Alliance Participation and Military Spending

Joshua Alley*

February 7, 2019

^{*}Graduate Student, Department of Political Science, Texas A&M University.

Abstract

How does alliance participation change military spending? Previous answers to this question are divided between assertions alliance participation increases or decreases military spending. I argue alliance participation can raise or lower growth in military expenditures, depending on treaty strength and state size. Greater treaty strength reduces growth in major power military spending because major powers use alliances for international influence. Reduced growth for non-major powers is attenuated under strong treaties because strong treaties give allies more influence. I test this argument by creating a measure of alliance treaty strength and employing that measure in a multilevel model. The research design generates novel empirical evidence linking alliance participation and growth in state military spending from 1816 to 2007. I find that greater treaty strength increases growth in military spending in non-major powers and decreases spending growth for major powers.

1 Introduction

Scholars of international relations have long acknowledged two ways for states to increase their security. States can invest in military capability, or form alliances (Morgenthau, 1948). Therefore, how states mix internal balancing through military spending and external balancing from alliances is an important issue. But scholars have made little progress in understanding the relationship between alliances and military spending.

How might alliance participation affect military spending? Scholarship on this issue is divided between two camps. The force multiplier perspective expects alliance participation to reduce military spending (Morrow, 1993; Conybeare, 1994; DiGiuseppe and Poast, 2016). The foreign entanglement group predicts alliance participants will spend more on defense. Both perspectives treat alliances and states as homogeneous, which hinders the accumulation of knowledge.¹

¹See DiGiuseppe and Poast (2016) for an important exception.

In this paper, I argue that whether alliance treaty participation increases or decreases military spending depends on state capability and alliance treaty strength. I provide a verbal argument and novel empirical analysis to back up this claim. By showing when alliance participation increases and decreases growth in military expenditures, I make theoretical and empirical contributions.

Unlike previous scholarship on this issue, I distinguish between states based on their capability, and alliances based on their strength. Major and non-major power states use alliances and military spending for different purposes, so they respond differently to changes in alliance treaty strength. Increasing treaty strength reflects greater depth and scope to the obligations of alliance partners, and is a key source of credibility.

Major powers use alliances to increase their influence—shaping international relations in ways that match their interests. Greater treaty strength provides extra influence and reduces growth in military expenditures from alliance participation for major powers. Stronger treaties require less growth in military spending to uphold an alliance commitment.

Non-major powers emphasize territorial security from alliances. Given the chance, these states will rely on their allies for security and reduce growth in military spending. Though strong treaties provide more security, they also constrain freedom to reduce military spending for greater security under a strong treaty. Weaker treaties still provide security without tying military support to other costly commitments, giving non-major powers the chance to reduce growth in military spending.

I test these predictions with a novel research design. First I develop a latent measure of alliance treaty strength. I then incorporate that measure into a multilevel model which estimates the impact of specific alliance treaty characteristics, and aggregate impact of each treaty on growth in military spending. Multilevel modeling links the alliance and state levels of analysis, showing how changes in treaty strength affects state military spending.

Understanding how alliance participation changes military spending can illuminate a salient policy issue. Policy debates emphasize reduced spending by alliance members— especially US allies. But the US and other democracies make weaker formal commitments and other kinds of

treaties could have different effects. My argument makes distinctions between treaties, adding nuance to policy discussions.

Alliance treaty design has distributional consequences in domestic and international politics. Treaty strength shapes how large and small alliance members allocate resources to the military. Large and small members will bear different security burdens under different treaties.

Growth in military spending has domestic opportunity costs—funds spent on security cannot be spent on other goods. Greater military spending impacts economic growth (Shin and Ward, 1999; Alptekin and Levine, 2012) and domestic politics (Narizny, 2003; Whitten and Williams, 2011; Williams, 2015). So alliances can shape domestic prosperity by shifting growth in military spending.

Another implication of this argument is that major and minor powers face different tradeoffs in alliance politics. Strong commitments give major powers more influence but lead to greater entanglement abroad. For non-major powers, strong treaties provide more security at the cost of freedom to reduce military spending.

The paper proceeds as follows. First, I summarize competing arguments and mixed empirical evidence on alliance participation and military spending. Then I describe my state capability and treaty strength argument in more detail. The third and fourth sections describe the research design and results. The final section concludes with a discussion of the implications for scholarship and policy.

2 Force Multiplier or Foreign Entanglement?

Scholarship on alliance participation and military spending is divided between two perspectives. The foreign entanglement view predicts alliance participation will increase military expenditures. The force multiplier school expects alliance participation will reduce military spending.

2.1 Force Multiplier

Force multiplier arguments start with the premise alliances and military spending both provide security. States substitute between these two foreign policy instruments (Most and Starr, 1989). Alliances provide security that states could not achieve without additional military spending (Morrow, 1993; Conybeare, 1994). Because military spending has opportunity costs, states rely on their allies for security and and reallocate military spending to other goods.

Allied military capability replaces defense expenditures of member states. DiGiuseppe and Poast (2016) refine the substitution logic by arguing that states will only reduce spending if the alliance is credible. Unreliable alliance capability cannot replace reliable domestic military spending.

Another argument in the force multiplier perspective links reduced military spending to a collective action problem. Olson and Zeckhauser (1966) argue that security from an alliance is a public good, so treaty members provide inadequate contributions of military spending. Each member free-rides on other states, and smaller members exploit larger states. Spending less allows alliance members to consume more non-defense goods, but the alliance provides suboptimal security.

Both the substitution and public goods models expect alliance participation will reduce spending. These arguments are rooted in the opportunity costs of military spending. But the foreign entanglement group predicts alliance participation increases military expenditures, because alliances provide more than security.

2.2 Foreign Entanglement

The foreign entanglement perspective is less cohesive. Most of these arguments emphasize non-security benefits of alliance participation. States then use additional military expenditures to reinforce gains from alliance participation.

Diehl (1994) argues that alliances increase foreign policy obligations, necessitating extra military spending. Because alliances expand what a state can achieve in international relations, states will increase military spending to pursue other foreign policy goals (Morgan and Palmer, 2006). Horowitz, Poast and Stam (2017) show that buffer states increase defense effort to make themselves a more attractive alliance partner, which is a more security-focused argument. Others assert that alliances generate cooperation, leading to higher defense spending (Palmer, 1990; Quiroz Flores, 2011).²

Arguing alliances do more than provide security is a crucial insight. However, the foreign entanglement perspective does not consider the opportunity costs of military spending. If military spending has opportunity costs, states have incentives to reduce spending where possible. Likewise, the force multiplier perspective does not acknowledge synergies between military spending and alliances. This divergence carries over into testing both predictions.

2.3 Mixed Evidence

The force multiplier or foreign entanglement dispute could be settled by a preponderance of empirical evidence. Unfortunately, the divided state of theory is reinforced by mixed empirical results.³ Some studies find a positive association between alliance participation and military spending. Others find a negative relationship.

The wide range of methodologies and samples in previous research can be divided into into specific and general research designs. Specific studies examine the impact of a few alliances, usually by tracking how a state responds to the military spending of a key ally. General studies compare many states through dummy indicators of alliance participation. Each design has different virtues and shortcomings.

² Senese and Vasquez (2008) argue that military spending and alliances are part of a conflict spiral that produces simultaneous growth in military expenditures and alliance participation. This argument suggests that any correlation between alliances and military spending is driven by conflict behavior, not treaty participation.

³Because tests of the public goods model regress military spending as a share of GDP on GDP, I ignore most tests of that theory while summarizing prior results. That research design suffers from an identification problem.

Specific designs have more detail on treaties, but lack generalizability. Most support for the substitution of arms and alliances comes from specific designs (Barnett and Levy, 1991; Morrow, 1993; Sorokin, 1994; Plümper and Neumayer, 2015). But other specific studies find increased spending by alliance members (Conybeare and Sandler, 1990; Chen, Feng and Masroori, 1996).

General models capture a wide range of state-year observations and compare states with an alliance to those without. Dummy indicators of alliance participation in a general study combine diverse treaties in a state-level measure. Therefore, general studies do not distinguish between alliances, omitting crucial differences between treaties.

Table 1 summarizes previous results from general models of alliance participation and military spending. General research designs also produce mixed results. There are two negative, four positive and two null estimates of the correlation between alliance participation and spending.

	Decrease	Increase	Null
Most and Siverson (1987)			X
Conybeare (1994)	X		
Diehl (1994)		X	
Goldsmith (2003)			X
Morgan and Palmer (2006)		X	
Quiroz Flores (2011)		X	
DiGiuseppe and Poast (2016)	X		
Horowitz, Poast and Stam (2017)		X	

Table 1: General Findings of Association Between Alliance Participation and Military Spending.

Mixed results are the result of inadequate attention to differences between alliance treaties and participants. There is substantial heterogeneity among alliances. Treaties vary in their obligations, membership, and capability. Alliance heterogeneity makes it difficult to infer general relationships from specific studies, and undermines binary measures of alliance participation in general studies.

Second, alliance members have different goals. Some states have extensive foreign policy ambitions, while others focus on defending their territory. My argument incorporates alliance heterogeneity and differences in member capability to explain how alliance participation is associated

with military spending.

3 Argument

My argument predicts growth in military spending. Annual growth in spending is equal to changes in spending as a share of the previous year's budget. So growth in military expenditures is calculated as:

Growth Mil. Expend =
$$\frac{\text{Change Mil. Expend}_t}{\text{Mil. Expend}_{t-1}}$$
 (1)

Growth in spending is an appropriate theoretical quantity of interest. By benchmarking changes in spending to a states budget, we get a better sense of the opportunity costs of spending for that state.

Predicting growth in military expenditures changes the interpretation of alliance participation. Only negative growth in spending reduces the level of military expenditures. Alliance participation can lower the growth of defense budgets without reducing the level of military expenditures. Increases and decreases in the level of spending from changes in treaty strength are relative to counterfactual spending at another level of strength (Fearon, 1991). For example, major powers would spend more on the military if an alliance was weaker, because the treaty would lead to higher spending growth.

While most studies focus on changes or levels of military expenditures, growth in military spending is a better outcome measure. The level of military spending rises over time for most states, especially in longer panels. Because growth is calculated relative to prior expenditures, it facilitates comparisons across diverse states and time periods. Using growth in spending in regression models also limits the risk of spurious inferences from non-stationarity in military spending.

The argument proceeds as follows. First, I describe key characteristics of states and the actions they take for foreign policy gain. Then, I summarize the sources and implications of alliance treaty strength. Last I describe how alliance formation and maintenance play out differently for major

and non-major powers as treaty strength changes.

3.1 States and Alliances

My argument focuses on the behavior of states. I assume states value both domestic consumption and foreign policy goods. The two major foreign policy goods are security and influence.

Security entails freedom from foreign aggression- the ability to hold territory and consume wealth as a state sees fit. Influence is the ability of a state to shape international relations in beneficial ways. As we will see, more capable states emphasize influence. To secure foreign policy goods, states can increase their military capability or participate in alliances.

Expanding military capability requires additional growth in military spending. I assume military spending has opportunity costs—funds spent on the military cannot be used for other goods. Greater military spending reduces domestic consumption (Fearon, 2018).

The opportunity costs of military spending are also decreasing in state size, as larger states have a lower tax price of spending, and benefit from economies of scale. As the number of tax-payers falls, the marginal cost per taxpayer of an increase in military spending rises (Dudley and Montmarquette, 1981). For economies of scale, producing more defense goods lowers the cost of additional units (Moravcsik, 1991; Alesina and Spolaore, 2006). Thus, larger states have lower marginal costs of military spending.

I assume alliances are a costly signal of shared foreign policy interests. Alliances promise military support in the event of conflict. A formal hands-tying signal generates costs for members and a credible commitment to intervene (Fearon, 1997; Leeds, 2003).

Alliances structure exchange among members. Potential alliance partners face a contracting problem— to realize gains from exchange they must address opportunism and distributional problems (Williamson, 1985; Koremenos, Lipson and Snidal, 2001). Like many other institutions, alliances are a kind of contract between states (Lake, 1996; Benson, Meirowitz and Ramsay, 2014). Members give up some autonomy and provide other goods in exchange for foreign policy benefits.

Alliance members can participate in symmetric or asymmetric exchanges Morrow (1991). In a symmetric treaty, both members receive the same good. In an asymmetric exchange, members receive different goods.

Alliance participation includes formation and maintenance (Snyder, 1997). Formation is the initial exchange. After a treaty forms, members bargain over the distribution of costs and benefits and work to maintain the treaty as their interests change.

Alliance treaties include a wide range of commitments. States design different treaties to address formation and maintenance. The formal strength of commitment is a crucial difference between treaties.⁴ Treaty content provides information to members and potential adversaries (Leeds, 2003).

3.2 Treaty Strength

Not all alliances make robust formal promises. Strong commitments stipulate deep and costly cooperation among members. Allies incur higher costs from forming the a strong treaty and risk high costs from breaking it as well. Therefore, treaty strength depends on the costs of treaty abrogation and sunk costs promises.

The costs of violating a treaty promise are a function of what kind of support was promised. Commitments to fight expose states to the risk of bearing the costs of war on behalf of their ally. Violating these promises has important audience and reputation costs (Gibler, 2008; Crescenzi et al., 2012; Mattes, 2012).

Placing few conditions on intervention further strengthens military support commitments (Benson, 2012). Expansive promises of provide military support make treaty invocation more likely. Once a treaty is invoked, unlimited promises of support can either be violated or honored—there is no way to disavow the obligation.

Unlike the potential costs of treaty abrogation, sunk costs apply whether or not military support

⁴I use treaty strength as shorthand for the costliness and depth of formal promises in an alliance treaty.

is invoked. Allies incur these costs by joining the treaty. An essential sunk cost is that backing one state often precludes alliances with potential antagonists (Snyder, 1997). Alliances can include wide range of sunk cost promises including aid, economic concessions, integrated military command, basing rights, international organization formation and concluding other agreements.

All of these commitments add greater depth to the agreement by expanding ties among partner states. Sunk cost promises create a web of additional obligations to reinforce the core promise of military support. By strengthening the treaty, sunk costs increase its credibility.

Higher sunk costs and costs of abrogation make strong formal treaties more credible. That credibility produces more foreign policy benefits for members. But those gains come at the cost of reduced freedom of action.

Greater treaty credibility follows from states imposing restrictions on themselves and limiting their ability to behave opportunistically. In a credible treaty, there is less doubt a state will honor its alliance commitments. That increased certainty implies that partners have ruled out other potential actions. Forming an alliance makes nonintervention more costly, rules out alternative treaties and requires coordination among members (Snyder, 1997). How states change their growth in military spending through the benefits and costs of stronger treaties depends on what they use alliances for.

The impact of greater treaty strength on growth in military spending depends on state capability. Less capable states focus on territorial security through military spending and alliances. More capable states use alliances and military spending to expand their influence in international relations. While some states focus on immediate security, others pursue more ambitious foreign policy goals (Fordham, 2011; Markowitz and Fariss, 2017).

3.3 Major Powers

Major powers are the most capable states in the system. These states have a wider range of foreign policy interests than other states due to their economic ties, size, and ability to pursue a wide range of issues. Therefore, major powers pursue interests beyond their immediate security. Major powers seek influence— changing the behavior of other states in beneficial ways and reshaping international relations to match their interests.

While increasing their influence, major powers face lower opportunity cost of defense spending. Their economic size and capability reduces the tax price of spending and generates economies of scale. As a result, major powers are more willing to grow their defense budget in pursuit of foreign policy gain.

Major powers gain influence by changing the expected outcome of conflicts between other states. How much influence a major power has depends on how likely they are to intervene and the amount of capability they bring to bear. Expressed as an abstract equation, influence is a product of the probability of intervention and capability: Influence = Change War Outcome = Probability Intervention × Capability.

Building influence requires a mix of military spending and alliances. Alliances increase the probability of intervention. Military spending adds capability.

For major powers, alliances and military spending are complementary policies. Growth in military spending makes alliances more effective and valuable. Supporting allies and maintaining influence will often require greater growth in military spending from major powers.

Therefore, major powers form alliances to provide military support in exchange for influence over their partner. This exchange is especially pronounced in asymmetric treaties between major and non-major powers (Morrow, 1993). In return for protection, non-major powers surrender some autonomy.

Symmetric exchange with other major powers also increase major power influence. While gaining a little territorial security, partners in these treaties dramatically increase their ability to reshape international relations. Clarifying alignment defines potential spheres of influence and creates expectations of support on other issues (Snyder, 1997).

Once major powers form an alliance, their increased influence comes at the cost of greater involvement abroad. Ongoing effort is needed to manage alliance partners and maintain commit-

ments. These "foreign entanglements" build influence at the cost of freedom of action.

Major powers balance entanglement and influence in alliance treaty design by adjusting the depth of their formal commitments. Strong alliance treaties provide increase both influence and entanglement. When major powers prioritize influence through alliances, they will make stronger formal commitments. But when they fear entanglement abroad, they will form weaker formal treaties. The depth of a formal commitment then alters how major powers manage their alliances.

Major powers must address fear of abandonment and distorted incentives in junior partners to maintain their treaties. Because major powers provide large amounts of capability, their partners have some fear of abandonment. Ongoing investments in military capability help major powers reassure their allies, but these investments distort allied incentives (Lake, 1996, 2009). Given the opportunity, allied states have incentives to reduce military spending and rely on their allies for protection.

The dilemmas for major powers is simple— they must reassure their allies without bearing overwhelming costs. Too much reassurance allows partners to reduce defense expenditures, placing more of the burden of providing capability on major powers. Too little reassurance leads allies to question the credibility of the alliance itself, jeopardizing influence.

So long as influence from a treaty outweighs the costs of maintaining it, major powers cannot credibly threaten to abandon free-riding allies. But adding depth to a treaty provides other ways to maintain a treaty. Forming a strong alliance with multiple costly promises gives major powers more leverage over partners. Instead of threatening to abandon the treaty, major powers can withhold other promises of cooperation.

Aid, economic agreements or integrated military command can all be made conditional on adequate defense effort through issue linkage strategies. Most sunk costs promises are ongoing commitments, not one-shot infusions of cash. Providing these side-payments and explicitly connecting them to the alliance can offset the costs of greater defense effort for allies. Failing to make promised payments can also impose costs on allies without destroying the treaty.

Strong formal commitments give major powers more influence through greater credibility during formation and additional bargaining leverage in alliance maintenance. That extra influence can substitute for growth in spending. By having allies maintain their growth in defense spending and providing extra credibility, strong formal commitments reduce the need to grow military spending to back a treaty. Strong and weak treaties can provide the same amount of influence, but weaker treaties will require additional defense spending.

3.3.1 Examples

There are several examples of how major powers combine alliance strength and defense spending to generate influence. After World War II, the UK faced acute economic challenges while attempting to influence in the Middle East. "In securing a victorious outcome to the war, the British had severely overstrained themselves" (Kennedy, 1987, pg. 367) The exertions of World War II bankrupted the UK economy, but the UK attempted to maintain an expansive foreign policy (Mayhew, 1950).

Despite their economic constraints, Britain wanted to secure the Suez Canal and oil (Rahman, 1982). Britain did not have the military capability to compete with the US and USSR. Instead, they created strong alliances with Jordan (ATOPID 3125), Libya (ATOPID 3235) and Iraq (ATOPID 3280). In return for basing rights, the UK promised aid, committed to defense consultations, and promised to resolve disputes through the International Court of Justice. Before World War II, London had exerted influence through a preponderance of capability in the region. Afterward World War II, the UK used strong alliance treaties to maintain influence in the Middle East without spending as much on the military.

US foreign policy after World War II also illustrates substitution between treaty strength and capability as tools of influence. The US balanced between fear of "foreign entanglements" and maintaining influence. The extensive network of alliance commitments to contain the USSR required massive defense outlays (Fordham, 1998). This was especially true because the US made a

series of relatively weak formal commitments.

Most US treaties contain few formal promises besides defense against aggression. A note-worthy exception is a 1959 alliance with Iran (ATOPID 3365). The US supplemented its defense commitment with formal promises of military aid, which was unusual. Unlike NATO other treaties with no formal promises of aid, the US did not establish permanent bases in Iran. The aid and defense commitment reinforced US influence in Iran.

These examples and the above verbal logic suggest that greater treaty strength should reduce growth in major power military spending from alliance participation. Consider a hypothetical major power choosing between a strong and weak formal treaty to achieve a particular level of influence. A strong treaty would provide the same amount of influence with less growth in defense expenditures. Therefore, growth in spending will be positive for major powers, and decreasing in treaty strength.

HYPOTHESIS 1: As alliance treaty strength increases, growth in major power military spending will decrease.

The logic of treaty strength and major powers also suggests that even relatively weak treaties should lower growth in major power defense spending. To achieve the kind of influence most major powers seek without alliances would require massive defense budget growth. A weak alliance is stronger than no alliance.

Hypothesis 1 should not apply to non-major powers. These states have different goals and constraints.

3.4 Non-Major Powers

Non-major powers emphasize immediate security. Small states use alliances and military spending to protect their homeland. In doing so, they have greater opportunity costs of military spending.

Small states face higher marginal costs of military spending. They are less able to access economies of scale in defense and the tax price of military spending is higher. To offset these opportunity costs, non-major power states will reduce growth in defense spending when possible.

Relying on allied capability is one way for non-major powers to maintain their security and lower military expenditures. In general, greater allied capability should reduce growth in non-major power military spending. Even so, participation does not always lead to lower growth in military spending. Non-major powers must balance reduced defense spending with the risk of losing access to the benefits of alliance participation.

Growth in military spending is a more serious constraint on domestic consumption for non-major powers. But they also must consider their security. Losing a war can lead to the elimination of non-major powers as a state, at which point they would have no control over domestic consumption at all (Fazal, 2011).

Therefore, non-major powers balance security and freedom to determine domestic consumption while forming alliances. Greater treaty strength increases security, but limits freedom to adjust military expenditures. Increased security follows from the credibility of a strong treaty. Limited freedom of action is the result of increased allied influence and deeper ties.

When security is more important, non-major powers will accept lost freedom of action. When external threats are less acute and domestic consumption is more important, weaker treaties will prevail. Alliance maintenance reinforces this tradeoff for non-major powers.

Non-major powers face the same issue as their partners— a need to signal ongoing commitment even as interests change. Because it is costly maintaining growth in military spending is a useful signal of commitment. As treaty strength rises, non-major powers face more inducements to signal commitment through growth in military spending.

Strong treaties are a more valuable source of security, so non-major powers are more willing to bear the opportunity costs of military spending. Deeper ties also give allies more influence to demand continued defense effort. Providing more security increases allied dependency. Influence

extends to more coercive bargaining that uses side payments from formal alliance promises as leverage.

In a weak treaty, non-major powers have more freedom of action, while still gaining some security. Allies have less bargaining leverage, because their main threat is withdrawing from the treaty. Threats to tear up an alliance are only credible if states interests have changed dramatically, which reduces the value of the treaty for all partners. These threats are usually incredible, which limits allied leverage.

NATO is an excellent example of these dynamics. The NATO treaty makes few costly promises besides the core defensive commitment in Article 5. The US has threatened to abandon NATO in response to European "free-riding," but those threats were not credible. US interests in containing the USSR trumped irritation with allied free-riding. But without other formal treaty commitments to influence NATO members, the US had few ways besides public statements to check allied desires to reduce growth in military spending.

As a result, non-major powers will reduce growth in military spending more under weak treaties. Weak formal commitments still provide more security than no alliance. But as treaty strength rises and constrains non-major powers' freedom of action, growth in military spending will rise.

The example of NATO and the verbal logic above suggest growth in non-major power military spending is increasing in alliance treaty strength. Weak commitments provide security and enough freedom of action for non-major powers to lower growth in military spending and increase domestic consumption. Greater treaty strength increases treaty value and allied influence, leading to higher growth in military expenditures.

HYPOTHESIS 2: As alliance treaty strength increases, growth in non-major power military spending will increase.

Hypotheses 1 and 2 compare strong and weak treaties, so the the research design must compare

treaties and measure alliance treaty strength. I use a measurement model to operationalize treaty strength and link alliances with state military spending using a multilevel model. The next section describes the research design in more detail.

4 Research Design

This research design makes two contributions. First, I develop a latent measure of alliance treaty strength. Then I employ that measure in a multilevel model, connecting alliance-level variation with state-level outcomes. To examine differences between major and non-major powers, I estimate the multilevel model in separate samples of major and non-major powers from 1816 to 2007. The next section describes my measure of alliance treaty strength.

4.1 Measuring Alliance Treaty Strength

Observed alliance promises reflect the underlying strength of the treaty. A stronger alliance contains more costly promises. Therefore, I use observed alliance characteristics to infer treaty strength.

Treaty strength and credibility depends on the costs of abrogation and other costly promises in the pact (Leeds, 2003). The costs of abrogation are tied to core commitments of defensive or offensive military support, and conditions on support.⁵ Sunk costs promises in alliances include integrated military command, forming international organizations, basing rights, promises to make other agreements, and economic or military aid.

Conceptualizing observed treaty conditions as indicators of underlying strength permits several measures of treaty strength. One is choosing a crucial indicator of treaty strength, such as unconditional military support, and coding measures of its presence. Treaty strength is multidimensional, however, so this measure is too coarse.

⁵Some alliances promise only neutrality, consultation, or non-aggression, rather than military support.

Another option is constructing an additive index of treaty strength. Treaties with more costly promises would have higher index values and greater strength. This assumes each indicator is equally important, which is unlikely. There are less restrictive ways to construct a measure.

Latent variable modeling is the best way to measure alliance treaty strength. It does not reduce strength to one alliance characteristic, or apply arbitrary weights to an index. Instead, latent variable models use observed treaty characteristics to infer an unobserved concept.

Measurement models have a rich history in political science (Clinton, Jackman and Rivers, 2004; Treier and Jackman, 2008; Fariss, 2014). Benson and Clinton (2016) use the mixed factor analysis model of Quinn (2004) to measure alliance scope, depth and capability. Like Benson and Clinton, I employ a latent variable model, but with another concept and estimator.

I use the Bayesian Gaussian Copula Factor Model of Murray et al. (2013) to measure alliance treaty strength. Murray et al's model improves on mixed factor analysis for continuous, ordinal, and binary observed data by relaxing distributional assumptions. With discrete observed variables and non-Gaussian latent variables, the dependence among the latent variables and their marginal distributions are both influenced by the latent variables. Their model encodes the dependence structure of multivariate latent data using a copula⁶ and expresses the latent variables and factor loadings as a series of latent normal variables. This semiparametric approach breaks the dependence between the latent factors and marginal distributions.

Beyond the semiparametric component, this measurement model employs a general factor analytic approach. Factor analysis estimates the association between observed variables and some latent factor. Each observed variable has a factor loading—the association between the observed variable and the latent variable. Like standardized regression coefficients, factor loadings range from -1 to 1, so observed variables are positively or negatively correlated with the latent variable.

For each observation, a linear combination of observed alliance characteristics predicts latent

 $^{^6}$ Copulas are distribution function on $[0,1]^p$ where each univariate marginal distribution is uniform on [0,1]. This function encodes the dependence structure of a multivariate distribution.

treaty strength, like a regression with an unobserved outcome. I took alliance characteristics for all 745 alliances in the alliance-level ATOP data (Leeds et al., 2002). Indicators of treaty strength are divided between the potential costs of abrogation and sunk costs commitments. The potential costs of abrogation depend on promises of defensive support, offensive support, neutrality, consultation, non-aggression and unconditional military support. Sunk costs include military aid, economic aid, bases, international organization formation, integrated military command, as well as promises to form new agreements in multiple issue areas and to forgo competing alliances. My argument suggests there is one latent factor underlying variation in all 13 indicators.

The Bayesian Gaussian copula factor model generates posterior distributions for the factor loadings and the latent factor. I used Parameter expanded Gibbs sampling, the default generalized double Pareto (GDP) prior, 10,000 burn-in iterations of the MCMC chain, and 20,000 samples thinned every 20 observations to ensure convergence. Because treaty strength is the main quantity of interest for this paper, I focus on the posterior distributions of the latent factor.

Each alliance has a unique posterior distribution of the latent strength measure. I use the mean of that posterior to measure treaty strength— the mean captures the expected strength of a treaty, given its formal commitments. Figure 1 describes the latent measure for ATOP alliances with military support from 1815 to 2016. I focus on treaties with military support because prior studies of alliance participation and military spending emphasize these treaties.⁷

As the top panel of Figure 1 shows, there is a wide range of strength among treaties with military support. Most treaties are concentrated between .5 and 1.5 on the latent scale, but there are 40 or so treaties that are stronger or weaker. The bottom panel of Figure 1 plots the posterior means and uncertainty in those estimates against the start year of the treaty. Even after accounting for posterior uncertainty, it is possible to distinguish between many stronger and weaker formal treaties.

⁷ I estimated the measurement model on all alliances to capture the contributions of defensive and offensive conditions to treaty strength relative to weaker promises.

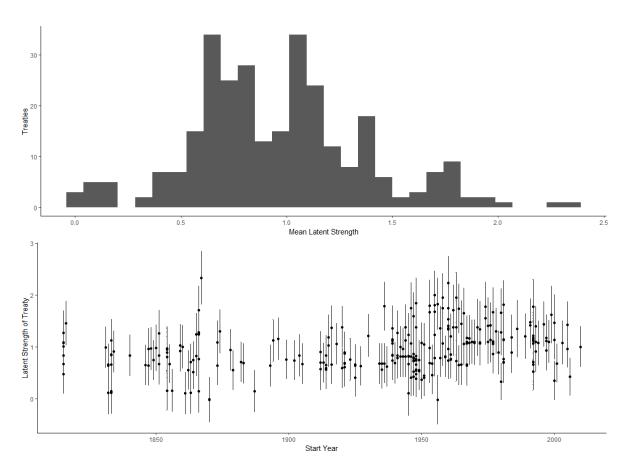


Figure 1: Summary of latent measure of alliance treaty strength for 289 alliances promising military support from 1816 to 2016. The top panel is a histogram of the expected of alliance treaty strength. The bottom panel plots mean treaty strength (points) and the standard deviation (error bars) against the start year of the treaty.

The values of the latent strength measure are not intrinsically informative. Differences between treaties on the latent strength scale are meaningful, however. The mean of treaty strength is 0.92, and the median is 0.90. The median treaty is an 1854 agreement between Austria, France, and Britain against Russia in the Crimean war (ATOP ID 1180).

The weakest treaty is an 1870 neutrality and offense pact between France and Britain (ATOPID 1300), which Britain used to protect Belgian neutrality during the Franco-Prussian war. Britain formed a similar and equally weak treaty with Prussia at the same time, which scores almost exactly the same on the latent measure. Both treaties have only offensive and neutrality promises, conditional on France and Prussia respecting Belgian neutrality.

NATO (ATOPID 3180) has mean latent strength of 0.73, placing it in the third quartile of treaty strength. NATO's main costly provisions are the defense obligations in Article 5 and establishing the Council. According to the ATOP coding sheet for NATO, "There are numerous bilateral agreements among NATO members re: military aid, bases, etc. but they do not qualify as separate alliances, nor are they part of the overall NATO structure." So while the NATO treaty is above average in strength, many additional costs fall outside the formal treaty.

The three strongest treaties are an 1867 alliance between Prussia and Hesse (ATOPID 1290), a 1955 treaty between Greece and Turkey governing relations in Cyprus (ATOPID 3400) and the United Arab Republic (ATOPID 3300). All of these treaties supplement promises of military support with costly promises of cooperation. In the alliance between Greece, Turkey, and Cyprus, two historical enemies set up military aid, integrated military command, international organizations to mange relations on the island. These extra costs made the commitment to defend Cyprus more credible.

These examples show some face, concept, and discriminant validity of the latent measure. The UAR is a more costly commitment than a functional promise to respect Belgian neutrality. The weakest treaties make few costly promises beyond military support, matching my conceptualization of treaty strength. This measure makes a clear distinction between weak and strong

commitments. I now describe how and why I use a multilevel model to estimate the association between this measure of treaty strength and alliance members' military spending.

4.2 Multilevel Model

Multilevel modeling incorporates elements of the specific and general research designs in previous research. Specific studies focus on responses to allied spending in particular treaties, while general studies in panel data rely on coarse aggregates of alliance participation. In this model, I estimate the specific impact of each alliance on member's military spending and the general association between treaty strength and military expenditures. To overcome common statistical challenges, I fit this model using Bayesian estimation in STAN (Carpenter et al., 2016).⁸

The multilevel model is more complex than traditional approaches. But added complexity has several benefits. Multilevel modeling connects the argument and research design. My predictions compare strong and weak treaties and an alliance level regression in this multilevel model contains a corresponding coefficient. Relying on a state-level proxy for alliance strength generates different comparisons and changes the variation in a key independent variable which may produce misleading inferences (McElreath, 2016).

Multilevel modeling matches the structure of the data. Alliances and states are separate levels of analysis. Connecting the alliance and state level of analysis allows us to infer how alliance variation impacts states' military expenditures.

Added complexity facilitates comparisons between alliances. An alliance-level regression estimates how multiple alliance characteristics are correlated with alliance strength and military spending. Partial pooling produces reasonable estimates of the impact of each alliance on members' military spending. Comparing patterns in these alliance-specific coefficients provides additional evidence to examine Hypotheses 1 and 2 as well as the importance of treaty strength.

This multilevel model connects two distinct regressions. The base is a state-level regression,

⁸See the appendix for details of the weakly informative prior distributions and evidence of convergence.

which is similar to a random effects panel data regression. A second alliance-level regression predicts parameters in the state-level regression, like an interaction.

The state-level regression starts with a distribution for the outcome:

$$y \sim student_t(\mu, \nu, \sigma)$$
 (2)

y is growth in military spending. I model growth in spending using a t-distribution with degrees of freedom ν to address outliers. σ is analogous to the error term in a frequentist regression—this captures unexplained variation in spending growth. μ , the mean of the outcome, depends on several covariates.

$$\mu = \alpha + \alpha^{st} + \alpha^{yr} + \mathbf{W}\gamma + \mathbf{Z}\lambda \tag{3}$$

Growth in spending is a function of an overall intercept α , state and year varying intercepts α^{st} and α^{yr} and a matrix of state-level control variables **W**. These components are a standard random effects model. The $\mathbf{Z}\lambda$ term is the innovation adding alliance participation.

Z is a matrix of state participation in alliances. Columns correspond to alliances, and rows to state-year observations. If a state is not part of an alliance, the corresponding cell of the matrix is zero. If a state is part of an alliance in a given year, the corresponding cell is the log of total allied military spending.

I use total allied spending in the alliance participation matrix because more capable alliances provide extra benefits. Increasing allied capability makes promises of military support more valuable (Johnson, Leeds and Wu, 2015). Treaty design then modifies the impact of allied capability. This measure also compares states inside and outside the treaty— allied spending only applies to treaty members. So estimates of λ also incorporate a change from no allied capability to some.

Because the non-zero elements of Z are allied spending, the λ parameters capture alliance members' responsiveness to greater allied capability. Each alliance has a unique λ , which I give a common distribution. The shared distribution assumes alliances are similar but different in how

they impact growth in military spending.

The second part of the multilevel model uses alliance characteristics to predict how allied spending is associated with growth in military spending. The λ parameters are the dependent variable in an alliance-level regression which includes treaty strength. Therefore, I focus interpretation on this alliance-level regression, where:

$$\lambda \sim N(\theta, \sigma_{all}) \tag{4}$$

and

$$\theta = \alpha_{all} + \beta_1 \text{Treaty Strength} + \mathbf{X}\beta \tag{5}$$

In this alliance-level regression, \mathbf{X} is a matrix of alliance-level control variables and α_{all} is the constant. Adding σ_{all} means predictions of λ are not deterministic—the alliance level regression contains an error term. Coefficients in the alliance-level regression are like marginal effects in an interaction. A change in treaty strength modifies λ , which alters growth in military spending. Hypothesis 1 predicts β_1 will be negative among major powers, and Hypothesis 2 expects β_1 will be positive for non-major powers.

Consider one observation as an example of how the model works. Growth in Argentina's military spending in 1955 depends on Argentina's economic growth, political regime, conflict participation, and rival military spending. Argentine participation in the Rio Pact and OAS also changes growth in spending through allied capability.

Argentina 1955 = Overall mean + Argentine Intercept + 1955 Intercept + Argentine Characteristics + λ_{OAS} * OAS Expenditure + λ_{Rio} * Rio Pact Expenditure

(6)

 λ_{OAS} and λ_{Rio} are modified by the alliance level regression. The institutional design and mem-

bership of these treaties alter the λ parameter. Alliances Argentina did not participate in have no impact on growth in military spending.

The multilevel model is interactive, which is appropriate for my conditional argument. Alliance characteristics modify the impact of allied spending on growth in state military spending. I now describe the sample and covariates in the analysis.

4.3 Sample and Covariates

I estimate this model on two samples of states from 1816 to 2007. Alliance participation data comes from the ATOP project (Leeds et al., 2002). I focus on participation in defensive and offensive treaties, because prior studies of alliances and military spending emphasize these treaties.

My argument suggests that major and non-major powers use alliances for different purposes. Major powers focus on influence, non-major powers emphasize immediate territorial security. Therefore, the entire data-generating process connecting alliance participation and military spending is different for major and non-major powers. To capture these differences, I estimate the model in separate samples- one sample of major powers, the other of non-major powers. I employ the classification of major power status from the Correlates of War Project.

The non-major power sample contains 8,668 observations in the state-level regression, and 192 alliances. There are 930 major power observations and 148 alliances. Though the major power sample is smaller and has fewer states, Bayesian estimation and partial pooling should give plausible estimates (Stegmueller, 2013).

The dependent variable is growth in military spending. I calculated growth in spending using the Correlates of War Project's measure of military spending (Singer, 1988). Growth in spending is equal to changes in spending as a share of the previous year's military spending, so changes are relative to previous levels of spending.

In the state-level regression, I control for several correlates of alliance participation and military spending. State-level covariates include GDP growth (Bolt et al., 2018), regime type, international

war (Reiter, Stam and Horowitz, 2016), civil war participation (Sarkees and Wayman, 2010), annual MIDs (Gibler, Miller and Little, 2016), rival military spending (Thompson and Dreyer, 2012) and a dummy for Cold War years. I include growth in GDP instead of levels of GDP because GDP levels are non-stationary, and economic growth shapes the opportunity costs of military spending (Kimball, 2010; Zielinski, Fordham and Schilde, 2017).

The alliance-level regression contains the mean of the latent treaty strength— the key independent variable. Other alliance level variables include the number of members and share of democracies in a treaty at time of formation (Chiba, Johnson and Leeds, 2015). I also control for superpower membership— whether the US or USSR participated in a treaty during the Cold War. Two dummy indicators of wartime alliances and asymmetric obligations (Leeds et al., 2002) complete the alliance-level regression specification.

Democratic membership is associated with limited obligations (Chiba, Johnson and Leeds, 2015) and lower military spending (DiGiuseppe and Poast, 2016) in alliances, making it a particularly important alliance-level control. State and alliance-level controls for threat and conflict participation capture situations where states are more likely to seek allies. The next section describes the results.

5 Results

Results are based on 2,000 total samples from four chains, with 1,000 warm-up iterations. To facilitate model fitting, I employed a non-centered parameterization of the varying intercepts and a sparse matrix representation of **Z**. Standard convergence diagnostics indicate the chains adequately explored the posterior density.⁹

Because I use Bayesian modeling to estimate the association between treaty strength and growth in military spending, there are no conventional indicators of statistical significance. In-

⁹See the appendix for more details on convergence.

stead, each coefficient has a posterior distribution—the likely values of the coefficient conditional on the prior and observed data. Thus I calculate the negative and positive posterior probability for the two treaty strength coefficients to assess Hypotheses 1 and 2.

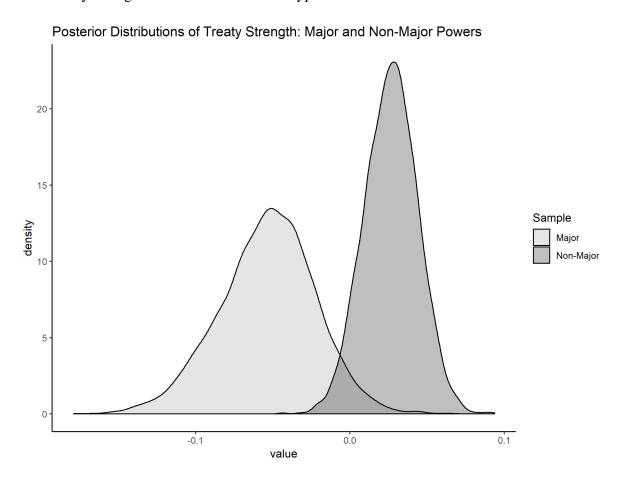


Figure 2: Posterior density of treaty strength coefficient in major and non-major power samples, 1816 to 2007. 96% of the major power posterior mass is negative. 94% of the non-major power posterior mass is positive.

Figure 2 plots the full posterior density of the treaty strength coefficients in the major and minor power samples. 10 96% of the posterior mass for major powers is negative. 94% of the posterior mass for minor powers is positive. There is little overlap between these two posteriors—there is a 99% chance that the association between treaty strength and military spending is larger for minor powers than major powers.

¹⁰The smaller sample for major powers produces more variance in all the coefficient estimates.

These two coefficient estimates match the predictions of Hypotheses 1 and 2. For major powers, there is a 96% chance increasing treaty strength is associated with lower growth in military spending. There is a 94% chance greater treaty strength is associated with higher growth in military spending for non-major powers.

How substantively important is treaty strength? Among major powers, the mean of the treaty strength coefficient is -0.05, and median growth in military expenditures is 0.04.¹¹ So a one-unit increase in treaty strength nearly offsets the typical annual growth in military spending.

For non-major powers, the mean of the treaty strength coefficient is 0.03, and median growth in military expenditures is 0.06. Greater treaty strength increases growth in minor power military expenditures by about half of typical growth. Higher treaty strength has a large substantive effect, relative to the scale of the data.

We can also examine how much changing treaty strength influences on the overall association between changes in allied spending and growth in defense spending. Each λ measures the aggregate impact of changes in allied capability for a treaty. If greater treaty strength has a large influence on the λ parameters, there will be a clear trend in the value of λ across the range of alliance treaty strength. We should observe a negative trend in the expected value of λ as treaty strength increases in major power alliances. There will be a positive trend in λ for non-major power alliances.

Figure 3 plots the expected value of λ against treaty strength in the two samples. In the major power sample, there is a negative trend in the scatter plot. For non-major powers, the trend is positive. In both samples, the correlation between mean λ and treaty strength is statistically significant.

These trends match the underlying logic of Hypotheses 1 and 2. Weaker treaties tend to increase growth in defense spending for major powers, but that positive correlation falls as treaty strength

¹¹The median is a better summary of the dependent variable because large positive and negative outliers influence the mean.

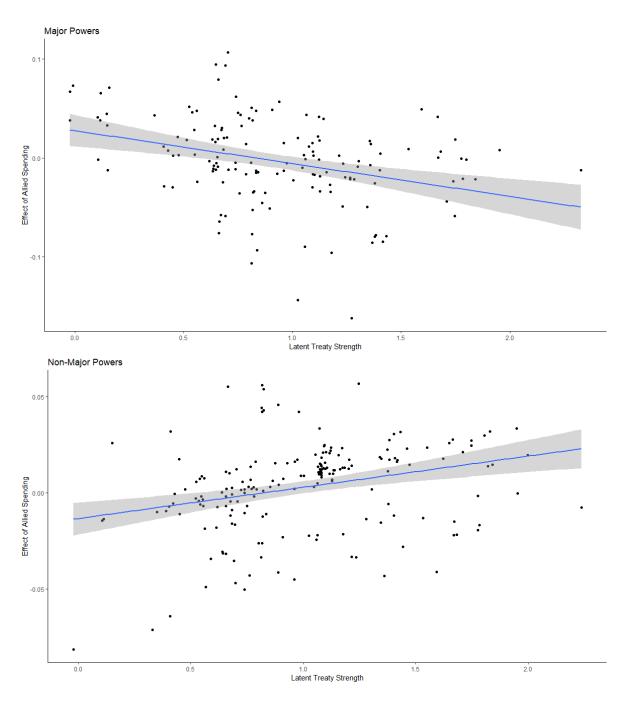


Figure 3: Scatter plots of trends in mean λ parameters and treaty strength. λ is the total impact of alliance participation on growth in military spending. The top panel is major powers, where this is a negative trend between λ and treaty strength. In the bottom panel the same trend is positive for non-major powers. Trend lines estimated using linear regression.

increases. In non-major powers, the trend starts negative and becomes more positive as treaty strength rises. Other alliance characteristics ensure trends in strength and the aggregate impact of a treaty are probabilistic— not all treaties conform to the expectations of decreasing or increasing growth in spending.

Because λ captures the total impact of an alliance, this pattern suggests that increasing alliance strength has an important role. Even after accounting for other alliance characteristics, alliance strength drives the overall effect of allied spending down for major powers, and up for non-major powers.

6 Discussion

The results conform to expectations of Hypotheses 1 and 2. Increasing treaty strength is positively associated with growth in military spending in non-major powers. Greater treaty strength is associated with lower growth in military spending for major powers, who use treaty strength and military capability as substitutes while seeking influence.

These results contribute to the debate over whether alliance participation increases or decreases military spending. Dissension between the force multiplier and foreign entanglement views of alliances is based on competing claims about the purposes of alliances. These mutually exclusive assertions are inaccurate.

My findings and argument suggest claims alliance participation only increases or decreases military spending are inappropriate. Instead, the association between alliance participation and growth in military spending depends on alliance member size and treaty strength. Alliance participation has heterogeneous effects because major powers and non-major powers employ treaties for different purposes.

The force multiplier perspective applies best to security-seeking non-major powers. But these states cannot reduce growth in military spending in all alliances, because strong treaties constrain

their freedom of action. Alliances are a foreign entanglement for major powers. But additional entanglement in a strong treaty provides more influence, attenuating the positive correlation between alliance participation and growth in military spending.

Comparing my results to prior evidence requires renewed attention to specific and general research designs. Some general studies compare states in a particular kind of alliances to those outside the treaty. Most specific studies responsiveness to allied military spending.

How do my results fit with other evidence on alliance participation and military spending? My key coefficient estimates compare strong and weak treaties, not states with a treaty to those without. However those estimates are like marginal effects- increasing treaty strength alters the effect of alliance participation.

 λ measures the impact of increasing allied spending *for states in a treaty*. These parameters capture the impact of alliance participation only for treaty members. Therefore, a comparison between treaty members and non-members is included in the statistical model. Greater treaty strength decreases the association between alliance participation and growth in military expenditures for major powers, and increases it for non-major powers.

This paper has several limitations. The argument does not address the domestic political economy of military spending. My argument reduces domestic politics to an assumption that military spending has opportunity costs, which are decreasing in state size.

For the research design, measures of military spending contain substantial measurement error. There is also a great deal of missing data in the 1816–2007 time frame of this study. I plan to check the robustness of my results to these issues by adding measurement error to the outcome and imputing missing data.

The multilevel model only incorporates time-invariant alliance characteristics, save for changing capabilities in the membership matrix. So I measure share of democratic members and the number of members at time of formation. Allowing time-varying alliance characteristics might improve the statistical model, but would require altering the model structure.

Strategic alliance design is the last major weakness of the research design. Non-random selection into different kinds of alliances might produce systematic differences between members that are not controlled for in my statistical model. I attempted to control for correlates of alliance treaty strength, especially democracy, but oversights are possible.

7 Conclusion

This paper presented an argument and empirical evidence linking alliance participation and military expenditures. I explain when alliance participation is associated more or less growth in military spending, addressing a debate between the force entanglement and foreign entanglement views of alliances. For major powers, greater treaty strength leads to lower growth in spending. Non-major power growth in spending is positively correlated with alliance treaty strength. I provide evidence for these predictions using a new measure of alliance treaty strength and a multilevel model.

Growing military spending growth has distributional consequences in the domestic economy. So the design of international alliances alters the domestic political economy of member states. Non-major powers confront the opportunity costs of additional defense spending in strong treaties. Major powers can use strong treaties to reduce to domestic costs of their foreign policy ambitions.

There are several next steps for research on alliances and military expenditures. One is extending the argument to other alliance characteristics. If major and non-major powers employ alliances for different ends, then other alliance characteristics may have different impacts on military spending. Large and small states should use wartime and asymmetric treaties differently, for instance.

Another task for future research is making more detailed comparisons of the λ parameters. Each λ captures the aggregate impact of alliance participation for individual treaties. As such, these parameters are a novel measurement, and additional evidence of when alliance participation

increases or decreases military spending.

The multilevel model estimates alone do not establish causality (Seawright, 2016). But the λ parameters can guide case selection for a process-tracing analysis to corroborate the regression results. One possible design is selecting the five largest and smallest λ values for major and minor powers, and determining whether the connection between alliance participation and military expenditures matches the theoretical process.

The research design in this paper applies to other international relations questions. If scholars are interested in a class of international organizations and states are members in multiple organizations, the multilevel model incorporates multiple membership. For example, international political economy scholars could apply this model to trade agreements. Studies of international law could examine the impact of membership in different conventions and international organizations on human rights.

The argument and evidence suggests that major and non-major powers each face a tradeoff in alliance treaty design. Major powers tradeoff between entanglement and greater influence in strong treaties. Non-major powers sacrifice freedom of action for greater security as treaty strength rises.

These twin tradeoffs have important consequences for policy debates. The United States has a long history of decrying "free-riding" by allies who provide too little for their own defense (Lanoszka, 2015). But allies may be able to free-ride because the US prefers to form relatively weak alliance commitments. "Entangling alliances" can provide greater influence to curb falling allied defense spending.

Therefore, growing institutionalization of NATO, including the agreement for all allies to spend at least 2% of GDP on defense, may be effective. However, treating alliances between major and non-major powers as a public good and decrying low defense effort as free riding, is inappropriate. Asymmetric alliances produce different goods for different members. Major powers seek influence, while non-major powers secure their homeland.

The US could use stronger formal commitments as a substitute for greater defense effort in

reassuring allies. The danger is that making stronger commitments could create a situation where obligations exceed capabilities (Kennedy, 1987). Emboldening junior partners with a strong treaty might have deterrent value (Benson, Meirowitz and Ramsay, 2014), or increase the risk of conflict (Benson, 2012).

The connection between alliance participation and military expenditures depends on state size and the strength of the treaty. Alliance participation does not exclusively increase or decrease military spending. Both the force multiplier and foreign entanglement views of alliance participation are correct, each in different circumstances.

References

- Alesina, Alberto and Enrico Spolaore. 2006. "Conflict, defense spending, and the number of nations." *European Economic Review* 50(1):91–120.
- Alptekin, Aynur and Paul Levine. 2012. "Military expenditure and economic growth: A meta-analysis." *European Journal of Political Economy* 28(4):636–650.
- Barnett, Michael N and Jack S Levy. 1991. "Domestic Sources of Alliances and Alignments: The Case of Egypt, 1962-73." *International Organization* 45(3):369–395.
- Benson, Brett V. 2012. Constructing International Security: Alliances, Deterrence, and Moral Hazard. Cambridge University Press.
- Benson, Brett V, Adam Meirowitz and Kristopher W Ramsay. 2014. "Inducing Deterrence through Moral Hazard in Alliance Contracts." *Journal of Conflict Resolution* 58(2):307–335.
- Benson, Brett V and Joshua D Clinton. 2016. "Assessing the Variation of Formal Military Alliances." *Journal of Conflict Resolution* 60(5):866–898.
- Bolt, J, R Inklaar, H de Jong and JL van Zanden. 2018. "Maddison Project Database, Version 2018." Rebasing Maddison: new income comparisons and the shape of long-run economic development.
- Carpenter, Bob, Andrew Gelman, Matt Hoffman, Daniel Lee, Ben Goodrich, Michael Betancourt, Michael A Brubaker, Jiqiang Guo, Peter Li and Allen Riddell. 2016. "Stan: A probabilistic programming language." *Journal of Statistical Software* 20:1–37.
- Chen, Baizhu, Yi Feng and Cyrus Masroori. 1996. "Collective action in the Middle East? A study of free-ride in defense spending." *Journal of Peace Research* 33(3):323–339.

- Chiba, Daina, Jesse C Johnson and Brett Ashley Leeds. 2015. "Careful Commitments: Democratic States and Alliance Design." *The Journal of Politics* 77(4):968–982.
- Clinton, Joshua, Simon Jackman and Douglas Rivers. 2004. "The Statistical Analysis of Roll Call Data." *American Political Science Review* 98(2):355–370.
- Conybeare, John AC. 1994. "Arms versus Alliances: The Capital Structure of Military Enterprise." *Journal of Conflict Resolution* 38(2):215–235.
- Conybeare, John AC and Todd Sandler. 1990. "The Triple Entente and the Triple Alliance 1880–1914: A Collective Goods Approach." *American Political Science Review* 84(4):1197–1206.
- Crescenzi, Mark JC, Jacob D Kathman, Katja B Kleinberg and Reed M Wood. 2012. "Reliability, Reputation, and Alliance Formation." *International Studies Quarterly* 56(2):259–274.
- Diehl, Paul F. 1994. "Substitutes or Complements?: The Effects of Alliances on Military Spending in Major Power Rivalries." *International Interactions* 19(3):159–176.
- DiGiuseppe, Matthew and Paul Poast. 2016. "Arms versus Democratic Allies." *British Journal of Political Science* pp. 1–23.
- Dudley, Leonard and Claude Montmarquette. 1981. "The demand for military expenditures: an international comparison." *Public Choice* 37(1):5–31.
- Fariss, Christopher J. 2014. "Respect for Human Rights has Improved Over Time: Modeling the Changing Standard of Accountability." *American Political Science Review* 108(2):297–318.
- Fazal, Tanisha M. 2011. State death: the politics and geography of conquest, occupation, and annexation. Princeton: Princeton University Press.
- Fearon, James D. 1991. "Counterfactuals and Hypothesis Testing in Political Science." World Politics 43(02):169–195.
- Fearon, James D. 1997. "Signaling Foreign Policy Interests: Tying Hands versus Sinking Costs." *Journal of Conflict Resolution* 41(1):68–90.
- Fearon, James D. 2018. "Cooperation, Conflict, and the Costs of Anarchy." *International Organization* pp. 1–37.
- Fordham, Benjamin. 1998. Building the cold war consensus: The political economy of US national security policy, 1949-51. Ann Arbor: University of Michigan Press.
- Fordham, Benjamin O. 2011. "Who wants to be a major power? Explaining the expansion of foreign policy ambition." *Journal of Peace Research* 48(5):587–603.
- Gibler, Douglas M. 2008. "The Costs of Reneging: Reputation and Alliance Formation." *Journal of Conflict Resolution* 52(3):426–454.

- Gibler, Douglas M, Steven V Miller and Erin K Little. 2016. "An Analysis of the Militarized Interstate Dispute (MID) Dataset, 1816–2001." *International Studies Quarterly* 60(4):719–730.
- Goldsmith, Benjamin E. 2003. "Bearing the Defense Burden, 1886-1989: Why Spend More?" *Journal of Conflict Resolution* 47(5):551–573.
- Horowitz, Michael C, Paul Poast and Allan C Stam. 2017. "Domestic Signaling of Commitment Credibility: Military Recruitment and Alliance Formation." *Journal of Conflict Resolution* 61(8):1682–1710.
- Johnson, Jesse C., Brett Ashley Leeds and Ahra Wu. 2015. "Capability, Credibility, and Extended General Deterrence." *International Interactions* 41(2):309–336.
- Kennedy, Paul. 1987. The Rise and Fall of the Great Powers. New York: Random House.
- Kimball, Anessa L. 2010. "Political Survival, Policy Distribution, and Alliance Formation." *Journal of Peace Research* 47(4):407–419.
- Koremenos, Barbara, Charles Lipson and Duncan Snidal. 2001. "The Rational Design of International Institutions." *International Organization* 55(04):761–799.
- Lake, David A. 1996. "Anarchy, Hierarchy and the Variety of International Relations." *International Organization* 50(1):1–33.
- Lake, David A. 2009. Hierarchy in International Relations. Ithaca: Cornell University Press.
- Lanoszka, Alexander. 2015. "Do Allies Really Free Ride?" Survival 57(3):133–152.
- Leeds, Brett Ashley. 2003. "Do Alliances Deter Aggression? The Influence of Military Alliances on the Initiation of Militarized Interstate Disputes." *American Journal of Political Science* 47(3):427–439.
- Leeds, Brett, Jeffrey Ritter, Sara Mitchell and Andrew Long. 2002. "Alliance Treaty Obligations and Provisions, 1815-1944." *International Interactions* 28(3):237–260.
- Markowitz, Jonathan N and Christopher J Fariss. 2017. "Power, Proximity, and Democracy: Geopolitical Competition in the International System." *Journal of Peace Research*.
- Mattes, Michaela. 2012. "Reputation, Symmetry, and Alliance Design." *International Organization* 66(4):679–707.
- Mayhew, Christopher. 1950. "British Foreign Policy Since 1945." *International Affairs* 26(4):477–486.
- McElreath, Richard. 2016. *Statistical Rethinking: A Bayesian course with examples in R and Stan.* Vol. 122 CRC Press.

- Moravcsik, Andrew. 1991. "Arms and Autarky in Modern European History." *Daedalus* 120(4):23–45.
- Morgan, T Clifton and Glenn Palmer. 2006. *A Theory of Foreign Policy*. Princeton: Princeton University Press.
- Morgenthau, Hans. 1948. *Politics among Nations: The Struggle for Power and Peace*. New York: Alfred A. Knopf.
- Morrow, James D. 1991. "Alliances and Asymmetry: An Alternative to the Capability Aggregation Model of Alliances." *American Journal of Political Science* 35(4):904–933.
- Morrow, James D. 1993. "Arms versus allies: trade-offs in the search for security." *International Organization* 47(2):207–233.
- Most, Benjamin A and Harvey Starr. 1989. *Inquiry, Logic and International Politics*. Columbia: University of South Carolina Press.
- Most, Benjamin A. and Randolph M. Siverson. 1987. Substituting Arms and Alliances 1870–1914: an Exploration in Comparative Foreign Policy. In *New Directions in the Study of Foreign Policy*, ed. Charles F Hermann, Charles W. Kegley Jr and James N. Rosenau. Boston: Allen & Unwin pp. 131–160.
- Murray, Jared S, David B Dunson, Lawrence Carin and Joseph E Lucas. 2013. "Bayesian Gaussian Copula Factor Models for Mixed Data." *Journal of the American Statistical Association* 108(502):656–665.
- Narizny, Kevin. 2003. "Both Guns and Butter, or Neither: Class Interests in the Political Economy of Rearmament." *American Political Science Review* 97(2):203–220.
- Olson, Mancur and Richard Zeckhauser. 1966. "An Economic Theory of Alliances." *The Review of Economics and Statistics* 48(3):266–279.
- Palmer, Glenn. 1990. "Alliance Politics and Issue Areas: Determinants of Defense Spending." *American Journal of Political Science* 34(1):190–211.
- Plümper, Thomas and Eric Neumayer. 2015. "Free-riding in alliances: Testing an old theory with a new method." *Conflict Management and Peace Science* 32(3):247–268.
- Quinn, Kevin M. 2004. "Bayesian Factor Analysis for Mixed Ordinal and Continuous Responses." *Political Analysis* 12(4):338–353.
- Quiroz Flores, Alejandro. 2011. "Alliances as Contiguity in Spatial Models of Military Expenditures." *Conflict Management and Peace Science* 28(4):402–418.
- Rahman, Habibur. 1982. "British post?-second world war military planning for the Middle East." *Journal of Strategic Studies* 5(4):511–530.

- Reiter, Dan, Allan C. Stam and Michael C. Horowitz. 2016. "A Revised Look at Interstate Wars, 1816–2007." *Journal of Conflict Resolution* 60(5):956–976.
- Sarkees, Meredith Reid and Frank Whelon Wayman. 2010. Resort to war: a data guide to interstate, extra-state, intra-state, and non-state wars, 1816-2007. Washington, DC: CQ Press.
- Seawright, Jason. 2016. *Multi-Method Social Science: Combining Qualitative and Quantitative Tools*. Cambridge University Press.
- Senese, Paul D and John A Vasquez. 2008. *The steps to war: An empirical study*. Princeton University Press.
- Shin, Michael and Michael D. Ward. 1999. "Lost in Space: Political Geography and the Defense-Growth Trade-Off." *Journal of Conflict Resolution* 43(6):793–817.
- Singer, J David. 1988. "Reconstructing the correlates of war dataset on material capabilities of states, 1816–1985." *International Interactions* 14(2):115–132.
- Snyder, Glenn H. 1997. Alliance Politics. Ithaca: Cornell University Press.
- Sorokin, Gerald L. 1994. "Arms, Alliances, and Security Tradeoffs in Enduring Rivalries." *International Studies Quarterly* 38(3):421–446.
- Stegmueller, Daniel. 2013. "How many countries for multilevel modeling? A comparison of frequentist and Bayesian approaches." *American Journal of Political Science* 57(3):748–761.
- Thompson, William R. and David R. Dreyer. 2012. *Handbook of International Rivalries 1494–2010*. Washington, DC: CQ Press.
- Treier, Shawn and Simon Jackman. 2008. "Democracy as a Latent Variable." *American Journal of Political Science* 52(1):201–217.
- Whitten, Guy D. and Laron K. Williams. 2011. "Buttery Guns and Welfare Hawks: The Politics of Defense Spending in Advanced Industrial Democracies." *American Journal of Political Science* 55(1):117–134.
- Williams, Laron K. 2015. "Estimating the defense spending vote." *Electoral Studies* 39:243–255.
- Williamson, Oliver E. 1985. The Economic Institutions of Capitalism. New York: Free Press.
- Zielinski, Rosella Cappella, Benjamin O Fordham and Kaija E Schilde. 2017. "What goes up, must come down? The asymmetric effects of economic growth and international threat on military spending." *Journal of Peace Research* 54(6):791–805.