# Alliance Participation, Treaty Depth, and Military Spending

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How does alliance participation affect military spending?

# A Tale of Two French Alliances

#### A Tale of Two French Alliances





#### A Tale of Two French Alliances





# Does alliance participation

increase military spending?

increase military spending?

Or decrease it?

Does alliance participation

Treaty depth increases free-riding in alliances by non-major powers.

### What Does That Mean?

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- **Depth**: The extent of military cooperation an alliance treaty promises.
- Free-riding: Low defense spending by alliance participants.
- Non-major powers: Countries with less capability and ambition in international politics.

Depth reveals a tradeoff between reassurance and free-riding in alliance politics.

# Why Should You Care?





# **Competing Claims and Results**

	Decrease	Increase	Null
Most & Siverson 1987			Χ
Conybeare 1994	Χ		
Diehl 1994		X	
Goldsmith 2003			Χ
Morgan & Palmer 2006		X	
Quiroz-Flores 2011		Χ	

# Alliance Heterogeneity

• Alliances can increase or decrease military spending.

# **Alliance Heterogeneity**

- Alliances can *increase or decrease* military spending.
- Depends on alliance characteristics.

Treaty depth is a key source of differences between alliances.

I make my claim about alliance participation and military spending in three ways:

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1. Argument: Treaty Depth and Non-Major Powers

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- 1. Argument: Treaty Depth and Non-Major Powers
- 2. Statistical Analysis
- 3. Evidence from US alliances

# **Argument**

# **Opportunism in Alliances**

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- 1. Abandonment.
- 2. Free-riding.

# Free-riding

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# **Free-riding**

Free-riding means alliance members:

- 1. Rely on partners for protection and
- 2. Reduce defense spending.

Deep alliances lead to more free-riding.

# **Treaty Depth**

Deep treaties stipulate extensive defense cooperation.

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- 1. Require more policy coordination and defense cooperation among alliance members.
- 2. Formal defense cooperation:
  - Bases, policy coordination, military aid, side agreements, formal institutions.

# **Limits on Free-Riding**

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# **Limits on Free-Riding**

There are two ways depth increases alliance members ability to free-ride.

- 1. Greater alliance credibility: reduces leverage over free-riding.
- 2. Efficiency gains from defense cooperation.

Depth is relevant for non-major powers because they are more prone to free-ride.

### **Non-Major Powers**

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- Emphasize immediate security.
- Constraint: Opportunity costs of military spending.
- Under some conditions, alliance participation decreases military spending.

Hypothesis 1: The impact of alliance participation on percentage changes in non-major power military spending will be lower in deep alliances, relative to shallow alliances.

# **Empirical Analysis**

#### Research Design

I need two things to test the prediction:

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- Connect alliance-level variation with state-level outcomes— multilevel Bayesian analysis.

## **Measuring Treaty Depth**

I use a latent variable model to infer treaty depth from observed promises.

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My measure of depth for each alliance is the posterior mean of a latent factor.

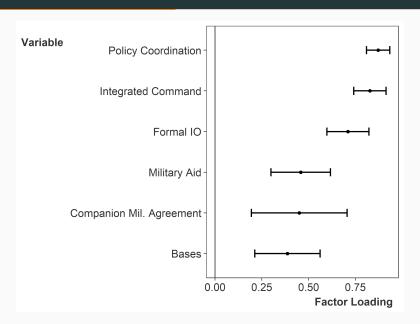
#### **Details of Measure**

- Multiple observed indicators of depth in ATOP alliances with military support:
  - Defense Cooperation: bases, integrated command, military aid, IO formation, defense policy coordination, other military agreements.

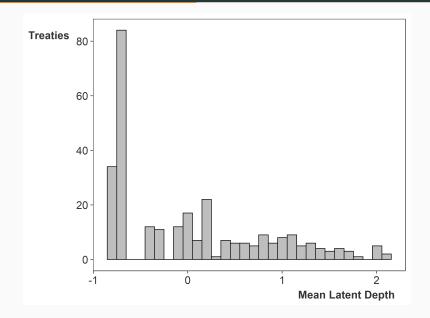
#### **Details of Measure**

- Multiple observed indicators of depth in ATOP alliances with military support:
  - Defense Cooperation: bases, integrated command, military aid, IO formation, defense policy coordination, other military agreements.
- Semiparametric mixed factor analysis. (Murray et al 2013)

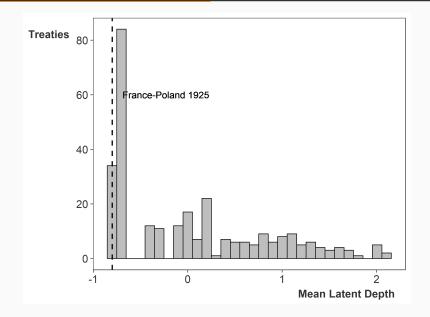
#### **Factor Loadings**



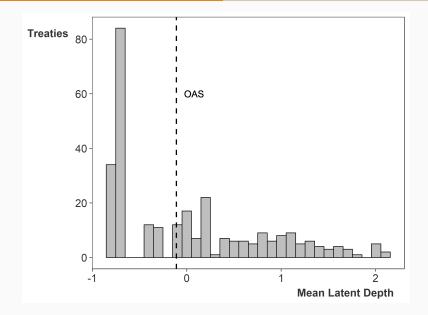
# **Latent Measure of Treaty Depth**



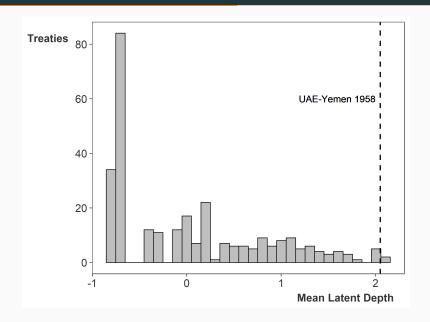
# Latent Measure of Treaty Depth: Shallow



# Latent Measure of Treaty Depth: Typical



### Latent Measure of Treaty Depth: Deep



### **Empirical Analysis: Multilevel Model**

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- Link alliance-level variation with state-level outcomes.
- Two connected regressions: alliance and state-level.
- Alliance characteristics modify the association between alliance membership and percentage changes in spending.

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- 2. Explicitly model heterogeneous effects of alliances.
- 3. States are members of multiple alliances.
- 4. Includes multiple salient alliance characteristics.

$$\%$$
 Change = Varying + State + Alliance Mil. Ex. Intercepts Vars. Participation



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**Alliance** 

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- Alliance-Level IV: Mean treaty depth

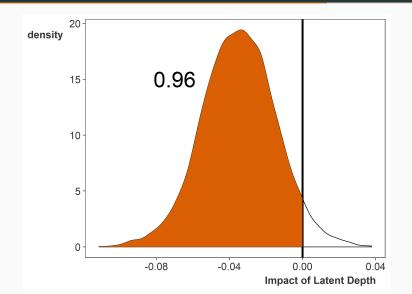
#### **Controls**

 State-Level Controls: Interstate war, civil War, annual MIDs, GDP growth, POLITY, Cold War, rival military expenditures.

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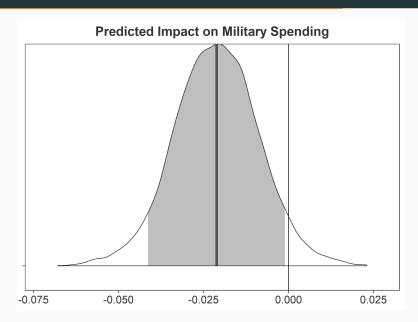
- State-Level Controls: Interstate war, civil War, annual MIDs, GDP growth, POLITY, Cold War, rival military expenditures.
- Alliance-Level Controls: Unconditional military support, economic issue linkages, foreign policy concessions, share of democracies, number of members, wartime, asymmetric obligations, US member (Cold War), USSR member.

# Association Between Treaty Depth and Changes in Military Spending

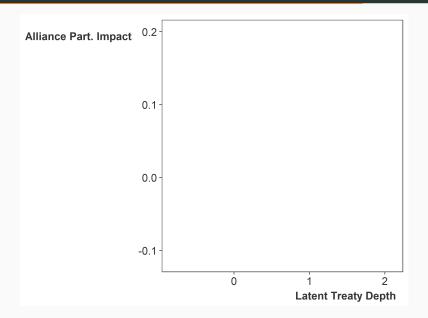


# **Substantive Importance**

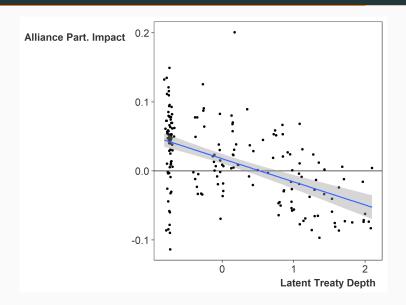
# **Substantive Importance**



# How Treaty Depth Modifies Alliance Impact



# **Treaty Depth and Alliance Impact**

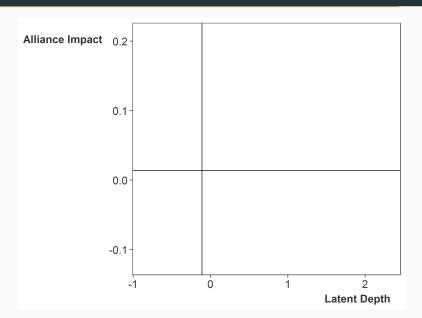


# **US Alliances**

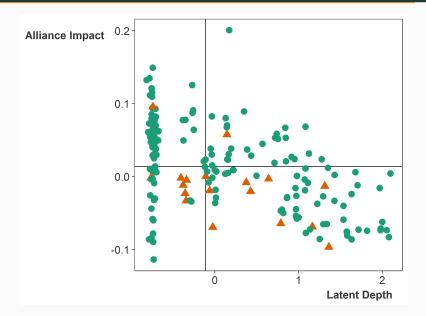
## Reassurance



#### **US Alliances in Context**



## **US Alliances in Context**



# Implication: What to do with US alliances?



Note: OAS stands for Organization of American States; NATO for North Atlantic Treaty Organization; and ANZUS for Australian, New Zealand, United States Security Treaty.

# Conclusion

How alliance participation affects military spending depends on treaty depth.

Deep alliances often reduce non-major

alliances often increase military

power military spending but shallow

spending.

There is a tradeoff between reassurance and free-riding in alliance treaty design.

# **Looking Ahead**

#### Dissertation

My dissertation articulates and tests a more general theory of alliance participation and military spending.

# My Research Agenda

The political economy of security, with a focus on formal institutions.

#### **International Security**

- Alliance Participation, Treaty Depth and Military Spending
- Reassessing the Public Goods Theory of Alliances

#### **Intra-State Conflict**

- Conflict Management Institutions and FDI
- Sanctioning Terrorist Groups: Can it Work?
- Weapon of the Weak?: Rebel Groups' International Law Talk, 1974-2011

Thank you! jkalley14@tamu.edu

#### Limitations

- 1. Domestic political economy of military spending.
- 2. Measurement error and missing data.
- 3. Formal depth only in the measure.
- 4. Strategic alliance design

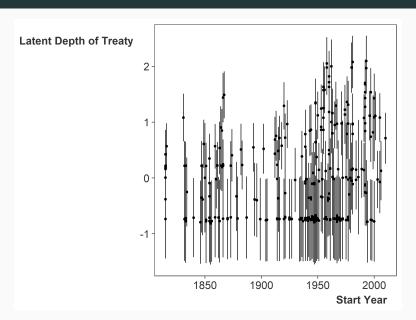
#### **Details of Measurement Model**

- Bayesian Gaussian Copula Factor Model: for mixed data.
- Uses copulas to break dependence between latent factors and marginal distributions.
- Treats marginals as unknown and keeps them free of dependence.
- IMH proposal, 10,000 iteration warmup, 20,000 samples, thinned every 20 draws.
- Generalized double Pareto prior for the factor loading flexible generalized Laplace distribution with a spike at zero and heavy tails.

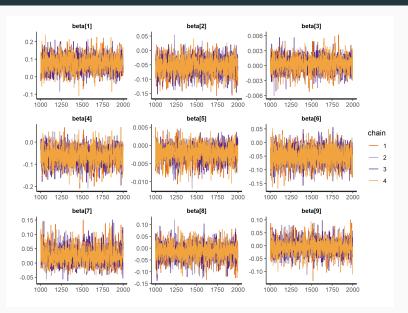
#### Aside: Benson and Clinton 2016

- Use a measurement model to infer alliance scope, depth and capability.
- Identify three separate dimensions, and use three modelsexplicit constraint.
- I use a different concept, which combines what they call scope and depth.
- Murray et al's model relaxes distributional assumptions in their estimator (Quinn 2004 Factor Analysis).

# Depth and First Year of the Alliance



# Trace plots: Non-Major



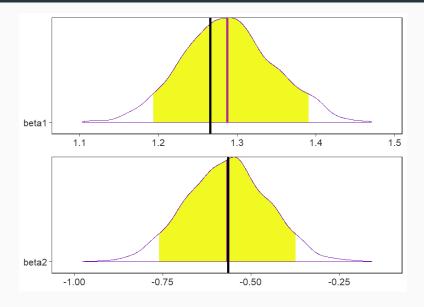
# Model Check: Recovering Known Parameters

Another way to check complicated models is simulating fake data with known parameters, then using the model to recover said parameters.

To check my model, I simulated a dataset of 2,000 observations with 50 states, 200 years, 100 alliances and 4 variables: 2 at each level.

The 90% credible intervals contain the known value for all regression parameters. 93 of 100 alliance specific parameter intervals contain the known value.

# **Simulated Parameters and Credible Intervals**

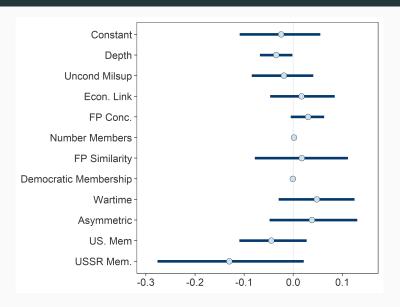


# Alliance-Level Regression Table: Non-Major Powers

8,668 observations and 192 alliances.

mean	sd	5%	95%	n_eff	Ŕ
-0.03	0.03	-0.08	0.02	1677.92	1.00
0.02	0.02	-0.00	0.05	2521.36	1.00
-0.02	0.02	-0.04	0.01	2997.70	1.00
0.01	0.01	-0.00	0.03	4019.10	1.00
0.00	0.00	-0.00	0.00	3820.06	1.00
0.00	0.03	-0.04	0.05	2254.34	1.00
-0.00	0.00	-0.00	0.00	4412.89	1.00
0.04	0.03	-0.01	0.08	3474.44	1.00
-0.03	0.02	-0.07	0.01	3474.45	1.00
0.02	0.02	-0.01	0.05	2330.47	1.00
0.04	0.05	-0.03	0.12	3859.50	1.00
0.02	0.01	0.00	0.03	1201.91	1.01
	-0.03 0.02 -0.02 0.01 0.00 0.00 -0.00 0.04 -0.03 0.02	-0.03 0.03 0.02 0.02 -0.02 0.02 0.01 0.01 0.00 0.00 0.00 0.03 -0.00 0.00 0.04 0.03 -0.03 0.02 0.02 0.02 0.04 0.05	-0.03 0.03 -0.08   0.02 0.02 -0.00   -0.02 0.02 -0.04   0.01 0.01 -0.00   0.00 0.00 -0.00   0.00 0.03 -0.04   -0.04 0.03 -0.01   -0.03 0.02 -0.07   0.02 0.02 -0.01   0.04 0.05 -0.03	-0.03 0.03 -0.08 0.02   0.02 0.02 -0.00 0.05   -0.02 0.02 -0.04 0.01   0.01 0.01 -0.00 0.03   0.00 0.00 -0.00 0.00   0.00 0.03 -0.04 0.05   -0.00 0.03 -0.01 0.08   -0.03 0.02 -0.07 0.01   0.04 0.05 -0.03 0.12	-0.03 0.03 -0.08 0.02 1677.92   0.02 0.02 -0.00 0.05 2521.36   -0.02 0.02 -0.04 0.01 2997.70   0.01 0.01 -0.00 0.03 4019.10   0.00 0.00 -0.00 0.00 3820.06   0.00 0.03 -0.04 0.05 2254.34   -0.00 0.00 -0.00 0.00 4412.89   0.04 0.03 -0.01 0.08 3474.44   -0.03 0.02 -0.07 0.01 3474.45   0.02 0.02 -0.01 0.05 2330.47   0.04 0.05 -0.03 0.12 3859.50

# Treaty Depth and Other Alliance Characteristics



#### **Priors**

4 Chains with 2,000 samples and 1,000 warmup iterations.

$$\begin{split} p(\alpha) &\sim \textit{N}(0,1) \\ p(\sigma) &\sim \text{half-N}(0,1) \\ p(\alpha^{\textit{yr}}) &\sim \textit{N}(0,\sigma^{\textit{yr}}) \\ p(\sigma^{\textit{yr}}) &\sim \textit{N}(0,1) \\ p(\alpha^{\textit{st}}) &\sim \textit{N}(0,\sigma^{\textit{st}}) \\ p(\sigma^{\textit{st}}) &\sim \text{half-N}(0,.5) \\ p(\sigma^{\textit{all}}) &\sim \text{half-N}(0,.5) \\ p(\beta) &\sim \textit{N}(0,.5) \\ p(\gamma) &\sim \textit{N}(0,.5) \\ p(\nu) &\sim \textit{gamma}(2,0.1) \end{split}$$

# **ML Model Specification**

$$y \sim student_t(\nu, \mu, \sigma)$$
 (1)

$$\mu = \alpha + \alpha^{st} + \alpha^{yr} + \mathbf{W}_{n \times k} \gamma + \mathbf{Z}_{n \times a} \lambda$$
 (2)

$$\lambda_a \sim N(\theta_a, \sigma_{all})$$
 (3)

$$\theta_{\mathsf{a}} = \alpha_{\mathsf{a}\mathsf{I}\mathsf{I}} + \beta_1 \mathsf{Treaty} \; \mathsf{Depth} + \mathbf{X}_{\mathsf{a}\times\mathsf{I}}\beta$$
 (4)

$$\mu_{it} = \alpha + \alpha^{st} + \alpha^{yr} + W_{it}\gamma + Z_{it}\lambda$$

#### Example year: Argentina 1955

- 1955 % Change Milex. = Overall mean
- + Argentine Intercept + 1955 Intercept
- + Argentine Characteristics
- $+\lambda_{OAS}*$  OAS Expenditure  $+\lambda_{Rio}*$  Rio Pact Expenditure

$$\lambda_{OAS} = \alpha_{all} + \beta_1 - 0.11 + \text{Controls}$$

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### Example

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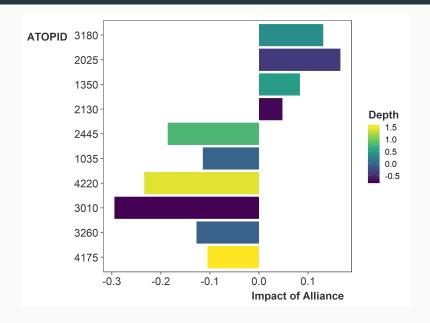
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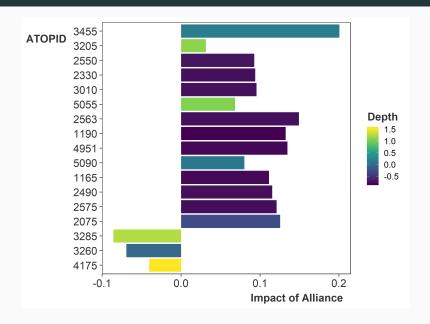
$$\lambda_{\textit{OAS}} = \alpha_{\textit{all}} + \beta_1 - 0.11 + \mathsf{Controls}$$

State-Year	Rio Pact	Warsaw Pact
Argentina 1954	.347	0
Argentina 1955	.418	0
1	:	1

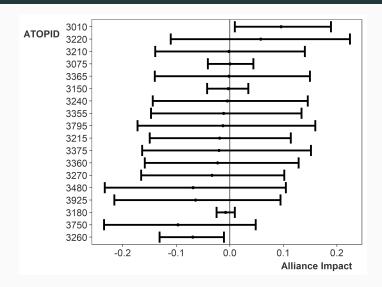
### **Notable Major Power Alliances**



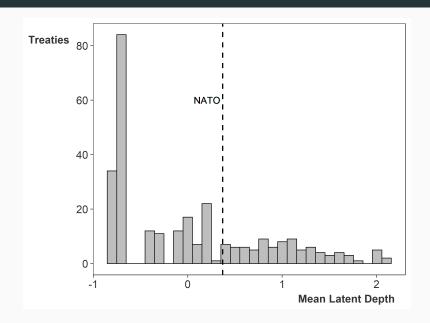
#### **Notable Non-Major Power Alliances**



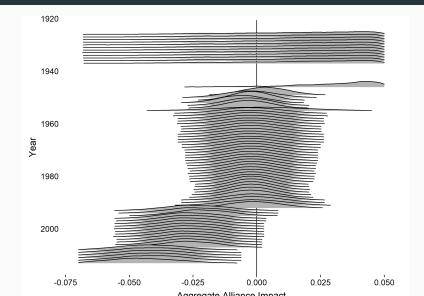
# Impact of US Alliance on Non-major Power Military Spending



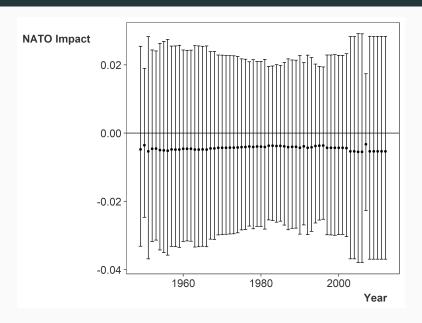
#### **NATO**



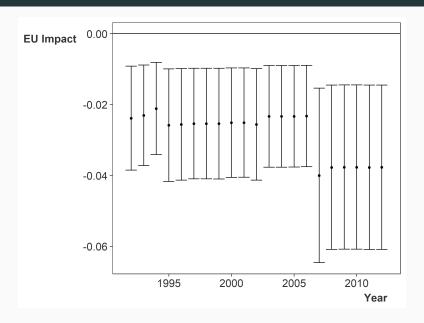
Alliance Participation and Military Spending: Belgium



# Impact of NATO on Belgium



# Impact of EU on Belgium



# Varying Slopes Model

Within each of the j groups of state capability, for i in  $1...n_j$ :

$$y_i \sim student_t(\nu_j, \alpha_j + \alpha^{st} + \alpha^{yr} + \mathbf{W}_i \gamma + \mathbf{Z}_{ji} \lambda_j, \sigma_j)$$

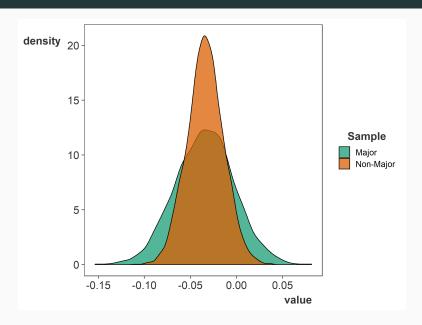
$$\lambda_j \sim N(\theta_j, \sigma_j^{all})$$

$$\theta_j = \alpha_j^{all} + \mathbf{X}\beta_j$$

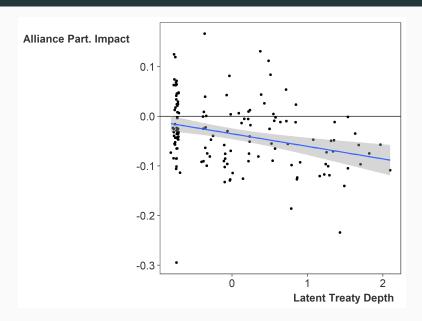
I give  $\beta_j$  a multivariate normal prior with prior scale  $\tau$ :

$$\beta_j \sim MVN(\mu_{\beta_i}, \Sigma_{\beta})$$

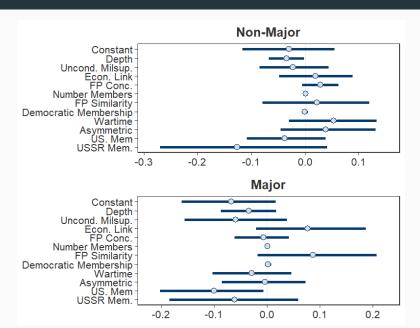
# Varying Slopes Results: Depth



# Treaty depth and $\lambda$ : Major Powers



### Full Varying Slopes Results



# **Correlates of War Spending Data**

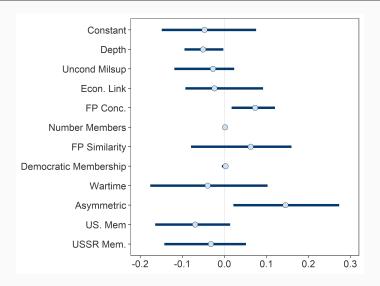
#### Is messy...

- Converted to standard units (British Pounds prior to 1914, US dollars thereafter).
- Occasionally smoothed with a seven-year moving average.
- Interpolation with stable currency.

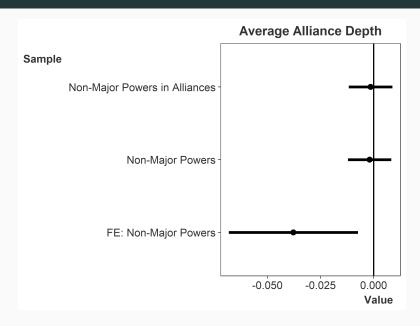
# Alternative Measure of Military Spending

- Nordhaus et al 2012 data: mix of COW and SIPRI- fully rebased
- 1949 to 2001
- Same model: use changes in spending instead of percentage changes.

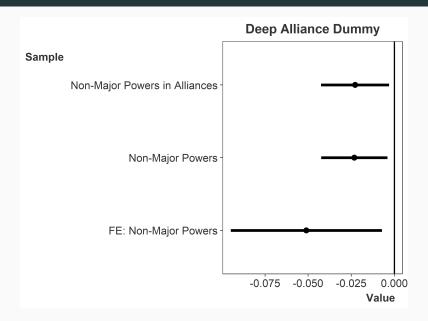
#### Alternative Measure of Military Spending: Results



### Single-Level Regression: Average Depth



# Single-Level Regression: Deep Alliance Dummy



# **Bounds Analysis of Single-Level Regression**

