

Problem Set # 8

Joshua Petitma

10/05/2020

1

1.a $\sum_{k=1}^{\infty} \frac{(-1)^k}{k \ln(k)}$

$$\lim_{k \rightarrow \infty} \frac{1}{k \ln(k)} = 0$$

$S_n < S_{n+1} \therefore \text{Converges}$

$$\frac{1}{k \ln(k)} < \frac{1}{k}$$

$$\frac{k}{1} * \frac{1}{k \ln(k)} = \frac{1}{\ln(k)}$$

$$\lim_{k \rightarrow \infty} \frac{1}{\ln(k)} = 0 \therefore \text{Divergent because of LCT}$$

Converges Conditionally

1.b $\sum_{k=1}^{\infty} \left(\frac{-4}{5}\right)^k$

$$\frac{-4}{5} * \frac{1}{1 + \frac{4}{5}}$$

$$\frac{4}{5 + 4}$$

$$\frac{4}{9}$$

Converges Absolutely

$$\mathbf{1.c} \quad \sum_{k=1}^{\infty} \frac{(-4)^k}{k^2}$$

$$\lim_{k \rightarrow \infty} \frac{(-4)^k}{k^2} \neq 0 \therefore \textit{Divergent}$$

$$\mathbf{1.d} \quad \sum_{k=1}^{\infty} \frac{2+(-1)^k}{k^2}$$

$$\lim_{k \rightarrow \infty} \frac{2+1}{k^2}$$

$$\frac{3}{k^2} \quad 2 > 1 \therefore \text{Convergent because of p-series}$$