Exercise 16.6 Let G = (V, E) be an undirected graph with distinct nonnegative edge weights $w : E \to \mathbb{R}$. For a spanning tree T, we say that the *bottleneck weight of* T is the maximum weight edge in T, $\max_{e \in T} w(e)$.

Exercise 16.6.1. Prove that the MST is also a minimum bottleneck weight spanning tree of G.

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Exercise 16.6.2. Design and analyze a O(m+n)-time algorithm for computing a minimum bottleneck weight spanning tree of G. (This is faster than any of our algorithms for MST.)⁴

⁴Here's step 1: compute the median edge weight in O(m) time.

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