1 GALOIS GROUPS II 1

## 1 Galois Groups II

**Lemma 1.1.** Suppose that L:K is a normal extension with  $K\subseteq L\subseteq \overline{K}$ . Then for any K-homomorphism  $\tau:L\to \overline{K}$ , we have  $\tau(L)=L$ .

**Lemma 1.2.** For  $n \geq 2$ ,  $S_n$  is generated by

- 1. transpositions(ij);
- 2. transpositions (1i);
- 3. adjacent transpositions  $(12), (23), \ldots, (n-1, n)$ ;
- 4. (12) and (12...n);
- 5. (12) and (23...n);
- 6. (ij) and  $(i \dots i_p)$  where p is prime.

**Lemma 1.3.** Let  $(i_1 \ldots i_k) \in S_n$ . Then for all  $\sigma \in S_n$ , one has  $\sigma(i_1 \ldots i_k) \sigma^{-1} = (\sigma(i_1) \ldots \sigma(i_k))$ .

Note:  $|Gal_K(f)| = [L:K]$  where L:K is a splitting field extension for f.