

ECS730

Revision Lecture

Topics

- Week 1: Mixing Consoles, Software Mixers
- Week 2: Fundamentals, Delay, Vibrato
- Week 3: Flanging, Chorus
- Week 4: Filters, Tone Controls, Graphic EQ
- Week 5: Parametric EQ, Wah-Wah, Phasers
- Week 6: Distortion, Ring Modulation
- Week 8: Compression, Expansion
- Week 9: Reverb, Phase Vocoder
- Week 10: Spatial Audio

Mixing consoles

- What is a mixing console?
 - ▶ Electronic device for **combining**, **routing**, and **modifying** audio signals (including level, tone and dynamics)
 - ▶ Analogue or digital signals, depending on type
 - ▶ Modified signals are summed to produce output
- Three main functions:
 - ▶ **Summing**: combining audio signals
 - Many channels can be summed to stereo (or mono) via mix bus
 - ▶ **Processing**: modifying audio signal properties
 - Consoles often have on-board equalisers and sometimes dynamics processors
 - ▶ **Routing**: grouping, sending and receiving signals
 - Enable use of external processors and effects
 - Insert points, auxiliary sends and receives

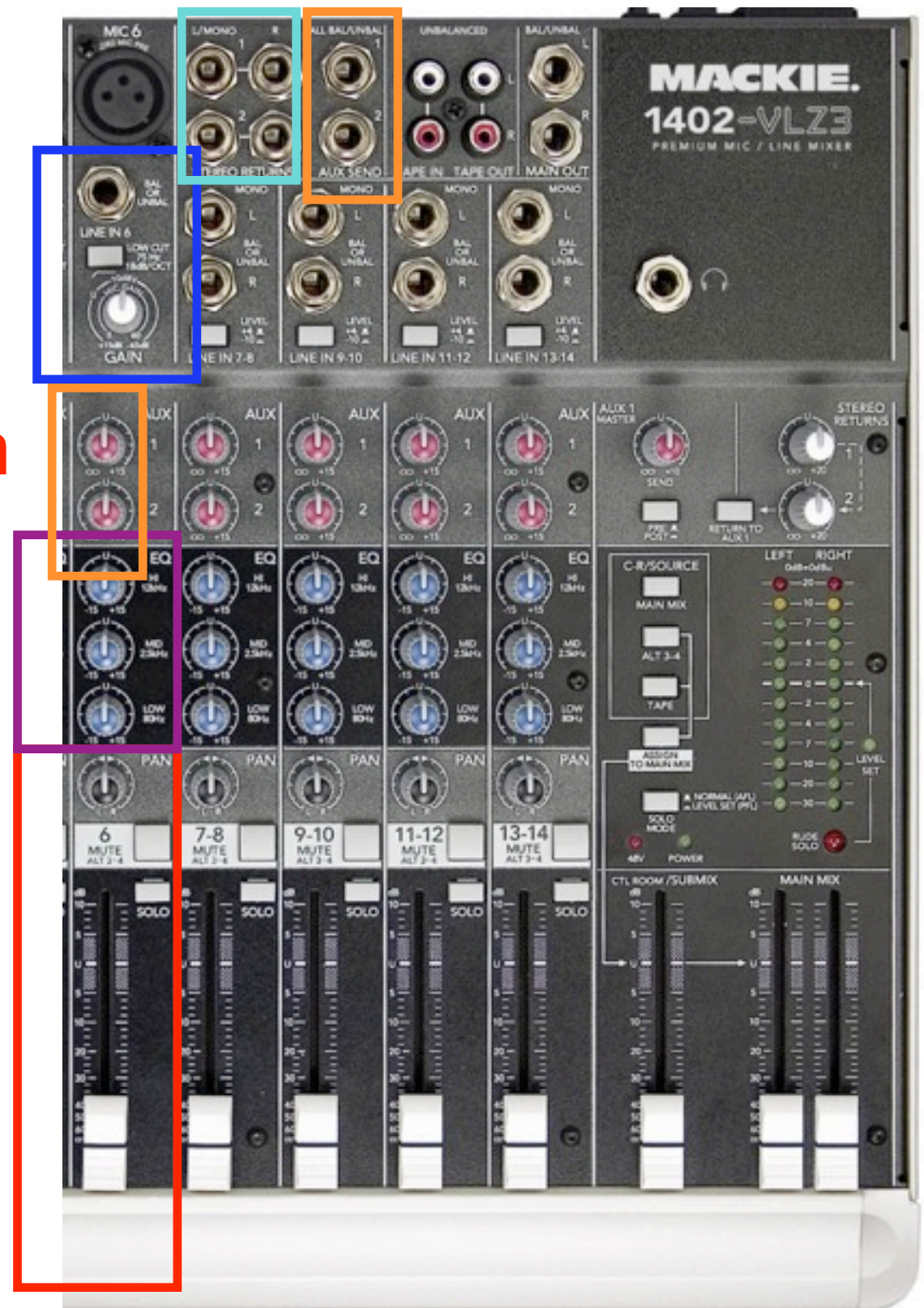
Mixing consoles

- A mixing console has two main sections:
 - ▶ **Channel** section
 - Collection of channels organised in physical **strips**
 - Each channel can correspond to an individual **track** on a multitrack recorder
 - Most channels support **mono** input; some support **stereo**
 - Some channels will have different types of equalisation, etc.
 - ▶ **Master** section
 - Central control over console (global functionality)
 - Includes master **aux sends**, **effect returns**, control room level, ...
- Other terms to know
 - ▶ **buss**, **group**, **effect** vs. **processor**
 - ▶ **tracks**, **mixer strips** (software mixers)

Signal flow in a mixing console

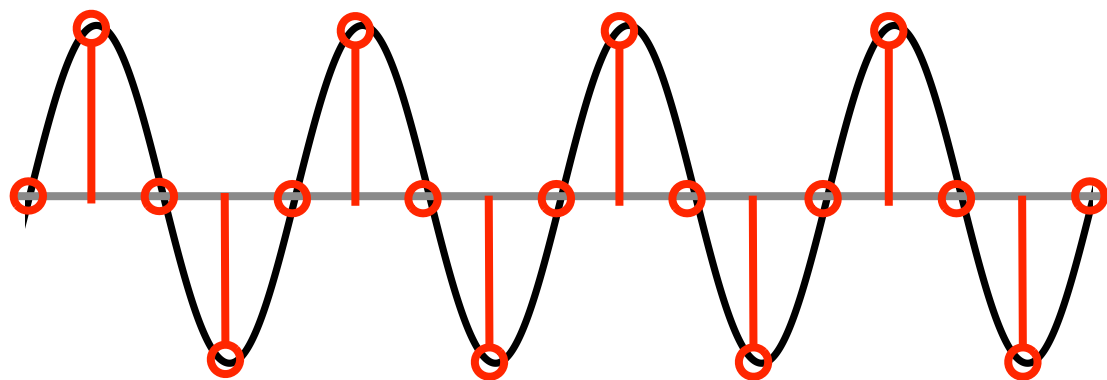
- Components

- ▶ Faders, pan pots & cut switch
- ▶ Line gains, phase invert & clip indicators
- ▶ On-board processors
- ▶ Insertion points (*not shown*)
- ▶ Auxiliary sends
- ▶ FX returns



Sampling

- Discrete **sequences** do not have to represent any continuous or physical quantity
 - ▶ But in the audio world, we often work with **sampled** audio
- **Sampling** = converting continuous time to discrete
- **Reconstruction** = discrete to continuous

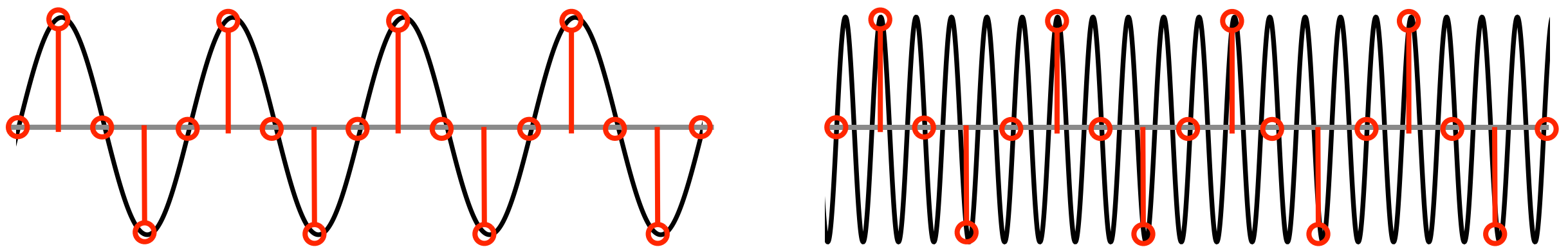


$$x[n] = x_a(nT), \quad -\infty < n < \infty$$

- T is called the **sampling period**
 - ▶ $1/T$ is the **sampling frequency** or **sample rate** (f_s)

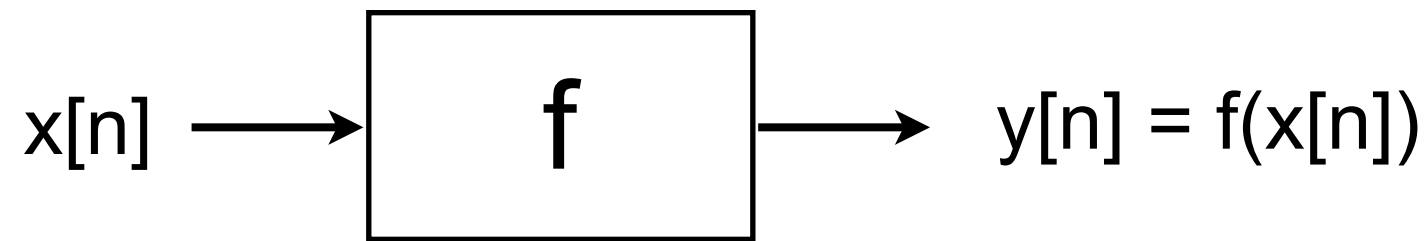
Sampling 2

- Reconstruction is harder than sampling
 - ▶ Sampling inherently loses information
 - ▶ How do we distinguish between these two cases?



- Need a **band-limited** input signal
 - ▶ Limited frequency range
- **Nyquist Sampling Theorem**
 - ▶ Need to sample a signal at twice its **highest frequency** to be able to uniquely reconstruct it
 - ▶ This frequency is called the **Nyquist frequency**

Properties of digital systems

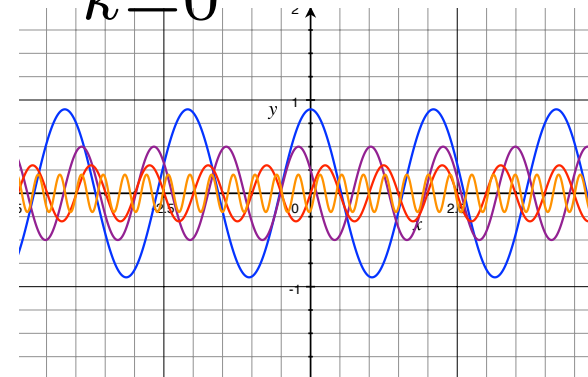
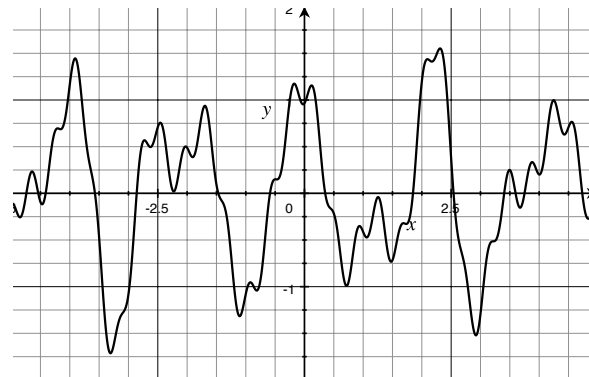


- **Linearity:** $f(x_1[n] + x_2[n]) = y_1[n] + y_2[n]$
- **Time invariance:** $f(x[n - N]) = y[n - N]$
 - ▶ Linear, Time-Invariant (LTI) systems are a common useful case
- **Stability:**
 - ▶ $x[n]$ bounded $\longrightarrow y[n]$ bounded
- **Causality:**
 - ▶ $x[n] = 0$ for $n < 0 \longrightarrow y[n] = 0$ for $n < 0$
 - ▶ f doesn't depend on any future sample (i.e. greater n)
- **Memorylessness:**
 - ▶ $y[n]$ only depends on the current value of $x[n]$

Time and frequency domain

- Any $x[n]$ can be represented as a **sum of sinusoids...**

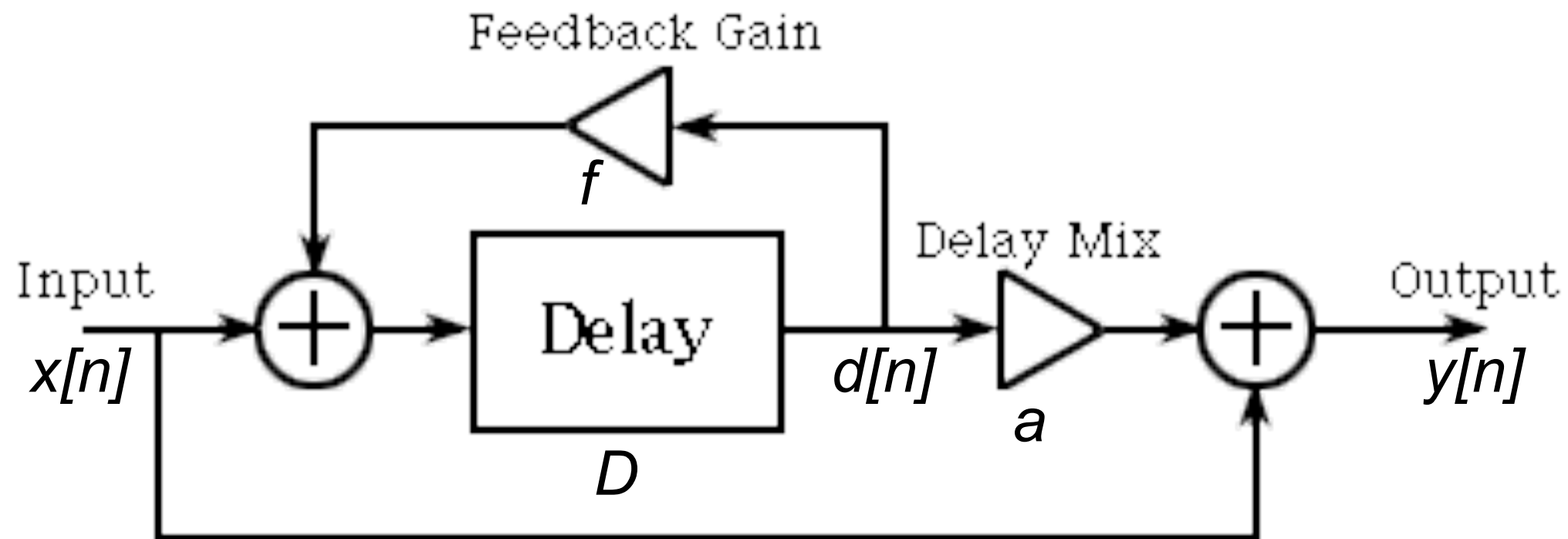
► So let's do that then!

$$x[n] = \frac{1}{N} \sum_{k=0}^{N-1} X_k e^{+j2\pi \frac{k}{N} n}$$


- The second version is called the **frequency domain** representation of x
 - * or at least discrete samples of the frequency domain...
- What **frequencies** are present, with what **amplitude** and what **phase**? From this we can exactly determine $x[n]$.
- Things to know:
 - **z-transform**, relationship to frequency response
 - Converting between time & z-domains

Delay (with feedback)

- Most delays have feedback control (**regeneration**)
 - ▶ Take the delay output, send it back to the input



$$d[n] = x[n - D] + f d[n - D] \quad |f| < 1 \text{ (strictly)}$$

$$y[n] = x[n] + a d[n] \quad |a| \leq 1 \text{ (usually)}$$

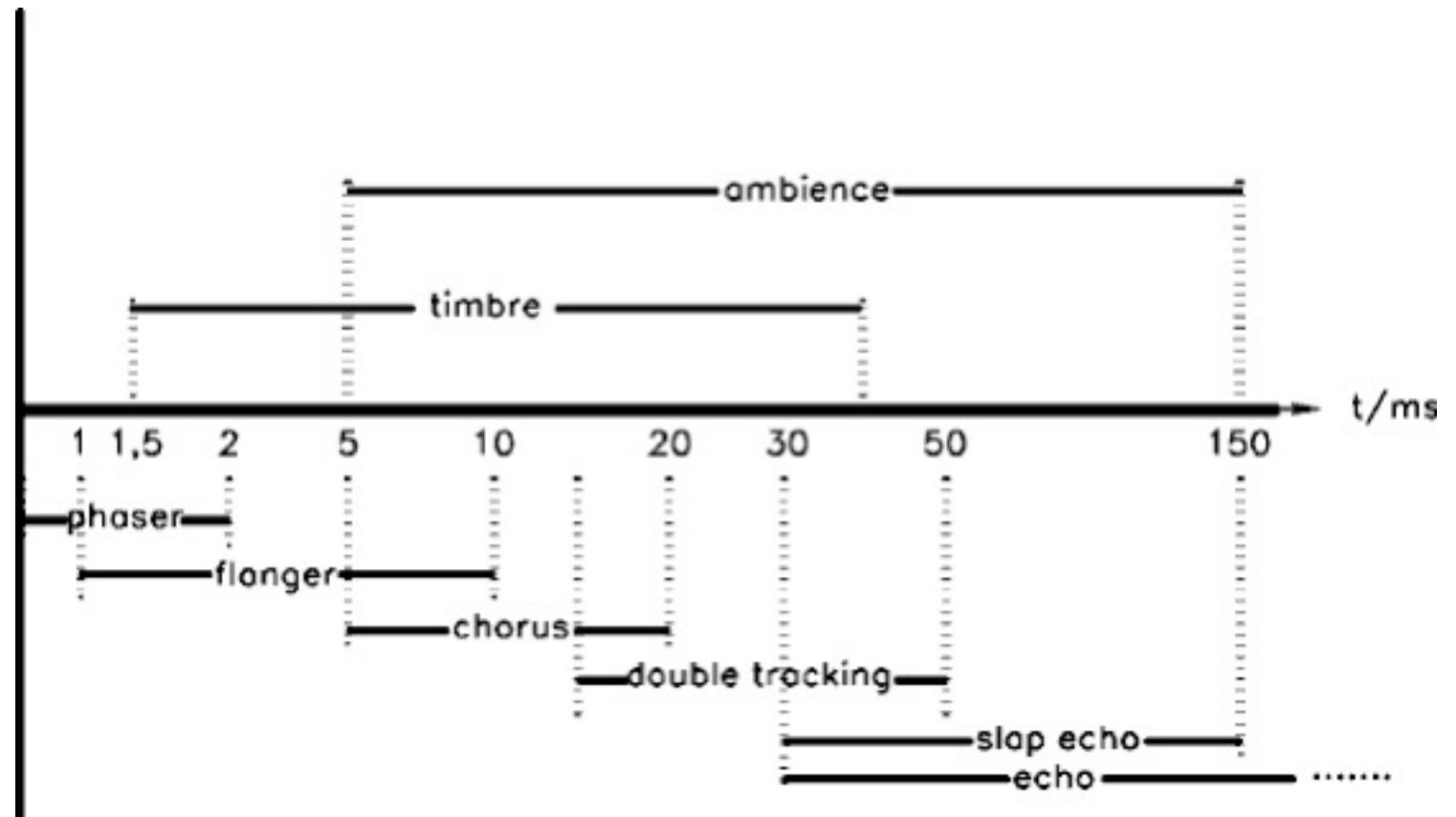
- ▶ To derive $y[n]$ in terms of $x[n]$:

$$y[n - D] = x[n - D] + a d[n - D] \implies d[n] = \frac{f}{a} y[n - D] + \left(1 - \frac{f}{a}\right) x[n - D]$$

$$\implies y[n] = f y[n - D] + x[n] + (a - f) x[n - D]$$

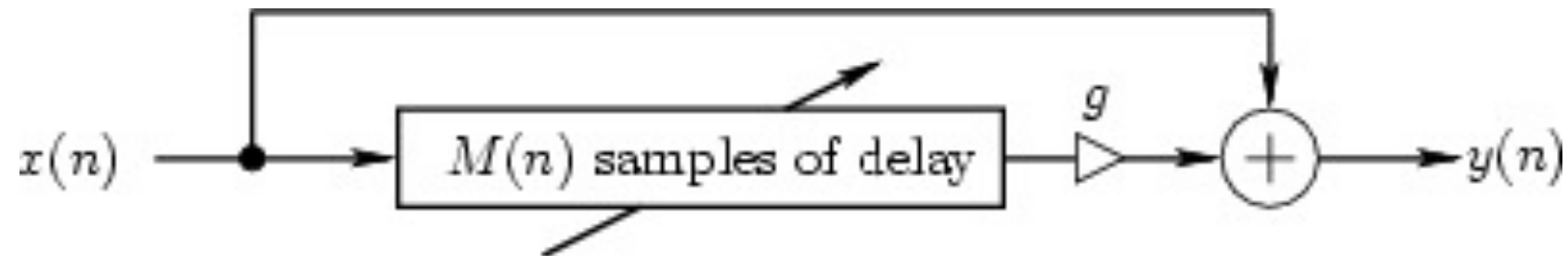
Delay 2

Delay range (ms) (Typ.)	Modulation (Typ.)	Effect name
0 ... 20	-	Resonator
0 ... 15	Sinusoidal	Flanging
10 ... 25	Random	Chorus
25 ... 50	-	Slapback
> 50	-	Echo



- Other things to know:
 - ▶ How to convert between block diagram & transfer function
 - ▶ Variations: [multi-tap](#), [ping-pong](#), etc.
 - ▶ [Fractional delay](#)
 - ▶ Implementation on a [circular buffer](#) (basics, not code)

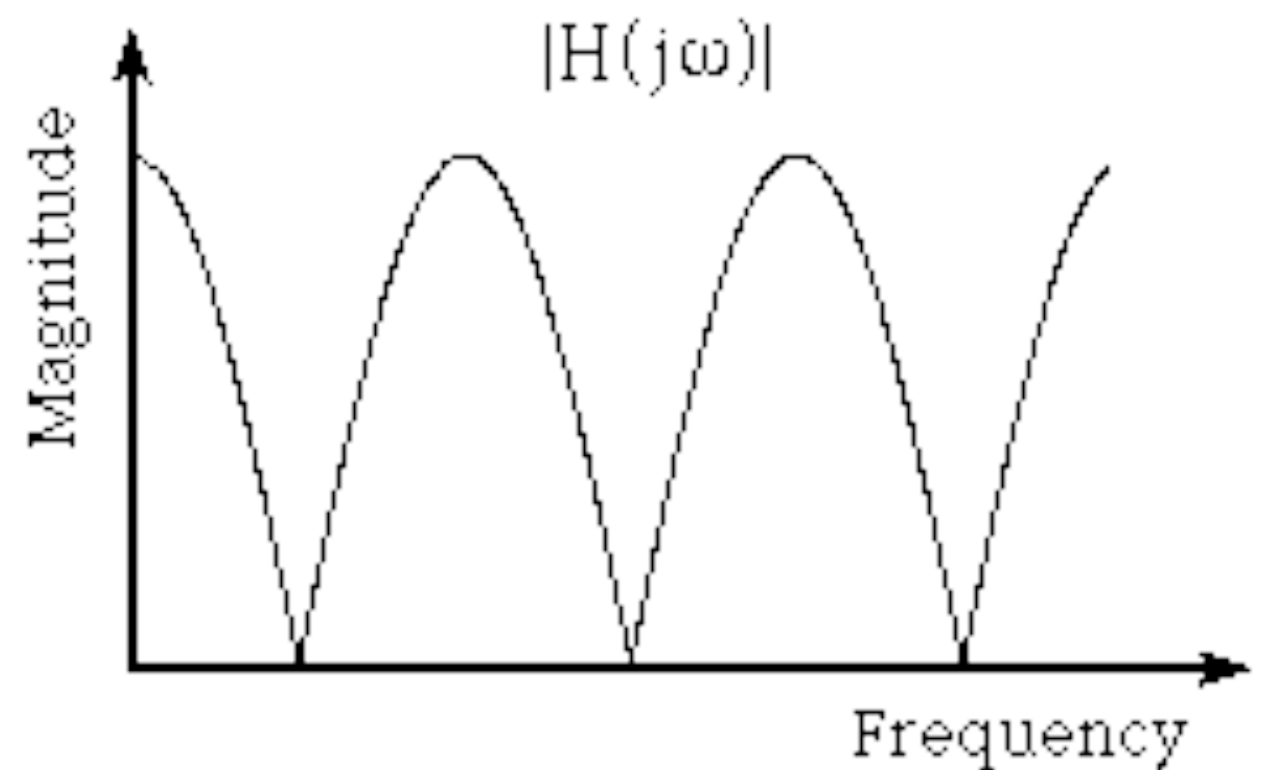
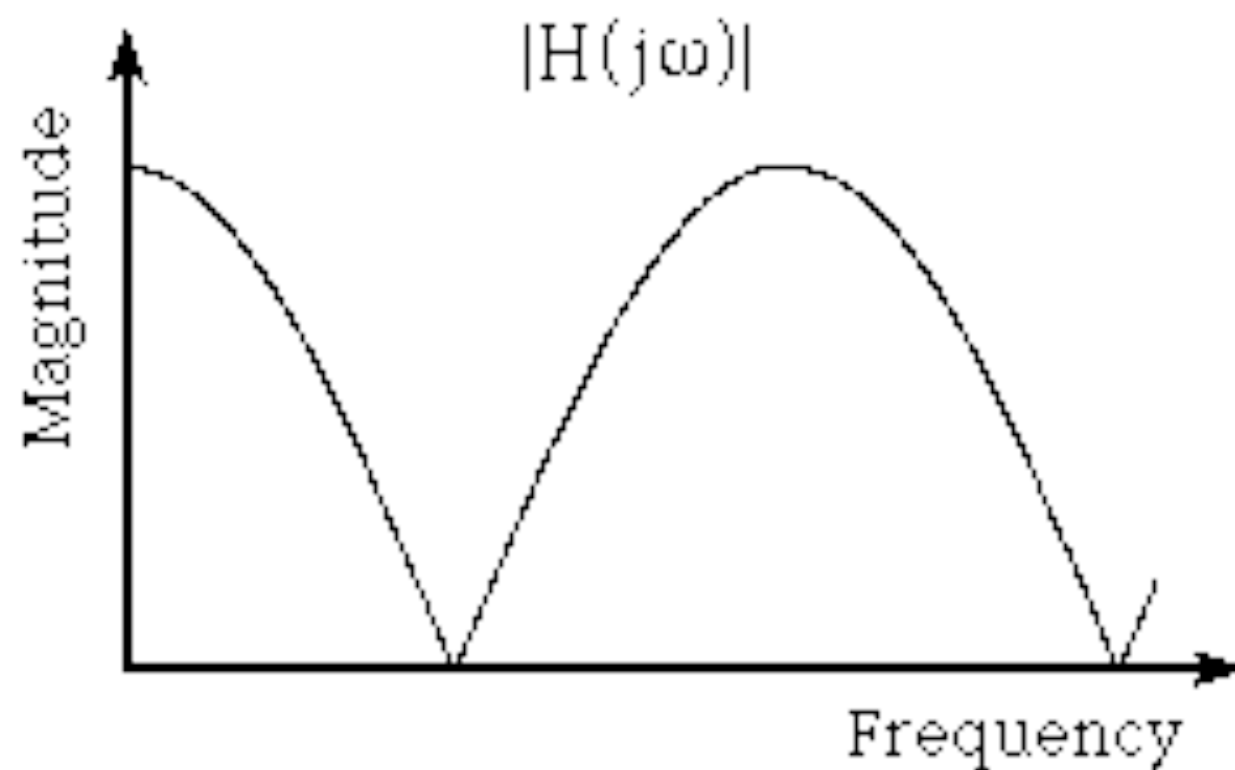
Flanging



- Feedforward comb filter
- Input-output relation: $y[n] = x[n] + gx[n - M(n)]$
 - ▶ $x[n]$ - input signal
 - ▶ $y[n]$ - output signal
 - ▶ g - depth of flanging effect
 - ▶ $M(n)$ - length of delay line at sample n
- $M(n)$ must vary smoothly over time
 - ▶ Interpolated (fractional) delay line allows noninteger M
- How are chorus and vibrato different?
- Also know:
 - ▶ Variations (feedback, stereo, etc.)
 - ▶ Parameters

Flanger frequency response

- Delay & add has **filtering** effect on signal
 - ▶ Creates series of notches in frequency response
 - ▶ Eliminates a periodically spaced set of frequencies
 - ▶ Other frequencies passed with amplitude change
- **Comb filter** (notches resemble teeth on comb)



Frequency response for two flangers with depth 1.
Which one has the smaller delay, and why?

IIR filters (also know FIR)

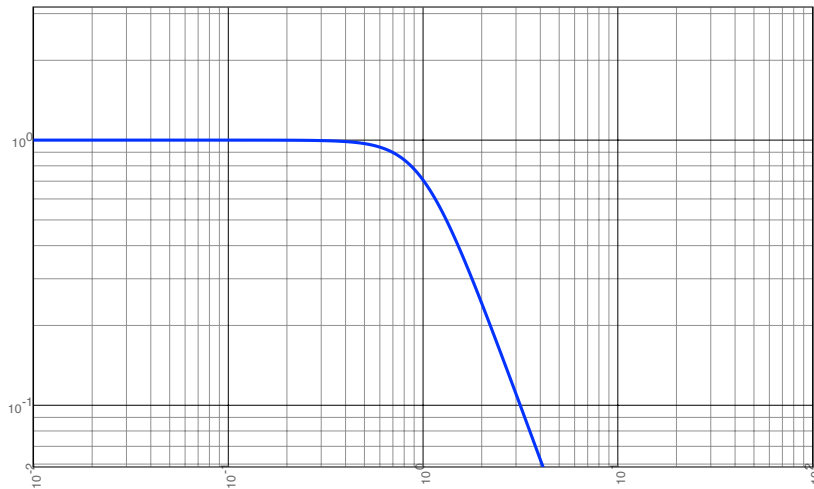
- More general form:

$$y[n] = \sum_{k=1}^N a_k y[n-k] + \sum_{k=0}^M b_k x[n-k]$$

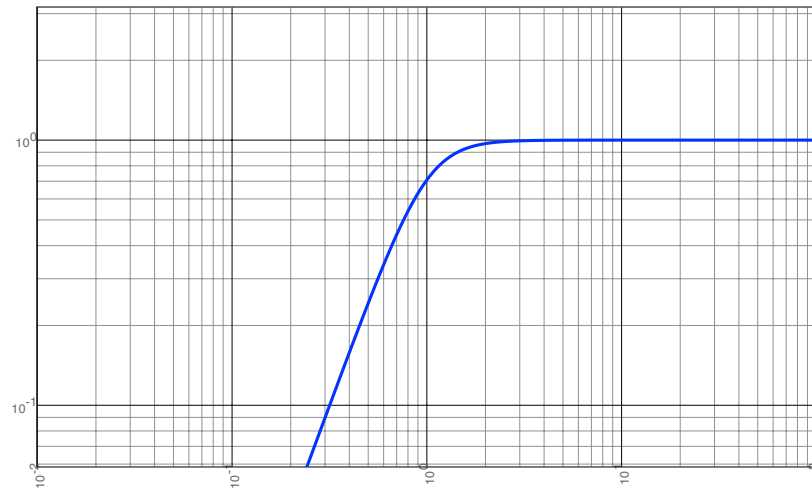
- ▶ Output depends on last M inputs and N outputs
- ▶ **Infinite Impulse Response** (IIR)
 - Unless all $a_k = 0$
- ▶ Often $N = M$ in practice, but this is not required
- ▶ $\max(N, M)$ called **order** of filter
- ▶ Properties of **IIR** filters
 - **Linear**
 - **Time-invariant**
 - **Stability** depends on coefficients a_k
- Most equalisers use IIR filters

Types of filters

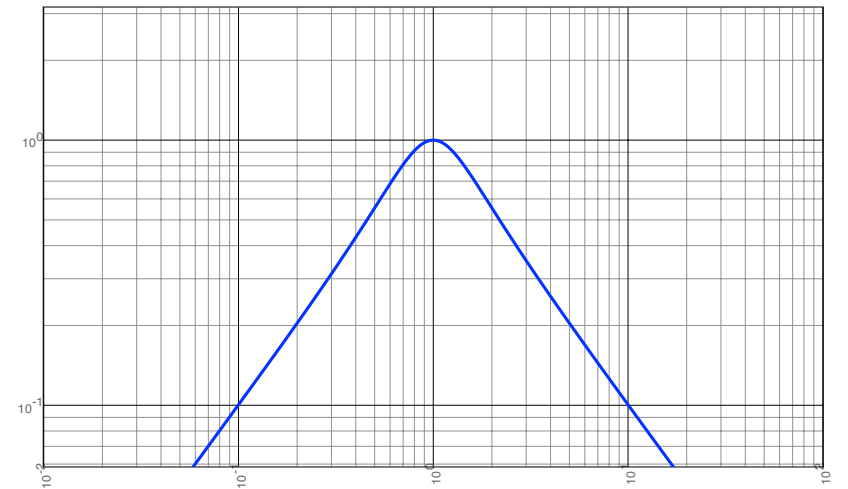
Types we frequently encounter in audio systems:



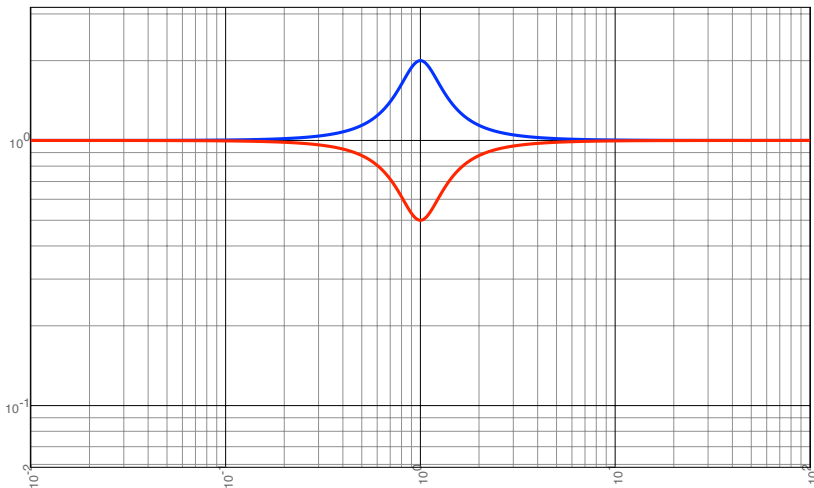
Lowpass



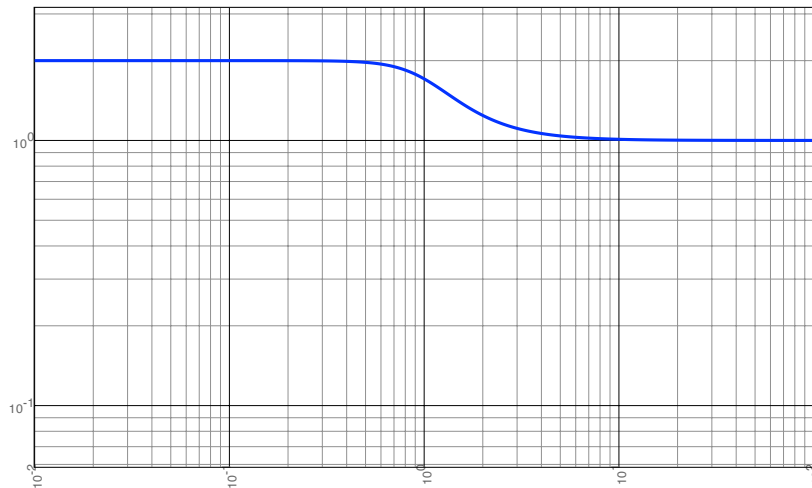
Highpass



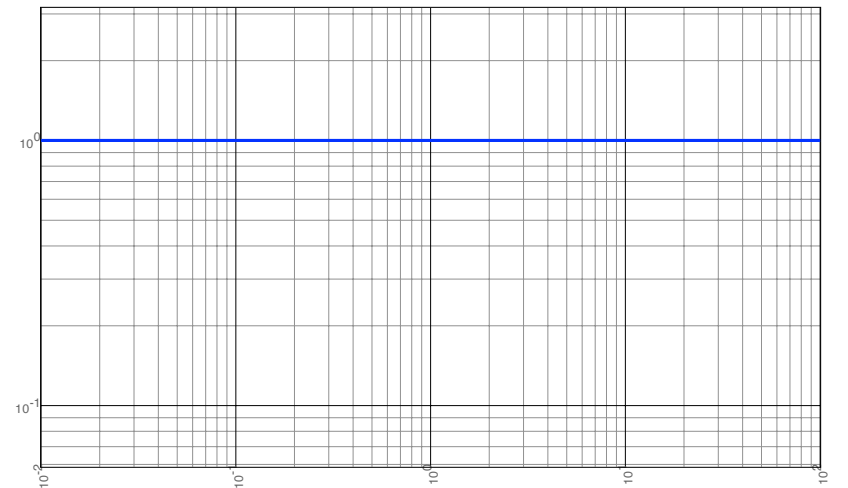
Bandpass



Peaking / Notch



Shelving

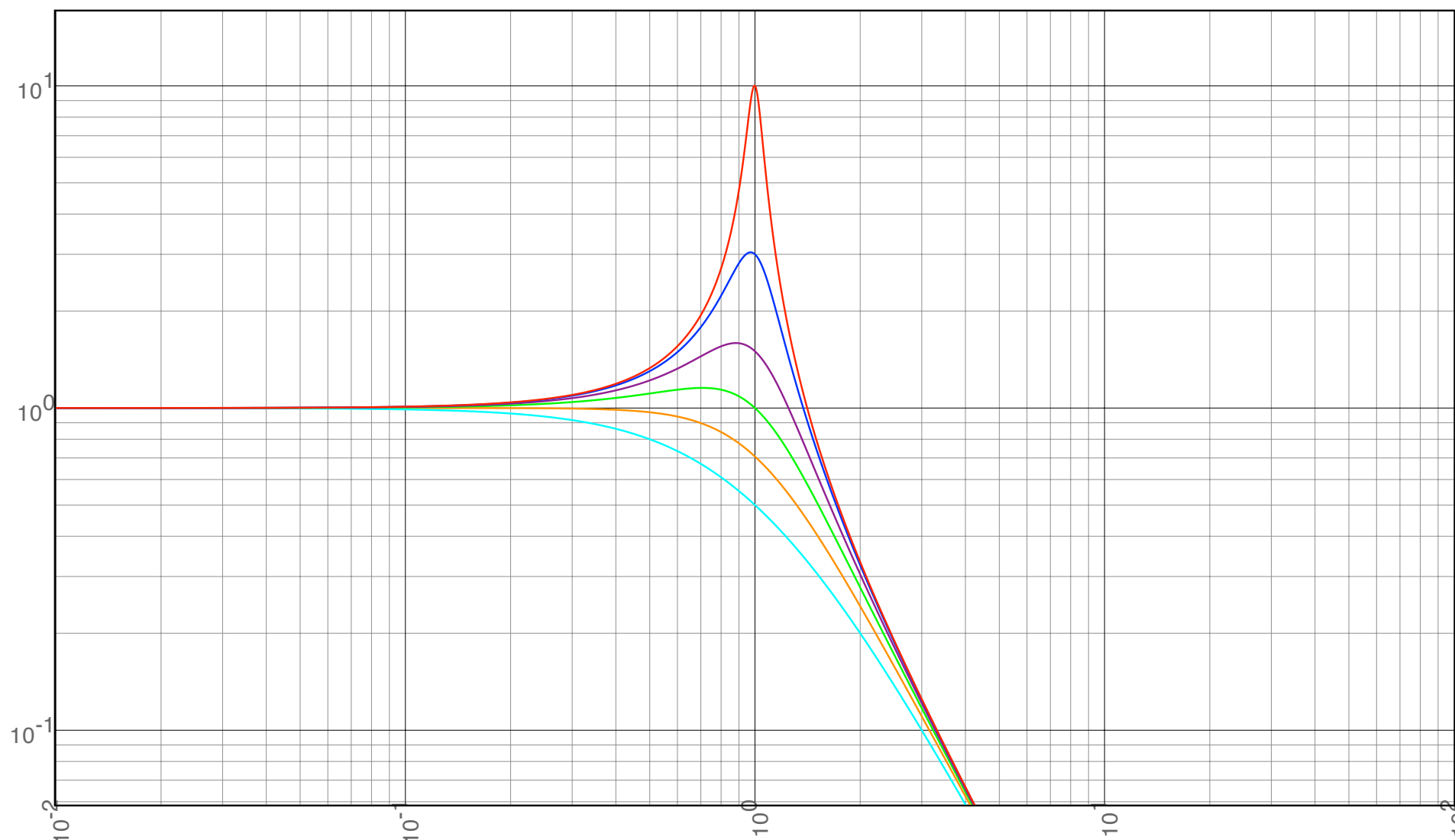


Allpass

Filter Q

- Filters can be described “quality factor” Q
 - ▶ Selectivity (bandwidth) relative to centre frequency

$$Q = \frac{f_0}{\Delta f}$$

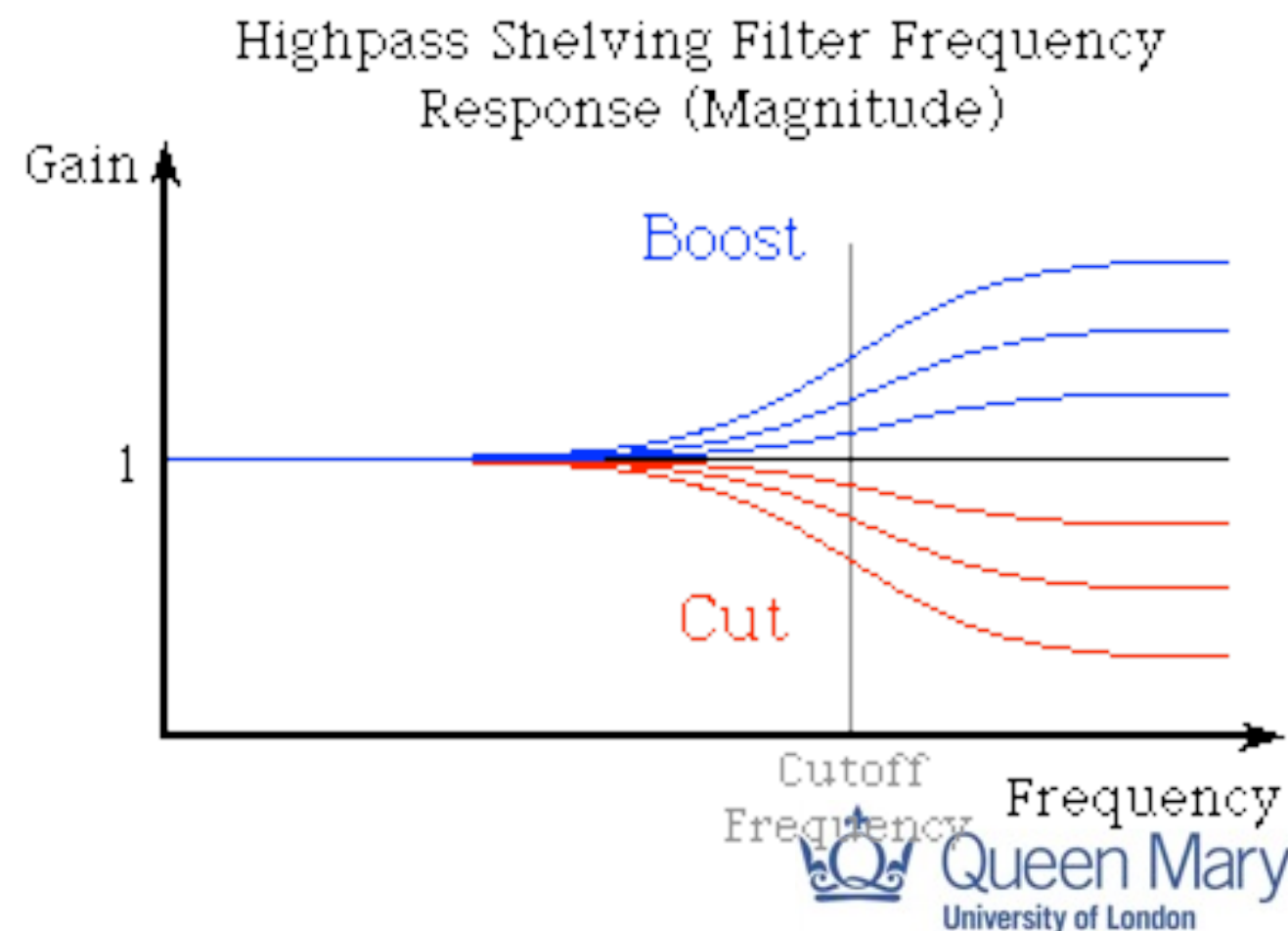
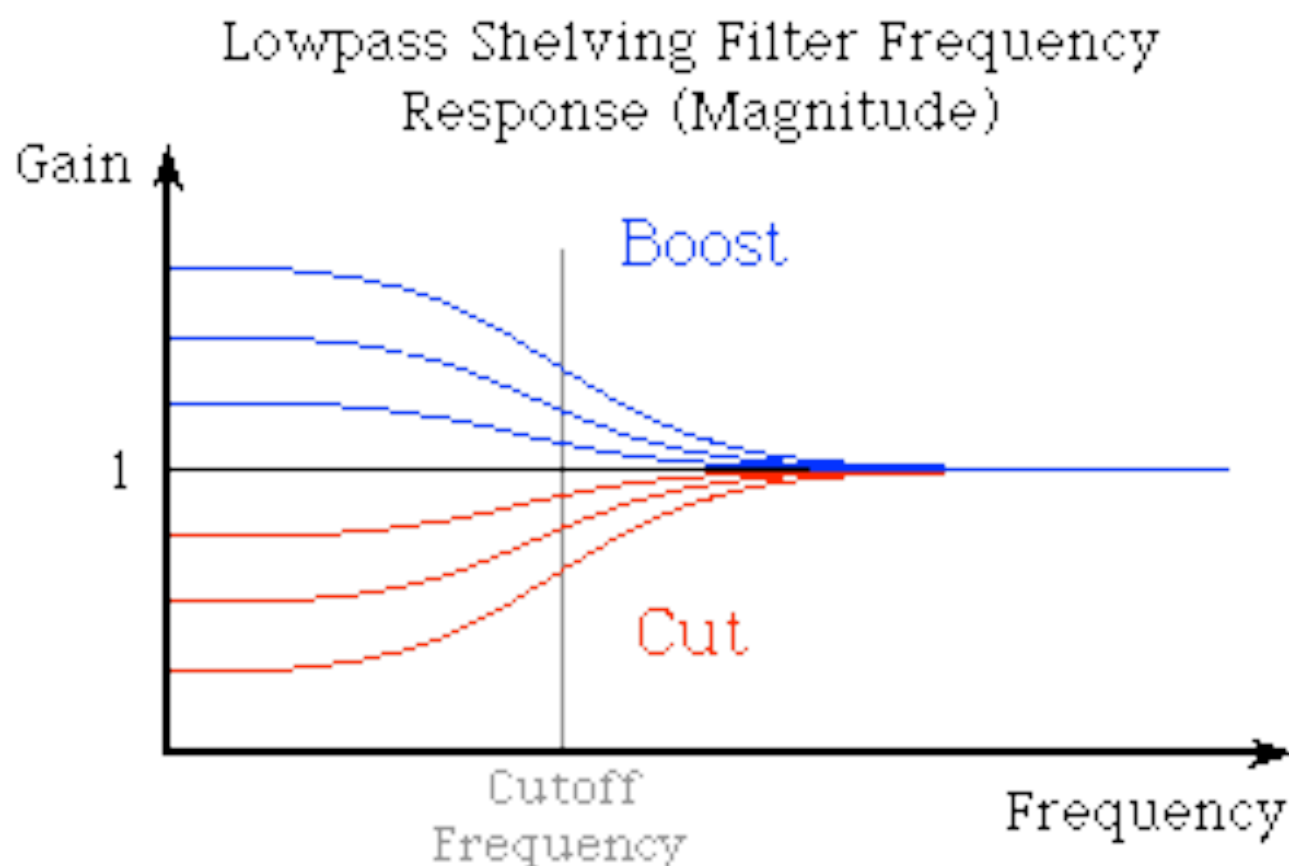


Second order
lowpass filters (all)

$Q = 0.5$
 $Q = 0.71$
 $Q = 1$
 $Q = 1.5$
 $Q = 3$
 $Q = 10$

Tone controls

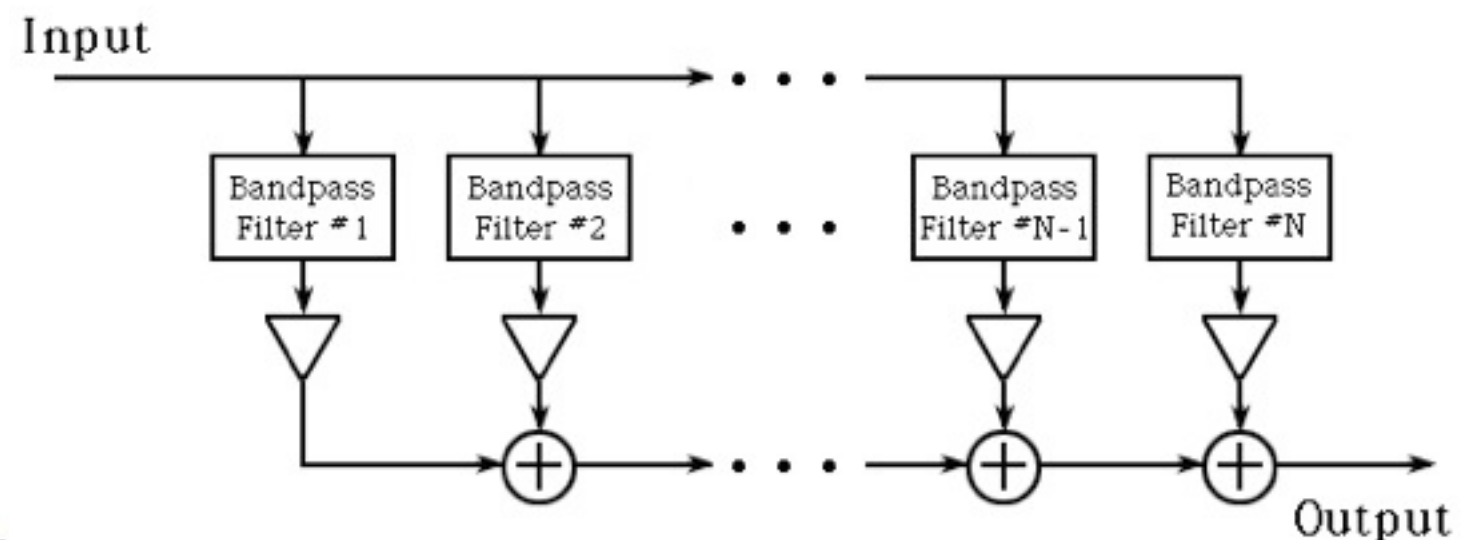
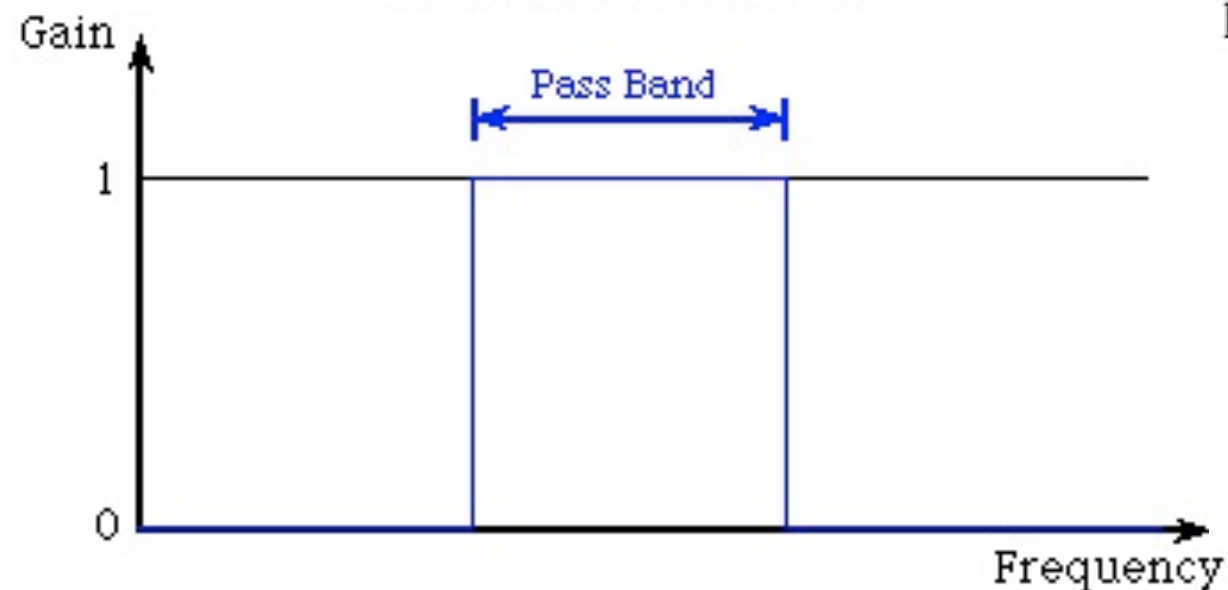
- Most common equalisation is the **tone control**
 - ▶ Controls: **bass** and **treble**
 - ▶ Adjust sound to suit your taste, or the room
 - ▶ Bass control = **lowpass shelving** filter
 - ▶ Treble control = **highpass shelving** filter
 - ▶ Control centred = unity gain = flat response



Graphic EQ (parallel implementation)

- Consider as bank of **bandpass filters**
 - ▶ Completely isolate individual frequency bands
 - ▶ Real bandpass filters have some **ripple** in passband and don't have a perfectly sharp cutoff

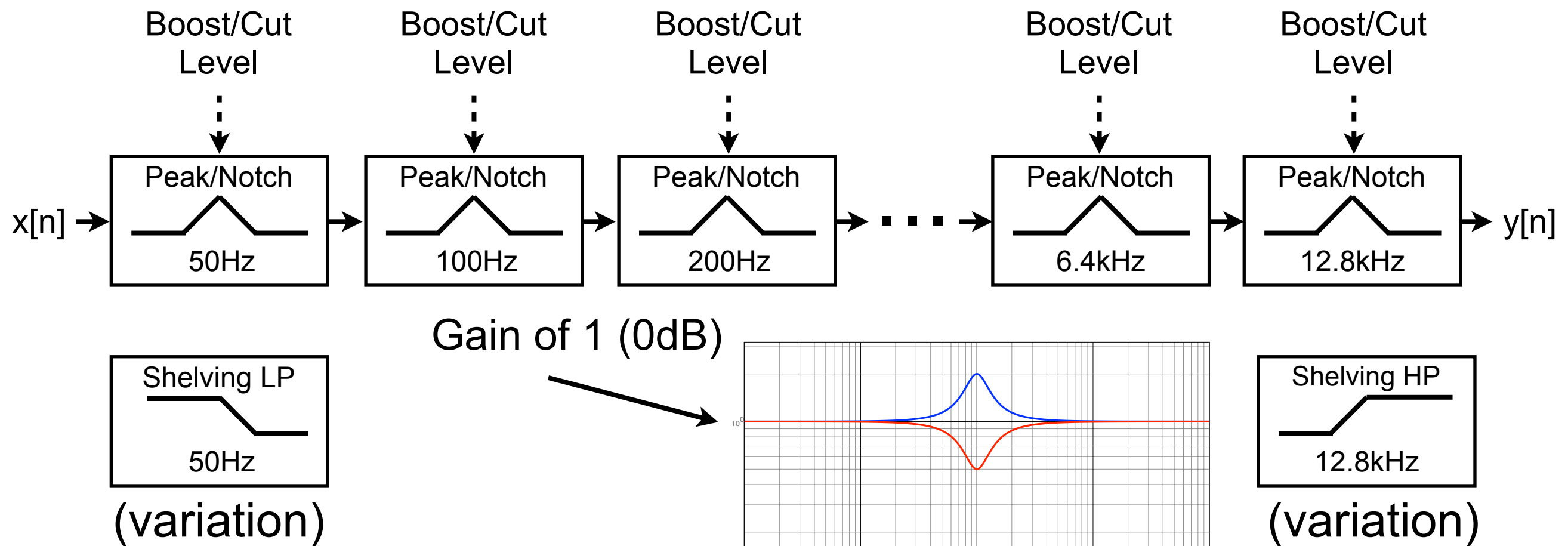
Frequency Response for an Ideal Bandpass Filter



- Arrange filters in **parallel**
 - ▶ Each has the same input
 - ▶ Outputs are summed (mixed) after band **gains** adjusted
 - ▶ Also know: how band frequencies are chosen

Graphic EQ (series implementation)

- Consider cascade of **peaking** or **shelving** filters
 - Add a boost or notch to a specific frequency band
 - Top and bottom bands may be shelving filters which extend to edge of spectrum
 - Each filter has a gain of **1** outside the band

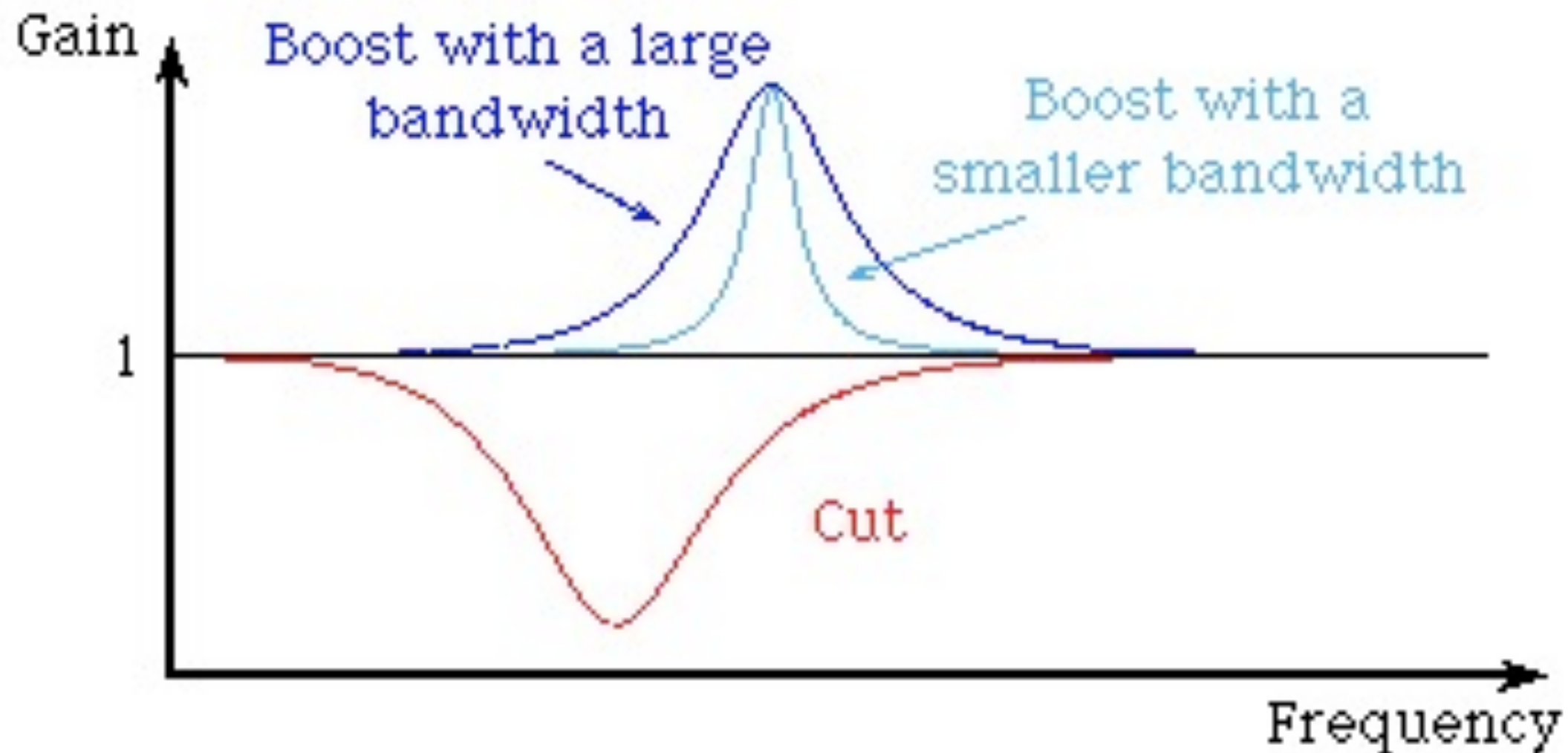


- Arrange filters in **series**
 - Each takes its input from the previous filter

Parametric EQ plots

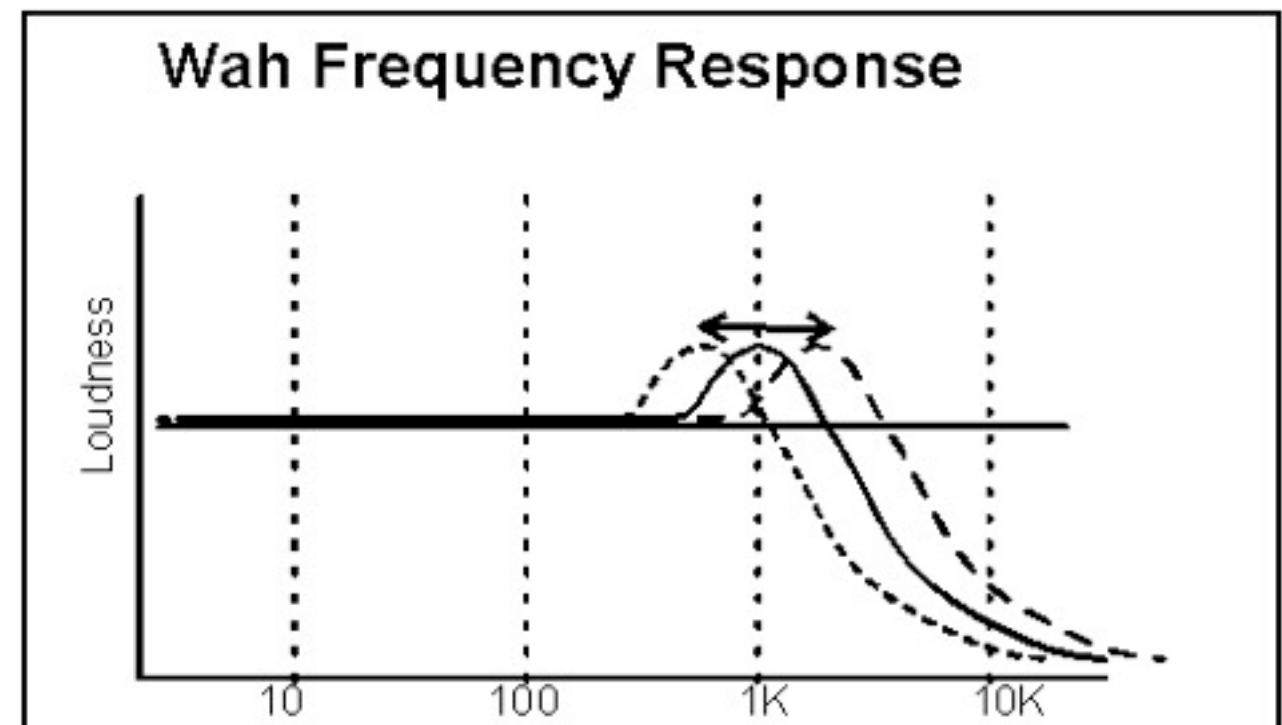
- Controls: **centre frequency**, **gain**, **bandwidth**
 - ▶ These plots for **peaking** filters (not shelving)

Possible Frequency Responses for a
Parametric Equalizer



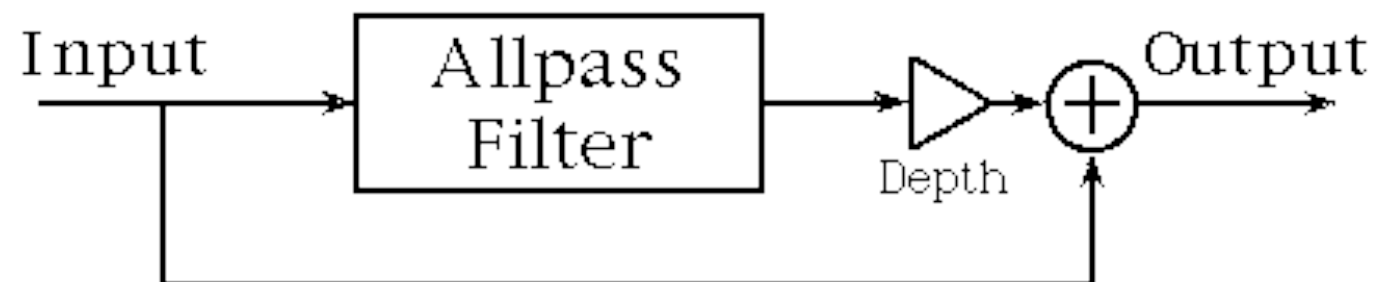
Wah-wah

- Resonant (**bandpass** or **peaking**) filter
 - ▶ Variable centre frequency
 - ▶ **Small bandwidth** (i.e. **high Q**)
- Standard wah-wah
 - ▶ Centre frequency controlled by pedal (manual control)
- **Auto-wah** (2 effects)
 - ▶ Centre frequency controlled by **LFO**
 - ▶ Frequency of LFO usually around 1-2 Hz
 - ▶ **OR**, could depend on **envelope** of input signal
- **Tremolo-wah**: also amplitude variations
- Centre frequency can vary from near 0 to $f_s/2$
 - ▶ In practice, varies across the midrange frequencies only



Phasing

- Notches implemented indirectly by **allpass filters**
 - ▶ Allpass filter passes all frequencies equally
 - ▶ No amplification or attenuation: $|H(\omega)| = 1$
 - ▶ It's all about the **phase**
- Add filtered output to original
 - ▶ Amount of filtered output controlled by *depth* or *mix* control
- **Where do the notches come from?**



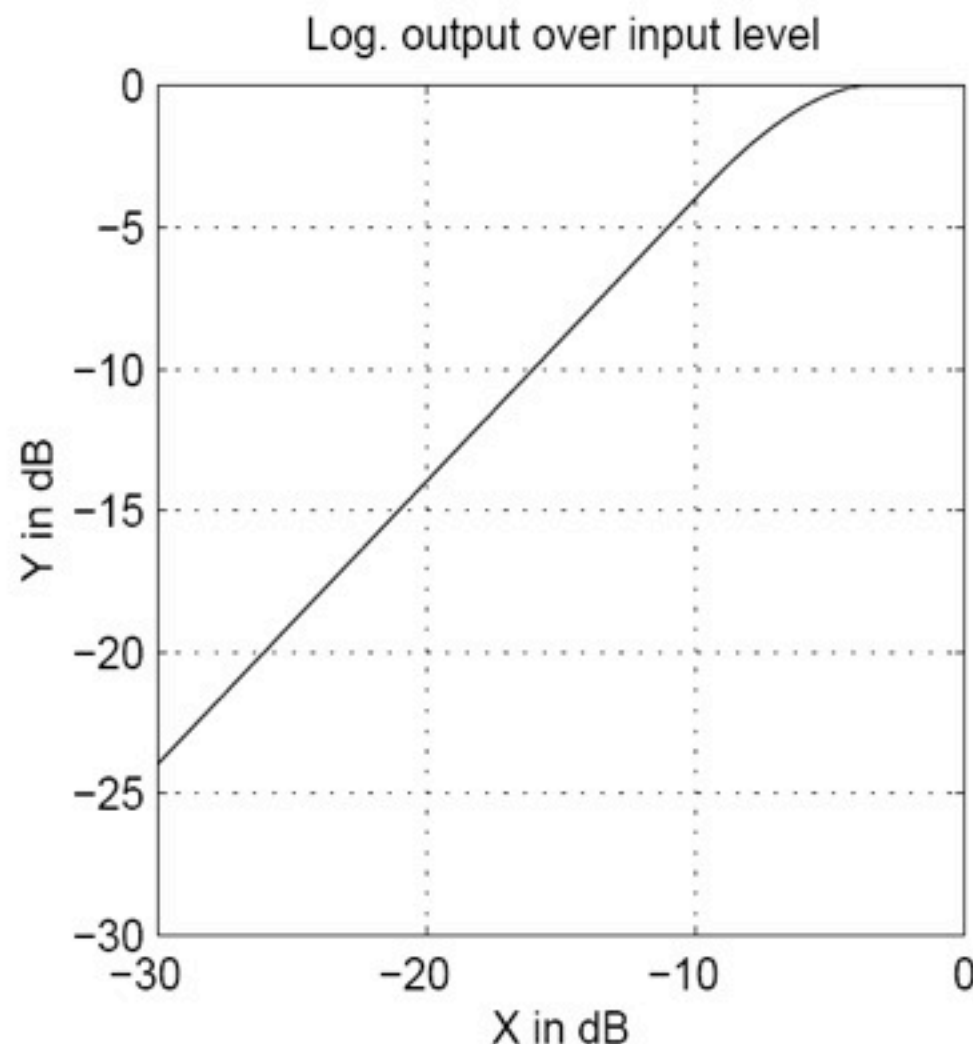
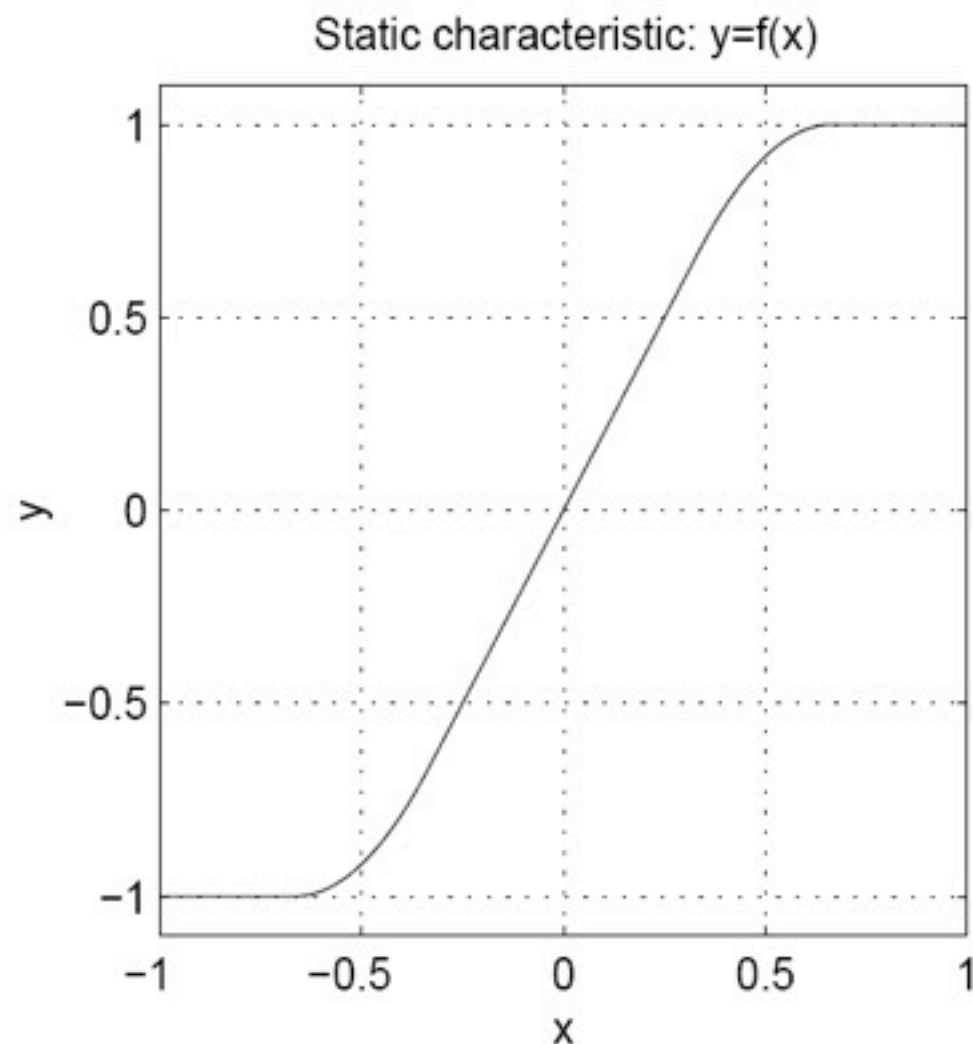
- Also know:
 - ▶ Parameters; variations (**stereo**, **feedback**, etc.)
 - ▶ Differences between phaser and flanger

Distortion (soft clipping variations)

- Most analogue systems have **smooth transition** from linear to non-linear
 - ▶ Rounded tops of waveforms known as **soft clipping**

$$f(x) = \begin{cases} 2x & \text{for } 0 \leq x \leq 1/3 \\ \frac{3-(2-3x)^2}{3} & \text{for } 1/3 \leq x \leq 2/3 \\ 1 & \text{for } 2/3 \leq x \leq 1. \end{cases}$$

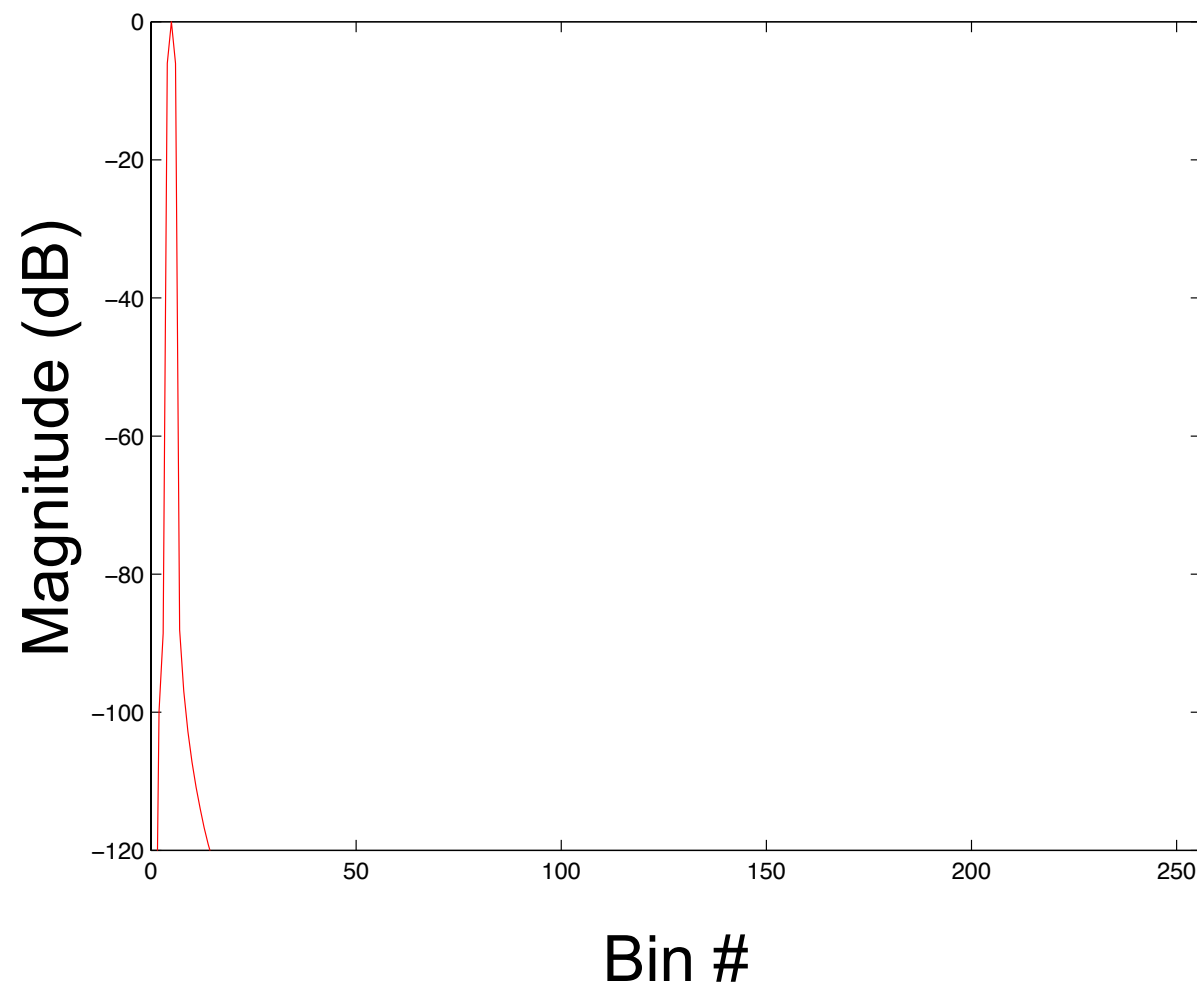
Notice: $G = 2$



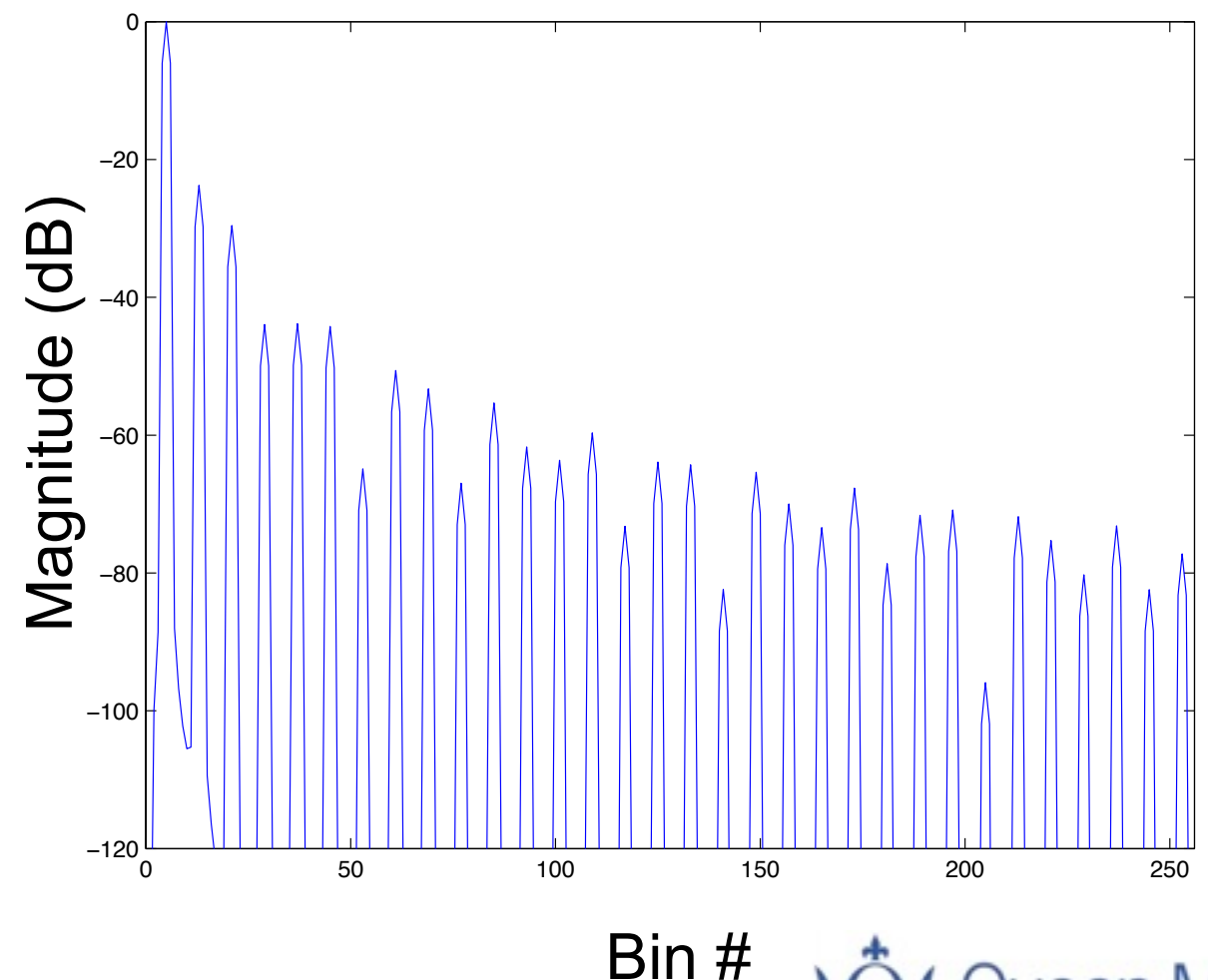
Distortion in the frequency domain

- Distortion is a **non-linear** effect (why?)
 - ▶ $f(x_1 + x_2) \neq f(x_1) + f(x_2)$
 - ▶ Non-linearity introduces **new frequency components** that weren't present in the original signal

Fourier Transform: Sine input



Fourier Transform: Hard clipping (G = 5)

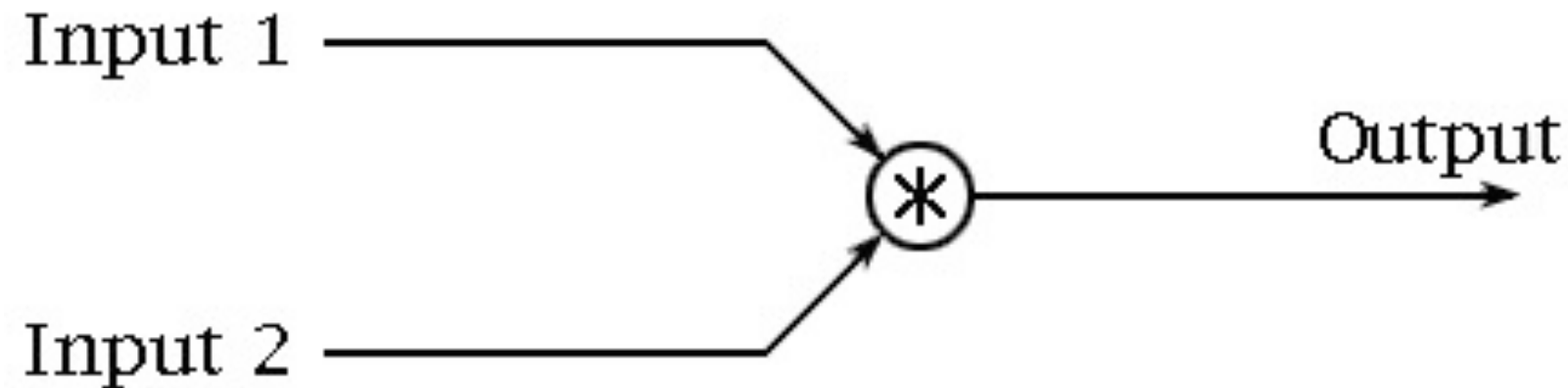


Intermodulation distortion

- The bane of fuzzbox technology
- Trig. identity: $\sin(x) + \sin(y) = 2 \sin\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right)$
 - ▶ Sum and difference frequencies are products of intermodulation between inputs
 - ▶ When we apply non-linear distortion, intermodulation products will show up in the spectrum
 - ▶ If two tones are harmonically-related
 - Intermodulation products will be harmonically-related as well
 - ▶ If two tones are not harmonically-related
 - Intermodulation products will be harsh and dissonant
 - Exact guitar tuning is *especially* important when using distortion!
- Also know:
 - ▶ Aliasing (and addressing it); hard clipping; (a)symmetry
 - ▶ Rectification, other variations

Ring modulation

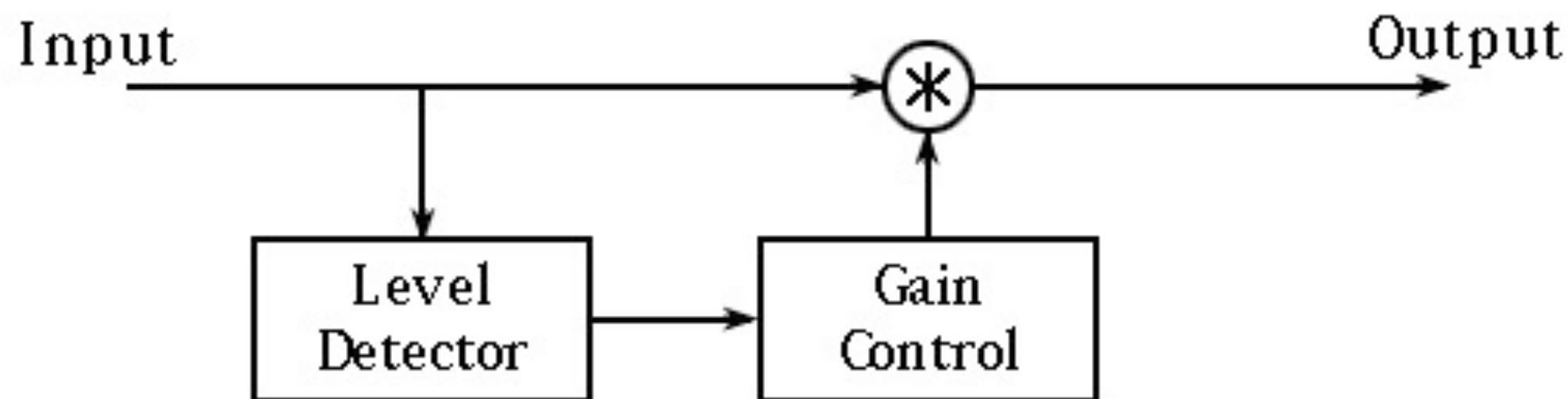
- Audio-frequency amplitude modulation



- ▶ Multiply signal by a sinusoid
- Resulting frequencies will differ from input
 - ▶ Sum and difference frequencies
 - Known as sidebands
 - ▶ Output not harmonic
 - Sounds can be quite dissonant, even for simple inputs
 - Not widely used for this reason

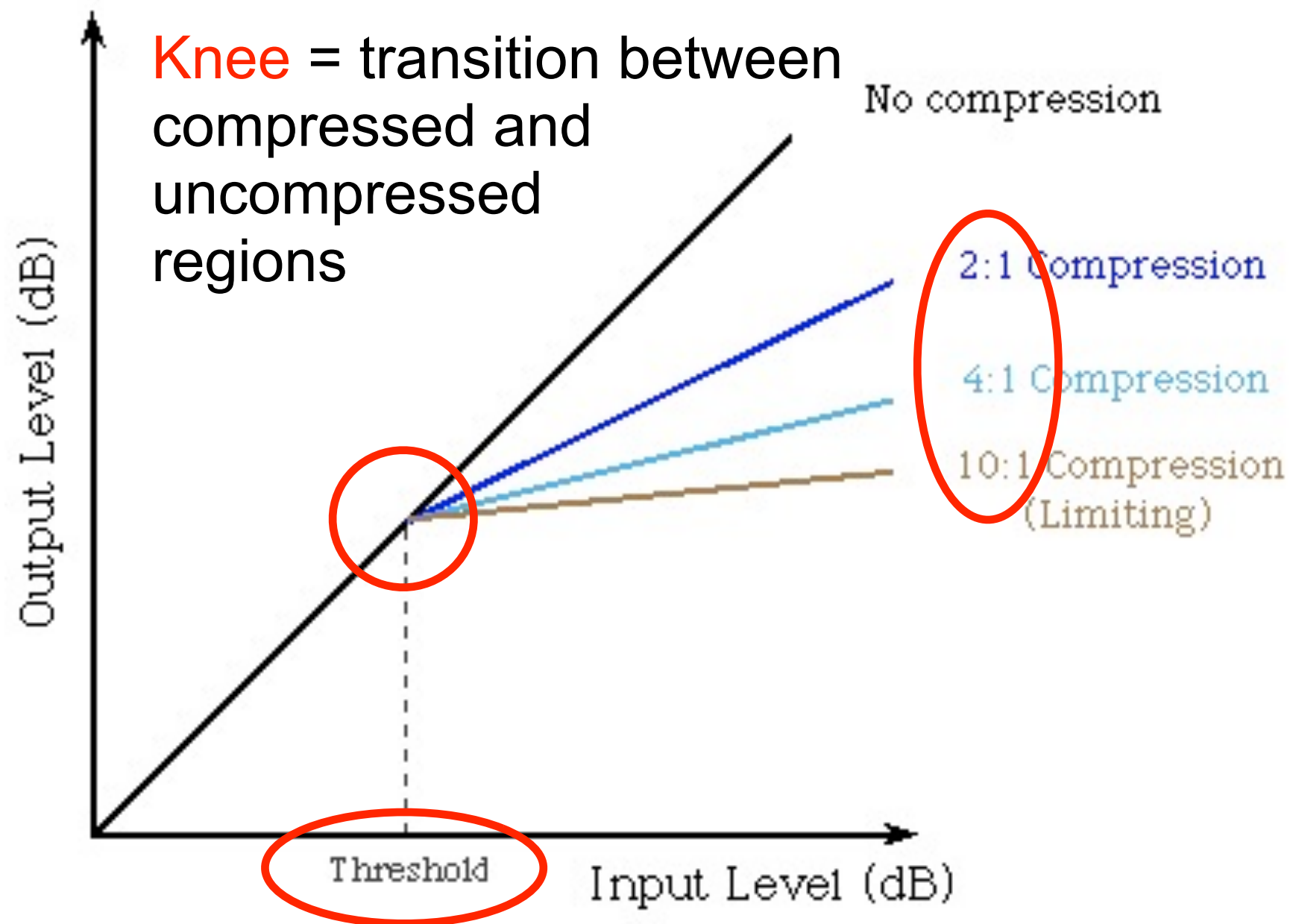
Compression

- Compressor = amplifier with **variable gain control**
 - ▶ Gain always ≤ 1
- Crucially: **gain controlled by level of input**
 - ▶ High signal level \rightarrow gain $\ll 1$
 - ▶ Low signal level \rightarrow gain ≈ 1



- Two ways to calculate signal level
 - ▶ Before or after compression is applied
 - “**Feedforward**” and “**feedback**” strategies
 - We have mostly seen feedforward version

Compression terminology



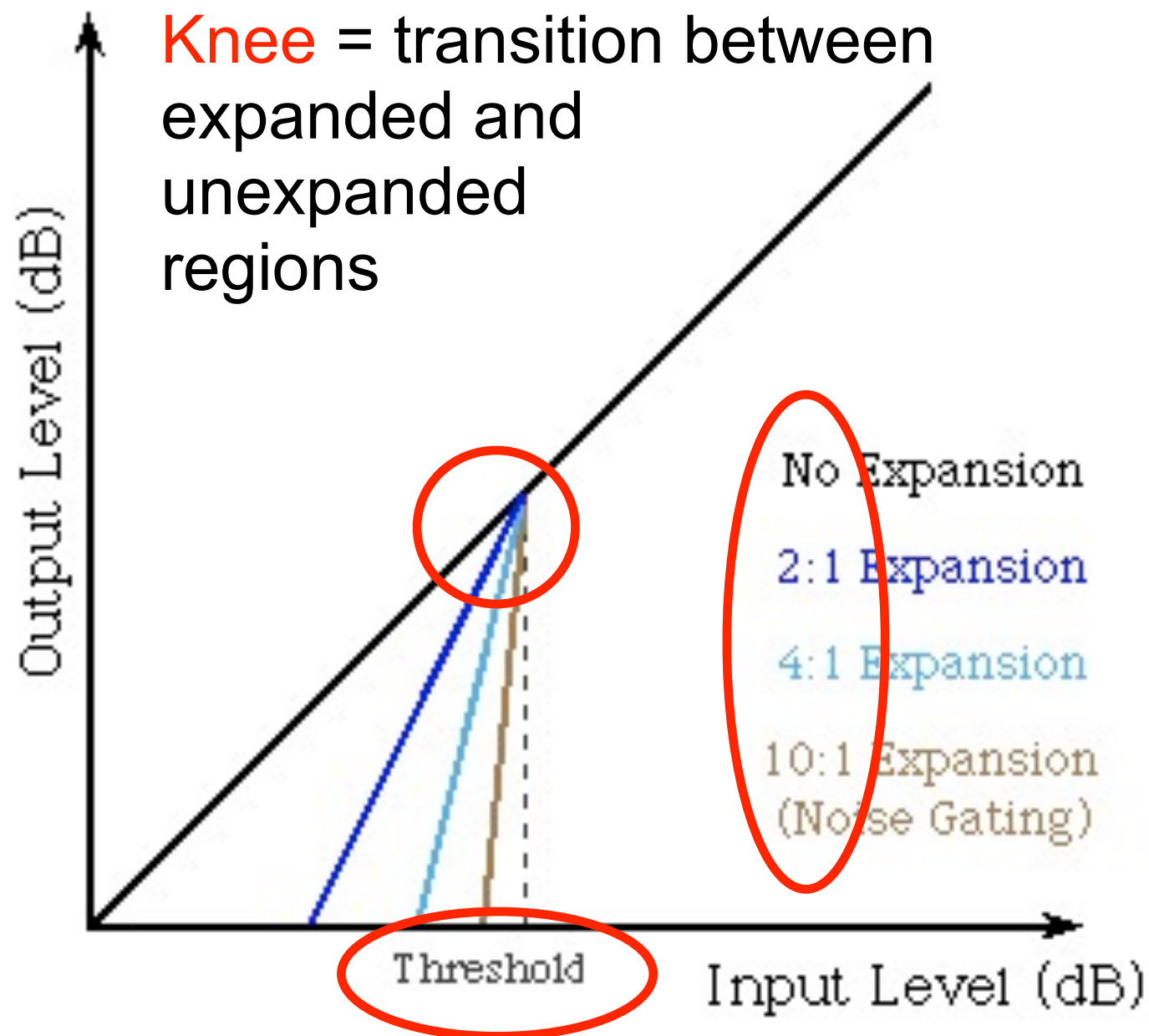
Threshold = input level at which compressor activates
(below this, gain = 1)

Ratio = amount that increasing input level affects output level
(not the same as gain -- why?)

Attack and release time

- **Attack time** and **release time** are properties of the level detector (not the gain control)
 - ▶ Assume level detector operates over a time window
 - ▶ Attack time = how long it takes to respond when input rises above the **threshold**
 - Usually short, less than 100ms
 - ▶ Release time = how long it takes to respond when input falls below the threshold
 - Usually larger than attack time, e.g. 1-2 seconds
- Also know:
 - ▶ **Limiting, ducking, look-ahead, de-essing**, etc.
 - ▶ Difference between compression and distortion
 - ▶ **Pumping** and **breathing** (and how to deal with them)

Expansion



Threshold = input level at which expander activates
(above this, gain = 1)

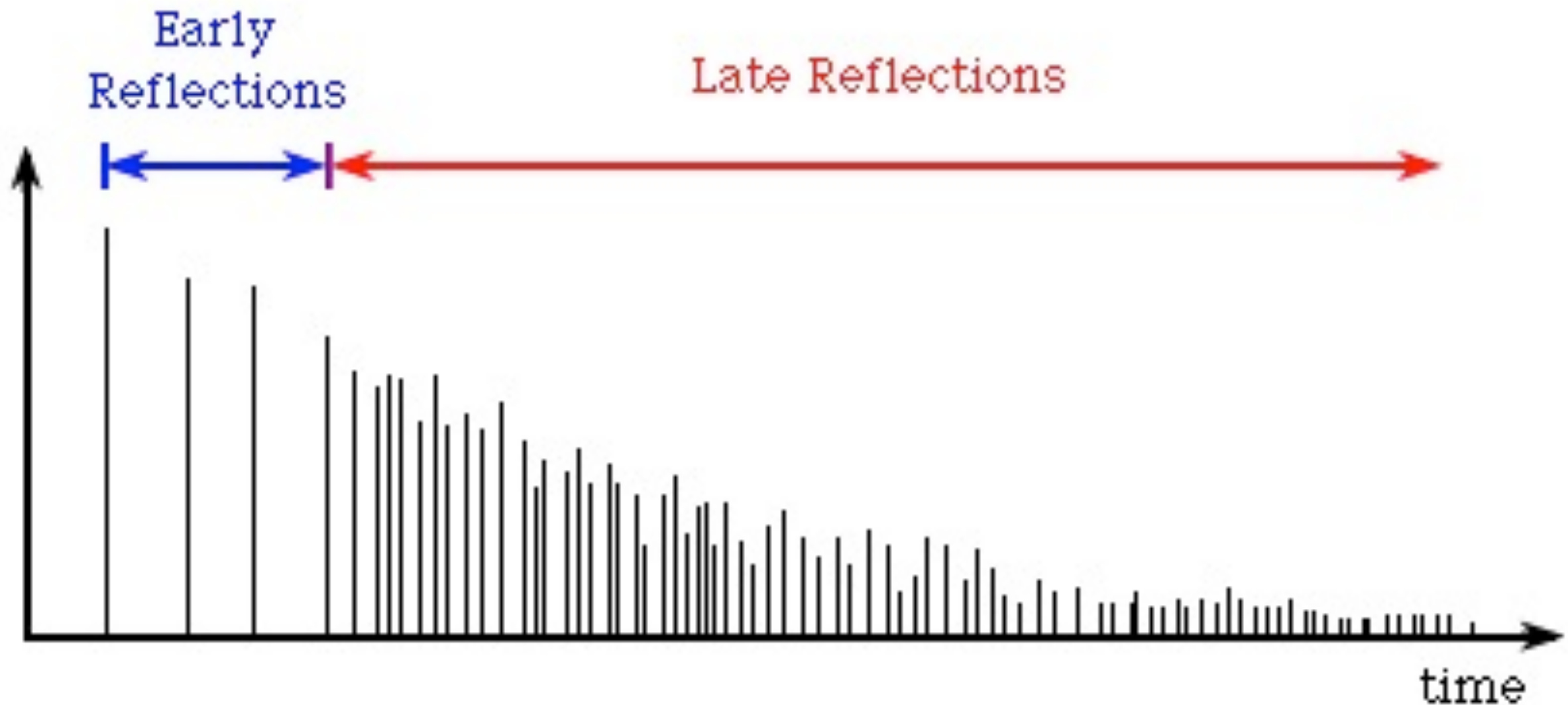
Ratio = amount that decreasing input level affects output level
(not the same as gain)

Also know: **noise gating**

Reverb, echo and delay

- Reverb is **not** just a series of echoes
 - ▶ **Echo**: distinct, delayed version of sound
 - Delay more than 0.1-0.2 seconds
 - ▶ **Reverb**: many closely-spaced copies of a sound
 - Do not perceive reflections as echoes
 - However, the overall effect is highly audible
- Delay with feedback does **not** produce reverb
 - ▶ **Delay**: reflections with fixed time interval
 - ▶ **Reverb**: rate of arriving reflections changes over time
 - Greater spacing of initial reflections, closer spacing later

Reverb impulse response



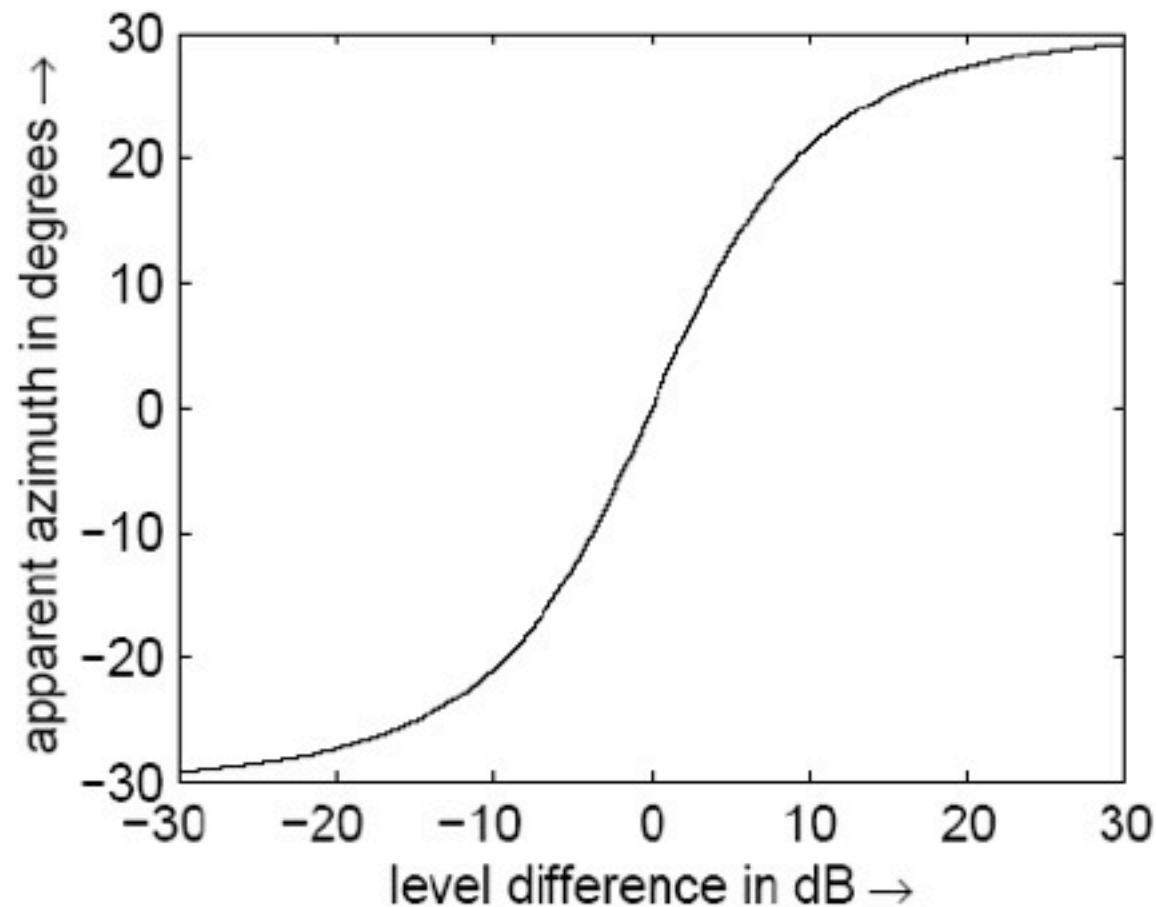
- Series of scaled **delta functions**
 - ▶ Each line represents a delayed, attenuated copy of sound
 - ▶ What would a simple feedback delay look like?

Phase vocoder

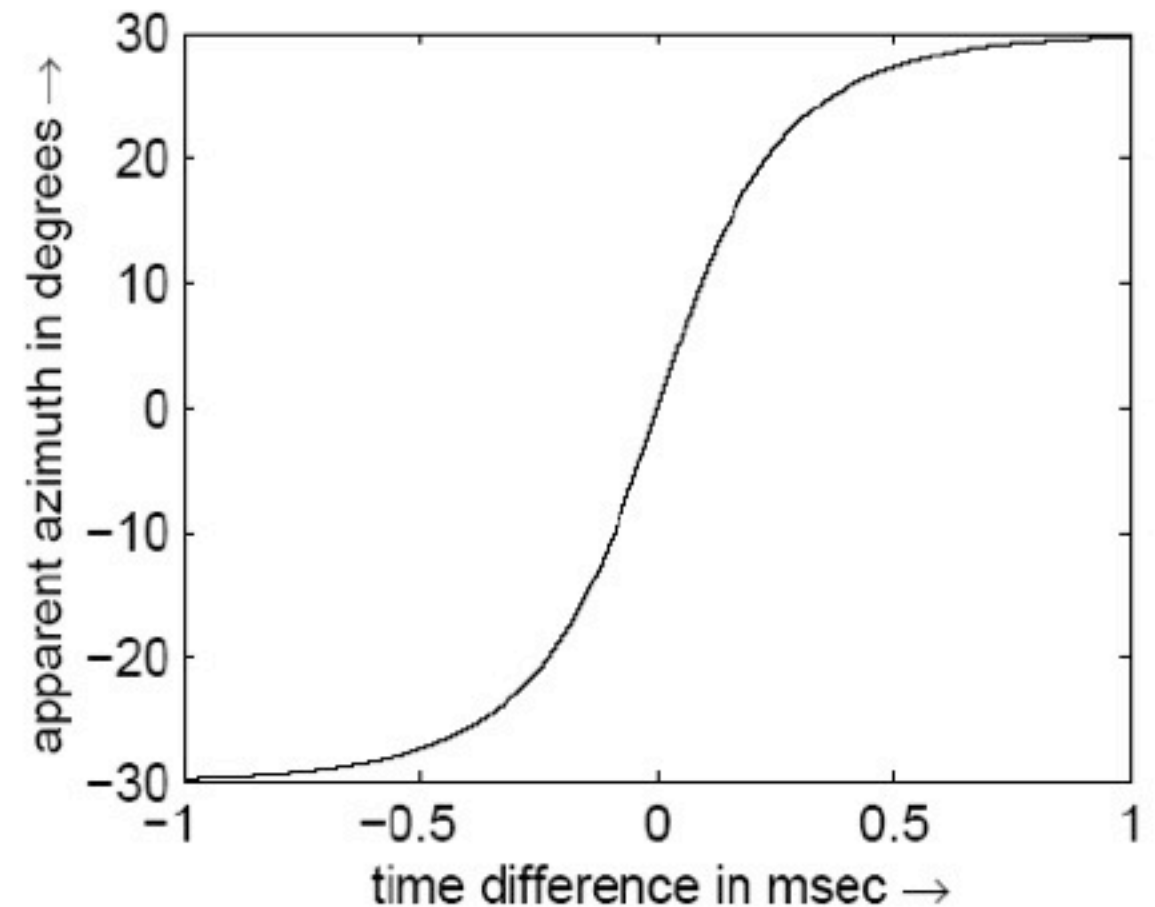
- Frequency-domain processing
 - ▶ Based on periodic **windows** processed by DFT/IDFT
- Overlap-Add processing method:
 1. Take m^{th} **segment** (frame) of length M using windowing function
 2. Take **DFT** of length $N \geq M$ of segment
 - If $N > M$, **zero-pad** the segment (add zeros to end)
 3. **Do something interesting to frequency data**
 4. Take **IDFT** to get back to time domain segment
 5. **Add** the result to the output buffer containing the prior segments
 6. Advance by the **hop size** to $(m+1)^{\text{th}}$ frame and repeat
- Also know:
 - ▶ **Robotisation, whisperisation, mutation, denoising, pitch-shift or time-stretch** (basics only)
 - ▶ **Latency** considerations

Spatial audio: gain and delay

- Two primary tools for placing sounds in space



Two simultaneous sounds
with level difference



Two equal amplitude sounds
with time difference

- ▶ Interaural Level Difference and Interaural Time Difference
- ▶ $> 1\text{ms}$ or $> 30\text{dB}$: sound localised to one source
- ▶ Also know: **HRTF** (basic concept, not equations)