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Define/State:

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- $\lim_{n \rightarrow \infty} x_n = L$
- $\lim_{x \rightarrow} f(x) = L$
- $f: A \rightarrow \mathbb{R}$ is cts at $c \in A$
- $f: A \rightarrow \mathbb{R}$ is uniformly cts on A
- $f, f_n: A \rightarrow \mathbb{R}$, $f_n \rightarrow f$ pointwise on A
- $f, f_n: A \rightarrow \mathbb{R}$, $f_n \Rightarrow f$ on A
- (f_n) is uniformly Cauchy on A

(2)

- (x_n) is Cauchy
- $\sum_{n=1}^{\infty} x_n = L$
- Cauchy criterion for $\sum_n x_n$
- Principle of Mathematical Induction
- Cantor's Theorem
- Bolzano - Weierstrass Theorem
- Monotone functions
- $f'(c)$
- Chain Rule

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- Completeness Property of \mathbb{R}
 - sup, inf
 - Bounded set, sequence, function
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You will be asked to give a full proof of the Nested Intervals Theorem.

(4)

• Show $\lim_{x \rightarrow 4} \sqrt{x} - 1 = 1$

• Show $\lim_{n \rightarrow \infty} \frac{1}{\sqrt{n} - 1} = 0$

• Show that if $f_n(x) = \frac{x^2 + 3}{\sqrt{n}}$
on $[-1, 1]$ then $f_n \rightarrow 0$.

• Show that if A is bounded above and B is bounded below then

$$A - B = \{x - y \mid x \in A, y \in B\}$$

is bounded above

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• Does $x_1 = 1$

$$x_{n+1} = \sqrt{x_n + 4}$$

converge?