

**Exercise 13.4.** Let  $G = (V, E)$  be a directed graph. We say that a set of vertices is *almost independent* if each  $v \in S$  has at most one neighbor in  $S$ .<sup>5</sup> Consider the problem of computing the maximum cardinality of any almost independent set of vertices. For this problem, either (a) design and analyze a polynomial time algorithm (the faster the better), or (b) prove that a polynomial time algorithm would imply a polynomial time algorithm for SAT.

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<sup>5</sup>Two vertices  $u$  and  $v$  are neighbors if they are connected by an edge.

*Solution.*

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