.4      | 0.517 | 0.150 |
| 93.5      | 0.230 | 0.040 |
| 100.0     | 0.000 | 0.000 |

The data in the table above shows the bubble and dew lines for the methanol-water system. The temperature is the bubble or dew point temperature at a specific composition.   
 Using this data, the dew point temperature at 70% methanol is found by determining the temperature when  $y_A = 0.70$ . The composition of the first droplet is then found by determining  $x_A$  at the dew point temperature.   
 The code below interpolates to find  $T$  when  $y_A = 0.70$  and then  $x_A$  at  $T$  using `scipy.interpolate.interp1d`

```
In [ ]: import matplotlib.pyplot as plt
import numpy as np
from scipy.interpolate import interp1d

molFrac = np.linspace(0,1,9999) #array of

T = np.array([64.5,66,69.3,73.1,78,84.4,89.3,93.5,100]) #temp dat
yA = np.array([1,.958,.87,.779,.665,.517,.365,.23,0]) #sat vap
xA = np.array([1,.9,.7,.5,.3,.15,.08,.04,0]) #sat liq

interpX = interp1d(xA,T,kind='cubic')
interpY = interp1d(yA,T,kind='cubic')
interpTx = interp1d(T,xA,kind='cubic')
interpTy = interp1d(T,yA,kind='cubic')
```

```
In [ ]: mix = 0.7 #mix comp
Tdew = interpY(mix) #dew point te

TdewApprox = [] #this loop fi
for i in range(100):
```

```

if i <=Tdew and i >Tdew-0.1:
    TdewApprox.append(i)

xDew = molFrac[interpX(molFrac).tolist().index(max(TdewApprox))] #comp of first droplet
print('T_dew =',Tdew)
print('x_dew =',xDew)

```

```

T_dew = 76.46925604119907
x_dew = 0.35247049409881975

```

The dew point temperature is about 76.5\degreeC and the composition of the first droplet is about 36% Methanol. </br></br> Below is the solution represented graphically

```

In [ ]: plt.figure(figsize=(12,7))
plt.plot(xA,T,label='Saturated liquid')
plt.plot(yA,T,label='Saturated vapor')

plt.vlines(mix,min(T),Tdew,linestyles='--',color='k')
plt.vlines(xDew,min(T),Tdew,linestyles='--',color='k')
plt.hlines(Tdew,xDew,mix,linestyles='--',color='k')

plt.text(.5,77,'Dew point T')
plt.text(.24,67,'Composition\nof first droplet')
plt.text(.6,65.5,'Mixture\ncomposition')
plt.xlabel(r'$x_A$, $y_A$')
plt.ylabel('Temperature (C)')
plt.grid()
plt.title('Methanol(A), Water(B)')
plt.legend()

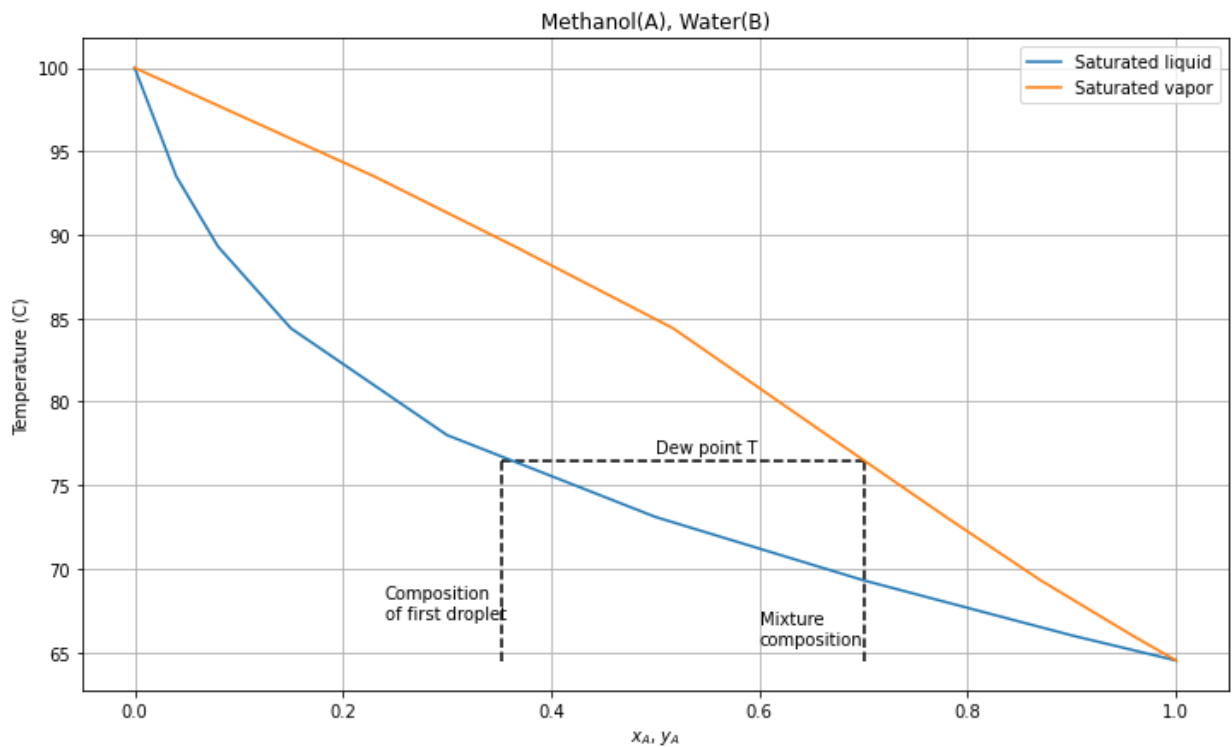
;

```

```

Out[ ]: ''

```



## Problem 1.2

Determine the bubble point temperature when  $x_A = 0.70$  and the composition of the first bubble  
  
Following similar logic as problem 1.1, the bubble point temperature can be found by using the data provided to determine  $T$  when  $x_A = 0.70$ . The composition of the first bubble is  $y_A$  at the bubble point temperature. Since there is a data point for  $x_A = 0.70$ , no interpolation is necessary  
  
The bubble point temperature is  $69.3^{\circ}\text{C}$  and the composition of the first bubble is 87.0%.

Below is the graphical representation of the solution along with the solution from problem 1.1

In [ ]:

```
Tbub = 69.3
yubub = 0.87
```

In [ ]:

```
plt.figure(figsize=(12,7))
plt.plot(xA,T,label='Saturated liquid')
plt.plot(yA,T,label='Saturated vapor')

plt.vlines(mix,min(T),Tdew,linestyles='--',color='k')
plt.vlines(xDew,min(T),Tdew,linestyles='--',color='k')
plt.hlines(Tdew,xDew,mix,linestyles='--',color='k')

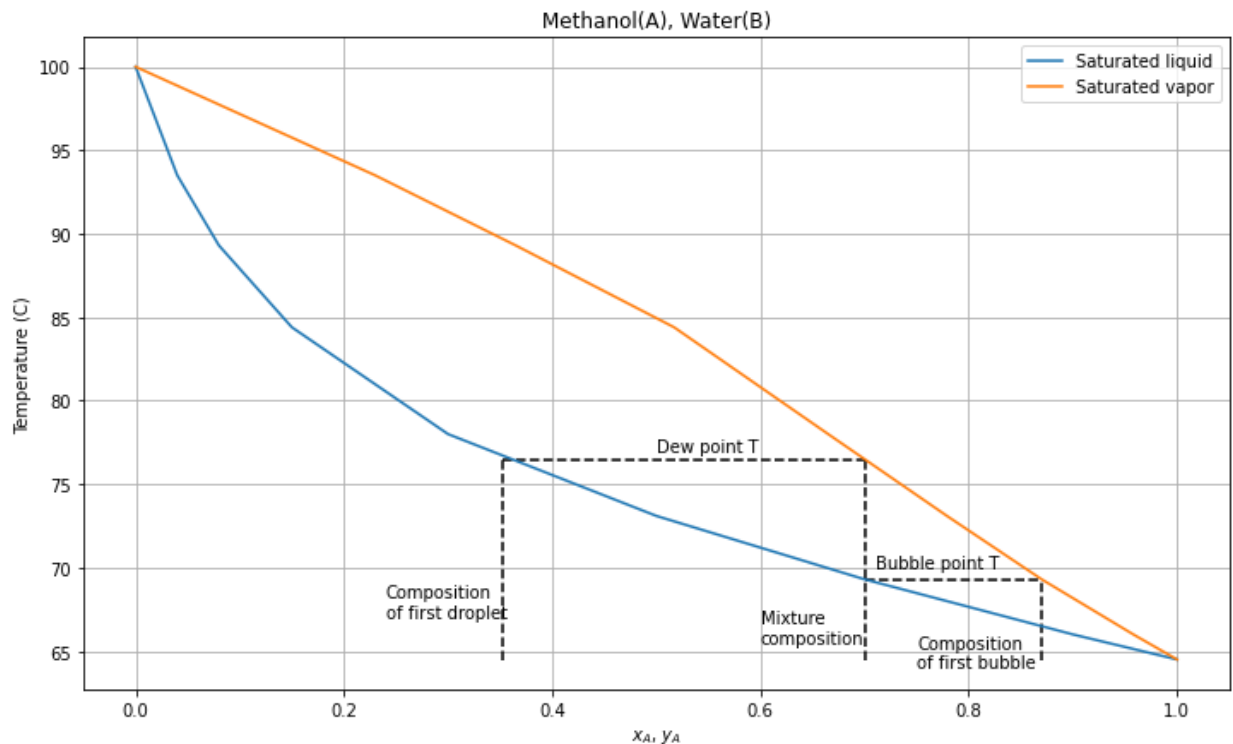
plt.hlines(Tbub,mix,yubub,linestyles='--',color='k')
plt.vlines(yubub,min(T),Tbub,linestyles='--',color='k')

plt.text(.5,77,'Dew point T')
plt.text(.24,67,'Composition\nof first droplet')
plt.text(.6,65.5,'Mixture\ncomposition')
plt.text(.71,70,'Bubble point T')
plt.text(.75,64,'Composition\nof first bubble')
```

```
plt.xlabel(r'$x_A$, $y_A$')
plt.ylabel('Temperature (C)')
plt.grid()
plt.title('Methanol(A), Water(B)')
plt.legend()

;
```

Out [ ]:



## Problem 1.3

Determine the temperature and composition of each phase when the mixture is is 70% methanol and 80% vapor  
Using the inverse lever arm rule,

$$\frac{V}{V+L} = \frac{\text{composition}_{mix} - x_A}{y_A - x_A} = 0.80 = \frac{0.70 - x_A}{y_A - x_A} \quad (1)$$

where V and L are the relative amounts of vapor and liquid respectively,  $x_A$  is the point on the saturated liquid line at a specified temperature and  $y_A$  is the point on the saturated vapor line at the same temperature. Below is a graphical representation

In [ ]:

```
plt.figure(figsize=(12,7))
plt.plot(xA,T,label='Saturated liquid')
plt.plot(yA,T,label='Saturated vapor')

plt.vlines(mix,min(T),Tdew,linestyles='--',color='k')
plt.hlines(73.1,.5,.779,linestyles='--',color='k')

plt.text(.6,65.5,'Mixture\ncomposition')
```

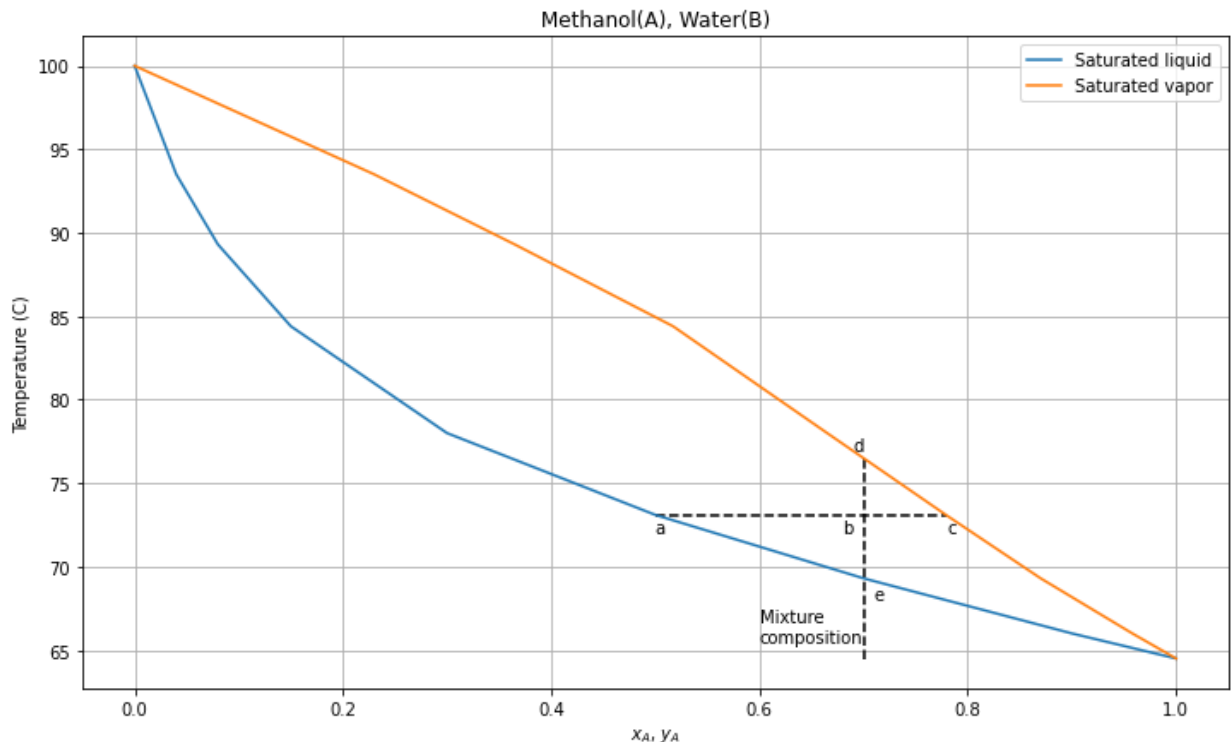
```

plt.text(.5,72,'a')
plt.text(.68,72,'b')
plt.text(.78,72,'c')
plt.text(.69,77,'d')
plt.text(.71,68,'e')
plt.xlabel(r'$x_A$, $y_A$')
plt.ylabel('Temperature (C)')
plt.grid()
plt.title('Methanol(A), Water(B)')
plt.legend()

;

```

Out[ ]:



In the diagram,  $\bar{ac}$  is relative and is not necessarily the correct temperature.  $a$  represents the liquid composition and  $c$  represents the vapor composition. To find the correct temperature, (1) needs to be solved as

$$0.8 = \frac{b - a}{c - a}$$

where  $b = 0.70$  This is one equation with two unknowns but since the total composition is 0.70, it is known that  $y_A$  in (1) must correlate with a temperature in between points  $d$  and  $e$ . The following code solves (1) using the interpolated set of data.

```

In [ ]:
possibY = []
for i in range(len(molFrac)):
    if molFrac[i] < ysub and molFrac[i] > mix:
        possibY.append(molFrac[i])
possibY = np.array(possibY)
possibX = interpTx(interpY(possibY))

```

*#Loop to make array of possible y values*

*#possible x values*

```
In [ ]: sol = (mix-possibX)/(possibY-possibX)           #solution to eq1
        sol = sol.tolist()

        for i in sol:                                   #loops to find x,y to ach
            if .8/i >=.9999 and .8/i <=1:
                percVap = i
                print(possibX[sol.index(i)],possibY[sol.index(i)],i)
        print(interpY(possibY[sol.index(percVap)]))
```

```
0.46138061015288967 0.7596519303860773 0.8000078239522271
73.92201066046555
```

When 80% of the mixture is vapor the temperature is about 73.9\degreeC, the liquid composition is about 46.1% methanol and the vapor composition is about 76.0% methanol.

## Problem 1.4

Solve problem 1.3 using the q-line </br></br> The equation for the q-line is

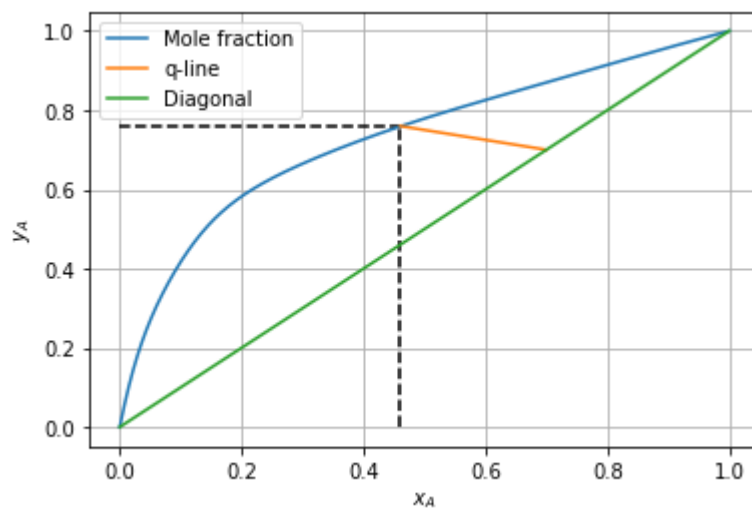
$$y_A = \frac{\frac{V}{F} - 1}{\frac{V}{F}} x_A + \frac{F}{V} z_A \quad (2)$$

where  $\frac{V}{F} = 0.80$  and  $z_A = 0.70$ . The composition of each phase is found by finding where the q-line crosses the  $x,y$  curve.

```
In [ ]: def qline(V,F,z,x):
        return (V/F-1)*F/V*x+F/V*z
        plt.plot(interpTx(interpX(molFrac)),interpTy(interpX(molFrac)),label='Mole fraction')
        plt.plot([.46,.7],qline(.8,1,.7,np.array([.46,.7])),label='q-line')
        plt.plot([0,1],[0,1],label='Diagonal')
        plt.hlines(qline(.8,1,.7,.46),0,.46,linestyles='--',color='k')
        plt.vlines(.46,0,qline(.8,1,.7,.46),linestyles='--',color='k')
        plt.xlabel(r'$x_A$')
        plt.ylabel(r'$y_A$')
        plt.grid()
        plt.legend()

        ;
        print(interpX(.46))
```

```
73.92669644249968
```



According to the q-line in the above plot,  $x_A \approx 0.46$  and  $y_A \approx 0.79$  which are similar to the solution found using the inverse lever-arm rule. The temperature of both phases is  $73.9^{\circ}\text{C}$