CPE466 Lab3

Gilbert, Andrew apgilber@calpoly.edu

Terrell, Josh jmterrel@calpoly.edu

Abstract

When working with a graph of social data, where nodes represent actors and edges represent relationships, it can be useful to determine the most influential nodes. The PageRank algorithm provides a straightforward way to rank nodes based on their influence. We implemented the PageRank algorithm and observed its results on various datasets.

1 Introduction

The PageRank algorithm, developed by Larry Page and Sergey Brin, and initially used in what became the Google search engine, is a technique for calculating the importance of nodes in a graph. We wrote and tested an implementation of this algorithm to better understand how it works as well as observe its behavior on various datasets.

2 Implementation Overview

We implemented our reading and writing system in Python. We wrote the PageRank algorithm in c, and used Python's cffi library to interface between the two languages.

The ranking process starts by loading a given file into memory by parsing each line as an edge between two nodes. Each edge can have an optional weight. If the --weighted flag is specified, the weight is read from file. Otherwise each line is expected to be an edge between the left node pointing to the right node.

Our implementation computes the standard PageRank with options to customize its behavior:

- --help display all the below options and descriptions
- $\operatorname{\mathtt{--dval}}$ $\operatorname{\mathtt{-int}}$ the d parameter of the PageRank algorithm; probability of following a link
- --epsilon <float> (per iteration) consider the algorithm to have converged if the maximum change in PageRank of each node in the graph is less than epsilon

--maxiterations <int> — the number of iterations the algorithm will run before before giving up and considering the graph converged

```
--threads <int> - the number of computation threads to use
```

--batchsize <int> — per iteration, each thread claims batchsize nodes at a time to compute PageRank for. Too small and the threads will spend all their time synchronizing around a mutex. Too large and all the threads may wait on one thread to finish so the algorithm can continue to the next iteration.

```
--fmt string — the data format; either csv (default) or snap
```

--scale — scale epsilon and the printed results by the size of the graph.

--weighted — specify if the graph includes weights per edge.

When the --weighted flag is enabled, our algorithm runs a modified version of PageRank which takes into account the weights of edges. The modified version computes PageRank such that the weight is the number of edges between the nodes. The result is that edges with higher weight indicate stronger relationships than edges with lower weights.

The in-memory representation of the graph, PageRank computation, and parallel execution all happen in C. In the parallelized PageRank computation, each thread asks the master thread for a block of nodes to work on. Each node has two page ranks—the page rank of the previous iteration and the page rank of this iteration. By having both page ranks, we were able to parallelize computation without forcing Nodes to be computed in a specific order.

The graph is composed of an array of Nodes, a c structure with six fields:

```
{
  unsigned int id;
  char active;
  double pageRank_a;
  double pageRank_b;
  int outDegree;
  struct LLNode *inNodes;
}
```

The PageRank fields allow us to switch between the page rank of the last iteration and this iteration. inNodes is a linked list of incomming edges. Each edge has a source node and weight.

Once the graph is built, many iterations of the PageRank are computed until the algorithm converges. On every iteration, worker threads calculate PageRank on blocks of nodes from the list of nodes that haven't been processed yet until there are no nodes left to process in the iteration.

For each node in the block, the current PageRank is read from either the pageRank_a or pageRank_b field and the new rank is written to the other. If the rank has changed more than the (configurable) epsilon, a flag is updated to inform the system that the algorithm has not converged. Once all the worker threads have completed their work,

if the "unconverged" flag is set, the master thread starts the workers again, this time telling them to read from the field they were just writing to and to write to the field they were reading from.

3 Results

In general, we ran all the computations with --threads 8--maxiterations 1000000 --epsilon 0.00000001--batchsize 5000. For the LES-MISERABLES, NCAA-FOOTBALL, and SLASHDOT-ZOO-NOV6-2008 datasets, we also added the --weighted flag.

The results below include 3 columns each. The first column is the node name, the second the page rank, and the third the change in pagerank on the final iteration before convergence.

3.1 STATES

MA	1.462869437832707	8.532877876499256e-09
PΑ	1.3524810393473186	7.338763104158819e-09
NY	1.3271898437852825	7.786156441813574e-09
TN	1.3246348667661838	5.411682039990762e-09
KY	1.2686518916839202	5.653326071164422e-09
VA	1.2149463457633922	5.519433868284018e-09
ID	1.1957384420210948	2.7722326170764866e-09
MO	1.1940810483446511	4.389067234655819e-09
AR	1.1802419201439789	4.378786742920138e-09
MD	1.1208570953850048	5.514879698742536e-09
GA	1.1115358233807457	3.888831097420553e-09
OK	1.100494937600193	3.6911694187291566e-09
NV	1.0631327348400668	2.5448008283968093e-09
TX	1.0454328357344842	3.6191985172684404e-09
NH	1.0356269847111486	5.2541955161689025e-09
OH	1.0345121503002406	4.7246054291072426e-09
WV	1.03418223392241	5.0745513693883915e-09
UT	0.9466970183172859	2.3233356211127543e-09
CO	0.9221848584696164	2.5064941441832467e-09
WY	0.9209460697948871	2.126906983868082e-09
OR	0.9207126832348004	2.0249385501713846e-09
NB	0.9198421526448283	2.550868544171081e-09
VT	0.9177377192802924	5.087968588113334e-09
SD	0.9152833803384534	2.0886851276324947e-09
ΙA	0.9032036994941208	2.6370548106280367e-09
CT	0.9024186330227187	5.056845046869096e-09
IL	0.8984584669948867	3.2521053558443036e-09
AL	0.8842034295692448	3.0377084528354636e-09
NC	0.8748931952085944	3.2286413126358937e-09
ΑZ	0.8727433468843778	2.167064097613469e-09

MS	0.8498202476500514	3.0223309965826672e-09
NM	0.8441587411421481	2.5198917605329108e-09
IN	0.8211997493904607	3.248204309691527e-09
NJ	0.7806691722936716	4.087988367956763e-09
WI	0.7768374932182449	2.376985327318115e-09
DE	0.7533367824707436	3.743891394819565e-09
MT	0.7484861114120919	1.597971061029213e-09
MN	0.7416542967907246	1.8177874136493521e-09
LA	0.7199422168746245	2.4283349636666784e-09
CA	0.71184196999972	1.5833141221721636e-09
MI	0.6654499776068552	2.3875423339758672e-09
RI	0.6543730809046352	3.4413492888685226e-09
ND	0.5963199812693003	1.2216931459529956e-09
KS	0.5846674144855015	1.6070394147360556e-09
FL	0.5268543174515771	1.5614288507992402e-09
SC	0.5248758926093655	1.6097755940747138e-09
WA	0.5150477236506844	9.847204648916197e-10
DC	0.5126631034791487	2.0536867345599674e-09
ME	0.44342764417947	1.7767023095804912e-09
NE	0.150000000000000002	0.0

3.2 NCAA-FOOTBALL

We observered that the NCAA data set is troublesome to run as unweighted because the nodes are in the opposite order from the other datasets. Typically edges in the dataset run from left (source) to right (destination), but for PageRank to do anything meaningful with this dataset, the edges must run from right to left. This is because the left team is always the winning team, and thus there should be an edge connecting from losing team (right) to winning team (left) to represent the winning team gaining prestige from the losing team. Our program only provides meaningful results for this dataset if the --weighted flag is provided, in which case the edges are flipped to go from right to left due to the weighting of edges.

```
Mississippi
                                            6.565710225503452e-09
                       15.35711933877105
             Florida
                       15.120842239804153
                                            5.958453064280889e-09
                 USC
                       9.709094062122265
                                            8.673411308612877e-09
        Oregon State
                                            9.268392678341009e-09
                       9.138868090363559
            Oklahoma
                       9.093401455685925
                                            2.0352699109382755e-09
          Texas Tech
                       6.933583512895485
                                            1.3122560954537121e-09
      South Carolina
                       6.186403273609781
                                            2.8357764469966185e-09
                       5.771265700405203
                                            1.2049815728554236e-09
               Texas
                       5.289853932502011
                                            2.11207079603426e-09
             Alabama
                                            4.5762501149626544e-09
          Penn State
                       5.107477363379916
          Vanderbilt
                                            2.353541389554792e-09
                       4.91241475509652
                Utah
                       4.589133042096809
                                            1.7619420089598492e-09
              Oregon
                       3.959113846990245
                                            4.055958388593517e-09
         Wake Forest
                       3.4167626140316907
                                            1.518014255963429e-09
North Carolina State
                       3.032703633203939
                                            7.923217221206258e-10
      North Carolina
                       2.9538761491670127
                                            6.973040513058582e-10
            Virginia
                       2.8493836410031554
                                            5.648575808481215e-10
                 TCU
                       2.8280597269404333
                                            8.340812832074995e-10
             Clemson
                       2.821228451582217
                                            7.64319538215652e-10
       Florida State
                       2.812912146215853
                                            9.765833107466815e-10
                      2.5124588409373794
            Richmond
                                            1.572353358625378e-14
       West Virginia
                       2.4976151735654684
                                            1.7437398747155441e-10
                       2.453766427549545
            Maryland
                                            1.178236914284314e-09
             Houston
                       2.396438567629544
                                            1.7840993266071692e-10
                 LSU
                       2.346431884334138
                                            4.135507318536735e-10
                Duke
                       2.30562119705057
                                            2.6866265809277756e-10
       East Carolina
                       2.2321091986673487
                                            2.525521111684803e-10
         Weber State
                       2.193510984452151
                                            3.180442020855878e-14
                       2.1863942302007753
                                            7.924707383366592e-10
             Georgia
                                            9.233255583718236e-10
                Iowa
                       2.1831728243586492
                       2.128782927459705
       James Madison
                                            5.0029425047171117e-14
                                            1.2653477918234124e-10
               Tulsa
                       2.1149560628489588
             Montana
                       2.085060469571556
                                            2.394265341543189e-14
           Villanova
                       2.0777466616365063
                                            1.139956185003399e-13
```

Ohio State	1.9451531483953115	5.106610620475571e-10
Rutgers	1.9222801960052662	3.638868789623828e-10
Georgia Tech	1.8968545355050521	3.867424644421469e-10
Boston College	1.8681267894126905	5.814044558294373e-10
Virginia Tech	1.8415554064606094	4.987176088766532e-10
Appalachian State	1.8242011043800201	0.0
Missouri	1.7670485311870654	1.626449461222812e-10
Boise State	1.7002205378957824	5.518713715180201e-10
Northwestern	1.6778533619258764	4.676507653345041e-10
Pittsburgh	1.5091825498165916	3.0892062172216406e-10
Oklahoma State	1.4936791322886462	1.0240791027682494e-10
Brown	1.4652285727750236	0.0
California	1.4472830308458573	1.1958478079304724e-09
South Florida	1.4306961347508518	2.52333589786935e-10
Connecticut	1.4294029846875864	2.237816182359964e-10
Brigham Young	1.3266992194196499	4.9976179444799484e-11
Miami (FL)	1.3159810118670185	3.2672823821466856e-10
Cincinnati	1.262196466866521	1.6483373346809493e-10
Michigan State	1.240934792324587	3.983605476737262e-10
Jacksonville	1.2029922142886587	0.0
Northern Iowa	1.184674785228468	1.8582357874663558e-14
Harvard	1.1761728795184991	0.0
Dayton	1.1713253672602455	0.0
Stanford	1.1329183472889885	1.1167182317750601e-09
Massachusetts	1.1326416303038789	0.0
Lafayette	1.1252191538695084	0.0
Rice	1.1202755174006902	7.798890526433677e-11
Albany	1.1112746522993475	0.0
South Carolina State	1.0704075410768772	0.0
Nevada	1.0416114046960527	2.1988468337785783e-11
Grambling State	1.0332130612004637	0.0
Tennessee	1.0066108109068825	3.9442448265814e-10
Central Arkansas	0.989009647450989	0.0
Hawaii	0.9405369871334621	5.933132457558443e-12
Rhode Island	0.9401492340320694	0.0
New Hampshire	0.937074042183389	1.5455518809215363e-13
Southern Miss	0.9352815534342132	8.705638120110049e-11
Cal Poly	0.9107993093752099	2.3406623861355058e-14
Arizona	0.8991217056106117	4.3395308874094596e-10
Delaware	0.893092987972269	0.0
Navy	0.8584636405949517	2.541105277586997e-10
Liberty	0.8568766385836117	0.0
Marshall	0.8442358052571748	6.044948222538871e-11
Central Connecticut State	0.8397495121899511	0.0

3.3 KARATE

34	3.431252149966154	8.707609577829345e-09
1	3.2979076567614305	8.195399414656634e-09
33	2.4375696493652135	6.146548853225298e-09
3	1.940669293582341	5.122124044354415e-09
2	1.7978153919561228	4.609911521957777e-09
32	1.2633749429357202	3.0732737188454706e-09
4	1.2192351473227652	3.073274190690256e-09
24	1.0717654878943703	2.5610611964488328e-09
9	1.012045892241893	2.5610617862548146e-09
14	1.0042394946523805	2.561061904216011e-09
6	0.9897792474544365	2.048849971625355e-09
7	0.9897792474544365	2.048849971625355e-09
30	0.8938102700237597	2.0488492638581768e-09
28	0.8717520828066848	2.0488492638581768e-09
31	0.8360652668415772	2.0488492638581768e-09
8	0.8326768875894534	2.048849617741766e-09
11	0.747250371688433	1.5366375671899135e-09
5	0.747250371688433	1.5366375671899135e-09
25	0.716585132305966	1.5366369773839317e-09
26	0.7142107027051523	1.5366369773839317e-09
20	0.6665576263645843	1.536637095345128e-09
29	0.6654976130625588	1.5366369773839317e-09
17	0.5706561792973743	1.024425162754472e-09
27	0.5114972890075956	1.0244244549872938e-09
13	0.49792632259874825	1.024424808870883e-09
18	0.49499501930165707	1.024424808870883e-09
22	0.49499501930165707	1.024424808870883e-09
15	0.49422379012424933	1.0244245729484902e-09
16	0.49422379012424933	1.0244245729484902e-09
19	0.49422379012424933	1.0244245729484902e-09
21	0.49422379012424933	1.0244245729484902e-09
23	0.49422379012424933	1.0244245729484902e-09
10	0.48651949658204574	1.0244246909096866e-09
12	0.32520134383007043	5.122124044354415e-10

3.4 DOLPHINS

Grin	1.9929584993071667	9.35167862592401e-09
Jet	1.967144665571631	7.040288171888953e-09
Trigger	1.9405600839191688	7.792422068719773e-09
Web	1.865912985987976	7.0405458685307565e-09
SN4	1.8522709448116916	8.572964761699442e-09
Topless	1.8298805734742087	8.57237666268551e-09
Scabs	1.7622302792686884	7.792798718819771e-09
Patchback	1.640430072175734	7.0131839918774475e-09
Gallatin	1.6217262752147679	6.259463475322136e-09
Beescratch	1.5283444092422989	6.251719669725375e-09
Kringel	1.5277369287435327	7.01561124472061e-09
Kringer SN63	1.4842331174368502	6.2342287790451145e-09
Feather	1.4544256882987086	5.477406223031167e-09
reacher SN9	1.3619146564136206	6.2369371750525815e-09
	1.3448497261403864	5.454560920992169e-09
Stripes	1.3423543472968191	5.473508507547464e-09
Upbang SN100	1.2780301140466968	5.460063970397222e-09
DN21	1.2433249899836387	4.694479728561962e-09
Haecksel	1.232751011081599	5.455429517853272e-09
	1.2025241103754618	
Jonah		5.454888742095765e-09
TR99	1.1923805400446332	5.4553137909807425e-09
SN96	1.092356294750833	4.677576721789922e-09
TR77	1.0750500910429874	4.678380571832008e-09
Number1	1.0620656262882313	3.908881406056164e-09
Double	1.0600946257920347	4.677003895281473e-09
Beak	1.051854260449204	4.676884296506145e-09
MN105	1.0502173585938894	4.675476644733223e-09
MN83	1.0481568452060985	4.675490411498728e-09
Hook	1.0308625908146938	4.6758578120531524e-09
SN90	1.0005291265651786	3.910992668609836e-09
Shmuddel	0.9870360026167347	3.896236201728076e-09
DN63	0.9698678669312149	3.905049943131456e-09
PL Edul	0.9487298836526632	3.901697090413769e-09
Fish	0.9367206252329705	3.897285272280726e-09
Oscar	0.9204357707648877	3.900529281508636e-09
Zap	0.9156110167179048	3.8974218644072245e-09
DN16	0.8945389354882448	3.130139578089164e-09
Bumper	0.8269609263282902	3.1175270698291513e-09
Ripplefluke	0.8251379772904986	2.347968319771354e-09
Knit	0.801548379168406	3.124906701457153e-09
Thumper	0.7955113488599097	3.117281204001454e-09
TSN103	0.7485005988393056	3.1173072317924877e-09
Mus	0.7132618077079809	2.3460650644402392e-09
Notch	0.6950285934747813	2.3454552397494943e-09

Zipfel	0.6844298328220967	2.3378478111735213e-09
MN60	0.6115368386324737	2.3384745216625813e-09
CCL	0.5970018365426253	2.3381971428482196e-09
TR88	0.5503584689495779	1.558313426214264e-09
TR120	0.5472055290102805	1.5582967555216598e-09
Wave	0.5162272293753949	1.5651356113921544e-09
TSN83	0.5072249656728637	1.5584277548996717e-09
SN89	0.4814144850067452	1.5623700510419836e-09
Vau	0.46463880001109403	1.5585150340419185e-09
Zig	0.38378909290038365	7.827573138274868e-10
MN23	0.33578588441684903	7.823388256666952e-10
Quasi	0.33578588441684903	7.823388256666952e-10
TR82	0.3262251146783684	7.823686715840994e-10
Cross	0.31494760647077347	7.792029070585738e-10
Five	0.31494760647077347	7.792029070585738e-10
Whitetip	0.30769976806527854	7.79240873216569e-10
SMN5	0.30492950615424086	7.792034448228513e-10
Fork	0.2997895730754506	7.792421100744074e-10

3.5 LES-MISERABLES

Valjean	7.665974282581213	9.349708741598906e-09
Marius	3.9784442848480737	6.154232121309555e-09
Myriel	3.020831596182633	1.8344405538876785e-09
Cosette	2.8420371738890955	4.023922938346108e-09
Enjolras	2.8194934790338655	5.384945372423344e-09
Thenardier	2.7475371663125885	3.6096958469164497e-09
Courfeyrac	2.5409217654001015	4.970718280993686e-09
Gavroche	2.179302801471389	3.313812536875904e-09
Fantine	2.0915902723875295	2.781246382938668e-09
Javert	2.0653543190409005	2.7812416640571325e-09
Combeferre	2.0505992845473897	4.023914287063293e-09
Bossuet	2.0170107783106874	3.9055639516720475e-09
MmeThenardier	1.543019540501597	2.011961993493225e-09
${\tt MmeMagloire}$	1.5040372211824298	1.1243338226586685e-09
Gillenormand	1.4095121514104394	1.7160836644943e-09
Joly	1.3606420733536875	2.5445336527922524e-09
MlleBaptistine	1.340072283463428	1.0059829629472522e-09
MlleGillenormand	1.284394920231858	1.3610323961604776e-09
Bahorel	1.2668098475120204	2.307832982009761e-09
Babet	1.20889623728762	1.5977341155833102e-09
Feuilly	1.1930561303835443	2.2486579453941807e-09
Gueulemer	1.1309018254952004	1.479383255871894e-09
Favourite	1.0882621697317887	1.5385631424490523e-09
Tholomyes	1.0832720590924592	1.538562880288967e-09
Dahlia	1.0516761942505566	1.4793877125933441e-09
Blacheville	1.0497067947878496	1.4793878436733868e-09
Zephine	1.0152931576783895	1.4202121516575933e-09
Fameuil	1.0133335333371034	1.420212282737636e-09
Listolier	1.0133335333371034	1.420212282737636e-09
Fauchelevent	0.9821008205449455	8.284549693395732e-10
Claquesous	0.9218615685465926	1.1835066309135236e-09
Eponine	0.8888680673937737	1.1243308078176875e-09
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3.8 P2P-GNUTELLA05

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3.9 SLASHDOT-ZOO-NOV6-2008

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3.10 AMAZON-MAY03

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3.11 LIVEJOURNAL1

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```

Dataset	Execution Time (seconds)
amazon0505	40.117672
dolphins	0.005594000000000002
karate	0.004950999999999997
lesmis	0.005074999999999996
NCAA_football	0.0063620000000000065
p2p-Gnutella05	0.01785999999999987
polblogs	0.04911300000000002
soc-LiveJournal1	1193.963033
soc-sign-Slashdot081106	2.74611
stateborders	0.004391999999999993
wiki-Vote	0.0008930000000000327

Table 12: Execution Times on Datasets

4 Overall Summary

Before implementing edge weights, page rank appeared to do decently on the graphs we manually tested. We created our own fakeball dataset, and analyzed carefully the results of the NCAA football dataset before and after weighting. As noted in the NCAA football section of Results, NCAA football was a bit troublesome to run unweighted.

Once we implemented edge weights, we noticed different rankings of the football teams, and the change in rankings seemed a bit more inline with the rankings from ESPN's 2008 data, though the rankings were far from perfect. We also compared the PageRank results with a ranking the teams by total score. Weighted PageRank matched much more closely to the teams sorted by total season score.

5 Performance Evaluation

All datasets were successfully executed in roughly 30 minutes (combined) on a 4-core hyperthreaded processor using 8 threads. The execution time for each dataset is provided in table 12. A visual representation is also included in fig. 1. Note that that on the graph, both the x and y axis are drawn in log10 so the outliers do not crowd out the trends. The visible trend on the graph suggests that the execution times increase roughly linearly as edge count increases to the max of our dataset.

6 Extra Credit

We added a weighted flag to our algorithm which takes into account a weight per edge when computing PageRank . We experimented with different ideas, but decided that simply using the weight as a multiplication factor for the importance of the edge would have the desired effect. We treated weights as edge counts. For instance, if the edge a->b had a weight of 7, we would compute page rank as if there were 7 edges from a to b. A weight of -7 would mean there were 7 edges in the opposite direction.

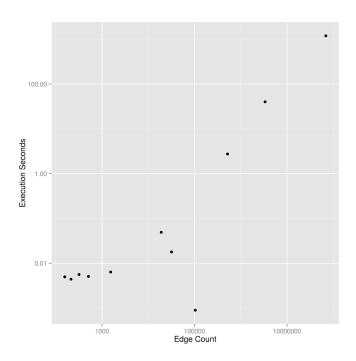


Figure 1: Graph of Execution Times on Datasets

Increasing the edges also involved increasing the node count. We discovered that PageRank would not converge unless we added an appropriate amount of fake nodes to the graph so that outdegree and other variables of the PageRank computation were accurate.

We used our weighted modification to the PageRank algorithm to compute PageRanks for the NCAA_football, lesmis, and SlashDot datasets.

The file extra-credit.txt contains the results of running our weighted PageR-ank using different d values. The top set of 25 teams is the actual rankings of teams from 2007 NCAA rankings, ESPN. The url to the actual rankings is included in the file. We found that changing the dval between 0.5, 0.9, and 0.97 had seemingly no significant impact on the amount of correct results found in the 25 nodes with the highest pagerank. Regardless of dval, PageRank resulted in typically 9 nodes correctly included in the top 25 results.

A README

Team: Andrew Gilbert, Josh Terrell

Important: Run everything from the project's root directory

A.1 Setup environment

```
pyvenv virtual
source virtual/bin/activate
pip install --upgrade -e .
```

A.2 Run all the tests

python3 -m unittest discover

A.3 Compute Page Rank

The ranker scripts assume the graph is directed.

Correctly parsed formats include:

SNAP (edges must be repeated if undirected) (weight is optional):

```
a b [weight]
```

CSVs, (edges must be repeated if undirected) (w_a and w_b are ignored unless --weighted flag is specified):

```
a,w_a,b,w_b
```

To run:

You can use ranker --help for more options such as setting the pagerank d parameter or tweaking parallel computation settings.

A.4 Deactivate environment

deactivate

$A. 5 \quad (Optional)\, Manual\, Rebuild\, of\, Page\, Rank\, C\text{-}Implementation$

python build_page_rank.py