One-Sample Procedure V1

The Federal Aviation Administration (FAA) requires that environmental documents address noise impact around airports using an impact threshold of Day Night Average Sound Level (DNL) 65(dBa). A sample of 112 residential homes in the vicinity of a major airport were selected and the average DNL noise level of these residents were measured with the owner's permission over a 1-month period. The data is used to assess if there is evidence at an 0.06 significance level that the DNL exceeds 65(dBa). The sample mean and sample standard deviation for these 112 observations for the average DNL noise level was found to be 66.00179(dBa) and 6.717169(dBa) respectively.

- a) Select the letter corresponding to the correct choice for the first step of the four-step hypothesis test process.
 - The parameter of interest is the true Day Night Average Sound Level (DNL) " μ_{DNL} " of the neighborhood of residential homes around this major airport; in units of dBA.
- b) Select the letter corresponding to the most appropriate choice for the second step (State the Hypothesis) of the four-step hypothesis test process.
 - [A] H_0 : $\mu_{DNL} \le 65$ (dBa), H_a : $\mu_{DNL} > 65$ (dBa)
- c) Which of the following would provide a result consistent with the hypothesis you selected above:
 - B Lower Confidence Bound
- d) What is the appropriate **confidence level** for the **interval or bound** that you selected above?

Please write your answer using 4 decimal places and write it as decimal value not as a percentage.

For example, if it was a **95.55% confidence level**, you would enter **0.9555**. You may drop any trailing zeros if you do not need the full 4 decimal places.

$$C = 100 \times (1 - \alpha) = 94\%$$

0.94 <-answer

e) An FAA researcher has determined from prior studies that the average DNL noise level in neighborhoods around airports is **known** to have a **standard deviation of 4(dBa)**.

Select the **correct critical value** from the **table below** for the **confidence interval** or **bound** that is **consistent** with your **stated hypothesis** and **confidence level**.

Note that more information is provided in the table than is needed to answer the question.

> qt(0.06, df = 111, lower.tail = FALSE)	> qt(0.06/2, df = 111, lower.tail = FALSE)
[1] 1.566834	[1] 1.90021
> qnorm(0.06, lower.tail = FALSE)	> qnorm(0.06/2, lower.tail = FALSE)
[1] 1.554774	[1] 1.880794

Your answer should be given using the full value of the critical value. Do not round and make sure you use the full value in subsequent questions.

 $\sigma = 4$ is known so we use normal distribution.

> qnorm(0.06, lower.tail = FALSE)

[1] 1.554774

f) Use the **critical value** you just obtained and the **population** standard deviation of 4 dBa to calculate the **confidence interval** or **bound** that is consistent with your stated hypothesis.

Your answer must be given in **interval notation** and any **numbers** should be **correctly rounded** to **four decimal places**.

We will use confidence lower bound since the alternative is greater than.

$$\left(\overline{x}_{\rm DNL} - z_{0.06} \frac{\sigma_{\rm DNL}}{\sqrt{n}}, \infty\right)$$

$$\left(66.00179 - 1.554774 \frac{4}{\sqrt{112}}, \infty\right)$$

$$\left(65.4141, \infty\right)$$

g) Using the confidence interval or bound that you computed above determine the conclusion of the hypothesis test.

Would you reject the null hypothesis? Select the most appropriate option from the choices below.

Confidence Lower Bound Choices

- The confidence lower bound value is greater than the null value of 65 (dBa). Therefore, we would reject the null hypothesis that the true DNL is at most 65 (dBa) and conclude that there is evidence at the 0.06 significance level that the true DNL is greater than 65 (dBa).
- h) Another researcher has identified that the design of the neighborhoods around this airport differs from those around typical airports and it would **not be appropriate** to **assume** that the **standard deviation is 4(dBa)**. Would the **critical value** of the **confidence interval** or **bound change**?

Select the letter of the most appropriate answer from the choices below.

- Yes, the critical value would change; in fact, it would be larger than what we found previously. The need for a new critical value is due to the added uncertainty of having to estimate the standard deviation from the data.
- i) What practical answer would you give to the FAA about the noise level around this particular major airport? Differences greater than 1.5(dBa) higher than the **impact threshold DNL** of **65(dBa)** are **considered problematic** and **require significant investment** to reduce the noise level. Use the **confidence interval or bound** found previously to provide a **practicality assessment** for the FAA. You may continue to assume the **population standard deviation** is **known**, regardless of your conclusion in the previous part.

You must report your conclusion, difference, and effect size.

Write your answer as follows: conclusion (yes or no), difference, effect size. Round your number to 2 decimal places for simplicity.

For example, if you concluded yes there is practical significance (investment is required to reduce the noise level), and found a difference of 3.2 dBa, with an effect size of 0.81 you would write your answer as: --> yes,3.2,0.81

Confidence lower bound value → 65.4141

Null value → 65

Difference → $65.4141 - 65 \approx 0.41$

Effect Size $\rightarrow \frac{0.41}{4} \approx 0.1$

Answer → no,0.41,0.1

One-Sample Procedure V2

The Federal Aviation Administration (FAA) requires that environmental documents address noise impact around airports using an impact threshold of Day Night Average Sound Level (DNL) 65(dBa). A sample of 160 residential homes in the vicinity of a major airport were selected and the average DNL noise level of these residents were measured with the owner's permission over a 1-month period. The data is used to assess if there is evidence at an 0.04 significance level that the DNL exceeds 65(dBa). The sample mean and sample standard deviation for these 160 observations for the average DNL noise level was found to be 65.82778 (dBa) and 6.523252 (dBa) respectively.

- a) Select the letter corresponding to the correct choice for the first step of the four-step hypothesis test process.
 - The parameter of interest is the true Day Night Average Sound Level (DNL) " μ_{DNL} " of the neighborhood of residential homes around this major airport; in units of dBA.
- b) Select the letter corresponding to the most appropriate choice for the second step (State the Hypothesis) of the four-step hypothesis test process.
 - [E] H_0 : $\mu_{DNL} \le 65$ (dBa), H_a : $\mu_{DNL} > 65$ (dBa)
- c) Which of the following would provide a result consistent with the hypothesis you selected above:
 - [A] Lower Confidence Bound
- d) What is the appropriate **confidence level** for the **interval or bound** that you selected above?

Please write your answer using 4 decimal places and write it as decimal value not as a percentage.

For example, if it was a **95.55% confidence level**, you would enter **0.9555**. You may drop any trailing zeros if you do not need the full 4 decimal places.

$$C = 100 \times (1 - \alpha) = 96\%$$

0.96 <-answer

e) An FAA researcher has determined from prior studies that the average DNL noise level in neighborhoods around airports is **known** to have a **standard deviation of 4(dBa)**.

Select the **correct critical value** from the **table below** for the **confidence interval** or **bound** that is **consistent** with your **stated hypothesis** and **confidence level**.

Note that more information is provided in the table than is needed to answer the question.

> qt(0.04, df = 159, lower.tail = FALSE)	> qt(0.04/2, df = 159, lower.tail = FALSE)
[1] 1.761947	[1] 2.070734
> qnorm(0.04, lower.tail = FALSE)	> qnorm(0.04/2, lower.tail = FALSE)
[1] 1.750686	[1] 2.053749

Your answer should be given using the full value of the critical value. Do not round and make sure you use the full value in subsequent questions.

 $\sigma = 4$ is known so we use normal distribution.

> qnorm(0.04, lower.tail = FALSE)

[1] 1.750686

f) Use the **critical value** you just obtained and the **population** standard deviation of 4 dBa to calculate the **confidence interval** or **bound** that is consistent with your stated hypothesis.

Your answer must be given in **interval notation** and any **numbers** should be **correctly rounded** to **four decimal places**.

We will use confidence lower bound since the alternative is greater than.

$$\left(\overline{x}_{\rm DNL} - z_{0.06} \frac{\sigma_{\rm DNL}}{\sqrt{n}}, \infty\right)$$

$$\left(65.82778 - 1.750686 \frac{4}{\sqrt{160}}, \infty\right)$$

$$(65.27416, \infty)$$

g) Using the confidence interval or bound that you computed above determine the conclusion of the hypothesis test.

Would you reject the null hypothesis? Select the most appropriate option from the choices below.

Confidence Lower Bound Choices

- The confidence lower bound value is greater than the null value of 65 (dBa). Therefore, we would reject the null hypothesis that the true DNL is at most 65 (dBa) and conclude that there is evidence at the 0.04 significance level that the true DNL is greater than 65 (dBa).
- h) Another researcher has identified that the design of the neighborhoods around this airport differs from those around typical airports and it would **not be appropriate** to **assume** that the **standard deviation is 4(dBa)**. Would the **critical value** of the **confidence interval** or **bound change**?

Select the letter of the most appropriate answer from the choices below.

- Yes, the critical value would change; in fact, it would be larger than what we found previously. The need for a new critical value is due to the added uncertainty of having to estimate the standard deviation from the data.
- i) What practical answer would you give to the FAA about the noise level around this particular major airport? Differences greater than 1.5(dBa) higher than the **impact threshold DNL** of **65(dBa)** are **considered problematic** and **require significant investment** to reduce the noise level. Use the **confidence interval or bound** found previously to provide a **practicality assessment** for the FAA. You may continue to assume the **population standard deviation** is **known**, regardless of your conclusion in the previous part.

You must report your conclusion, difference, and effect size.

Write your answer as follows: conclusion (yes or no), difference, effect size. Round your number to 2 decimal places for simplicity.

For example, if you concluded yes there is practical significance (investment is required to reduce the noise level), and found a difference of 3.2 dBa, with an effect size of 0.81 you would write your answer as: --> yes,3.2,0.81

Confidence lower bound value → 65.27416

Null value → 65

Difference → $65.27416 - 65 \approx 0.27$

Effect Size $\rightarrow \frac{0.27}{4} \approx 0.07$

Answer → no,0.27,0.07

Two-Sample Procedure V1

A university department is conducting research to enhance the undergraduate learning environment. The department aims to investigate whether there is a **positive** impact on learning outcomes when the emphasis of a course is shifted from **traditional lecture-based instruction (T)** to new **Al-enhanced instruction (A)**.

To accomplish this, the department separated its **56 undergraduate courses randomly** into two groups: **28 courses** would be taught using the new **Al-enhanced instruction**, and the **remaining 28 courses** would be taught using the **traditional lecture-based** instruction. At the end of the semester, they collected the **average final grades from each course**.

The summary statistics of the semester are provided in the table below.

Course Type	n	X	S
A	28	78.82809	2.810766
T	28	77.59551	3.182277
A-T	28	1.232584	4.161893

a) Which analysis method is appropriate for the given situation: **two-sample independent** or **two-sample paired**?

Select the correct approach and the most appropriate reasoning from the choices below.

Two-Sample Independent Choices

The situation calls for a **two-sample independent analysis**. The department randomly assigned 28 courses to receive the AI-enhanced instruction and the remaining 28 courses to receive traditional lecture-based instruction. Since the courses were assigned independently and there is no common factor to pair on, a two-sample independent analysis is appropriate.

b) The department will conduct a statistical hypothesis for this investigation at a **0.02 significance level**. Select the most appropriate hypothesis for the given statistical question from the choices below.

Let **A** denote the enhanced AI-based instruction, and **T** denote the traditional lecture-based instructional method and μ denote the true average grades.

[B]
$$H_0$$
: $\mu_A - \mu_T \le 0$, H_a : $\mu_A - \mu_T > 0$

c) Calculate the appropriate test statistic. (Use 4 decimal places in your answer)

$$t_{\text{TS}} = \frac{(\overline{x}_{\text{A}} - \overline{x}_{\text{T}})}{\sqrt{\frac{s_{\text{A}}^2}{n_{\text{A}}} + \frac{s_{\text{T}}^2}{n_{\text{T}}}}} = \frac{78.82809 - 77.59551}{\sqrt{\frac{2.810766^2}{28} + \frac{3.182277^2}{28}}} = 1.536133$$

d) Indicate which of the options below is **most likely** to be the correct R code for directly computing the appropriate p-value for the hypothesis test?

Let **TS** denote the assumed correctly computed test statistic value you computed above.

e) Assume that the following interval and bounds are computed correctly using the data and at a confidence level of 0.98.

Choose the appropriate confidence bound/interval for this situation.

- A 98 percent confidence interval: -0.4567313 Inf
- f) Select an appropriate interpretation of your confidence interval or bound.

- I am 98% confident that the difference in the true means between Al-enhanced instruction and traditional lecture-based instruction is greater than -0.4567313.
- g) Based **solely** on the **appropriate confidence interval/bound** that you selected above, what is the most **appropriate conclusion** for the **hypothesis test** from the choices below.
 - **E Do not reject the null hypothesis.** Since the constructed **98% confidence interval** or **bound** is complementary to the hypothesis test (**with** α+C=1), is in the **direction** of the **alternative hypothesis**, and **contains 0**, we would **not reject** the **null hypothesis** and therefore we **do not have sufficient evidence** to suggest that the AI-enhanced instruction has a positive impact on learning outcomes in comparison to traditional based instruction.

Two-Sample Procedure V2

A university department is conducting research to enhance the undergraduate learning environment. The department aims to investigate whether there is a positive impact on learning outcomes when the emphasis of a course is shifted from traditional lecture-based instruction (T) to new Al-enhanced instruction (A). To accomplish this, the department collected data from a course that has run two sections for the past 4 semesters. One section has an Al-enhanced instruction emphasis (Group A), while the other section has a traditional lecture emphasis (Group T). The department collected historical average final grades for both sections over these 4 semesters.

The summary statistics of these 4 semesters are provided in the table below.

Course Type	n	X	S
A	4	79.41944	2.894922
T	4	77.03067	2.625191
A-T	4	2.38877	4.468147

a) Which analysis method is appropriate for the given situation: **two-sample independent** or **two-sample paired**?

Select the correct approach and the most appropriate reasoning from the choices below.

Two-Sample Paired Choices

The situation calls for a **two-sample paired analysis** because each **AI-enhanced instruction** section is **paired** with a **lecture-based instruction** section based on similar content and difficulty. This matching ensures that each pair of sections is directly comparable in terms of subject matter and instructional level.

b) The department will conduct a statistical hypothesis for this investigation at a **0.02 significance level**. Select the most

appropriate hypothesis for the given statistical question from the choices below.

Let $\bf A$ denote the enhanced AI-based instruction, and $\bf T$ denote the traditional lecture-based instructional method and μ denote the true average grades.

E
$$H_0$$
: $\mu_D \le 0$, H_a : $\mu_D > 0$

c) Calculate the appropriate test statistic. (Use 4 decimal places in your answer)

$$t_{\rm TS} = \frac{\overline{x}_{\rm D}}{s_{\rm D}/\sqrt{n}} = \frac{2.38877}{4.468147/\sqrt{4}} = 1.069244$$

d) Indicate which of the night options below is **most likely** to be the correct R code for directly computing the appropriate p-value for the hypothesis test?

Let **TS** denote the assumed correctly computed test statistic value you computed above.

e) Assume that the following interval and bounds are computed correctly using the data and at a **confidence level** of **0.98**.

Choose the appropriate confidence bound/interval for this situation.

- **B** 98 percent confidence interval: -10.16761 Inf
- f) Select an appropriate interpretation of your confidence interval or bound.

- I am 98% confident that the true mean difference between Al-enhanced instruction and traditional lecture-based instruction is greater than -10.16761.
- g) Based **solely** on the **appropriate confidence interval/bound** that you selected above, what is the **most appropriate conclusion** for the **hypothesis test** from the choices below.
 - **Do not reject the null hypothesis.** Since the constructed 98% confidence interval or bound is complementary to the hypothesis test (with $\alpha + C = 1$), is in the direction of the alternative hypothesis, and contains 0, we would not reject the null hypothesis and therefore we do not have sufficient evidence to suggest that the AI-enhanced instruction has a positive impact on learning outcomes in comparison to traditional based instruction.

Suppose the **heights** of **adult oak trees** in a large forest follow a **slightly positively skewed distribution** with an **average height** of **60 feet** and a **standard deviation** of **8 feet**. A researcher randomly selects a **sample** of **36 adult oak trees** from this **population**.

a) What is the distribution of the mean heights for random samples of 36 adult oak trees? Clearly specify the name of the distribution and its parameter(s).

Let T denote the height of adult oak trees in this large forest and \overline{T} denote the random variable measuring the average height of a random sample of 36 adult oak trees in this large forest.

$$\overline{T} \sim N \left(\mu_{\overline{T}} = 60, \sigma_{\overline{T}} = \frac{8}{\sqrt{36}} = \frac{4}{3} = 1.3333 \right)$$

b) Given that the **mean height** of the **36 adult oak trees** is known to be **at least 59 feet**, what is the **probability** that the **mean height** is **more than 62 feet**?

Clearly set up the probability to be calculated and show the mathematical steps required to obtain the probability.

pnorm(-0.75, lower.tail = TRUE)	pnorm(-0.75, lower.tail = FALSE)
0.2266274	0.7733726
pnorm(-0.125, lower.tail = FALSE)	pnorm(-0.125, lower.tail = FALSE)
0.4502618	0.5497382
pnorm(0.25, lower.tail = TRUE)	pnorm(0.25, lower.tail = FALSE)
0.5987063	0.4012937
pnorm(1.5, lower.tail = TRUE)	pnorm(1.5, lower.tail = FALSE)
0.9331928	0.0668072

$$P(\overline{T} > 62 | \overline{T} \ge 59) = \frac{P(\overline{T} > 62)}{P(\overline{T} \ge 59)} = \frac{P(Z > \frac{62 - 60}{4/3})}{P(Z > \frac{59 - 60}{4/3})}$$
$$= \frac{P(Z > 1.5)}{P(Z > -0.75)} = \frac{0.0668072}{0.7733726} = 0.0864$$

c) What is the **mean height value** that **separates** the **top 1%** of the mean height of a sample of 36 adult oak trees? Show your work.

You may use the following R output in your calculations.

qnorm(0.01/2, lower.tail = FALSE) 2.575829	qnorm(0.01, lower.tail = FALSE) 2.326348
gnorm(0.05/2, lower.tail = FALSE)	gnorm(0.05, lower.tail = FALSE)
1.959964	1.644854

Top 1% standard normal quantile →

qnorm(0.01, lower.tail = FALSE)

$$z^* = 2.326348$$

Move to the sampling distribution for the sample mean of adult oak tree heights for samples of size 36.

$$\bar{t} = \mu_{\bar{T}} + z^* \sigma_{\bar{T}} = 60 + 2.326348 \times \frac{4}{3} = 63.1018$$

Suppose the **diameters** of **adult pine trees** in a large forest follow a **slightly positively skewed distribution** with an **average diameter** of **30 inches** and a **standard deviation** of **5 inches**. A researcher randomly selects a sample of **64 adult pine trees** from this **population**.

a) What is the **distribution** of the **average diameter** of a **random sample** of **64 adult pine trees**? Clearly specify the **name** of the **distribution** and its **parameter(s)**.

Let T denote the diameter of adult pine trees in this large forest and \overline{T} denote the random variable measuring the average diameter of a random sample of 64 adult pine trees in this large forest.

$$\overline{T} \sim N \left(\mu_{\overline{T}} = 30, \sigma_{\overline{T}} = \frac{5}{\sqrt{64}} = \frac{5}{8} = 0.625 \right)$$

b) Given that the **mean diameter** of the **64 adult pine trees** is known to be **at most 31 inches**, what is the probability that the **mean diameter** is **less than 28 inches**?

Clearly set up the probability to be calculated and show the mathematical steps required to obtain the probability.

pnorm(-3.2, lower.tail = TRUE)	pnorm(-3.2, lower.tail = FALSE)
0.0006871379	0.9993129
pnorm(-0.4, lower.tail = FALSE)	pnorm(-0.4, lower.tail = FALSE)
0.3445783	0.6554217
pnorm(0.2, lower.tail = TRUE)	pnorm(0.2, lower.tail = FALSE)
0.5792597	0.4207403
pnorm(1.6, lower.tail = TRUE)	pnorm(1.6, lower.tail = FALSE)
0.9452007	0.05479929

$$P(\overline{T} < 28 | \overline{T} \le 31) = \frac{P(\overline{T} < 28)}{P(\overline{T} \le 31)} = \frac{P\left(Z < \frac{28 - 30}{5/8}\right)}{P\left(Z < \frac{31 - 30}{5/8}\right)}$$

$$=\frac{P(Z<-3.2)}{P(Z<1.6)}=\frac{0.0006871379}{0.9452007}=0.0007$$

c) What is the mean diameter value that separates the top 5% of the mean diameters of a sample of 64 adult pine trees? Show your work.

You may use the following R output in your calculations.

qnorm(0.01/2, lower.tail = FALSE)	qnorm(0.01, lower.tail = FALSE)
2.575829	2.326348
qnorm(0.05/2, lower.tail = FALSE)	qnorm(0.05, lower.tail = FALSE)
1.959964	1.644854

Top 5% standard normal quantile →

qnorm(0.05, lower.tail = FALSE)

$$z^* = 1.644854$$

Move to the sampling distribution for the sample mean of adult pine tree diameters for samples of size 64.

$$\bar{t} = \mu_{\overline{1}} + z^* \sigma_{\overline{1}} = 30 + 1.644854 \times \frac{5}{8} = 31.028$$

Suppose the wingspan of adult eagles in a national park follow a slightly positively skewed distribution with an average wingspan of 7 feet and a standard deviation of 3.5 feet. A researcher randomly selects a sample of 49 adult eagles from this population.

a) What is the distribution of the mean wingspans of a random sample of 49 adult eagles? Clearly specify the name of the distribution and its parameter(s).

Let W denote the wingspan of adult eagles in this national park and \overline{W} denote the random variable measuring the average wingspan of a random sample of 49 adult pine trees in this large forest.

$$\overline{W} \sim N\left(\mu_{\overline{W}} = 7, \sigma_{\overline{W}} = \frac{3.5}{\sqrt{49}} = \frac{3.5}{7} = 0.5\right)$$

d) Given that the mean wingspan of the 49 adult eagles is known to be at least 6.625 feet, what is the probability that the mean wingspan is more than 7.75 feet?

Clearly set up the probability to be calculated and show the mathematical steps required to obtain the probability.

pnorm(-0.75, lower.tail = TRUE)	pnorm(-0.75, lower.tail = FALSE)
0.2266274	0.7733726
pnorm(-0.11, lower.tail = FALSE)	pnorm(-0.11, lower.tail = FALSE)
0.4562047	0.5437953
pnorm(0.21, lower.tail = TRUE)	pnorm(0.21, lower.tail = FALSE)
0.5831662	0.4168338
pnorm(1.5, lower.tail = TRUE)	pnorm(1.5, lower.tail = FALSE)
0.9331928	0.0668072

$$P(\overline{W} > 7.75 | \overline{W} \ge 6.625) = \frac{P(\overline{W} > 7.75)}{P(\overline{W} \ge 6.625)} = \frac{P\left(Z < \frac{7.75 - 7}{1/2}\right)}{P\left(Z < \frac{6.625 - 7}{1/2}\right)}$$

$$=\frac{P(Z>1.5)}{P(Z>-0.75)}=\frac{0.0668072}{0.7733726}=0.0864$$

b) What is the **mean wingspan value** that separates the **top 5%** of the **mean wingspans** of a **sample** of **49 adult eagles**? Show your work.

You may use the following R output in your calculations.

qnorm(0.01/2, lower.tail = FALSE) 2.575829	qnorm(0.01, lower.tail = FALSE) 2.326348
qnorm(0.05/2, lower.tail = FALSE)	qnorm(0.05, lower.tail = FALSE)
1.959964	1.644854

Top 5% standard normal quantile →

qnorm(0.05, lower.tail = FALSE)

$$z^* = 1.644854$$

Move to the sampling distribution for the sample mean of adult wingspans for samples of size 49.

$$\overline{\mathbf{w}} = \mu_{\overline{\mathbf{W}}} + z^* \sigma_{\overline{\mathbf{W}}} = 7 + 1.644854 \times \frac{1}{2} = 7.8225$$

Suppose the **lengths** of **adult salmon** in a river follow a **slightly positively skewed distribution** with an **average length** of **28 inches** and a **standard deviation of 5 inches**. A researcher randomly selects a **sample** of **64 adult salmon** from this population.

a) What is the distribution of the mean lengths of a random sample of 64 adult salmon? Clearly specify the name of the distribution and its parameter(s).

Let S denote the length of adult salmon in this river and \overline{S} denote the random variable measuring the average length of a random sample of 64 adult salmon in this large river.

$$\bar{S} \sim N\left(\mu_{\bar{S}} = 28, \sigma_{\bar{S}} = \frac{5}{\sqrt{64}} = \frac{5}{8} = 0.625\right)$$

b) Given that the mean length of the 64 adult salmon is known to be at most 29 inches, what is the probability that the mean length is less than 26 inches?

Clearly set up the probability to be calculated and show the mathematical steps required to obtain the probability.

pnorm(-3.2, lower.tail = TRUE)	pnorm(-3.2, lower.tail = FALSE)
0.0006871379	0.9993129
pnorm(-0.4, lower.tail = FALSE)	pnorm(-0.4, lower.tail = FALSE)
0.3445783	0.6554217
pnorm(0.2, lower.tail = TRUE)	pnorm(0.2, lower.tail = FALSE)
0.5792597	0.4207403
pnorm(1.6, lower.tail = TRUE)	pnorm(1.6, lower.tail = FALSE)
0.9452007	0.05479929

$$P(\overline{S} < 26|\overline{S} \le 29) = \frac{P(\overline{S} < 26)}{P(\overline{S} \le 29)} = \frac{P(Z < \frac{26 - 28}{5/8})}{P(Z < \frac{29 - 28}{5/8})}$$
$$= \frac{P(Z < -3.2)}{P(Z < 1.6)} = \frac{0.0006871379}{0.9452007} = 0.0007$$

c) What is the **mean length value** that separates **the top 1%** of the **mean lengths** of a **sample** of **64 adult salmon**? Show your work.

You may use the following R output in your calculations.

qnorm(0.01/2, lower.tail = FALSE)	qnorm(0.01, lower.tail = FALSE)
2.575829	2.326348
qnorm(0.05/2, lower.tail = FALSE)	qnorm(0.05, lower.tail = FALSE)
1.959964	1.644854

Top 1% standard normal quantile →

qnorm(0.01, lower.tail = FALSE)

$$z^* = 2.326348$$

Move to the sampling distribution for the sample mean of adult salmon for samples of size 64.

$$\bar{s} = \mu_{\bar{S}} + z^* \sigma_{\bar{S}} = 28 + 2.326348 \times \frac{5}{8} = 29.454$$